Linear Programming and its Applications Assignment Project Exam Help Sanjay Dominik Jena

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MBA 8419 - Decision Making Technology

Overview of the presentation

Assignment of Problem optimization model Assignment of Problem optimization model

- General Form
- Applications and the use of EXCEL's Solver OM COGEL.COM
 - Finance
 - Operations management
- Haward he wheels solved? powcoder
 - Sensitivity analysis

Problem ⇒ optimization model



FIGURE – Taken from Anderson et. al. (2012), Chap.2

Problem ⇒ optimization model

General characteristics Project Exam Help

- Desire to max or min some quantity
 - Objective of the LP
- pttpstrestroowcoelens com
 - limit the values the decisions can take
 - implicitly limit the degree to which the objective can be

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- Satisfying customer demands
- Budgets
- Limited supplies
- Limited capacities (space, time, employees, etc.)
- etc.



Problem ⇒ optimization model

Assignment Project Exam Help variables

do they influence the state of solving the problem or in the system under study.

Characteristics:

- Varying impacts
- category
- Can made over multiple time periods

modifying the system (i.e., what criteria is used to evaluate the decisions).

Thracter tics:

decisions

enforced and that define admissible/feasible decisions.

Characteristics:

- Soft
- Non-negativity
- Integrity

FIGURE – Process to formulate a problem

General form

Decision variables

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max **or** min
$$z = c_1 x_1 + c_2 x_2 + ... + c_n x_n$$

Subject that ps://powcoder com $a_{11}x_1 powcoder com$

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 $a_{m1}x_1 + a_{m2}x_2 + \ldots + a_{mn}x_n \begin{pmatrix} \leq \\ \geq \\ - \end{pmatrix} b_m$

 $x_1, x_2, \ldots, x_n \ge 0$ and x_i is integer, $\forall j \in E$ and given $E \subseteq \{1, 2, \ldots, n\}$

Marketing

Types of problems

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Description: Choose between a set of available media options such as to maximize the promotional effort for a given set of products or services, targeted at specific segments of a given population

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Sales territory coverage

Description: Assign a set of salespersons to a set of existing or potential customers such as to priminize costs, or, ensure that the workload (or value and gold the value spersons are unifor typically but of the costs.)

Marketing research

Description : To understand the composition and nature of a targeted market, establish the number and types of studies that need to be performed to obtain the desired information while minimizing the costs

Assignment Project Exam Help

Context: Market Survey Inc. (MSI), specializes in evaluation of consumer reaction to new products, services, and advertising cantrages. A climating the consumer reaction to a recently marketed household product.

Stratedy coor-ty-toge (erspre) interviews with families (re., households) that either have, or don't have, children.

Contract: MSI must conduct 1 000 interviews

Marketing research (cont'd)

Assignidelines of Project Exam Help

- 2 Interview at least 400 households without children
- The total number of households interviewed during the evening must the arrival as great as the number of households interviewed during the day
- At least 40% of the interviews for households with children must be conducted during the evening
- At east 60% of the inter fiews for households without children must be conducted during the evening.

	interview cost				
Household	Day	Evening			
Children	20\$	25\$			
No Children	18\$	20\$			

TABLE - Unitary costs per interview_type

Marketing

Marketing research (cont'd)

Model: Project Exam Help DC = the number of daytime interviews of households with children,

EC = the number of evening interviews of households with children,

DNC = the number of daytime interviews of households without children,

ENC = the fumber of evening interviews of hor schools without thildren.

Objective Function: min 20DC + 25EC + 18DNC + 20ENC

Subject to :

$$\textit{DNC} + \textit{ENC} \geq 400$$

$$EC + ENC \ge DC + DNC$$

$$EC \geq 0, 4(DC + EC)$$

$$ENC \ge 0,6(DNC + ENC)$$

DC, EC, DNC, ENC > 0 and integer.

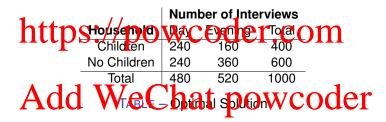
Marketing

Solving the problem using EXCEL

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- Each column is associated with a specific decision variable frach line is associated to a linear function (i.e. objective dan bonstrail its) WCOUCI. COM
- Use of the Solver function
 - Define the variable cells
 - A Petine the object ve dell and morniwcoder Add the different constraints
 - Make Unconstrained Variables Non-Negative
 - Select solving method :
 - GRG Nonlinear ⇒ for nonlinear optimization models
 - Simplex LP ⇒ exact method for linear optimization models
 - Evolutionary ⇒ heuristic method for optimization models

Assignment Project Exam Help Optimal solution to the MSI problem



Finance

Types of problems

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Description: Considering a set of available stocks and bonds, determine the amount of investment that a company (or particular) should make in each financial instrument with the objective of minimizing risk, https://powcoder.com

- Valuation of financial instruments
 - **Description**: In the context of trading within financial markets, determae what's the value of the largest that ye being traded der
- Financial planning

Description: Figure out what funding decisions should be made to best raise the necessary capital from the financial markets to finance an organization's activities



Finance

Description: Portfolio models are used to determine the % port the investment for the inv of the investment funds that should be made in each available assets.

