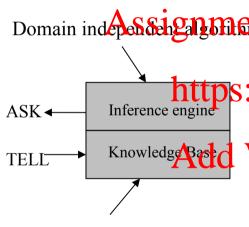
Knowledge and reasoning – second part

- Knowledge representation
- Logic and representation
- Propositional (Page in Project Exam Help
- Normal forms
- Inference in proposition in propositio
- Wumpus world example

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Knowledge-Based Agent



Domain specific content

- Agent that uses **prior** or **acquired** knowledge to achieve its goals
 - Can make more efficient decisions
- Knowledge Base (KB): contains a set of prepresentations of facts about the Agent's environment.
- Each representation is called a **sentence**Wellston

 Representation

 language, to TELL it what to know e.g.,
 (temperature 72F)
 - ASK agent to query what to do
 - Agent can use inference to deduce new facts from TELLed facts

Generic knowledge-based agent

```
function KB-AGENT( percept) returns an action static: KB, a knowledge base t, a counter, initially 0, indicating time t Tell(KB, MASSIGNIME ITELL(KB, MAKE-ACTION-QUERY(t)) action \leftarrow ASK(KB, MAKE-ACTION-QUERY(t)) Tell(KB, MAKE-ACTION-SENTENCE(action, t)) t \leftarrow t+1 https://powcoder.com return action
```

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- 1. TELL KB what was perceived
 Uses a KRL to insert new sentences, representations of facts, into KB
- 2. ASK KB what to do.
 Uses logical reasoning to examine actions and select best.

Wumpus world example

Percepts Breeze, Glitter, Smell

Actions Left turn, Right turn,

Assign friendle spoject Examination

Goals Get gold back to start

without entering proposed or valor assignment of the start of the st

Environment

Squares adjacent to workplace professional Squares adjacent to pit are breezy
Glitter if and only if gold is in the same square
Shooting kills the wumpus if you are facing it
Shooting uses up the only arrow
Grabbing picks up the gold if in the same square
Releasing drops the gold in the same square



Wumpus world characterization

Deterministic?

Accessible?

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Static?

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Discrete?

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Episodic?

Wumpus world characterization

Deterministic?

Yes – outcome exactly specified.

Accessible?

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Static?

Yes – Wumpus and pits do not move.

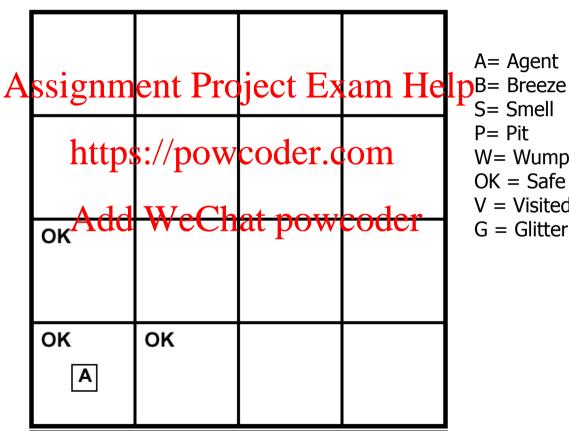
https://powcoder.com

Discrete?

Yes

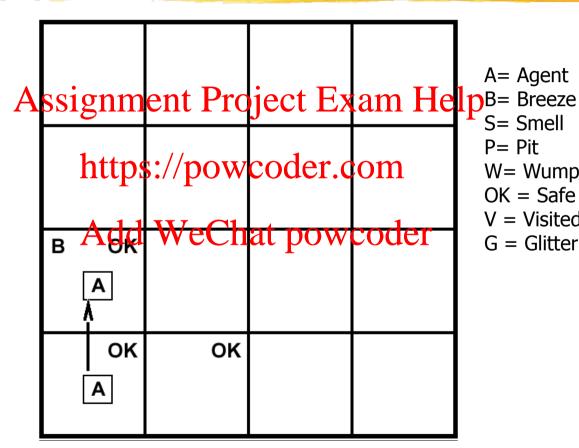
• Episodic?

Add WeChat powcoder (Yes) – because static.



