#### Faculty of Information Technology

Monash University

#### FIT2014 Theory of Computation FINAL EXAM SAMPLE SOLUTIONS

## Assignment Project Exam Help

Instructions: https://powcoder.com

10 minutes reading time.

3 hours writing thedd WeChat powcoder

No books, calculators or devices.

Total marks on the exam = 120.

Answers in blue.

Comments in green.

#### Working Space

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Question 1 (3 marks)

You are choosing a main course at a restaurant, from a menu containing three items: bibim-bap, haggis and manakish.

Suppose we have propositions B, H and M, with the following meanings.

B: You choose bibimbap.

H: You choose haggis.

M: You choose manakish.

Use B, H and M to write a proposition, in Conjunctive Normal Form, that is True precisely when you choose either the bibimbap or both the other items.

Allowing either *or both* of these two options:

 $(B \vee H) \wedge (B \vee M)$ 

Allowing exactly one of these two options:

(B v HAssignment Project Exam Help

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Question 2 (5 marks)

Suppose you have predicates belongsToP and belongsToNP with the following meanings, where variable X represents an arbitrary language:

belongsToP(X): the language X belongs to the class P. belongsToNP(X): the language X belongs to the class NP.

(a) In the space below, write a statement in predicate logic with the meaning:

P is a proper subset of NP (i.e.,  $P \subseteq NP$  and  $P \neq NP$ ).

To do this, you may only use: the above two predicates; quantifiers; logical connectives; equality. (In particular, you may not use  $\subseteq$  or  $\subset$  or  $\neq$ , etc, and in fact they would not help.)

 $(\forall X : belongsToP(X) \Rightarrow belongsToNP(X)) \land (\exists X : belongsToNP(X) \land \neg belongsToP(X))$ 

Some other equivalent correct answers:

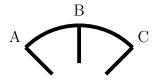
 $(\forall X \text{ belongsToP}(X) \Rightarrow \text{belongsToNP}(X)) \land (\neg \forall X \neg \text{belongsToNP}(X) \lor \text{belongsToP}(X)) \\ (\forall X \text{ belongsToP}(X) \Rightarrow \text{belongsToNP}(X) \land (\neg \forall X \text{ belongsToNP}(X) \rightarrow \text{belongsToP}(X)) \\ \textbf{ASSIGNMENT} \textbf{Project Exam} \textbf{Help}$ 

- (b) For the statement "P is a proper subset of NP", which one of the following holds? Circle
- $(A), \ (B), \ (C) \ or \ (D) \\ \textbf{https://powcoder.com}$ 
  - (A) The statement is True.
  - (B) The statement is False WeChat powcoder
  - (C) It is not known whether it's True or False, but it's generally believed to be True.
  - (D) It is not known whether it's True or False, but it's generally believed to be False.

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Question 3 (7 marks)

A knob is used to select one of three positions A, B, C, as shown in the following diagram.



The position of the knob is recorded every second for some nonzero period of time.

The knob can never be turned from A to C, or from C to A, without spending at least one second in position B. The initial position of the knob can be any of A, B, C.

Consider the language of all possible strings of knob positions recorded in this way.

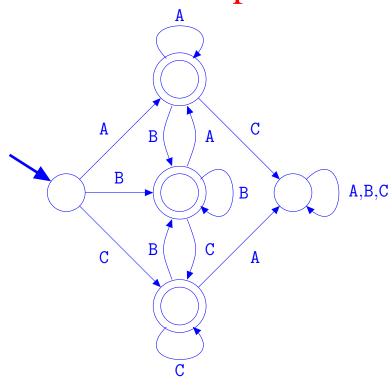
Give a regular expression for this language.