Goal Det to Brown to Plant Gorde Elsk Gnormn.

Context: Hauck Investment Services designs annuities and long term investment plans for investors with a variety of risk tolerances Hauck Volate like to plevelop a control mobel that can be used to determine an optimal portfolio involving a mix of six mutual funds. A variety of measures can be used to indicate risk, but for portfolios of financial assets all are related to variability in return.

Finance

Designing Portfolio of Mutual Funds (cont'd)

Managers at hands Fina Pial Services think that the returns of past years can be used to represent the possibilities (i.e., scenarios) for the next year. Therefore, the following information will be used as planning scenarios for the next 12 months:

OALITE RETURN M Mutual Fund Year 2 Year 3 Year 4 Year 5 Year 1 Foreign Stock 10.06 13.12 13.47 45.42 -21.93 Intermediate Term Bond 17 64 3.25 7.51 -1.33 7.36 18.7 33.28 -23,26 artie-Gap Grown 32,36 20,61 -5,37Large-Cap Value 12,93 7,06 Small-Cap Growth 33.44 3.85 -9.02 19.40 58.68 Small-Cap Value 24.56 25.32 -6.70 5.43 17.31

TABLE – Mutual fund performance in 5 selected years

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Conservative Portfolio Project Exam He

to risk. Determine the proportion of the portfolio to invest in each of the six mutual funds so that the portfolio provides the best return possible with a

Decision variables://powcoder.com

FS = proportion of portfolio invested in the Foreign Stock mutual fund

IB = proportion of portfolio invested in the Intermediate-Term Bond fund

LG = proportion of portrolic mestern that Large Oat Crown in the Car

LV = proportion of portfolio invested in the Large-Cap Value fund

SG = proportion of portfolio invested in the Small-Cap Growth fund

SV = proportion of portfolio invested in the Small-Cap Value fund

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Assignment Project Exam Help FS + IB + LG + LV + SG + SV = 1

The pertfolio return over the next year will depend on which scenario will occur nttps://powcoder.com

$$R_1 = 10.06FS + 17.64IB + 32.41LG + 32.36LV + 33.44SG + 24.56SV$$

$$R_2 = 13,12FS + 3,25IB + 18,71LG + 20,61LV + 19,40SG + 25,32SV$$

$$R_4 = 45,42FS + 1,33IB + 41,46LG + 7,06LV + 58,68SG + 5,43SV$$

$$R_5 = -21,93FS + 7,36IB - 23,26LG - 5,37LV - 9,02SG + 17,31SV$$

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M = minimum return for the portfolio

To define M, we need to add the following minimum-return constaiteps://powcoder.com

 $R_1 > M$ Scenario 1 minimum return Scenario 2 minimum return Scenario 4 minimum return

Scenario 5 minimum return

Finance

on, provides the following five minimum-return constraints:

```
10,06FS + 17,64IB + 32,41LG + 32,36LV + 33,44SG + 24,56SV > M
                                                                        Scenario 1
13, 12F5 + 3, 25/B + 18/71LG + 20, 61/V + 19 10SG + 25, 32SV > M
13, 14SL 205/B + 33, 23/G+VX, 92/O GEL - GOS LM
                                                                        Scenario 2
                                                                        Scenario 3
 45,42FS+1,33IB+41,46LG+7,06LV+58,68SG+5,43SV>M
                                                                        Scenario 4
-21,93FS+7,36IB-23,26LG-5,37LV-9,02SG+17,31SV \ge M
                                                                        Scenario 5
```

Objective that powcoder Apply a maximin approach

max M

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s.t.

$$\begin{array}{c} 10.06FS + 17,64/B + 32,41LG + 32,36LV + 33,44SG + 24,56SV \geq M \\ 13,12FS + 3,25/BP + 18,712G + 20,01LV + 19,40SG + 25,32SV \geq M \\ 13,47FS + 7,51/B + 33,28LG + 12,93LV + 3,85SG - 6,70SV \geq M \\ 45,42F3 + 1,83/B + 1,46LG + 7,06LV + 58,68SG + 5,43SV \geq M \\ -21,93FS + 1,36/B - 23,26LG - 5,97LV - 9,02SG + 17,51SV \geq M \\ FS + 1B + LG + LV + SG + SV = 1 \\ FS,1B,LG,LV,SG,SV \geq 0 \end{array}$$