A= Agent S= Smell P= Pit W= Wumpus OK = Safe

V = VisitedG = Glitter



A= Agent

S= Smell

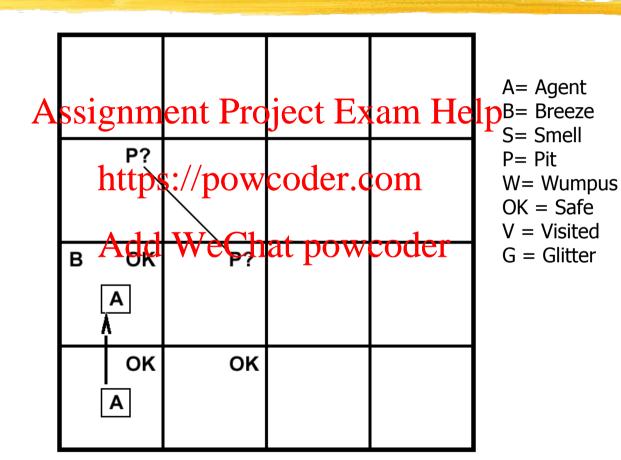
P= Pit

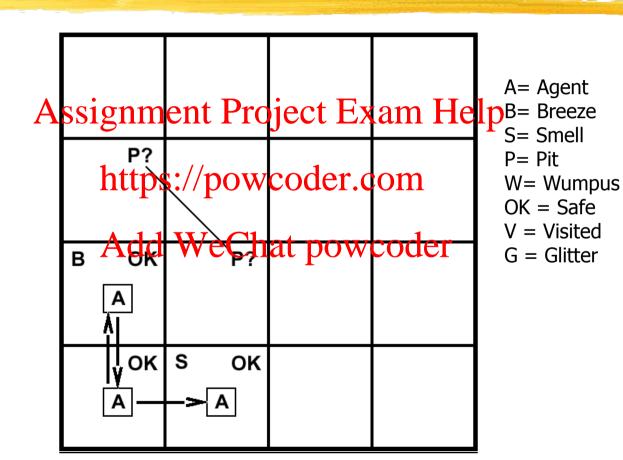
W= Wumpus

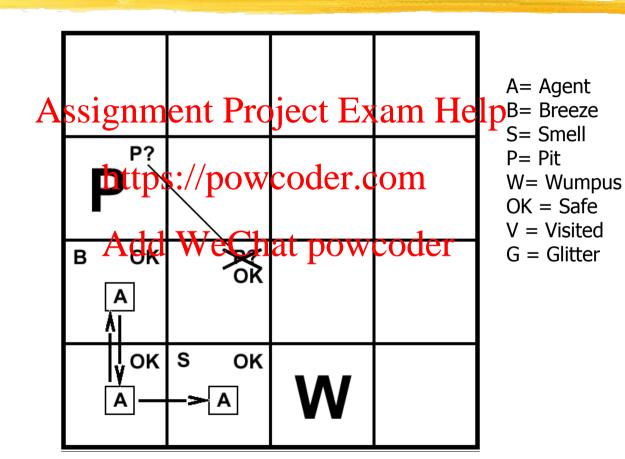
OK = Safe

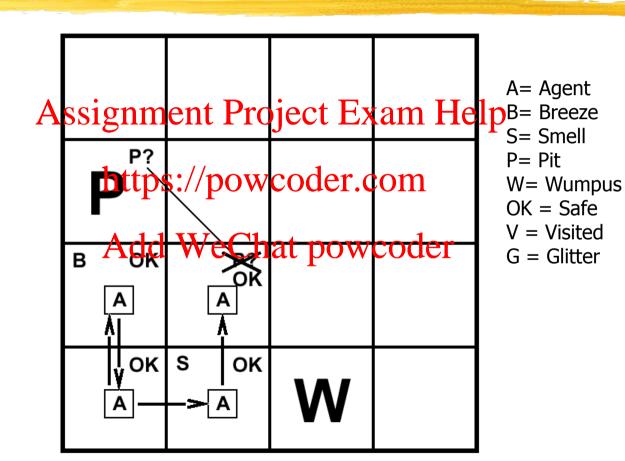
V = Visited

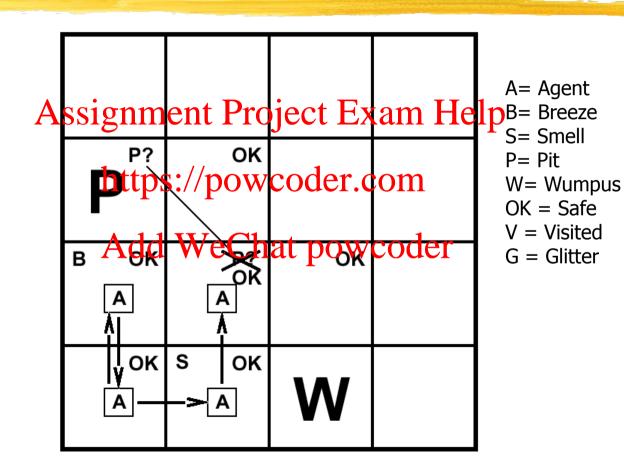
G = Glitter

