Logical reasoning systems

- Theorem provers and logic programming languages
- Production systems Assignment Project Exam Help

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Frame systems and semantic networks

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Description logic systems

Logical reasoning systems

- Theorem provers and logic programming languages Provers: use resolution to prove sentences in full FOL. Languages: use backward chaining on restricted set of FOL constructs.
- chaining on restricted set of FOL constructs.

 Production systems based on interpreted as action (e.g., insertion & deletion in KB). Based on forward chaining + confliction by the particular of the particular o
- Frame systems and semantic networks objects as nodes in a graph, nodes organized as taxonomy links represent binary relations.
- Description logic systems evolved from semantic nets. Reason with object classes & relations among them.

Basic tasks

- Add a new fact to KB TELL
- Given KB and new fact, derive facts implied by conjunction of KB and new fact. In forward chaining: part of TELSSIGNMENT Project Exam Help
- Decide if query entailed by Keps howcoder.com
- Decide if query explicitly stored in KB restricted ASK Add WeChat powcoder
- Remove sentence from KB: distinguish between correcting false sentence, forgetting useless sentence, or updating KB re. change in the world.

Indexing, retrieval & unification

 Implementing sentences & terms: define syntax and map sentences onto machine representation.

```
Compound: has operate garments. Project Exam Help e.g., c = P(x) \land Q(x)   
Op[c] = \land; Args[c] = [P(x), Q(x)]
```

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FETCH: find sentences in KB that have same structure as query.

ASK makes multiple calls to FETCH Add WeChat powcoder

STORE: add each conjunct of sentence to KB. Used by TELL.

```
e.g., implement KB as list of conjuncts TELL(KB, A \land ¬B) TELL(KB, ¬C \land D) then KB contains: [A, ¬B, ¬C, D]
```

Complexity

With previous approach,

FETCH takes Of Stingenmenten Fetch Exam Help

STORE takes O(n) tining top st- plement (Rdifficheolof) report deplicates)

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Faster solution?

Table-based indexing

What are you indexing on? Predicates (relations/functions).

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letters //waxxxaadar aara				
Key	Positive https://p	Negative Chot povyco	Conclu- sion	Premise
Mother	Mother(ann,sam) Mother(grace,joe)	-Mother(ann,al)	XXXX	xxxx
dog	dog(rover) dog(fido)	-dog(alice)	xxxx	xxxx

Table-based indexing

Use hash table to avoid looping over entire KB for each TELL or FETCH

e.g., if only allowed literals are single letters, use a 26-element array to store their values. Assignment Project Exam Help

- More generally:
 - convert to Hattps://powcoder.com
 - index table by predicate symbol
 - for each symbol stprewe Chat powcoder list of positive literals

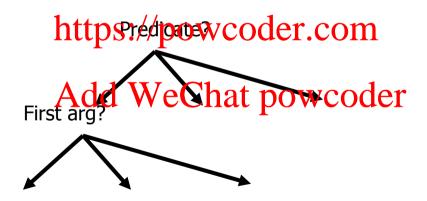
list of negative literals

list of sentences in which predicate is in conclusion

list of sentences in which predicate is in premise

Tree-based indexing

- Hash table impractical if many clauses for a given predicate symbol
- Tree-based indexing (or more generally combined indexing):
 compute indexing key from predicate and argument symbols.



Tree-based indexing

Example:

```
Person(age,height/weight/income) Project Exam Help
Person(30,72,210,45000)
Fetch( Person(age,72,210t/ipsom/e))owcoder.com
Fetch(Person(age,height>72,weight<210,income))
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```

Unification algorithm: Example

Understants (granne interpretation Help

Understands(httpsetepolowschlesystem) o substitute pete for x and make the implication that

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IF Understands(mary,pete) THEN Loves(mary,pete)

Unification algorithm

Using clever indexing, can reduce number of calls to unification

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Still, unification called very often (at basis of modus ponens) => need efficient implementation://powcoder.com

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See AIMA p. 303 for example of algorithm with O(n^2) complexity (n being size of expressions being unified).

Logic programming

Remember: knowledge engineering vs. programming...

Sound bit Assignment Project Exame Help

Logic programming
Identify problem Programming

Assemble information

Tea break Add WeChat
Encode information in KB

Encode problem instance as facts

Encode problem instance as facts

Apply program to data

Debug procedural errors

Should be easier to debug Capital(NewYork, US) than x := x + 2!

Logic programming systems

e.g., **Prolog:**

- Program = sequence of sentences (implicitly conjoined)
 All variables implicitly universally quantified ject Exam Help
- Variables in different sentences considered distinct
- Horn clause sentences on the company of the company and atomic consequent)
- Terms = constant symbols, variables, or functional terms
- Oueries = conjunctions, disjunctions, variables, functional terms
- Instead of negated antecedents, use negation as failure operator: goal NOT P considered proved if system fails to prove P
- Syntactically distinct objects refer to distinct objects
- Many built-in predicates (arithmetic, I/O, etc)

Prolog systems

Basis: backward chaining with Horn clauses + bells & whistles Widely used in Europe, Japan (basis of 5th Generation project) Compilation Seignment Project Expen Help

```
Program = set offchuses provided different, ... literal.

