

Assignment Project Exam Help

Trees

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[Announcements
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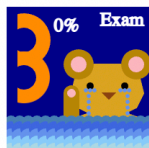
Hog Contest Winners

Strategy contest: <https://hog-contest.cs61a.org/>

3-way tie for first: Nishant Bhakar, Toby Worledge, Asrith Devalaraju & Aayush Gupta

After bug fix: (1) Nishant Bhakar (2) Toby Worledge (3) liayin Lin & Roger Yu

Dice contest: <https://dice.cs61a.org/>



(1) Bella Lee & Dayeon Jang

(2) Michelle Wu & Kevin Xu

(3) Taylor Moore

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Box-and-Pointer Notation
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The Closure Property of Data Types

- A method for combining data values satisfies the *closure property* if:

The result of combination can itself be combined using the same method

- Closure is powerful because it permits us to create hierarchical structures
- Hierarchical structures are made up of parts, which themselves are made up of parts, and so on

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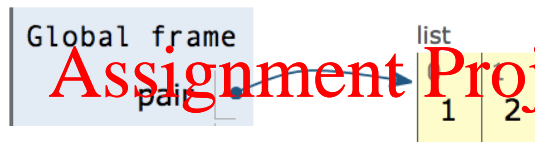
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Lists can contain lists as elements (in addition to anything else)