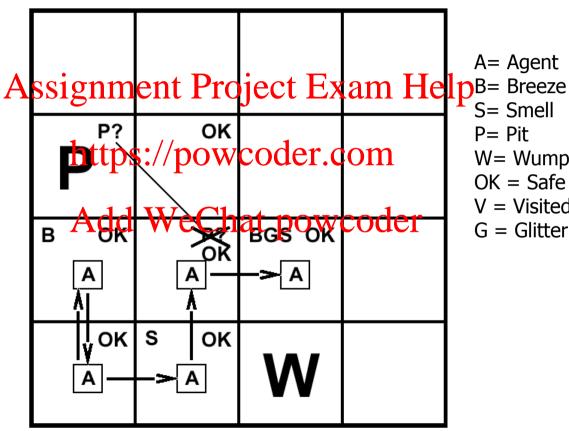












A= Agent

P= Pit

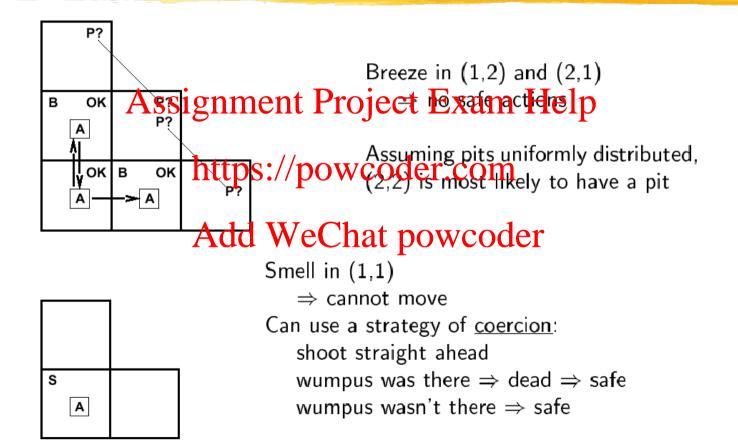
W= Wumpus

OK = Safe

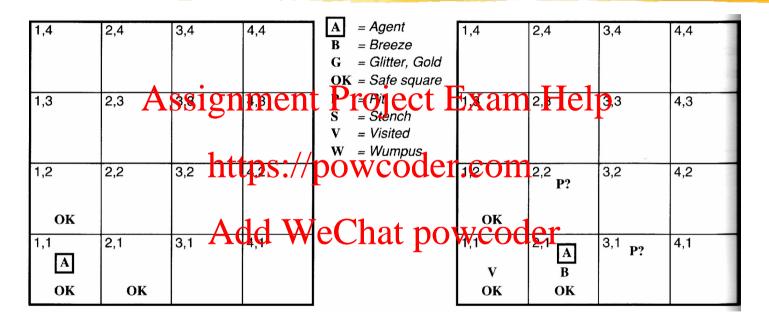
V = Visited

G = Glitter

Other tight spots



Another example solution



No perception \rightarrow 1,2 and 2,1 OK

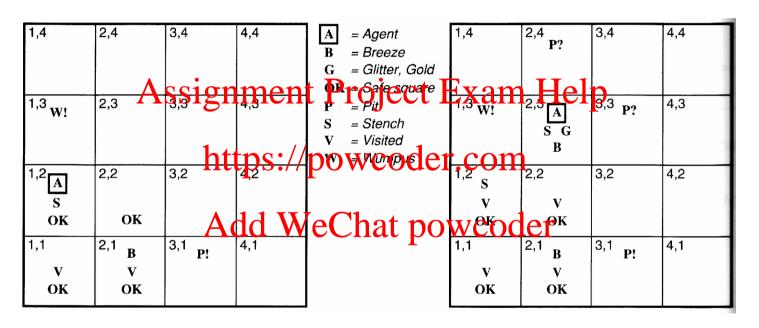
Move to 2,1

B in 2,1 \rightarrow 2,2 or 3,1 P?