If empty string forbidden:

AA\*  $\cup$  ASSISTMENT Project Exam Help Many alternatives are possible, e.g.:  $((AA* \cup CC*)(B(A* \cup C*))*) \cup B(A* \cup C*)(B(A* \cup C*))*, \dots$ 

If empty string allowed:  $((A^* \cup C^*)B)^*(A^*)$  type://powcoder.com

Many alternatives are possible, e.g.:  $((A^*B)^*(C^*B)^*)^*(A^* \cup C^*), (A^* \cup C^*)(BA^* \cup BC^*)^*, \dots$  Give a Finite Auditon Witerian B. powcoder



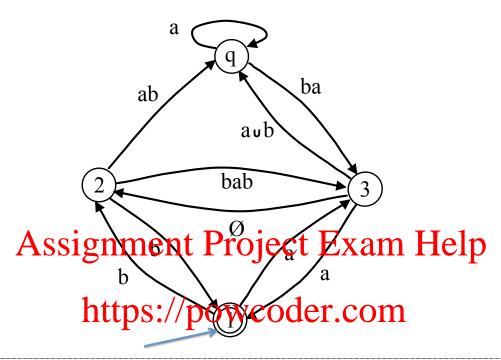
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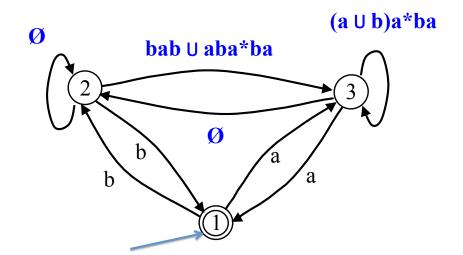
Question 4 (5 marks)

Consider the following Generalised Nondeterministic Finite Automaton (GNFA). Construct an equivalent GNFA with the top state, q, removed.

Show your answer by writing in the four missing transition labels, on the dotted lines, in the second diagram below.



YOUR ANSWER: Add WeChat powcoder

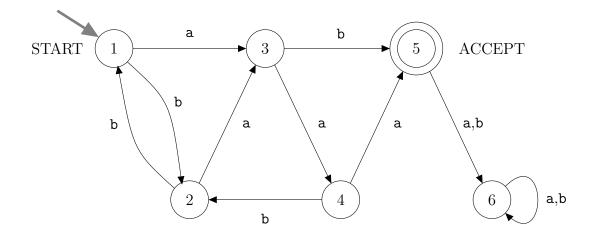


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Question 5
Consider the following Finite Automaton.

(6 marks)



- (a) Which is a granteent ship is certain a telephe ones that are accepted.
  - ab https://powcoder.com
- (b) Consider the standard above how as hip to with the last xyz such that, for all  $i \ge 0$ , the string  $xy^iz$  is also accepted by the FA.

Do this by drawing vertical lines between the parts of the string given on the next line:

This question is about the ideas behind the Pumping Lemma for Regular Languages.

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Question 6 (4 marks)

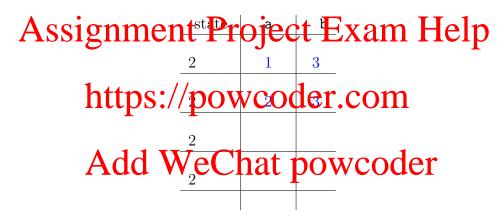
The following table describes part of a Finite Automaton with three states. The second row, for state 2, has not been filled in.

What could the state-2 row be, if you are given that the number of states of this FA is **not minimum**?

Write all possible state-2 rows in the second table below. Use as many rows as you need, one for each possible state-2 row. You may not need all the rows available.

state	e a	b
Start 1	2	3
2		
Final 3	1	2

YOUR ANSWER:



By allowing State 2 to be a Final State, some extra possibilities arise, shown in the third and fourth rows below.

state	a	b
2	1	3
2	2	3
Final 2	1	2
Final 2	1	3

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Question 7 (6 marks)

This question uses the following **Definitions** and **Facts**.

#### **Definitions:**

- If L is any language, the reversal of L is the set of all reversals of strings in L. In other words, you obtain the reversal of L by taking every string in L and writing it backwards. So, for example, the string abb becomes bba.
- If L is any language over the alphabet {a,b}, then the interchange of a and b forms a new language as follows: take every string in L, and replace every **a** by **b** and every **b** by a, simultaneously. So, for example, the string abb becomes baa.