Box-and-Pointer Notation in Environment Diagrams

Lists are represented as a row of index-labeled adjacent boxes, one per element

Each box either contains a primitive value or points to a compound value



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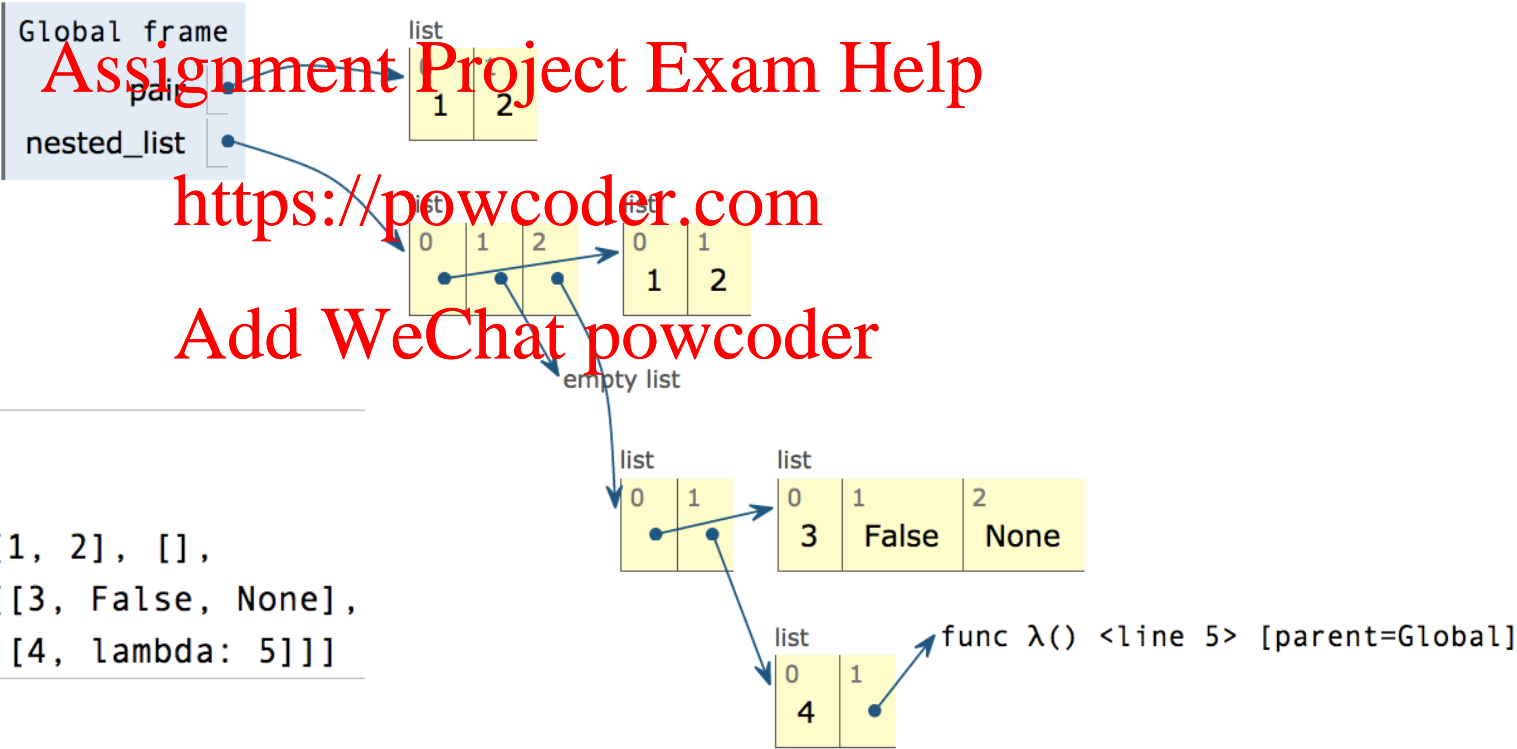
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```
pair = [1, 2]
```

Box-and-Pointer Notation in Environment Diagrams

Lists are represented as a row of index-labeled adjacent boxes, one per element
Each box either contains a primitive value or points to a compound value



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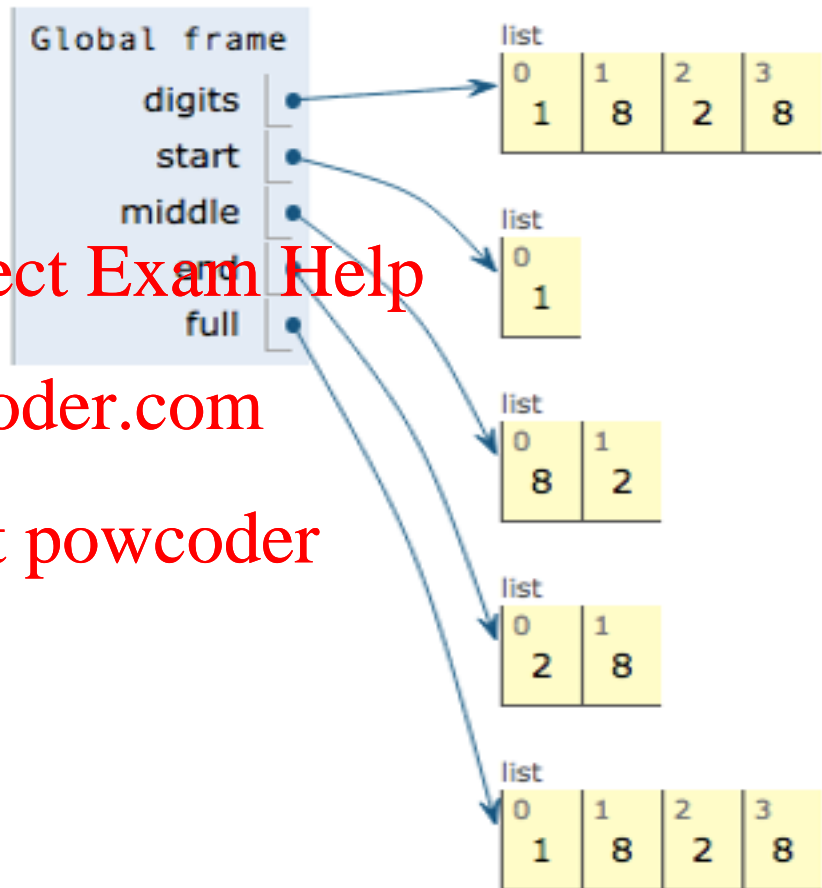
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(Demo)

Slicing Creates New Values