 $1,1 \text{ V} \rightarrow \text{no P in } 1,1$

Move to 1,2 (only option)

Example solution



S and No S when in 2,1 \rightarrow 1,3 or 1,2 has W

 $1.2 \text{ OK} \rightarrow 1.3 \text{ W}$

No B in 1,2 \rightarrow 2,2 OK & 3,1 P

Logic in general

<u>Logics</u> are formal languages for representing information such that conclusions can be drawn

Syntax déliges itgnente nets Projecte Lexam Help

Semantics define the "meaning" of sentences; i.e., define traff pfs: semantics define traff pfs: semantics define the "meaning" of sentences;

E.g., the language of arithmetic

 $x+2 \ge y$ is a sentence; x2+y > 1 is not a sentence

 $x+2 \geq y$ is true iff the number x+2 is no less than the number y

 $x+2 \ge y$ is true in a world where x=7, y=1

 $x+2 \ge y$ is false in a world where x=0, y=6

Types of logic

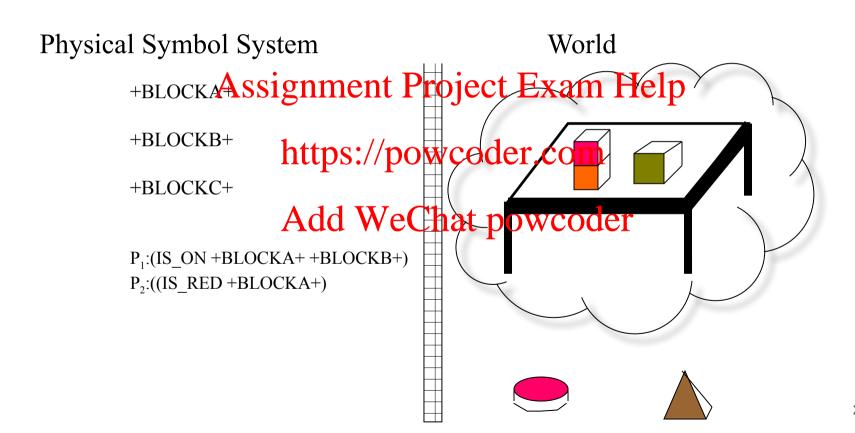
Logics are characterized by what they commit to as "primitives"

Ontologica Assignmenta Princett Exams Help beliefs?

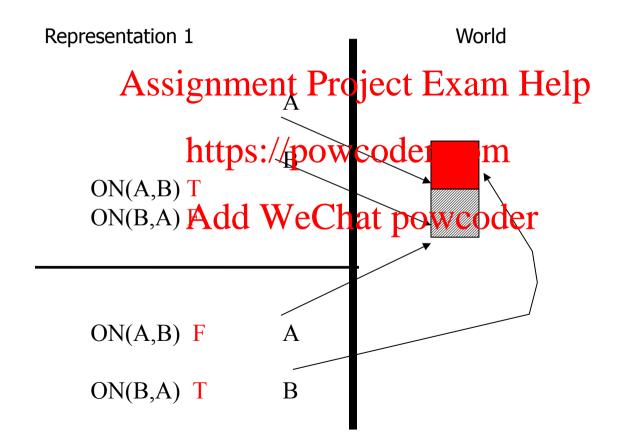
Epistemological commitment; what states of knowledge?

Language	Ontological Commitment	Epistemological Commitment
Propositional logic	facts	true/false/unknown
First-order logic	Addi Weathat po	W/ue/falg dilknown
Temporal logic	facts, objects, relations, times	true/false/unknown
Probability theory	facts	degree of belief 01
Fuzzy logic	degree of truth	degree of belief 01

The Semantic Wall



Truth depends on Interpretation



Entailment

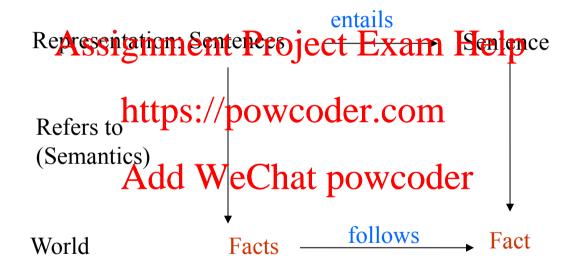
 $KB \models \alpha$

Knowle As singential the single of the sing

E.g., the KB containing "the Giants won" and "the Reds won" entails "Either Alde Giants What po Reds don'