#### Facts:

- The class of regular languages is closed under reversal.
- The class of regular languages is closed under interchange of a and b.
- The language AB := {  $a^n b^n : n \in \mathbb{N}$  } is not regular.

Your task: Assignment Project Exam Help Using these facts, and any other closure properties of regular languages you like, prove by contradiction that the language

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is not regular.

Assume, by way Acouradi Vine at hading by WEOGEIn } is regular. Then its reversal, namely  $\{b^n a^m : m \le n\}$ , is regular, since the class of regular languages is closed under reversal (using the first fact). Then we interchange a and b, giving the language  $\{a^nb^m: m \leq n\},$  which must be regular, since the class of regular languages is closed under interchange of a and b (using the second fact). Take the intersection of the language we started with, and this last language. The former's b-part is at least as long as its a-part, while the latter's a-part is at least as long as its b-part. Their intersection consists of strings where the two parts have the same size:

$$\{ \mathbf{a}^m \mathbf{b}^n \ : \ m \le n \ \} \cap \{ \mathbf{a}^n \mathbf{b}^m \ : \ m \le n \ \} = \{ \mathbf{a}^n \mathbf{b}^n \ : \ n \in \mathbb{N} \ \} = \mathrm{AB},$$

which must be regular, since the class of regular languages is closed under intersection (as discussed in lectures). But we know that AB is not regular (third fact). So we have a contradiction. So the original assumption, that the language given in the question is regular, is wrong. So that language is not regular.

Question 8 (3 marks)

Explain how to derive, for any Finite Automaton, a regular grammar for the language recognised by the FA.

For each state, create a new non-terminal symbol to represent that state. The initial state is represented by the start symbol S.

For each transition, create a production rule as follows. If the transition has label x and goes from state P to state Q, the production rule is  $P \to xQ$ . For each final state, create a production rule whose right-hand side is the empty string. So, for a final state represented by non-terminal symbol P, we create the rule  $P \to \varepsilon$ .

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Question 9 (12 marks)

Consider the following Context-Free Grammar:

$$S \rightarrow X$$
 (1)

$$X \rightarrow sXh$$
 (2)

$$X \to \varepsilon$$
 (3)

(a) Give a derivation for the string ssshhh.

Each step in your derivation must be labelled, on its right, by the number of the rule used.

$$S \Rightarrow X \qquad (1)$$

$$\Rightarrow sXh \qquad (2)$$

$$\Rightarrow ssXhh \qquad (2)$$

$$\Rightarrow sssXhhh \qquad (2)$$

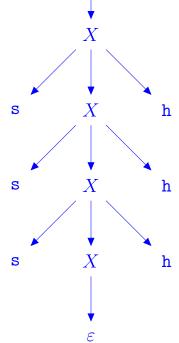
$$\Rightarrow ssshhh \qquad (3)$$

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(b) Give a parse tree for the same string, ssshhh.

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(c) Prove by induction on n, that for all  $n \ge 0$ , the string  $\mathbf{s}^n \mathbf{h}^n$  has a derivation in this grammar of n + 2 steps.

Inductive basis: when n=0, the string is empty. The empty string can be derived from this grammar in two steps:  $S \Rightarrow X \Rightarrow \varepsilon$ , which is n+2 steps with n=0. So the statement is true for n=0.

Now suppose  $n \ge 1$ , and assume that the statement is true for n-1, i.e., any string  $\mathbf{s}^{n-1}\mathbf{h}^{n-1}$  has a derivation of length (n-1)+2=n+1 steps. (This is our Inductive Hypothesis.)

This derivation looks like

$$\underbrace{S \Rightarrow X \Rightarrow \cdots \Rightarrow \mathbf{s}^{n-1}\mathbf{h}^{n-1}}_{n+1 \text{ steps}}.$$

Observe here that the first rule must be rule (1), since that is the only one that uses S.