Efficient unification by open coding

Efficient retrieval of mytter flags why differ linking

Depth-first, left-to-right backward chaining

Built-in predicates for arithmetic etc., e.g., X is Y*Z+3

Closed-world assumption ("negation as failure")

e.g., not PhD(X) succeeds if PhD(X) fails
```

Basic syntax of facts, rules and queries

Nice very concise intro to prolog:

https://www.cis.upenn.edu/~matuszek/Concise%20Guides/Concise%20Prolog.html

Basic syntax of facts, rules and queries

```
/* program P
                          clause #
                                    */
p(a).
p(X) := q(X), r(X).
g(x) :- g(x) Assignment Project Exam Help
r(a).
              https://powcoder.com
r(b).
s(a).
              Add Wechat powcoder
s(b).
s(c).
                          /* #10 */
u(d).
```

Basic syntax of facts, rules and queries

```
*/
/* program P
                                clause #
p(a).
                                                                   Ouery for p(X) (i.e., for which values
                                /* #2 */
p(X) := q(X), r(X).
                                                                   of X is p(X) true):
                                /* #3 */
p(X) := u(X).
                         Assignment Project Exam Help
q(X) := s(X).
                                https://powcoder.com
r(a).
                                                                         | #2
                                                                                                  | #3
r(b).
                                                                    q(X),r(X)
                                                                                                u(X)
                                /* #7 */
s(a).
                                Add WeChat powcoder"
                                                                                                  #10(X=d)
s(b).
s(c).
                                                                     s(X), r(X)
                                                                                                 true
                                /* #10 */
u(d).
                                                                                                X=d
                                                          |#7(X=a)
                                                                         |#8(X=b)
                                                                                         |#9(X=c)
                                                         r(a)
                                                                        r(b)
                                                                                       r(c)
                                                     | #5
                                                             #61
                                                                    | #5
                                                                           #6 I
                                                                                    | #5
                                                                                            #6|
                                                              fail fail
                                                                                   fail
                                                                                            fail
                                                    true
                                                                           true
                                                                           X=b
                                                    X=a
```

A PROLOG Program

- A PROLOG program is a set of facts and rules.
 A simple program with just facts:

```
https://powcoder.com
parent(alice, fim).
parent (jim We Chat powcoder
parent (jim, sharon).
parent(tim, james).
parent(tim, thomas).
```

A PROLOG Program

- c.f. a table in a relational database. Assignment Project Exam Help
- Each line is a **fact** (a.k.a. a tuple or a row). https://powcoder.com
- Each line states that some person x is a parent of some (other) person Y.
- In GNU PROLOG the program is kept in an ASCII file.

A PROLOG Query

• Now Assign ask PRPLOGENESSIONS Help
| ?- parent(alice, jim).

yes https://powcoder.com
| ?- parent(jim, herbert).

no Add WeChat powcoder
| ?-

A PROLOG Query

Not very exciting. But what about this :
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```
| ?- parent(alice, Who).
Who = jhttps://powcoder.com
yes
| ?- Add WeChat powcoder
```

- Who is called a *logical variable*.
 - PROLOG will set a logical variable to any value which makes the query succeed.

A PROLOG Query II

- Sometimes there is more than one correct answer to a query. Assignment Project Exam Help
- PROLOG gives the answers one at a time. To get the next answer type https://powcoder.com

```
| ?- paradd W.eChoat powcodeNB: The;
Who = tim ?;
Who = dave ?;
Who = sharon ?;
yes
| ?-
```

A PROLOG Query II

```
| ?- parent (jim, Who).
Who = tim Assignment Project Exam
Who = dave ?
Who = sharon https://powcoder.com
yes
| ?- Add WeChat powcoder
```

• After finding that jim was a parent of sharon GNU PROLOG detects that there are no more alternatives for parent and ends the search.

