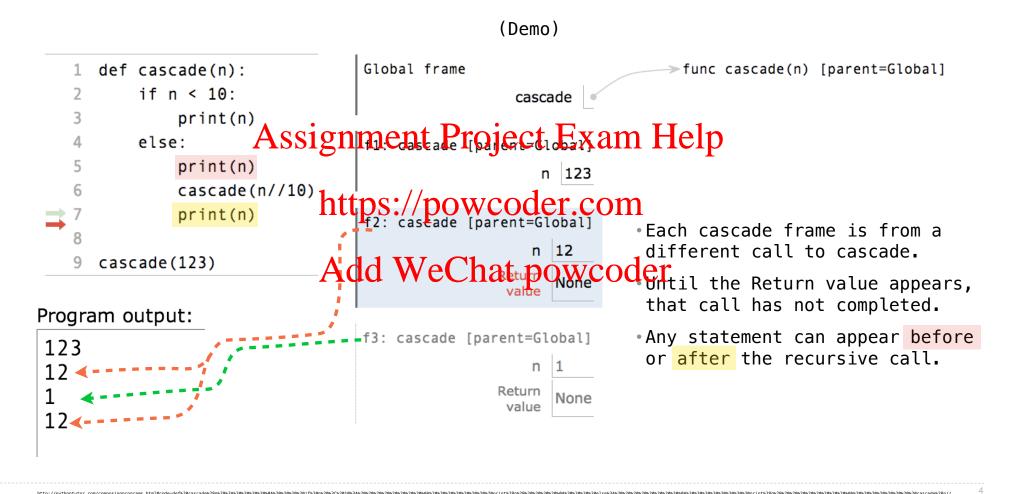
**Tree Recursion** 

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### The Cascade Function



#### Two Definitions of Cascade

(Demo)

```
def cascade(n):
    if n < Assignment Project Examinate);
    else:
        print(n)
        cascade(n)/ttps://powcoder.com
        print(n)
        cascade(n)/ttps://powcoder.com
        print(n)</pre>
```

- If two implementations are equally clear, then shorter is usually better
- In this case, the longer implementation is more clear (at least to me)
- When learning to write recursive functions, put the base cases first
- Both are recursive functions, even though only the first has typical structure

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### **Inverse Cascade**

Write a function that prints an inverse cascade:

- /

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### **Tree Recursion**

Tree—shaped processes arise whenever executing the body of a recursive function makes more than one recursive call

```
n: Assignment Project Exam Help

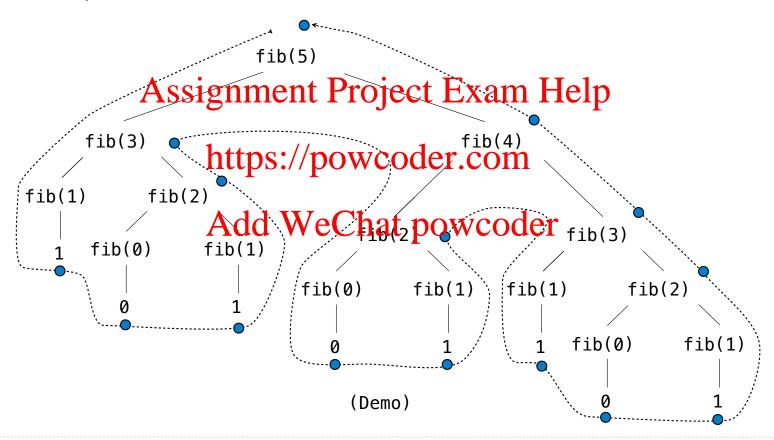
fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 9,227,465

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def fib(n):
    if n == 0:
        return 0
    elif n == 1:
        return 1
    else:
        return fib(n-2) + fib(n-1)
```

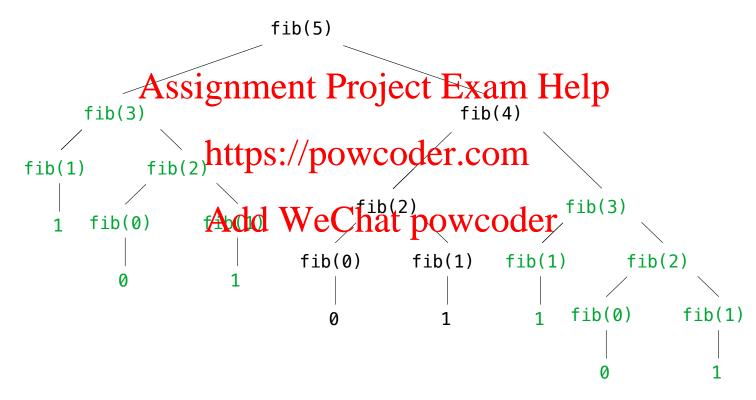
### A Tree-Recursive Process

The computational process of fib evolves into a tree structure



### Repetition in Tree-Recursive Computation

This process is highly repetitive; fib is called on the same argument multiple times



(We will speed up this computation dramatically in a few weeks by remembering results)

Example: Counting Partitions

### **Counting Partitions**

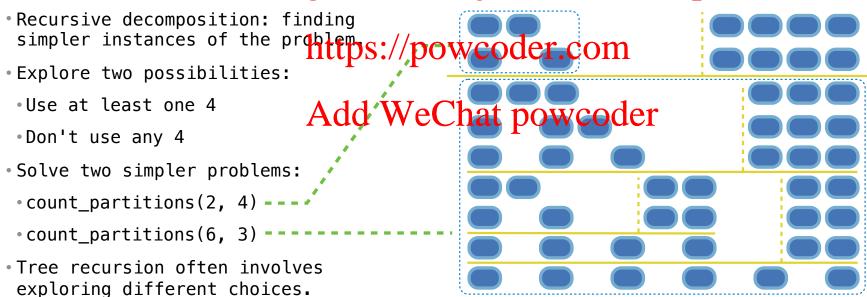
The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

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### **Counting Partitions**

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in non-decreasing order.

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### **Counting Partitions**

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

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```
def count_partitions(n, m):
Recursive decomposition: finding
 simpler instances of the problems://powcoderecom
Explore two possibilities:
                                             elif n < 0:
                                                 return 0
 •Use at least one 4
                           Add WeChatepow€oder
Don't use any 4
                                                 return 0
• Solve two simpler problems:
                                             else:
                                           \rightarrow with m = count partitions(n-m, m)
 • count partitions(2, 4) --
                                                 without m = count partitions(n, m-1)
 count partitions(6, 3) ----
                                                  return with m + without m

    Tree recursion often involves

 exploring different choices.
                                          (Demo)
```

 $py thontutor.com/composing programs. html#code=def%20count_partitions \com/sologos \composing \co$