Now consider the string  $s^n h^n$ . Since  $n \ge 1$ , we can write this as:

Assignment Project Exam Help Take the derivation  $S \Rightarrow X \Rightarrow \cdots \Rightarrow s^{n-1}h^{n-1}h$  given above, and do the following. First, omit S and the first production, at the very start. Then we have a derivation from X to  $s^{n-1}h^{n-1}$  in n steps. Then, for each string in this derivation, but an extra s at the start and an extra h at the energy of the partial derivation.

(The fact that it's still a valid derivation follows from the context-free property.)

We now prepend this derivation with the two-step derivation of sXh from S, which is  $S \Rightarrow X \Rightarrow sXh$ , to give the n + 2-step derivation of  $s^nh^n$ :

$$\underbrace{S \Rightarrow X \Rightarrow \mathtt{s}X\mathtt{h} \Rightarrow \cdots \Rightarrow \mathtt{s}\mathtt{s}^{n-1}\mathtt{h}^{n-1}\mathtt{h}}_{n+2 \text{ steps}} = \mathtt{s}^n\mathtt{h}^n.$$

This completes the inductive step.

The statement is therefore true for all  $n \geq 0$ , by the Principle of Mathematical Induction.

Question 10 (6 marks)

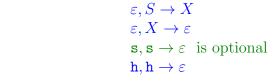
This question uses the same Context-Free Grammar as the previous question. Here it is again for convenience:

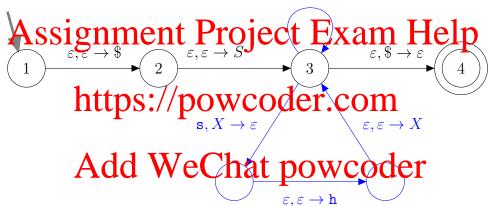
$$S \rightarrow X$$
 (1)

$$X \rightarrow sXh$$
 (2)

$$X \to \varepsilon$$
 (3)

Complete the following diagram to give a Pushdown Automaton for the language generated by this grammar.





Instead of the triangle below state 3, you could have a 2-cycle with two transitions  $s, X \to h$  then  $\varepsilon, \varepsilon \to X$ . (This effectively combines the first two arcs of the triangle.)

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Question 11 (5 marks)

State (without proof) the Pumping Lemma for Context-Free Languages, and briefly describe its main purpose.

Let L be a Context-Free Language with k non-terminal symbols in Chomsky Normal Form. For any string w of length  $\geq 2^{k-1}$ , there is a partition of w into five substrings, w = uvxyz, such that:

- at least one of v, y is nonempty,
- $|vxy| \leq 2^k$ , and
- for all  $i \geq 0$ , the string  $uv^i x y^i z$  belongs to L.

Its main purpose is to help show that certain languages are *not* context-free.

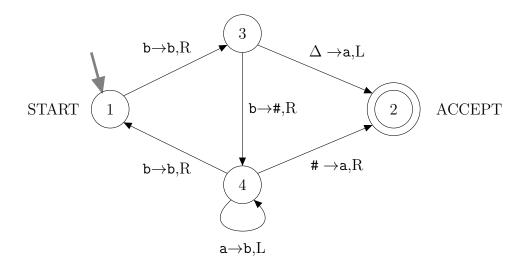
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Question 12 (6 marks)

Consider the following Turing machine.



Trace the stituting in the page. Trace the state of the page provided on the next page.

The lines show the configuration of the Turing machine at the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step. For each line, fill in the start of each step.

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To get you started, the first line has been filled in already.