```
1 digits = [1, 8, 2, 8]
2 start = digits[:1]
3 middle = digits[1:3]
4 end = digits[2:]
5 full = digits[:]
```



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Processing Container Values
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Sequence Aggregation

Several built-in functions take iterable arguments and aggregate them into a value

- **sum**(iterable[, start]) -> value

Return the sum of a 'start' value (default: 0) plus an iterable of numbers.

- **max**(iterable[, key=func]) -> value
max(a, b, c, ...[, key=func]) -> value

With a single iterable argument, return its largest item.

With two or more arguments, return the largest argument.

- **all**(iterable) -> bool

Return True if bool(x) is True for all values x in the iterable.

If the iterable is empty, return True.

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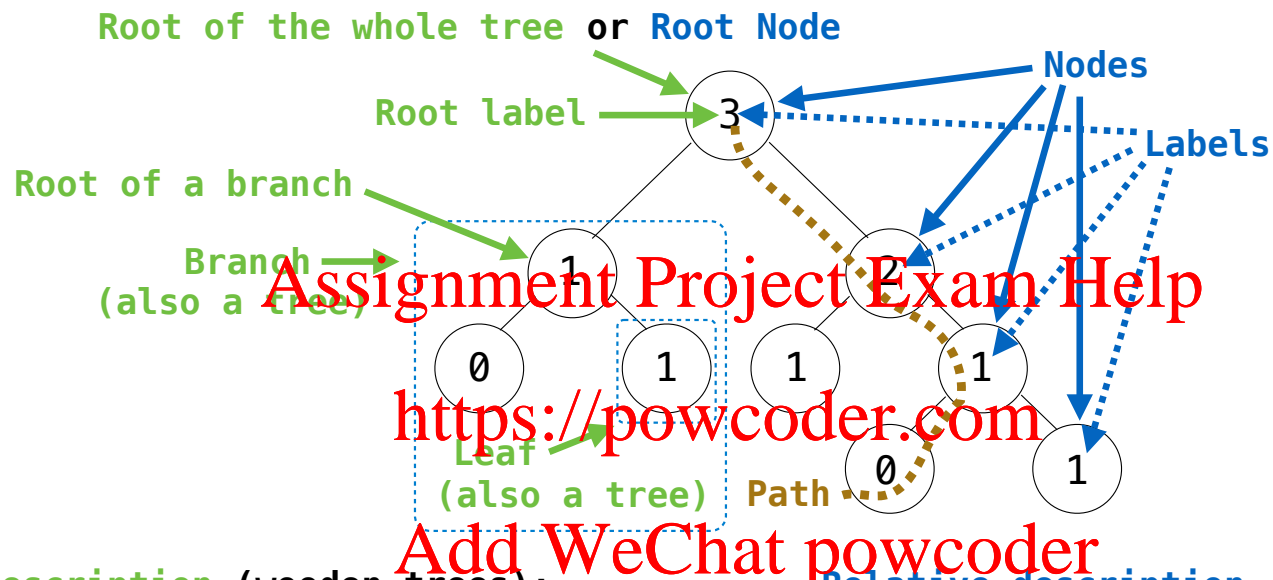
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Tree Abstraction



Recursive description (wooden trees):

A **tree** has a **root label** and a list of **branches**

Each **branch** is a **tree**

A **tree** with zero **branches** is called a **leaf**

A **tree** starts at the **root**

Relative description (family trees):

Each location in a tree is called a **node**

Each **node** has a **label** that can be any value

One node can be the **parent/child** of another

The top node is the **root node**

People often refer to labels by their locations: "each parent is the sum of its children"

Implementing the Tree Abstraction

```
def tree(label, branches=[]):  
    return [label] + branches
```

```
def label(tree):  
    return tree[0]
```

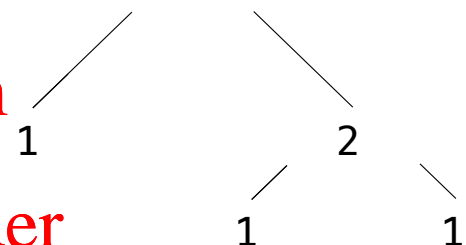
```
def branches(tree):  
    return tree[1:]
```

- A **tree** has a root **label** and a list of **branches**
- Each branch is a tree

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```
>>> tree(3, [tree(1),  
...         tree(2, [tree(1),  
...                 tree(1)])])  
[3, [1], [2, [1], [1]]]
```

