Each node of a BST can be filled with a height value, which is the height of the subtree rooted at that node. The height of a node is the maximum of the height of its children, plus one. The height of an empty tree is -1. Here's an example, with the value in parentheses indicating the height of the corresponding node:

 P(3)

```
2.  / \
3.  M(1) V(2)
4.  / \
5.  A(0) R(1) X(0)
6.  \
7.  S(0)
8.
```

Complete the following recursive method to fill each node of a BST with its height value. public class BSTNode<T extends

```
9. com Assignment Project Exam Help
```

```
10. BSTNode<T> left, right;

11. ihttp://powcoder.com

13. }
```

14. Add WeChat powcoder
15. // Recursively fills height values at all nodes

15. // Recursively fills height values at all node
 of a binary tree
16. public static <T extends Comparable>
17. void fillHeights(BSTNode<T> root) {
18. // COMPLETE THIS METHOD

19. ...

20. }
21.

## **SOLUTION**

```
// Recursively fills height values at all nodes
of a binary tree

22. public static <T extends Comparable>
23. void fillHeights(BSTNode root) {
   if (root == null) { return; }
   fillHeights(root.left);
```

```
26.
         fillHeights(root.right);
         root.height = -1;
27.
28.
         if (root.left != null) {
            root.height = root.left.height;
29.
30.
31.
         if (root.right != null) {
32.
            root.height = Math.max(root.height,
   root.right.height);
33.
34.
         root.height++;
35.
      }
36.
```

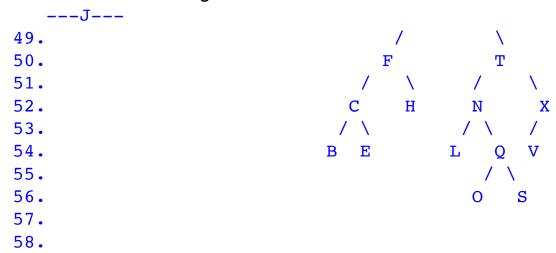
37. In the AVL tree shown below, the leaf "nodes" are actually subtrees whose lipitals are marked in partitlesses:

- 1. Mark the heights of the subtrees at every node in the tree. What is the height of the tree?
- 2. Mark the balance factor of each node.

## 46. SOLUTION

Heights/Balance factors A:h+1/right, C:h/equal, E:h+2/left, G:h+1/equal, B:h+2/left, F:h+3/left, D:h+4/right Height of the tree is h+4

## 48. Given the following AVL tree:



- 1. Determine the height of the subtree rooted at each node in the tree.
- Assignment Project Exam Help.

  2. Determine the balance factor of each hode in the lee.
- 3. Show the resulting AVL tree after each insertion in the following requence: (In all AVL trees you show, mark the balance factors next to the nodes.)
  - WeChat powcoder
  - Insert A

# 59. SOLUTION

1 and 2:

	Node	Height	Balance factor
60.			
61.	В	0	_
62.	E	0	_
63.	С	1	_
64.	F	2	/
65.	H	0	_
66.	0	0	_
67.	S	0	_
68.	Q	1	_
69.	L	0	_
70.	N	2	\

```
71.
72.
                                 1
73.
74.
75.
   3:
     1. After Inserting Z:
          ---J---
     2.
      3.
      4.
     5.
     6.
     7.
     <sup>8</sup>Assignment Project Exam Help \s
     10.
         https://powcoder.com
Only the balance factors of Z and X are changed; others
     11.
         remain the same
     Add WeChat powcoder

12. After inserting P (in the tree above):
         ---J---
      13.
      14.
      15.
                                                             N \
      16.
      17.
      18.
      19.
     20.
     21.
                                                               - P
     22.
     23.
               Insert P as the right child of O
               Set bf of P to '-'
```

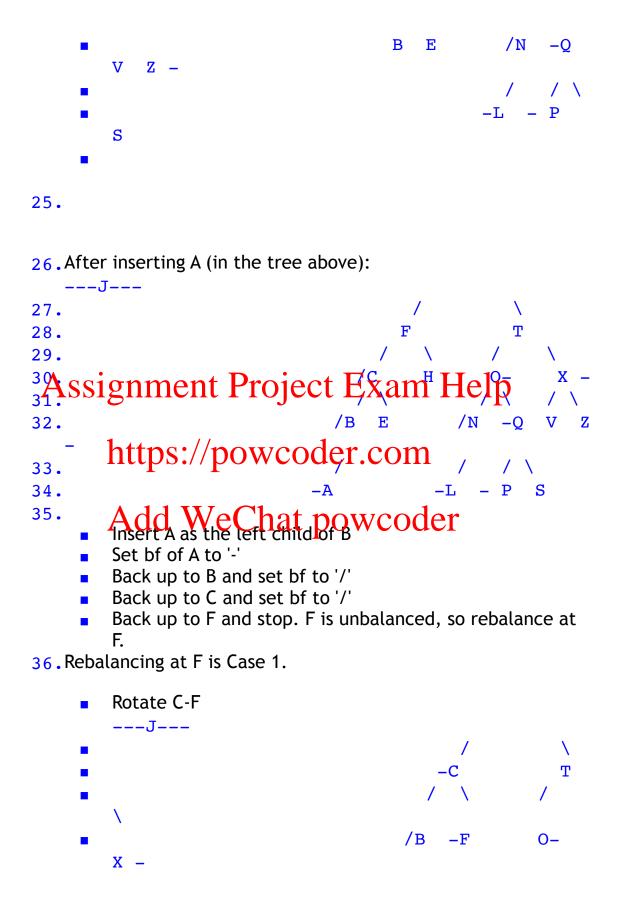
Back up to Q and set bf to '/' Back up to N and stop. N is unbalanced, so rebalance at N. 24. Rebalancing at N is Case 2. First, rotate O-Q ---J---Assignment Project Exam. Help. **Z** https://powcoder.com • Add WeChat powcoder P S Then, rotate O-N ---J---