Prolog example

conjunction

Depth-first search from a start state X: dfs(X) := goal(X).Appending https://powcoder.com append([],Add.WeChat powcoder append([X|L],Y,[X|Z]) :- append(L,Y,Z). query: append(A,B,[1,2])? answers: A=[] B=[1,2]A = [1] B = [2]A=[1,2] B=[]

Append

- append([], L, L)
- · append([HAL1]ghmeHt Project append(L1pL2, L3)
- Example join [a, bhttpwithpdwegoder.com
 - [a, b, c] has the recursive structure [a| [b, c]].
 - Then the rule says Add We Chat powcoder
 - IF [b,c] appends with [d, e] to form [b, c, d, e] THEN [a|[b, c]] appends with [d,e] to form [a|[b, c, d, e]]
 - i.e. [a, b, c, d, e]

Tower of Hanoi in Prolog

```
% move(N,X,Y,Z) - move N disks from peg X to peg Y, with peg Z being the
                 auxilliary peg
용
욯
 Strategy: Assignment Project Exam Help isc from
    peg X to peg Y, simply move that disc from X to Y
% Recursive Case: To transfer n discs from X to Y, do the following:
        Transfer the tringst point of X to Y of the Cthern peg Z
        Transfer the n-1 discs from 7 to peg Y
                       Anonymous variable
                                 hat powcoder
        write('Move top disk from
        write(X),
        write(' to '),
        write(Y),
                      Write a newline
    move(N,X,Y,Z) :-
        N>1,
        M is N-1,
        move(M,X,Z,Y),
        move(1,X,Y,),
        move(M,Z,Y,X).
```

Tower of Hanoi in Prolog

```
move(N,X,Y,Z) - move N disks from peg X to peg Y, with peg Z being the
                 auxilliary peg
 Strategy:
 Base Case: One disc - To transfer a stack consisting of 1 disc from
    peg X to peg Y, simel Solenment reolect Exam Help
% Recursive Case: To transfer A discs from X to Y, do the following:
        Transfer the first n-1 discs to some other peg 7
        Move the last disc on X to Y
        Transfer the n-1 dischtique: ** powcoder.com
    move(1,X,Y,):-
        write('Move top disk from d'WeChatispownCocker Prolog solves the case N=3.
        write(Y),
                                                ?- move(3,left,right,center).
        nl.
                                                Move top disk from left to right
    move(N,X,Y,Z) :-
                                                Move top disk from left to center
        N>1,
                                                Move top disk from right to center
        M is N-1,
                                                Move top disk from left to right
        move(M,X,Z,Y),
                                                Move top disk from center to left
        move(1,X,Y,),
                                                Move top disk from center to right
        move(M,Z,Y,X).
                                                Move top disk from left to right
                                                yes
```

+Vars ins +Domain

The key to solving Sudoku puzzles with Prolog is to use the clpfd (constraint logic programming over finite domains) library to restrict the search space to numbers 1-9. Then, it's just a matter of describing what a solution looks like.



True if Goal can successfully he possed open security of the contract of the c



The variables in the list *Vars* are elements of *Domain*. See $\frac{\ln n}{2}$ for the syntax of *Domain*.

https://www.swi-prolog.org/pldoc/doc/ CWD /index.html

The key to solving Sudoku puzzles with Prolog is to use the clpfd (constraint logic programming over finite domains) library to restrict the search space to numbers 1-9. Then, it's just a matter of describing what a solution looks like.

```
% need the module "choic constraint togic regregation of the search we can specify the range of numbers to search
?- use_module(library(clpfd)).
                         https://powcoder.com
sudoku(Rows) :-
       length(Rows, 9), % ensure there are 9 rows
       append(Rows, Vs), % combined all rows into the variable Vs
       Vs ins 1..9, % ensure that the elements of Vs should be numbers 1-9
       maplist(all_distinct, Rows), % ensure each row is distinct
       transpose(Rows, Columns), % flip the matrix
       maplist(all_distinct, Columns), % ensure each column is distinct
       Rows = [A,B,C,D,E,F,G,H,I], % create variables A-I for each row
       blocks(A, B, C), % make sure all values in these three rows (three 3x3 blocks) are distinct
       blocks(D, E, F), % ... and these rows/blocks
       blocks(G, H, I). % ... and these rows/blocks
```

```
length_(L, Ls) :- length(Ls, L). % version of length that's easierto use with maplist (above)

% this predicate ensures a "block" (3x3 grid) contains only distinct values
blocks([], [], []). Assignment Project Exam Help
blocks([A,B,C|Bs1], [D,E,F|Bs2], [G,H,I|Bs3]) :-
    all_distinct([A,B,C,D,E,F,G,H,I]),
    blocks(Bs1, Bs2, Bs3). https://powcoder.com

problem([[_-,-,-,-,-], Add WeChat powcoder
```

```
problem(Rows) Assignment Project Exam Help statistics(runtime, _), % builtin function, establishes "runtime" variable sudoku(Rows), % solve the puzzle maplist(writeln, Rows), ttp Show pro Wictor CuriceO.M.e., println each row) statistics(runtime, [_,T]), % use "runtime" variable to compute total time write('CPU time = '), write(T) write('msec'), nl, nl, false. % write total time Add WeChat powcoder
```

```
itti@iLab0:~$ prolog sudoku.pl
Welcome to SWI-Prolog (threaded, 64 bits, version 7.6.4)
SWI-Prolog comes with ABSOLUTELY NO WARRANTY. This is free software.
Please run ?- license. for legal details.
For online help and packground, Project, Exam Help
For built-in help, use ?- help(Topic). or ?- apropos(Word).
?- solve_problems. https://powcoder.com
[2,4,6,1,7,3,9,8,5]
[3,5,1,9,2,8,7,4,6] Add WeChat powcoder
                                  Note: returned false here
[6,3,4,8,9,2,1,5,7]
[7,9,5,4,6,1,8,3,2]
                                  Only so that the program would
[5,1,9,2,8,6,4,7,3]
[4,7,2,3,1,9,5,6,8]
                                  Then try to solve any other declared
[8,6,3,7,4,5,2,1,9]
CPU time = 44 msec
                                  Instance of problem().
false.
```

