Higher-Order

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Class outline:

- Iteration example
- Designing functions
- Generalization
- Higher-Aderigumment Project Exam Help
- Lambda expressions
- Conditional expression powcoder.com

Iteration example

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Discovered by Virahanka in India, 600-800 AD, later rediscovered in Western mathematics and commonly known as Fibonacci numbers.

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0 1 1 2 3 5 8 13 21 34 ... https://powcoder.com

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$$0 + 1 = 1$$
 2 3 5 8 13 21 34 ...
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$$0 1 + 1 = 2 3 5 8 13 21 34 ...$$

Discovered by Virahanka in India, 600-800 AD, later rediscovered in Western mathematics and commonly known as Fibonacci numbers.

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0 1 1 + 2 = 3
$$5$$
 8 13 21 34 ...
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0 1 1 2 + 3 = 5 8 13 21 34 ... https://powcoder.com

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0 1 1 2 3 + 5 = 8 13 21 34 ... https://powcoder.com

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0 1 1 2 3 5 +8 = 13 21 34 ... https://powcoder.com

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0 1 1 2 3 5 8 + 13 = 21 34 ... https://powcoder.com

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Virahanka's question

How many poetic meters exist for a total duration?

S =short syllable, L =long syllable

Duration Ameigrament Project Exam Help		Total
1	S 1-44 1 1	1
2	ss, https://powcoder.com	2
3	sssAstd WeChat powcoder	3
4	SSSS, SSL, SLS, LSS, LL	5
5	SSSSS, SSSL, SSLS, SLSS, SLL, LLS, LSL, LSSS	8

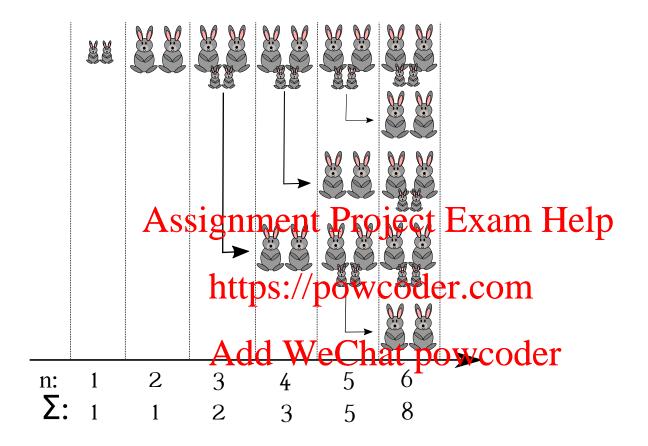
The So-called Fibonacci Numbers in Ancient and Medieval India

Fibonacci's question

How many pairs of rabbits can be bred after N months?

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Attribution: Fschwarzentruber, Wikipedia

Virahanka-Fibonacci number generation

```
VF 0 1 1 2 3 5 8 13 21 34 55 ...
N 0 1 2 3 4 5 6 7 8 9 10 ...
```

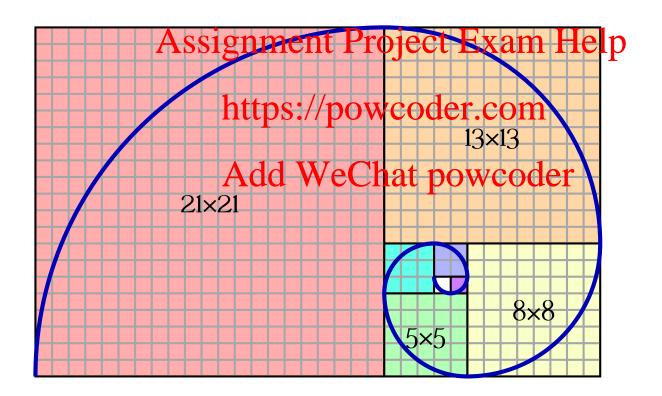
```
def vf_number(n):
    """ComputA SS renumenta Projectnum rather Welp
>>> vf_number(2)

1
>>> vf_number(6) https://powcoder.com
8
"""

prev = 0  # First Fibenary number to powcoder
curr = 1  # Second Project number to powcoder
k = 1
while k < n:
    (prev, curr) = (curr, prev + curr)
    k += 1
return curr</pre>
```

Golden spiral

The Golden spiral can be approximated by Virahanka-Fibonacci numbers.



Go bears!

The Golden spiral is found everywhere in nature...

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Designing Functions

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Describing Functions

```
def square(x):
     """Returns the square of X."""
     return x * x
          Assignment Project Exam Help
Aspect
A function's domainties the set of albiquits om is a number
it might possibly take as arguments.
A function's range is the set of putput
                                       Wcoder returns a non-negative real
values it might possibly return.
                                            number
A pure function's behavior is the
                                            square returns the
relationship it creates between input and
                                            square of x
output.
```

Designing a function

Give each function exactly one job, but make it apply to many related situations.

```
round (1.23) ssignment Project Exam Help round (1.23, 1) https://powcoder.com
```

Don't Repeat Yourself (DP(Y)) amplement deprocess just once, execute it many times.