At start of step	1:	State: _	1	Tape:	<u>b</u>	b	a	Δ		
At start of step	2:	State: _	3	Tape:	b	<u>b</u>	a	Δ		
At start of step	3:	State: _	4	Tape:	b	#	<u>a</u>	Δ		
At start of step	4:	State: _	4	Tape:	b	#	b	Δ		
At start of step	5:	State: _	2	Tape:	b	a	<u>b</u>	Δ		
At start of step	6:	State:	ent Pr	Tape:	4 E	W O		Ца	12	
AS	812	$\mathbf{IIIII}$	ent Pi	Ojec	ιC	Xa		ПС	TD.	
At start of step	7:	State:		Tape:				ПС	ıр	
At start of step	7: <b>h</b>	State:	://pov	Tape:				ПС	ıp	
	7: <b>h</b>	State:State:	://pov	Tape: <b>VCOC</b> Tape:	er.	CO	m		ф	
At start of step	7: <b>h</b>	State:State:		Tape: <b>VCOC</b> Tape:	er.	CO	m		ф	
At start of step  At start of step	7: h 8: 9:	State: ttps State: Add	://pov	Tape: VCOd Tape: hat p	er.	CO	m		ф	
At start of step  At start of step  At start of step	7: 8: 9:	State: State: Add State: State:	://pov	Tape: VCOd Tape: hat p Tape:	er.	CO	m		ip	

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Question 13 (4 marks)

For each of the following decision problems, indicate whether or not it is decidable.

You may assume that, when Turing machines are encoded as strings, this is done using the Code-Word Language (CWL).

Decision Problem your answer (tick **one** box in each row) Input: a Turing machine M. Question: Does there exist a string w that is accepted by Decidable Undecidable M in at most 7 steps? Input: a Turing machine M. Question: Does there exist a string w that is accepted by M? Decidable Undecidable Input: a string w. Question: Does there exist a Turing machine that accepts w? Decidable Undecidable Input: a Turing machine M, and a string w. Question: Is w the encoding, in CWL, of M? Decidable Undecidable https://powcoder.com

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Question 14 (10 marks)

The Venn diagram on the right shows several classes of languages. For each language (a)–(j) in the list below, indicate which classes it belongs to, and which it doesn't belong to, by placing its corresponding letter in the correct region of the diagram.

If a language does not belong to any of these classes, then place its letter above the top of the diagram.

You may assume that, when Turing machines are encoded as strings, this is done using the Code-Word Language (CWL), with input alphabet  $\{a,b\}$  and tape alphabet  $\{a,b,\#,\Delta\}$ .

- (a) The set of all palindromes of even length.
- (b) The set of all positive integers, in binary, whose number of bits is odd.
- (c) The set of all strings of correctly matched parentheses.
- (d) The set of all encodings of Turing machines that have at least three states.
- (e) The set of all encodings of Turing machines that have at most three states.
- (f) The set of all encodings of Turing machines that halt for some input.
- (g) The set of all groungs of ruring macrines that loop forever for all imputs.
- (h) The set of all satisfiable Boolean expressions.
- (i) The set of all stiff B Book Societ of the Normal Form in which every variable appears at most once (so each variable has only one literal).
- (j) The set of all nondecreasing strings of digits, i.e., strings over the digits 0,1,...,9 such that no digit is ever followed by Worldigit at to 1948 W.R.D.C.28 is not ok.)

 $\boldsymbol{g}$ 

recursively	enumerable (r.e.)
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	Regular
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Question 15 (6 marks)

If L is a language and s is a string, then  $L\Delta s$  denotes the language formed by removing s from L if it is there already, and adding s to L otherwise. In other words,

$$L\Delta s := \left\{ \begin{array}{l} L \setminus \{s\}, & \text{if } s \in L, \\ L \cup \{s\}, & \text{if } s \notin L. \end{array} \right.$$

Prove that L is decidable if and only if  $L\Delta s$  is decidable.

Suppose L is decidable. Let D be a decider for L. We use it to build the following decider for  $L\Delta s$ .

Input: string x. If x = s then return the opposite answer to D(s), else return D(x).

This works because the only difference between the two languages is for the string s, on which they disagree; but any other string is either in both the languages or in neither of them. Assignment Project Exam Help Therefore  $L\Delta s$  is decidable.