Implementing the Tree Abstraction

```
def tree(label, branches=[]):  
    for branch in branches:  
        assert is_tree(branch)  
    return [label] + list(branches)
```

Verifies the tree definition

- A **tree** has a root **label** and a list of **branches**
- Each branch is a tree

```
def label(tree):  
    return tree[0]
```

Creates a list from a sequence of branches

```
def branches(tree):  
    return tree[1:]
```

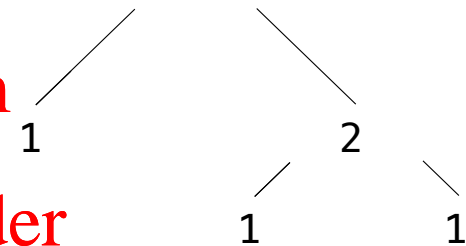
Verifies that tree is bound to a list

```
def is_tree(tree):  
    if type(tree) != list or len(tree) < 1:  
        return False  
    for branch in branches(tree):  
        if not is_tree(branch):  
            return False  
    return True
```

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```
>>> tree(3, [tree(1),  
...         tree(2, [tree(1),  
...                 tree(1)])])  
[3, [1], [2, [1], [1]]]
```

```
def is_leaf(tree):  
    return not branches(tree) (Demo)
```

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(Demo)

Tree Processing Uses Recursion

Processing a leaf is often the base case of a tree processing function

The recursive case typically makes a recursive call on each branch, then aggregates

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```
def count_leaves(t):  
    """Count the leaves of a tree."""  
    if is_leaf(t):  
        return 1  
    else:  
        branch_counts = [count_leaves(b) for b in branches(t)]  
        return sum(branch_counts)
```

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(Demo)

Discussion Question

Implement `leaves`, which returns a list of the leaf labels of a tree

Hint: If you `sum` a list of lists, you get a list containing the elements of those lists

```
>>> sum([ [1], [2, 3], [4] ], [])
[1, 2, 3, 4]
>>> sum([ [1] ], [])
[1]
>>> sum([ [[1]], [2] ], [])
[[1], 2]
```

`def leaves(tree):`
 "Returns a list containing the leaf labels of tree."
 >>> leaves(fib_tree(5))
 [[0, 1], [1, 0], [1, 1], 0, 1]
 """
 if is_leaf(tree):
 return [label(tree)]
 else:
 return sum(List of leaf labels for each branch, [])

`branches(tree)`

`leaves(tree)`

`[branches(b) for b in branches(tree)]`

`[leaves(b) for b in branches(tree)]`

`[b for b in branches(tree)]`

`[s for s in leaves(tree)]`

`[branches(s) for s in leaves(tree)]`

`[leaves(s) for s in leaves(tree)]`

Creating Trees

A function that creates a tree from another tree is typically also recursive

```
def increment_leaves(t):  
    """Return a tree like t but with all labels incremented."""  
    if is_leaf(t):  
        return tree(label(t) + 1)  
    else:  
        bs = [increment_leaves(b) for b in branches(t)]  
        return tree(label(t), bs)  
  
def increment(t):  
    """Return a tree like t but with all labels incremented."""  
    return tree(label(t) + 1, [increment(b) for b in branches(t)])
```

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Example: Printing Trees
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(Demo)

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Example: Summing Paths
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(Demo)

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Example: Counting Paths

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Count Paths that have a Total Label Sum

```
def count_paths(t, total):  
    """Return the number of paths from the root to any node in tree t  
    for which the labels along the path sum to total.  
  
    >>> t = tree(3, [tree(-1), tree(1, [tree(2, [tree(1)])], tree(3))], tree(1, [tree(-1)]))  
    >>> count_paths(t, 3) 2  
    >>> count_paths(t, 4) 2  
    >>> count_paths(t, 5) 0  
    >>> count_paths(t, 6) 1  
    >>> count_paths(t, 7) 2  
    """  
    if label(t) == total:  
        found = 1  
    else:  
        found = 0  
  
    return found + sum([count_paths(b, total - label(t)) for b in branches(t)])
```

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