Generalization

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Generalizing patterns with arguments

Geometric shapes have similar area formulas.



A non-generalized approach

```
from math import pi, sqrt
def area_square(r):
    returAssignment Project Exam Help
def area_circlettps://powcoder.com
return r * r * pi
def area_hexagon(r): WeChat powcoder
    return r * r * (3 * sqrt(3) / 2)
```

How can we generalize the common structure?

Generalized area function

```
def area(r, shape_constant):

"""Return the area of a shape from length measurement R."""

if r < 0:

return Assignment Project Exam Help

def area_square(r):
return area(r, 1) https://powcoder.com

def area_circle(r):
return area(r, pi) Add WeChat powcoder

def area_hexagon(r):
return area(r, 3 * sqrt(3) / 2)
```

Higher-order functions

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What are higher-order functions?

A function that either:

- Takes another function as an argument
- Returns a function as its result Assignment Project Exam Help

All other functions are considered first-order functions.

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Generalizing over computational processes

$$\sum_{k=1}^{5} k = 1 + 2 + 3 + 4 + 5 = 15$$
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$$\sum_{k=1}^{5} k^{3} = \frac{1^{3} + 2^{3} + 3^{3} + 4^{3} + 5^{3}}{\text{https://powcoder.com}} = 225$$

$$\sum_{k=1}^{5} \frac{\text{Add WeChat powcoder}}{(4k-3)\cdot(4k-1)} = \frac{8}{3} + \frac{8}{35} + \frac{8}{99} + \frac{8}{195} + \frac{8}{323}$$

The common structure among functions may be a computational process, not just a number.

Functions as arguments

```
def cube(k):
   return k ** 3
def summation(n, term):
    """Sum Assignments Project Exam Help
   >>> summation(5, cube)
   225
                https://powcoder.com
    0.00
   total = 0
   _{\text{while }k \leq n}^{\text{k = 1}}. Add WeChat powcoder
       total = total + term(k)
       k = k + 1
   return total
```

Functions as return values

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Locally defined functions

Functions defined within other function bodies are bound to names in a local frame.

```
make_adder(1)( 2 )
Assignment ProjecttExam Helpand

https://powcoder.com
```

```
make_adder(1)( 2

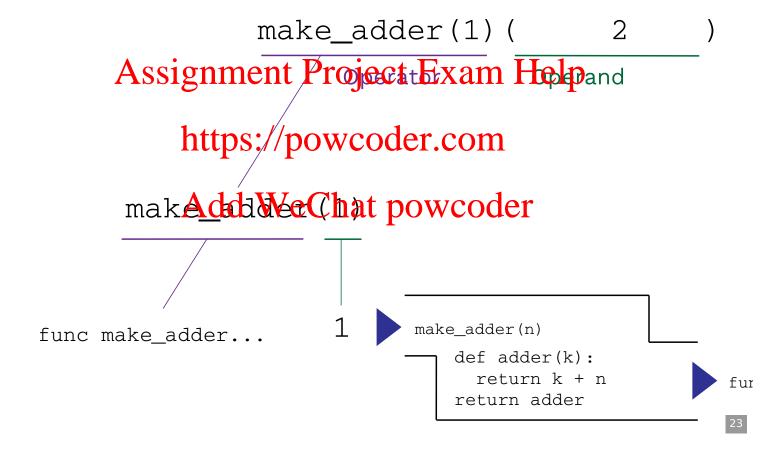
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https://powcoder.com

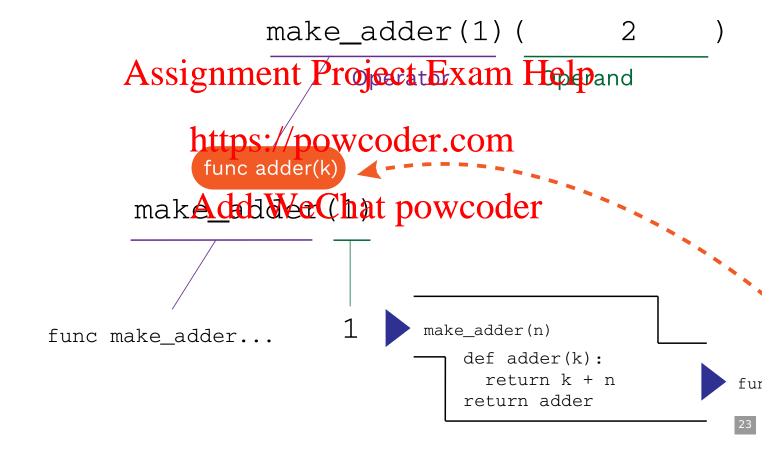
make_dddiweChat powcoder
```

```
make_adder(1)(
    Assignment Project Exam Helpand
         https://powcoder.com
     mak Add We Chat powcoder
func make adder ...
```