Expanding Prolog

Parallelization:

OR-parallelism: goal may unify with many different literals and implications in KB

AND-parallelism: 1301/10016 Portuget of body of 131 implication in parallel

- Compilation: generate built in theorem prover por different predicates in KB
- Optimization: for example through the order powcoder e.g., "what is the income of the spouse of the president?"

Income(s, i) \land Married(s, p) \land Occupation(p, President)

faster if re-ordered as:

Occupation(p, President) \(\text{Married(s, p)} \(\text{N Income(s, i)} \)

Theorem provers

- Differ from logic programming languages in that:
 - accept full FOL
 - results independent to From the Which & Bre Herto

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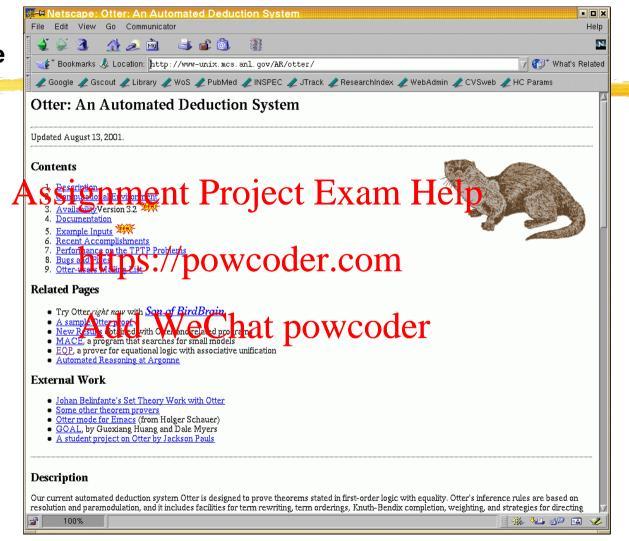
OTTER

- Organized Techniques for Theorem Proving and Effective Research (McCune, 1992)
- Set of support (sos): set of clauses defining facts about problem Each resolution step: Set of clauses defining facts about problem to be supported by the support of solution step: Set of clauses defining facts about problem.
- Usable axioms (outside sos): provide background knowledge about domain
- Rewrites (or demodulator) the converge E.g., x+0=x
- Control strategy: defined by set of parameters and clauses. E.g., heuristic function to control search, filtering function to eliminate uninteresting subgoals.

OTTER

- Operation: resolve elements of sos against usable axioms
- Use best-first search: heuristic function measures "weight" of each clause (lighter weight preferred; thus in general weight bleekted weight.
- At each step: move lightest to usable list consequences of resolving that close against usable list
- Halt: when refutation found dos Weigh Chat powcoder

Example



Example: Robbins Algebras Are Boolean

• The Robbins problem---are all Robbins algebras Boolean?---has been solved: Every Robbins algebra is Boolean. This theorem was proved automatically by EQP, a theorem proving program developed at Argonne National Laboratory

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Example: Robbins Algebras Are Boolean

Historical Background

```
In 1933, E. V. Huntington presented the following basis for Boolean algebra: Assignment Project Examp Help
x + y = y + x.
(x + y) + z = x + (y + z).
                                                 [associativity]
n(n(x) + y) + n(n(x) + n(y)) = x.//pow[Huntington_equation]
```

Shortly thereafter, Herbert Robbins conjectured that the Huntington equation can be replaced with a simple work WeChat powcoder

```
n(n(x + y) + n(x + n(y))) = x. [Robbins equation]
```