Finance

Moderate Risk Portfolio

Note ocentain clientstare willing joacstpt amoderate amount 1 p

Assumption

Clients in this category are willing to a cept some risks but do not want the annual neturn for the portfolio to drop below 2%

Therefore, M=2Ve Chahatin DO WG oder

- $R_2 > 2$ Scenario 2 minimum return
- Scenario 3 minimum return $R_3 > 2$
- $R_4 \geq 2$ Scenario 4 minimum return
- $R_5 > 2$ Scenario 5 minimum return



Finance

Objective Function

A different objective is needed here \Rightarrow Maximize the expected Project Exam Help

Assumption

Assuming that p_i, for i = 1,....5, are the probabilities of observing the Scenar WCOGET.COM

Then, $\overline{R} = p_1R_1 + p_2R_2 + p_3R_3 + p_4R_4 + p_5R_5$, defines an estimator of the expected value of the return

Therefored WeChat powcoder

$$\max p_1 R_1 + p_2 R_2 + p_3 R_3 + p_4 R_4 + p_5 R_5$$

If all scenarios are equiprobable, then

$$\max \frac{1}{5}R_1 + \frac{1}{5}R_2 + \frac{1}{5}R_3 + \frac{1}{5}R_4 + \frac{1}{5}R_5$$

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s.t.

Assignment Project Exam Help

10,06FS + 17,64/B + 32,41LG + 32,36LV + 33,44SG + 24,56SV = R_1 , 13,47FS + 7,51/B + 33,28LG + 12,93LV + 3,85SG - 6,70SV = R_3 , 45,42FS + 1,33/B + 41,46LG + 7,06LV + 58,68SG + 5,43SV = R_4 , A2 CLFS + V, 66 - 23, R/A V 5, V 5 - V 6 - V 7 - V 6 - V 7 - V 6 - V 8 - V 7 - V 8 - V 7 - V 8 - V 7 - V 8 - V 8 - V 9 - V 8 - V 9 -

FS + IB + LG + LV + SG + SV = 1,FS, IB, LG, LV, SG, SV > 0

Operations management

Types of problems

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Description: Planning and executing the various distribution operations of a company to serve its clients in a timely manner, while minimizing

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Description: Planning and scheduling the production operations of a company which may include the procurement processes, the management oviverby, establishing the wild the low the frough time, assigning ressources, etc., while minimizing the overall costs.

Logistics Network Design

Description: Design, manage and coordinate a logistics network such as to perform the necessary operations while minimizing costs.

Operations management

Production Scheduling

Description to the property of airplane engine manufacturer. The airplane engine manufacturer notifies the Bollinger sales office each quarter of its month requirements by comported to be a comported to be comported to be a comported to be a comported to be a comported three months. The requirements may vary considerably, depending on the type of engine the manufacturer is produdno.

> May Component April June 322A 3 000 5 000 1 000 802B 500 1 000 3 000

TABLE – Three-month demand schedule for BEC



Operations management

Production Scheduling (cont'd)

signmente, Kradenti Lexanno Help tion control department. The production control department then develops a three-month production plan for the components. The production manager will want to identify the following:

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- Inventory holding cost
- Change-in-production-level costs

Costs :/

- osts: Add Wechat power of the solution of the
- Inventory holding costs are 1.5% of the cost of the product (monthly)
- Cost associated with ↑ the production level for any month is 0.50\$ per unit increase
- Oost associated with ↓ the production level for any month is 0.20\$ per unit decrease

Operations management

Production Scheduling (cont'd)

A SSI SI Nachre dapatity Cultr Carlacty Xxioride Capatry Month (hours) (hours) (square feet) April 400 300 10 000 May 500 DOWCOGET. CO110 000 Jurettps 600 DOWCOGET. CO110 000

TABLE - Machine, Labor and Storage Capacities for BEC

campala	Machine (nours/unit)	halfs (Mt)	Storage Vsquale teaturit)
322A	0.10	0.05	2
802B	0.08	0.07	3

TABLE – Machine, Labor and Storage requirements for components 322A and 802B

Operations management

Assignment Project Exam Help

- x_{im} = production volume in units for product *i* in month *m*
- s_{im} = inventory, level for product i at the end of month m
- hat the self of the the local say during month m
- D_m = decrease in the total production level necessary desired and Chat powcoder where.

```
i=1 \Rightarrow 322 \text{A} and i=2 \Rightarrow 802 \text{B}

m=1 \Rightarrow \text{April}, m=2 \Rightarrow \text{May and } m=3 \Rightarrow \text{June}
```