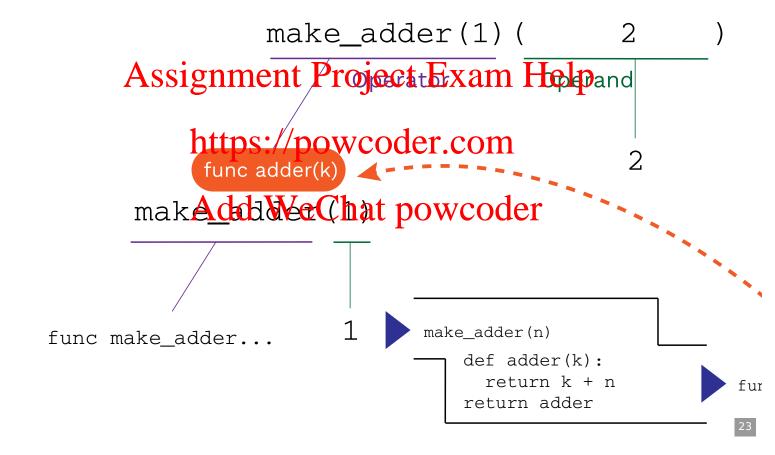
```
make_adder(1)(
    Assignment Project Exam Helpand
         https://powcoder.com
     mak Add We Chat powcoder
func make adder ...
```



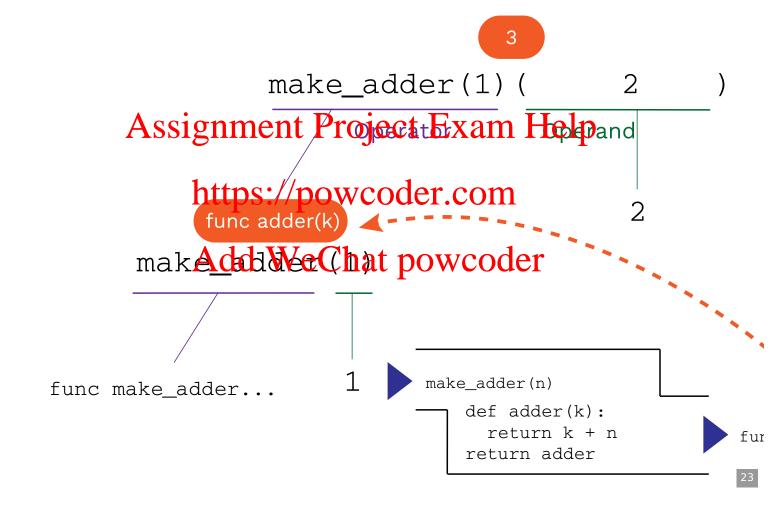
Call expressions as operator expressions



Call expressions as operator expressions



Call expressions as operator expressions



Lambda expressions

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Lambda syntax

A **lambda expression** is a simple function definition that evaluates to a function.

The syntax: Assignment Project Exam Help

lambda <parameters>: <expression>

A function that takes in parameters and returns the result of expression. Add WeChat powcoder

Lambda syntax

A **lambda expression** is a simple function definition that evaluates to a function.

The syntax: Assignment Project Exam Help

```
lambda <parameters>: <expression>
```

A function that takes in parameters and returns the result of expression.

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A lambda version of the square function:

```
square = lambda x: x * x
```

A function that takes in parameter x and returns the result of x * x.

Lambda syntax tips

A lambda expression does **not** contain return statements or any statements at all.

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```
square = lambda x: return x * x
```

Correct:

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square = lambda Add WeChat powcoder

Def statements vs. Lambda expressions

```
def square(x):
    return x * x
square = lambda x: x * x
```

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Both create a function with the same domain, range, and behavior.

Both bind that function to the name square.

Only the def statement westheat powcoder function an intrinsic name, which shows up in environment diagrams but doesn't affect execution (unless the function is printed).

Lambda as argument

It's convenient to use a lambda expression when you are passing in a simple function as an argument to another function.

Instead of... Assignment Project Exam Help

```
def cube(k): https://powcoder.com
return k ** 3

summation(5, cubeAdd WeChat powcoder
```

We can use a lambda:

```
summation(5, lambda k: k ** 3)
```

Conditional expressions

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Conditional expressions

A conditional expression has the form:

Evaluation Assignment Project Exam Help

- Evaluate the spredicate expression.
 If it's a true value, the value of the whole expression is the value of the <consequent>.
 Otherwise, the value of the whole expression is the
- value of the <alternative>.

Lambdas with conditionals

This is invalid syntax:

```
lambda x: if x > 0: x else: 0

Conditional spendicult Project Exam Help

lambda x: x ifhttps://powcoder.com
```

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