Robbins and Huntington could not find a proof, and the problem was later studied by Tarski and his students

```
Searching ...
Success, in 1.28 seconds!
                                                                                    Given to
                   PROOF
                                                                                    the
          n(n(A)+B)+n(n(A)+n(B))!=A.
                                                                                    system
          x=x.
3
5,4
          X+V=V+X.
          (x+y)+z=x+(y+z).
          n(n(x+y)+n(x+n(y)))=x.
          X+X=X.
         n(n(A)+n(B))+n(n(A)+B)!=A

x+ (A)SSIGNMENT Projected Example 112

x+ (y+z)=y+ (yz).
13
23, 22
          x + (y + x) = x + y
                                                            [para into, 13, 3]
          n(n(x)+n(x+n(x)))=x.
26
                                                           [para into, 6, 8]
         n(n(x)+x)+n(x))=n(x)

n(n(x+n(y))+n(x+y))=n(x)

x+(y+z)=x+(z+y)
                                                WCOder com
36
42
52
                                                            para into, 15, 3, demod, 5]
81,80
          n(n(x+n(x))+n(x))=x.
                                                           [para into, 26, 3]
82
                                                           [para from, 26, 6, demod, 23]
          n(n(n(x)+x)+x)=n(x).
          n(n(n(x+n(x))+(n(y)+x))+x) = n(x+n(y))+n(x). [para into, 80, 80, demod, 5, 81] n(n(n(x+n(x))+x)+x) = n(x+n(x)) + n(x)
125
                                                          pave@der
139
166, 165
          n(n(x+n(x))+x)=n(x).
180, 179
          n(n(x)+x)=n(x+n(x)).
                                                           [back demod, 139, demod, 166]
195
          n(n(x+n(x))+n(n(x)))=n(x).
                                                           [back demod, 36, demod, 180]
197
          n(n(x+(n(x)+n(x+n(x))))+(n(x+n(x))+x))=n(x). [para into, 165, 165, demod, 5, 180, 5, 166]
206,205 \quad n(n(x+(n(x)+n(x+n(x))))+n(x))=n(x+n(x))+x. [para from, 165, 80, demod, 166, 5, 180, 5]
223, 222 n(n(x+y)+(y+x))=n(x+(y+n(x+y))).
                                                           [para into, 179, 52, demod, 5]
231,230 n(n(x+(n(x)+n(x+n(x))))+x)=n(x+n(x))+n(x). [back demod, 125, demod, 223]
564,563 \quad n(x+n(x)) + x=x
                                                           [para into, 195, 80, demod, 5, 223, 81, 206, 81]
582,581 \quad n(x+n(x))+n(x)=n(x).
                                                           [back demod, 197, demod, 564, 231]
586,585 n(n(x))=x.
                                                           [back demod, 80, demod, 582]
606,605
         n(x+n(y))+n(x+y)=n(x).
                                                           [para into, 585, 42, flip. 1]
621
          A!=A.
                                                           [back demod, 10, demod, 606, 586]
622
          ŠF.
                                                           [binary, 621, 2]
----- end of proof ------
```

Forward-chaining production systems

 Prolog & other programming languages: rely on backward-chaining (I.e., given a query, find substitutions that satisfy it)

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- Forward-chaining systems: infer everything that can be inferred from KB each time new senters: infer everything that can be inferred from KB
- Appropriate for agent design as returns best action

Implementation

- One possible approach: use a theorem prover, using resolution to forward-chain over KB
- More restricted systems can be more efficient.
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- Typical components:
 - KB called "white sempo (wesited the rate of provided the rate of provi
 - rule memory (set of inference rules in form
 - at each cycle: find rules whose premises satisfied
 - - by working memory (match phase)
 - decide which should be executed (conflict resolution phase)
 - execute actions of chosen rule (act phase)

Match phase

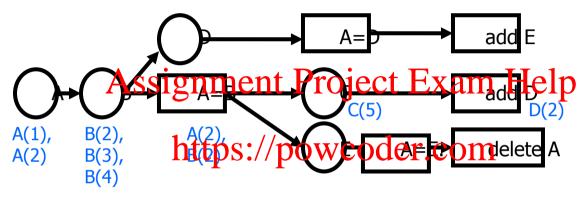
- Unification can do it, but inefficient
- Rete algorithm (used in OPS-5 system): example ASSIGNMENT Project Exam Help

rule memory:

```
A(x) \land B(x) \land C(y) \Rightarrow add
A(x) \land B(y) \land D(x) \Rightarrow add E(x)
A(x) \land B(y) \land D(x) \Rightarrow add E(x)
A(x) \land B(x) \land E(x) \Rightarrow delete A(x)
A(x) \land
```