Entailment is different than inference

Logic as a representation of the World



Models

Logicians typically think in terms of <u>models</u>, which are formally structured worlds with respect to which truth can be evaluated We say m is a <u>model</u> of a sentence α if α is true in m

 $M(\alpha)$ is the set of the set of

Inference

 $KB \vdash_i \alpha = \text{sentence } \alpha \text{ can be derived from } KB \text{ by procedure } i$

Soundness: i is sound if
where ignment i Paroject between Help

Completeness: i is complete if whenever $\frac{\text{Complete}}{\text{MHPS}} \dot{\alpha} / \frac{\text{DOWNCOLLETATEORS}}{\text{COLLETATEORS}} i$

Preview: we will define a logic (first-order logic) which is expressive enough to say almost onything of hater of WCOCATICH there exists a sound and complete inference procedure.

That is, the procedure will answer any question whose answer follows from what is known by the KB.

Basic symbols

Expressions only evaluate to either "true" or "false."

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- Р
- PVO
- P ^ O
- P => 0
- P ⇔ O

- "Phttps://powcoder.com
- "P is false"
- "either Pris true or or both" der "both P and Q are true"
- "if P is true, then O is true"

- negation
- disjunction
- conjunction
- implication
- "P and Q are either both true or both false" equivalence

Propositional logic: syntax

Propositional logic is the simplest logic

The proposition symbols P_1O_1 etclare sentence S_1 is a sentence S_1 and S_2 is a sentence, $S_1 \land S_2$ is a sentence of S_1 and S_2 is a sentence of

Propositional logic: semantics

Each model specifies true/false for each proposition symbol

Rules for evaluating truth with respect to a model m:

```
\neg S
 is true iff S is false S_1 \wedge S_2 is true iff S_1 \wedge S_2 is false S_2 \wedge S_2 is true iff S_1 \wedge S_2 is false S_2 \wedge S_2 is false iff S_1 \wedge S_2 is true and S_2 \wedge S_2 is false S_1 \leftrightarrow S_2 is true iff S_1 \Rightarrow S_2 is true and S_2 \Rightarrow S_1 is true
```

Truth tables

- Truth value: whether a statement is true or false.
- Truth table: complete list of truth values for a statement given all possible values of the individual atomic expressions.

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Example:

		ht	ttps://powcoder.com
	Р	Q	PVQ
•	Т	T 🔥	dd We Chat powcoder
	T	F A	du _T weChai powcoder
	F	Т	Т
	F	F	F

Truth tables for basic connectives

P Q	¬P	Assignment Project Exam Help
тт	F	F https://powcoder.com T
ΤF	F	T T F F F
FΤ	Т	F Add WeChat powcoder
FF	Т	T Add We Clifat Poweodel

Propositional logic: basic manipulation rules

```
• \neg(\neg A) = A
                                     Double negation
• ¬(A ^ B) = (¬A) Assignment Projected Excam Help
• \neg (A \lor B) = (\neg A) \land (\neg B)
                               Negated "or"
· A ^ (B V C) = (A ^ B) V https://powcoder.com
• A V (B ^ C) = (A V B) ^ (A V C) Distributivity of V on ^

    A => B = (¬A) V B
    ¬(A => B) = A ^ (¬B)

Add b we fitting powcoder using negated or

• A \Leftrightarrow B = (A => B) \land (B => A) by definition
• \neg (A \Leftrightarrow B) = (A \land (\neg B))V(B \land (\neg A)) using negated and & or
```

Propositional inference: enumeration method

Let
$$\alpha = A \vee B$$
 and $KB = (A \vee C) \wedge (B \vee \neg C)$

Is it the case that $KB \models \alpha$?