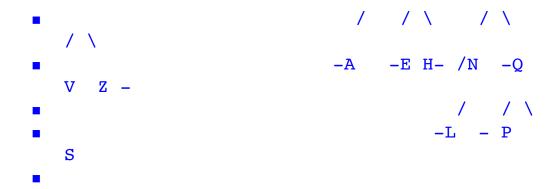
C

/ \

Back up to O and set bf '\'

X -





76.

- 77. Starting with an empty AVL tree, the following sequence of keys are inserted one at a time: 1, 2, 5, 3, 4
- Assume the the allows the insertion of auplicate keps. What is the total units of work performed to get to the final AVL tree, counting only key-to-key comparisons and pointer assignments? Assume each top parison is a William Read Bach pointer assignment is a unit of work. (Do not count pointer assignments used in traversing the tree Count only assignments used in changing the tree structure) We Chat powcoder

## SOLUTION

Since the tree allows duplicate keys, only one comparison is needed at every node to turn right (>) or left (not >, i.e. <=) when descending to insert.

- 1. To insert 1: 0 units 1
- 2.
- 3. To insert 2: 1 comparison + 1 pointer assignment = 2 units
- 1 4. \
- 5. 2
- 6.
- 7. To insert 5: 2 comparisons + 1 pointer assignment: 1
- 8.
- 9. 2

```
10.
11.
12.
   Then rotation at 2-1, with 3 pointer assignments:
   root=2, 2.left=1, 1.right=null
13.
   Total: 2+1+3 = 6 units, resulting in this tree:
                                                    2
14.
       1
15.
16.
17. To insert 3: 2 comparisons + 1 pointer assignment = 3 units:
   2
18.
19.
<sup>2</sup>Assignment Project Exam Help
21.
22.
https://powcoder.com
23. To insert 4: 3 comparisons + 1 pointer assignment:
                                                          2
24.
       <sup>1</sup>Add WeChat powcoder
25.
26.
27.
          3
28.
29.
30.
   Then a rotation at 4-3, with 3 pointer assignments:
31.
                 Pointer assignments: 5.left=4,
32.
   3.right=null, 4.left=3
33.
34.
35.
36.
       3
37.
   And a rotation at 4-5, with 3 pointer assignments:
                                                         2
38.
```

79. Grand total: 21 units of work

80. \* After an AVL tree insertion, when climbing back up toward the root, a node x is found to be unbalanced. Further, it is determined that x's balance factor is the same as that of the root, r of its taller subtree (Case 1). Complete the following rotateCase1 method to perform the required rotation to repeal ance the tree its red x. You may assume that x is not the root of the tree. public class AVLTreeNode<T extends Comparable<T>> { phttps://powcoder.com public AVLTreeNode<T> left, right; 81. 82. public char balanceFactor; 83. Add WeChat powcoder public AVLTreeNode<T> parent; 84. 85. public int height; 86. } 87. public static <T extends Comparable<T>> 88. 89. void rotateCase1(AVLTreeNode<T> x) { 90. // COMPLETE THIS METHOD 91. } 92. SOLUTION public static <T extends Comparable<T>> void rotateCase1(AVLTreeNode<T> x) { 93. // r is root of taller subtree of x 94. r = x.balanceFactor == '\' ? x.right : x.left; if (x.parent.left == x) { x.parent.left = r; } else { x.parent.right = r; }

```
97.
        r.parent = x.parent;
        if (x.balanceFactor == '\') { // rotate
98.
  counter-clockwise
99.
           AVLTreeNode temp = r.left;
100.
            r.left = x;
101.
            x.parent = r;
102.
            x.right = temp;
103.
            x.right.parent = x;
         } else { // rotate clockwise
104.
            AVLTreeNode temp = r.right;
105.
106.
            r.right = x;
107.
            x.parent = r;
            x.left = temp;
108.
109.
            x.left.parent = x;
110.
                       roject Exam Help
111.
112.
         x.balanceFactor =
113.
         r.balanceFactor = '-';
            ttps://poweoder.comr's is
114.
  unchanged
         Add WeChat powcoder
115.
116.
117.
118.
```