Build Rete network from rule memory, then pass working memory through it

Rete network



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Circular nodes: fetches to WM; rectangular nodes: unifications

$$A(x) \wedge B(x) \wedge C(y) \Rightarrow \text{add } D(x)$$

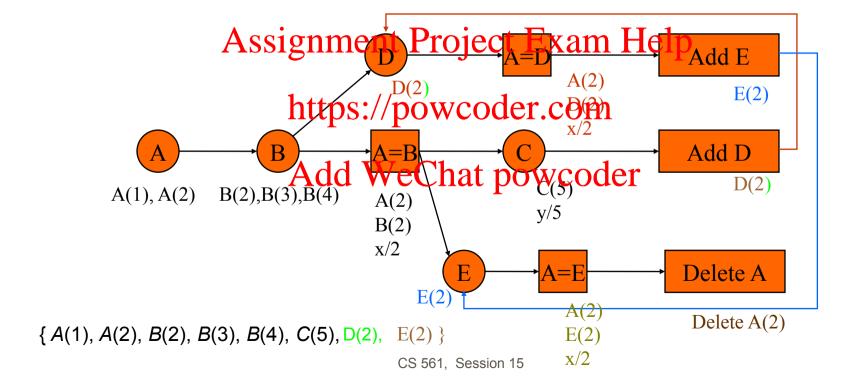
 $A(x) \wedge B(y) \wedge D(x) \Rightarrow \text{add } E(x)$
 $A(x) \wedge B(x) \wedge E(x) \Rightarrow \text{delete } A(x)$

 $\{A(1), A(2), B(2), B(3), B(4), C(5)\}$

Rete match

$$A(x) \wedge B(x) \wedge C(y) \Rightarrow \text{add } D(x)$$

 $A(x) \wedge B(y) \wedge D(x) \Rightarrow \text{add } E(x)$
 $A(x) \wedge B(x) \wedge E(x) \Rightarrow \text{delete } A(x)$



Advantages of Rete networks

- Share common parts of rules
- Eliminate duplication over time (since for most production systems only a few rules change at each time step) ASSIGNMENT Project Exam Help

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Conflict resolution phase

- one strategy: execute all actions for all satisfied rules
- or, treat them as suggestions and use conflict resolution to pick one action. Assignment Project Exam Help
- Strategies:
 - no duplication (do not executes w/cerame no de la company en la compan
 - regency (prefer rules involving recently created WM elements)
 - specificity (prefer more specific rules) Chat powcoder operation priority (rank actions by priority and pick highest)

Frame systems & semantic networks

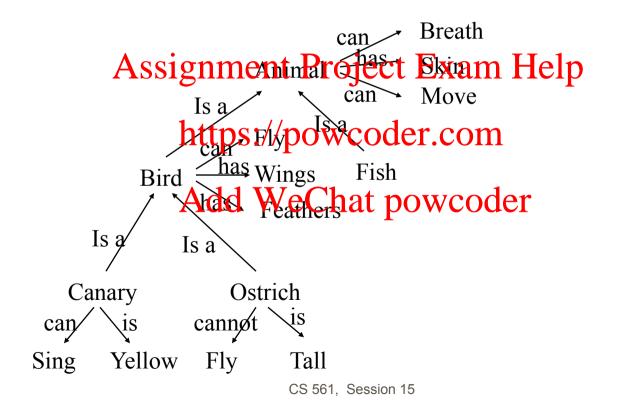
- Other notation for logic; equivalent to sentence notation
- Focus on categories and relations between them (remember ontologies)
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- e.g., Cats Mammals https://powcoder.com

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Syntax and Semantics

Assignment Project Exam Help				
Link Type	Semantics			
$A \stackrel{\text{Subset}}{\rightarrow} B \text{https}$://poweoder.com			
I K	WeChat ^B powcoder			
$A \rightarrow B$	R(A,B)			
$A \xrightarrow{\mathbb{R}} B$	$\forall x \ x \in A \Rightarrow R(x,y)$			
$A \xrightarrow{\square} B$	$\forall x \exists y \ x \in A \Rightarrow y \in B \land R(x,y)$			

Semantic Network Representation



Semantic network link types

Link type	Semantics	Example
$A \xrightarrow{Subset} B$	Assignment Project Exam He	Cats Mammals
$A \xrightarrow{Member} B$	https://powcoder.com A ∈ B	Bill <u>Member</u> Cats
$A \xrightarrow{R} B$	Add WeChat powcoder R(A, B)	$Bill \xrightarrow{Age} 12$
$A \xrightarrow{R} B$	$\forall x x \in A \Rightarrow R(x, B)$	Birds Legs 2
$A \xrightarrow{R} B$	$\forall x \; \exists y \; x \in A \Rightarrow y \in B \land R(x, y)$	Birds Birds

Goal: Make it easier to describe categories (as opposed to objects)
Popularized by projects such as the Semantic Web