Check al possible models—reprust be true wherever He is thrue

A	B	C	$A \lor C$	$B \lor \neg C$	KB	α
False	False	False	.//20	wood	er.cor	2
False	False	Thue	•.//po	wcou	er.cor	
	True					
False	True	Artel	We(hat n	owco	der
True	False	False		Pilat p		acı
True	False	True				
True	True	False				
True	True	True				

Enumeration: Solution

	Assi	gnme	ent P	roiect	Exan	n Help
A	$ \tilde{B} $	C	$\overline{A} \lor \overline{C}$	$B \lor \neg C$	KB	α
1	1		False	1	False	False
False	False	nttps	:///po`	WGOE	er.oon	$\Omega False$
		False		True	False	True
False	True	True	True	True	True	True
True	False	Fatse	True	True	Yrue	
True	False	True	True	False	False	True
True	True	False	True	True	True	True
True	True	True	True	True	True	True

Propositional inference: normal forms

 $B \Rightarrow A \text{ and } (C \land D) \Rightarrow B$

Other approaches to inference use syntactic operations on sentences, often expressed in standardized forms

Conjunctive Normal Form (CNE project of sums of conjunction of disjunctions of literals regarded simple variables" E.g.,
$$(A \lor \neg B)$$
 in the clauses regarded simple variables or negated simple variables of disjunction of Architecture (DNF—universal) sum of products of simple variables or regarded simple variables or regarded simple variables or regarded simple variables" E.g., $(A \land B) \lor (A \land \neg C) \lor (A \land \neg D) \lor (\neg B \land \neg C) \lor (\neg B \land \neg D)$

Horn Form (restricted) conjunction of Horn clauses (clauses with ≤ 1 positive literal) E.g., $(A \lor \neg B) \land (B \lor \neg C \lor \neg D)$ Often written as set of implications:

Deriving expressions from functions

- Given a boolean function in truth table form, find a propositional logic expression for it that uses only V, ^ and ¬.
- Idea: We can easily do it by disjoining the "T" rows of the truth table.

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Example: XOR function

```
P Q RESULT https://powcoder.com
T T F
T F
F T Add We@hat powcoder
F F F
```

RESULT = (

Deriving expressions from functions

- Given a boolean function in truth table form, find a propositional logic expression for it that uses only V, ^ and ¬.
- Idea: We can easily do it by disjoining the "T" rows of the truth table.

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Example: XOR function

$$RESULT = (P \land (\neg Q)) \lor ((\neg P) \land Q)$$

A more formal approach

- To construct a logical expression in disjunctive normal form from a truth table:
- Build a "minterm" for each row of the table, where Assignment Project Exam Help
 - For each variable whose value is T in that row, include the wattable in/the water der.com
 - For each variable whose value is F in that row, include the negation of the variable in the minterm
 - Link variables in minterm by conjunctions

The expression consists of the disjunction of all minterms.

Example: adder with carry

Takes 3 variables in: x, y and ci (carry-in); yields 2 results: sum (s) and carry-out (co). To get you used to other notations, here we assume T = 1, F = 0, V = OR, A = AND, A = NOT.

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The logical expression for | co is:

```
(NOT x AND y AND ci) OR (x AND NOT y AND ci) OR (x AND y AND NOT ci) OR (x AND y AND ci)
```

The logical expression for s is:

```
(NOT x AND NOT y AND ci) OR (NOT x AND y AND NOT ci) OR (x AND NOT y AND NOT ci) OR (x AND y AND ci)
```

Tautologies

Logical expressions that are always true. Can be simplified out.

Examples:

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T T V A A V (¬A)

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 $\neg(A \land (\neg A))$ $A \Leftrightarrow A$

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 $((P \lor Q) \Leftrightarrow P) \lor (\neg P \land Q)$ $(P \Leftrightarrow Q) \Rightarrow (P \Rightarrow Q)$

Validity and satisfiability

A sentence is valid if it is true in all models

e.g.,
$$A \vee \neg A$$
, $A \Rightarrow A$, $(A \wedge (A \Rightarrow B)) \Rightarrow B$

Validity is connected to inference via the Deduction Theorem $KB \models \alpha$ if and only if $(KB \Rightarrow \alpha)$ is valid

A sentence is satisfiable for the same model e.g., $A \lor B$,

A sentence is Asstribitive Clisatupio we coder e.g., $A \wedge \neg A$

Satisfiability is connected to inference via the following: $KB \models \alpha$ if and only if $(KB \land \neg \alpha)$ is unsatisfiable i.e., prove α by reductio ad absurdum

Proof methods

Proof methods divide into (roughly) two kinds:

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truth table enumeration (sound and complete for propositional) heuristic searchtphiodepsixe (sound and complete for propositional) e.g., the GSAT algorithm (Ex. 6.15)

Application of inference rules Chat powcoder

Legitimate (sound) generation of new sentences from old

Proof = a sequence of inference rule applications

Can use inference rules as operators in a standard search alg.