Operations management

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min Total Cost = Total production cost + Inventory holding cost + Change-in-production-level costs

Inventory holding cost = $(0.015 \times 20)(s_{11} + s_{12} + s_{13}) + (0.015 \times 10)(s_{21} + s_{22} + s_{23})$

Change-in-production-level costs = $0.50(I_1 + I_2 + I_3) + 0.20(D_1 + D_2 + D_3)$

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min $20x_{11} + 20x_{12} + 20x_{13} + 10x_{21} + 10x_{22} + 10x_{23} + 0.30s_{11} + 0.30s_{12} + 0.30s_{13} + 0.15s_{21} + 0.15s_{22} + 0.15s_{23} + 0.50l_1 + 0.50l_2 + 0.50l_3 + 0.20D_1 + 0.20D_2 + 0.20D_3$

Operations management

Subject to:



Inventories at the beginning of the three-month scheduling period were 500 units for comporent 324 has 200 units (r) duy vien 80 B (the compary) duff ike to have 400 and 200 units, respectively for each product, in the inventory at the end of the planning.

Month 1:
$$500 + x_{11} - s_{11} = 1000$$

Month A 2001 + X1 - X1 - 100 Chat powcoder

Month 3:
$$s_{12} + x_{13} - s_{13} = 5000$$

$$s_{22} + x_{23} - s_{23} = 3000$$

Ending inventory:

$$s_{13} \ge 400$$

 $s_{23} > 200$

Operations management

Subject to (cont'd): Project Exam Help Machines:

```
Month 1: 0.10x_{11} + 0.08x_{21} \le 400
\begin{array}{l} \text{Month}_2: 0.10x_{12} + 0.08x_{22} \leq 500 \\ \text{Month}_3: 0.08x_{21} = 0.08x_{22} \leq 500 \\ \text{Month}_3: 0.08x_{22} = 0.08x_{22} \leq 0.08x_{22} \leq 0.08x_{2
    Labor:
```

Month 1: $0.05x_{11} + 0.07x_{21} < 300$

Storage:

Month 1 : $2s_{11} + 3s_{21} \le 10000$ Month 2 : $2s_{12} + 3s_{22} < 10000$ Month 3: $2s_{13} + 3s_{23} < 10000$

Operations management

Subject to (cont'd):

and 1 000 units of 802B

Production levels during the month of March were 1 500 units of 322A

Month 1: $(x_{11} + x_{21}) - 2500 = l_1 - D_1$ Note $\frac{1}{n}$ Note $\frac{1}{n}$ Note three possible cases:

- If $(x_{11} + x_{21}) 2500 > 0$ then $I_1 > 0$ and $D_1 = 0$
- $\begin{array}{c} \bullet & \text{if } A_{11} A_{21} A_{30} A_{$

Month 2:
$$(x_{12} + x_{22}) - (x_{11} + x_{21}) = I_2 - D_2$$

Month 3:
$$(x_{13} + x_{23}) - (x_{12} + x_{22}) = I_3 - D_3$$

Non-negativity and integrality:

 $x_{im}, s_{im}, I_m, D_m > 0$ and integer, $\forall i, m$.

Graphical solution

Consider the optimization problem (P):

ssignment Project Exam Help subject to

```
(C1) 10x_1 + 5x_2 < 200
```

$$(C2) 2x_1 + 3x_2 \le 60$$

 $(C2) 2x_1 + 3x_2 \le 60$ (C3) https://powcoder.com

(C4)
$$x_2 \le 14$$

(C5)
$$x_1, x_2 \ge 0$$

Dimeración de that powcoder

- 2 decision variables
- 4 technological constraints
- 2 non-negativity constraints

The feasible region of the model can be graphically represented

Graphical solution

Graphical representation of the feasible region

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Graphical solution

Solving the problem graphically

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z = 12000

Graphical solution

Extreme points and the optimal solution Assage in the project me Exam Help

- Interior : none of the constraints is satisfied as an equation
- Border: at least one constraint is satisfied as an equation
- Experience at the intersector of woodstraints in constraints are satisfied as equations)

Theorem

If an orthon to the found at an extreme point of the feasible region.

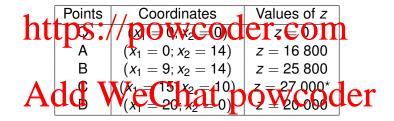
Note: This result means that if you are looking for the optimal solution to a linear program, one does not need to evaluate all feasible solution points.