DL Syntaxssignment Project Exam Help

- Signature
 - Concept (aka class names s.g/, Cat Animal Doctoler.com
 - Equivalent to FOL unary predicates
 - Role (aka property) names, e.g., sits-on, hasParent, loves
 - · Equivalent to FOL Anar pedial seChat powcoder
 - Individual names, e.g., Felix, John, Mary, Boston, Italy
 - · Equivalent to FOL constants
- Operators
 - Many kinds available, e.g.,
 - Standard FOL Boolean operators (□, □, ¬)
 - Restricted form of quantifiers (∃, ∀)
 - Counting (≥, ≤, =)

- Concept expressions, e.g.,
 - Doctor ⊔ Lawyer
 - Rich □ Happy
 - Cat n 3sig Angerignment Project Exam Help
- Equivalent to FOL formulae with one free variable
 - Doctor(x) \(\forall \) Lawy f(t) by (t) \(\forall \) powcoder.com
 - Rich $(x) \wedge \text{Happy}(x)$

- $\exists y.(Cat(x) \land sits-on(x,y))$ Add WeChat powcoder

- Special concepts
 - (aka top, Thing, most general concept)
 - (aka bottom, Nothing, inconsistent concept)

used as abbreviations for

- (A ⊔ ¬ A) for any concept A
- (A □ ¬ A) for any concept A

```
Role expressions, e.g.,
  - loves

    hasParent o hasBrother

Equivalent to ASS signal as with two free variables t Exam Help
  - loves(y, x)
  =\exists z.(\text{hasParent}(x,z) \land \text{hasBrother}(z,y))
"Schema" Axioms, e.https://powcoder.com
 Rich □ ¬Poor
                                                   (concept inclusion)

    Cat □ ∃sits-on.Mat ⊑ Happy -

                                                   (concept inclusion)
                                                   (role inclusion)
 sits-on 

touches
 Trans(part-of)
                                                   (transitivity)
Equivalent to (particular form of) FOL sentence, e.g.,
 - \forall x.(Rich(x) \rightarrow \neg Poor(x))
 - \forallx.(Cat(x) \land \existsy.(sits-on(x,y) \land Mat(y)) \rightarrow Happy(x))
 - \forall x.(BlackCat(x) \leftrightarrow (Cat(x) \land \exists y.(hasColour(x,y) \land Black(y)))
 - \forall x,y.(sits-on(x,y) \rightarrow touches(x,y))
```

 $- \forall x,y,z.((sits-on(x,y) \land sits-on(y,z)) \rightarrow sits-on(x,z))$

- "Data" Axioms (aka Assertions or Facts), e.g.,
 - BlackCat(Felix) (concept assertion)
 - Mat(Mat1) (concept assertion)
 - Sits-on(FANSignment Projects-Exam Help
- Directly equivalent to FOL "ground facts"
 - Formulae with no hardeless://powcoder.com

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Knowledge base = set of axioms (TBox) + set of facts (ABox)

The DL family

- Many different DLs, often with "strange" names
 - E.g., Assignment Project Exam Help
- Particular DL defined by:
 - Concept operators (7 L)/powcoder.com
 Role operators (-, o, etc.)

 - Concept axioms (□, □, etc.)
 Role axioms (□, Trans, etc.)

The DL family

- E.g., EL is a well known "sub-Boolean" DL
 - Concept operators: □, ¬, ∃
 - No role operators (only atomic roles)
 - Concept Axioms ig ment Project Exam Help
- E.g.:

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- ALC is the smallest propositionally closed DL
 - Concept operators: □, ⊔, ¬, ∃, ∀
 - No role operators (only atomic roles)
 - Concept axioms: ⊑, ≡
 - No role axioms
- E.g.:

The DL family

- S used for ALC extended with (role) transitivity axioms
- Additionalseiten immigate Pariges extensions, Idelp
 - — H for role hierarchy (e.g., hasDaughter
 — hasChild)
 - R for role both (1995 has Brown to the Brother 15 has Uncle)
 - O for nominals/singleton classes (e.g., {Italy})
 - I for inverse poles (evo is child of has Child of has Child of the has C
 - N for number restrictions (e.g., ≥2hasChild, ≤3hasChild)
 - Q for qualified number restrictions (e.g., ≥2hasChild.Doctor)
 - \mathcal{F} for functional number restrictions (e.g., ≤ 1 has Mother)
- E.g., SHIQ = S + role hierarchy + inverse roles + QNRs

Example

- W3C's OWL 2 (like OWL, DAML+OIL & OIL) based on DL
 - OWL 2 based en FRETH, Projecte ded with Help transitive roles, a role box nominals, inverse roles and qualified number restrictions