Inference Rules

♦ Modus Ponens or Implication-Elimination: (From an implication and the premise of the implication, you can infer the conclusion.)

And-Elimination: (From a conjunction you can infer any of the conjuncts.)

$$\alpha_1 \wedge \alpha_2 \wedge \ldots \wedge \alpha_n$$

And-Introduction: (From Wise Content of South Card Card their conjunction.)

$$\frac{\alpha_1, \alpha_2, \ldots, \alpha_n}{\alpha_1 \wedge \alpha_2 \wedge \ldots \wedge \alpha_n}$$

♦ Or-Introduction: (From a sentence, you can infer its disjunction with anything else at all.)

$$\frac{\alpha_i}{\alpha_1 \vee \alpha_2 \vee \ldots \vee \alpha_n}$$

Inference Rules

Double-Negation Elimination: (From a doubly negated sentence, you can infer a positive sentence.)

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♦ Unit Resolution: From a disjunction if one of the disjuncts is false, then you can infer the other one is true.)

$$\frac{\alpha \vee \beta,}{\alpha}$$
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 \Diamond **Resolution**: (This is the most difficult. Because β cannot be both true and false, one of the other disjuncts must be true in one of the premises. Or equivalently, implication is transitive.)

$$\frac{\alpha \vee \beta, \quad \neg \beta \vee \gamma}{\alpha \vee \gamma} \quad \text{or equivalently} \quad \frac{\neg \alpha \Rightarrow \beta, \quad \beta \Rightarrow \gamma}{\neg \alpha \Rightarrow \gamma}$$

Show that the hypotheses:

- It is not sunny this afternoon and it is colder than yesterday.
- We will go swimming only if it is sunny.
- If we do not go swimming, then we will take a canoe trip.
 If we take Standard then we will take a canoe trip.

lead to the conclusion:

• We will be holdethe she some will be holdethe she saw.coder.com

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- Show that the hypotheses:
 - It is not sunny this afternoon and it is colder than yesterday. $\neg s \land c$
 - We will go swimming only if it is sunny. $w \to s$
 - If we do not go swimming, then we will take a canoe trip. $\neg w \to t$ If we take \$1.50 then we will take a canoe trip. $t \to t$

lead to the conclusion:

• We will be holdetto she pow coder.com

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Where:

- s: "it is sunny this afternoon"
- c: "it is colder than yesterday"
- w: "we will go swimming"
- t: "we will take a canoe trip.
- h: "we will be home by the sunset."

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- If we take ssignmenth in the length of the larger than the second of the larger than the la

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• We will be holdethe she pow coder.com

Step	Reason	
1. $\neg s \wedge c$	hypathelisWeChat po	wcoder

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Step	Reason
1. $\neg s \wedge c$	hypatdedisWeChat powcoder
2. <i>¬s</i>	simplification

Where:

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Step	Reason	
1. $\neg s \wedge c$	hypatdedisWeChat po	owcoder
2. <i>¬s</i>	simplification	,,,
3. $w \rightarrow s$	hypothesis	Where: s: "it is sunny this afternoon"
'		 c: "it is colder than yesterday" w: "we will go swimming"
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Step	Reason	
1. $\neg s \wedge c$	hy Atdedis We Chat po	wcoder
2. <i>¬s</i>	simplification	
3. $w \rightarrow s$	hypothesis	Where: s: "it is sunny this afternoon"
4 . ¬ <i>w</i>	modus tollens of 2 and 3	c: "it is colder than yesterday" w: "we will go swimming"
ı	1	t: "we will take a canoe trip. h: "we will be home by the sunset."