Exactly the same argument shows that, if  $L\Delta s$  is decidable, then so is L. (In fact, if we now make D a decider for the above decider feeting that the decidable if and only if  $L\Delta s$  is decidable.)

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Question 16 (5 marks)

Below is a proof that the Halting Problem is undecidable. But some parts are missing; these are shown as blank spaces, underlined.

Your task is to fill in the underlined spaces to complete the proof. In some cases, options are given in square brackets.

*Proof.* Assume that the Halting Problem is actually decidable.

Then the Halting Problem has a decider D.

Using D, we can construct a Turing machine E that does the following:

- 1. Input: encoding of a Turing machine M.
- 2. Run decider D to determine whether or not M halts when given itself as input.
- 3. **IF** the answer from D is **Yes**, then

loop forever

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Now consider what happens if E is given, as input, an encoding of *itself*.

If E halts on input E, then running E in line 2 gives the answer \_\_Yes\_ [Yes/No].

So, using statement  $\_3\_$  [3 or 4], we see that D actually  $\_\_$  loops forever  $\_\_$ 

On the other hand,

if E does not halt on input E, then running D in line 2 gives the answer  $\_No\_$  [Yes/No].

So, using statement  $\_4\_$  [3 or 4], we see that D actually  $\_\_\_$  stops  $\_\_\_$ .

This is a contradiction.

So the Halting Problem must be undecidable.

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Question 17 (6 marks)

Suppose you have an enumerator  $M_1$  for a language L and another enumerator  $M_2$  for its complement  $\overline{L}$ .

(a) Explain how to construct a decider for L that uses the enumerators  $M_1$  and  $M_2$ .

Decider for L:

Input: string x.

Run  $M_1$  and  $M_2$  in parallel. (This can be done by a loop which keeps track of the entire configuration of both machines and, in each iteration, simulates one step of each machine.) Whenever either machine outputs a string, we check if that string equals x.

If we see x as an output string from  $M_1$ , then we know  $x \in L$ , and we stop and output Yes. If we see x as an output string from  $M_2$ , then we know  $x \in \overline{L}$ , and we stop and output No.

We must eventually see x as an output string from exactly one of the two machines (not both, not neither), since one machine enumerates L and the other enumerates its complement, namely  $\overline{L}$ . (Every string belongs either to L or to  $\overline{L}$ .) So the above computation must always halt eventually.

Other algorithms are possible. E.g., for each  $i \in \mathbb{N}$ , simulate the first i steps of  $M_1$  and then the first i steps of  $M_2$ . If either produces x, then output Yes or No according as x was produced by  $M_1$  or  $M_2$ . If neither produces x, continue.

(b) What does this tell you about recursively enumerable (r.e.) languages whose complements

(b) What does this tell you about rechrsively enumerable (r.e.) languages whose complements are also recursively enumerable? (Only one short sentence is required here.)

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Question 18 (13 marks)

A **perfect matching** in a graph G is a subset X of the edge set of G that meets each vertex exactly once. In other words, no two edges in X share a vertex, and each vertex of G is incident with exactly one edge in X.

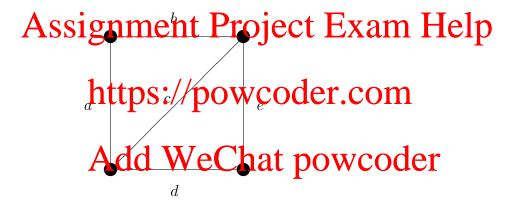
The PERFECT MATCHING decision problem is as follows.

#### PERFECT MATCHING

Input: Graph G.

Question: Does G have a perfect matching?

For example, in the following graph, the edge set  $\{a, e\}$  is a perfect matching. But  $\{a, b, e\}$  is not a perfect matching (since, for example, a and b share a vertex), and  $\{a\}$  is not a perfect matching (since some vertices are not incident with the edge in this set).



Let W be the above graph.