OWL 2 EL LATTERSEL/powcoder.com

- · OWL 2 QL based on DL-Lite
- · OWL 2 EL badd We Chat powc
- OWL was based on \mathcal{SHOIN}
 - only simple role hierarchy, and unqualified NRs



Example: OWL2

OWL Constructor	DL Syntax	Example
intersectionOf	$C_1 \sqcap \ldots \sqcap C_n$	Human □ Male
unionOf	$C_1 \sqcup \ldots \sqcup C_n$	Doctor ⊔ Lawyer
complementOf	$\neg C$	Jean Exam Help
oneOf ASS1	gainenr faro	Jean Examy Help
allValuesFrom	$\forall P.C$	∀hasChild.Doctor
someValuesFrom	$\exists P_i C$	∃hasChild.Lawyer
_	nttps://pow	1
minCardinality	$ $ $\geqslant n\bar{P}$	≥2hasChild

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OWE Syllian -	-5E-3yi tak	LXanipie -
subClassOf	$C_1 \sqsubseteq C_2$	Human <u></u> Animal □ Biped
equivalentClass	$C_1 \equiv C_2$	Man ≡ Human □ Male
subPropertyOf	$P_1 \sqsubseteq P_2$	hasDaughter <u>□</u> hasChild
equivalentProperty	$P_1 \equiv P_2$	cost ≡ price
transitiveProperty	$P^+ \sqsubseteq P$	ancestor ⁺ ⊑ ancestor

OWL Syntax	DL Syntax	Example
type	a:C	John : Happy-Father
property	$\langle a,b angle$: R	$\langle John, Mary \rangle$: has-child

Example: OWL2

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```
E.g., Person \sqcap \forall hasChild.(Doctor \sqcup \exists hasChild.Doctor):
         <owl:intersectionOf rof:parseType=" collection">
                    <owl:Class rdf:about="#Person"/>
                    <owl:Restriction>-
                             <owl: checket water to the control of the cont
                              <owl:allValuesFrom>
                                         <owl:unionOf rdf:parseType=" collection">
                                                  <owl:Class rdf:about="#Doctor"/>
                                                  <owl:Restriction>
                                                            <owl:onProperty rdf:resource="#hasChild"/>
                                                            <owl:someValuesFrom rdf:resource="#Doctor"/>
                                                  </owl:Restriction>
                                         </owl:unionOf>
                             </owl:allValuesFrom>
                    </owl:Restriction>
          </owl:intersectionOf>
</owl:Class>
```

Why description logics?

- OWL exploits results of 20+ years of DL research
 - Well defined (model theoretic) semantics



I can't find an efficient algorithm, but neither can all these famous people.

[Garey & Johnson. Computers and Intractability: A Guide to the Theory of NP-Completeness. Freeman, 1979.]

- Known reasoning algorithms
- Scalability demonstrated by implemented systems

Why description logics?

Major benefit of OWL has been huge increase in range and sophistication of tools and refrestructure in Help

- Editors/development environments
- Reasoners http://pack.gr/pood.com/pack
- Explanation, justification Add and pinpointing
- Integration and modularisation
- y McCll ratios to ht in the cody of anchester

 McCll ratios to ht in the cody of the pyrion of their

 of the modifications may be determined from the Changelog placed at

 the end of this file.

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 * This library is distributed in the hope that it will be useful,

 but WITHOUT ANY WARRANTY; without even the implied warranty of

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 Lesser General Public License for more details.

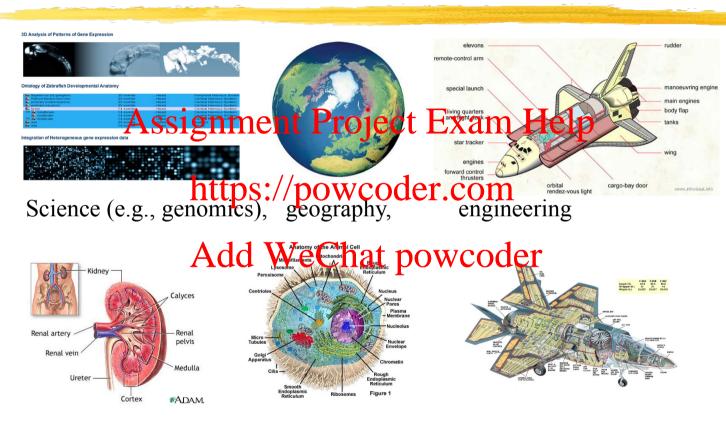
mport org.semanticweb.owlapi.apibinding.OWLManager:

import org.semanticweb.owlapi.util.DefaultPrefixManager;

import org.semanticweb.owlapi.model.*;

APIs, in particular the OWL API

Many applications



Medicine, biology,

defense