Only the feasible solutions that occur at the extreme points of the feasible region need to be evaluated.



Graphical solution

Assignment Project Exam Help Evaluation of z at the extreme points



Sensitivity analysis

Sufficient Project Exam Help To what extent is the optimal solution obtained for a linear programming model

sensitive to modifications to the values of the parameters of the model?

When the value of the coefficient of a decision variable in the objective function changes does that neges sin en avach in the optimal soulidn obtained?

What is the impact of a change in the right-hand side value of a constraint with respect to the optimal solution found?

Types A and yels We Chat powcoder We will consider two types of modifications in the model:

- Modification of the value of a c_i (a coefficient in the objective function)
- Modification of the value of a b_i (the right-hand side of a constraint)

Sensitivity analysis

Modifying a ci SS1 Sent Ment bje Live funcije et Exam Help

$$\max z = c_1 x_1 + c_2 x_2$$

In the standard form, the previous function can be expressed as : $x_2 = \frac{-c_1}{c_2} x_1 + \frac{z}{c_2}$

Therefore ttps://powcoder.com

when code or the value of the slope or the objective function to the objective function function function function function to the objective function f

- When $c_1 \downarrow$ or $c_2 \uparrow \Rightarrow$ the value of the slope of the objective function \uparrow

Observation: When the modification brings the objective function to cross the feasible region of the more the we opin also diorical and the conclusion of the conclusion of

As long as:

slope of (C1)
$$\leq \frac{-c_1}{c_2} \leq$$
 slope of (C2)

The optimal solution remains the same



Sensitivity analysis

Modifying a b_i

The optimal solution extreme point $G(x_1 - 15)x_2 = 10)$ vis cat the intersection of points are solutions:

- A constraint is active at a given solution if the solution satisfies the constraint as an equation
- Apistan is nactive a Own dution the solution satisfier the constraint as an inequality

Therefore

- If $b_1 \uparrow 1$ (i.e., $200 \Rightarrow 201$) and b_2 remains the same Integral C Optimal solution becomes $C' = (x_1 = 15.15 \downarrow x_2 = 9.9)$ Value of the solution : $z' = 27\,030$ (i.e., $\Delta = +30$)
- If $b_2 \uparrow 1$ (i.e., $60 \rightarrow 61$) and b_1 remains the same Impact :

Optimal solution becomes $C'' = (x_1 = 14.75, x_2 = 10.5)$

Value of the solution : z'' = 27 350 (i.e., $\Delta = +350$)

Sensitivity analysis

Assignment Project Exam Help

Parameters	X1	X2				Model					
Values cj	1000	1200		,	,	Variables	X1 -	X2			
h1	11	10	•	//	'n	Value	$C \cap C$	er.c	nor	n	
111	1	be	b3 /	b#			COU		Z.W.S.	ш	L.H.S
Values bj	200	60	34	14	-	(C1)	10	5	200	<=	200
						(C2)	2	3	60	<=	60
						(C3)	1	0	15	<=	34
A	1	1	T	•	7	(04)	0	1	10	<	14
\mathbf{A}		\cap	1	Λ	/ C	'In	at r		CO		er_
	·U	u	1	/ 1	•		ui p		√al. Z	U.	
						cj	1000	1200	27000		

Sensitivity analysis

Answer Report

As summarizes the values of the pjective function, the decision variables, and the project Exam Help

Objective Cell (Max) Cell Name Original Value Final Value \$1\$11 cj yal, Z 27000 27000 TOWCODER.COM

Variable Cells

	Cell	Name	Original Value		Final Value	Integer
\$H\$3 Values X1		Values X1	15		15	Contin
4	\$1\$3	Value X2	10)	, 10	Contin

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Constraints

Cell	Name	Cell Value	Formula	Status	Slack
\$J\$5	(C1) R.H.S	200	\$J\$5<=\$L\$5	Binding	0
\$J\$6	(C2) R.H.S	60	\$J\$6<=\$L\$6	Binding	0
\$J\$7	(C3) R.H.S	15	\$J\$7<=\$L\$7	Not Binding	19
\$J\$8	(C4) R.H.S	10	\$J\$8<=\$L\$8	Not Binding	4

Sensitivity analysis

Assignment Project Exam Help



Variables: if reduced cost is 0, the current objective coefficient can be increased or decreased by the indicated "allowable" values without changing the current optimal solution.

Constraints: the RHS of the constraint can be increased or decreased by up to the indicated "allowable" amount, and for any unit increase/decrease the objective function will increase/decrease by the amount indicated as shadow price.