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lead to the conclusion:

• We will be holdethest pow.coder.com

Step	Reason	
1. $\neg s \wedge c$	hypatdelisWeChat po	wcoder
2. <i>¬s</i>	simplification	
3. $w \rightarrow s$	hypothesis	Where: s: "it is sunny this afternoon"
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lead to the conclusion:

• We will be holdethest for the will be a wil

C.	<u> </u>	1
Step	Reason	
1. $\neg s \wedge c$	hypatdelisWeChat po	wcoder
2. ¬ <i>s</i>	simplification	
3. $w \rightarrow s$	hypothesis	Where: s: "it is sunny this afternoon"
4 . ¬ <i>w</i>	modus tollens of 2 and 3	 c: "it is colder than yesterday" w: "we will go swimming"
$5. \ \neg w \rightarrow t$	hypothesis	t: "we will take a canoe trip.h: "we will be home by the sunset."
6. <i>t</i>	modus ponens of 4 and 5	the time set items of the contest.

Show that the hypotheses:

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- If we do not go swimming, then we will take a canoe trip. $\neg w \to t$ If we take a same trip. $\neg w \to t$

lead to the conclusion:

• We will be holdettoshe to the will be holder.com

Step	Reason	
1. $\neg s \wedge c$	hypatdelisWeChat po	wcoder
2. <i>¬s</i>	simplification	
3. $w \rightarrow s$	hypothesis	Where: s: "it is sunny this afternoon"
4 . ¬ <i>w</i>	modus tollens of 2 and 3	c: "it is colder than yesterday" w: "we will go swimming"
$ 5. \ \neg w \rightarrow t $	hypothesis	 t: "we will take a canoe trip. h: "we will be home by the sunset."
6. <i>t</i>	modus ponens of 4 and 5	
7. $t \rightarrow h$	hypothesis	

Show that the hypotheses:

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- We will go swimming only if it is sunny. $w \to s$
- If we do not go swimming, then we will take a canoe trip. $\neg w \rightarrow t$
- If we take ssignment her with the Example of $t \rightarrow h$

lead to the conclusion:

• We will be holdettoste/soow.coder.com

Step	Reason	
1. $\neg s \wedge c$	hypathelisWeChat posimplification	wcoder
2. <i>¬s</i>	simplification	
3. $w \rightarrow s$	hypothesis	Where: s: "it is sunny
4 . ¬w	modus tollens of 2 and 3	c: "it is colder w: "we will go
$5. \neg w \rightarrow t$	hypothesis	t: "we will take h: "we will be
6. t	modus ponens of 4 and 5	
7. $t \rightarrow h$	hypothesis	
8. <i>h</i>	modus ponens of 6 and 7	

here:

- "it is sunny this afternoon"
- "it is colder than yesterday"
- : "we will go swimming"
- "we will take a canoe trip.
- "we will be home by the sunset."

Wumpus world: example

STERRY SHORE PIT START

- Facts: Percepts inject (TELL) facts into the KB
 - [stench at 1,1 and 2,1] \rightarrow S1,1; S2,1
- Rules: if square has no stench then neither the square pradjacent squares contain the wumpus
 - R1: ¬S1,1 ⇒¬W1,1 htt\\s2/\p0\\v0coder.com
 - R2: $\neg S2,1 \Rightarrow \neg W1,1 \land \neg W2,1 \land \neg W2,2 \land \neg W3,1$
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Inference:

- KB contains ¬S1,1 then using Modus Ponens we infer ¬W1,1 ∧ ¬W1,2 ∧ ¬W2,1
- Using And-Elimination we get: ¬W1,1 ¬W1,2 ¬W2,1
- ...

Limitations of Propositional Logic

- 1. It is too weak, i.e., has very limited expressiveness:
- Each rule has to be represented for each situation:
 e.g., "don't go forward if the wumpus is in front of you" takes 64 rules

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- 2. It cannot keep track of changes:
- If one needs to track changetpss, perwheader the open before then we need a timed-version of each rule. To track 100 steps we'll then need 6400 rules for the previous example.
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Its hard to write and maintain such a huge rule-base Inference becomes intractable

Summary

Logical agents apply <u>inference</u> to a knowledge base to derive new information and make decisions

Basic consignament Project Exam Help – syntax: formal structure of sentences

- semantics: truth of sentences wrt models
 entailment: heressary truth of one sentence given another
- <u>inference</u>: deriving sentences from other sentences
- soundess: Acidation od hatopowieldentences
- completeness: derivations can produce all entailed sentences

Wumpus world requires the ability to represent partial and negated information, reason by cases, etc.

Propositional logic suffices for some of these tasks

Truth table method is sound and complete for propositional logic