(a) Construct a Boolean expression  $E_W$  in Conjunctive Normal Form such that the satisfying truth assignments for  $E_W$  correspond to perfect matchings in the above graph W.

$$\begin{array}{l} (a \vee b) \wedge (\neg a \vee \neg b) \wedge \\ (a \vee c \vee d) \wedge (\neg a \vee \neg c) \wedge (\neg a \vee \neg d) \wedge (\neg c \vee \neg d) \wedge \\ (b \vee c \vee e) \wedge (\neg b \vee \neg c) \wedge (\neg b \vee \neg e) \wedge (\neg c \vee \neg e) \wedge \\ (d \vee e) \wedge (\neg d \vee \neg e). \end{array}$$

(b) Give a polynomial-time reduction from PERFECT MATCHING to SATISFIABILITY.

```
Input: graph G.

For each vertex v:

{

Let the edges incident with v be e_1, e_2, \ldots, e_d.

We need to create clauses which, when AND-ed together, say:

Exactly one of these edges is in the matching.

Create a new clause, e_1 \lor \cdots \lor e_d.

This says: at least one of e_1, \ldots, e_d is in the matching.

For each pair e_i, e_j of edges incident with v:

Create a new clause, \neg e_i \lor \neg e_j.

This says: at least one of e_i, e_j is not in the matching.

}

Combine all these clauses using \land, to create the conjunction of all of them.

Output the resulting expression.
```

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Question 19 (8 marks)

Prove that the GRAPH 4-COLOURABILITY problem is NP-complete, by reduction from GRAPH 3-COLOURABILITY. You may assume that GRAPH 3-COLOURABILITY is NP-complete.

#### Definitions:

For any positive integer k, a k-colouring in a graph G is an assignment of "colours" from the set  $\{1, 2, ..., k\}$  to the vertices of G such that (a) each vertex gets exactly one colour from the set, and (b) adjacent vertices get different colours.

#### **GRAPH 3-COLOURABILITY**

Input: Graph G.

Question: Does G have a 3-colouring?

## GRAPH 4-ACCEPTATION OF THE INPUT: Graph

Question: Does G have a 4-colouring?

GRAPH 4-COLOUPABILITY is in NP, since it has a polynomial-time verifier: the certificate is a 4-colouring, and this can be checked in polynomial time: for each edge, check that its endpoints are differently coloured, and check that the total number of colours used is at most 4.

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We now prove that GRAPH 3-COLOURABILITY is polynomial-time reducible to GRAPH 4-COLOURABILITY. The reduction works as follows.

Input: graph G.

Create a new vertex v, and join it to every vertex of G. Denote the resulting graph by G + v.
Output G + v.

This reduction is polynomial-time computable, since we just have to add one new vertex, and the number of new edges is at most the number of vertices in G.

If G is 3-colourable, then we can give a new colour to v, different to the three colours used on G. This gives a 4-colouring of G + v, since each new edge is properly coloured. (For each new edge, one of its endpoints is the new colour, which cannot appear on the other endpoint.) So we have shown that, if G is 3-colourable, then G + v is 4-colourable.

Now suppose G + v has a 4-colouring. We will show that G is 3-colourable. Consider v. Since it is adjacent to every vertex of G, the colour given to v (in the 4-colouring) cannot appear on any vertex of G. Once that colour is excluded, there are only three colours left, so we must have a 3-colouring of G. So we have shown that, if G + v is 4-colourable, then G is 3-colourable.

We therefore have: G is 3-colourable if and only if G+v is 4-colourable. This, together with its polynomial-time computability, shows that the reduction given above is a polynomial-time reduction from GRAPH 3-COLOURABILITY to GRAPH 4-COLOURABILITY. Since GRAPH 3-COLOURABILITY is known to be NP-complete, and since we showed at the start that GRAPH 4-COLOURABILITY is in NP, we conclude that GRAPH 4-COLOURABILITY is NP-complete.

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**END OF EXAMINATION**