ABSTRACT

Title of Dissertation:	MEASURING NETWORK DEPENDEN-CIES FROM NODE ACTIVATIONS
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	Doctor of Philosophy,
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My abstract for this dissertation.

MEASURING NETWORK DEPENDENCIES FROM NODE ACTIVATIONS

by

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Dissertation submitted to the Faculty of the Graduate School of the
University of Maryland, College Park in partial fulfillment
of the requirements for the degree of
Doctor of Philosophy

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Acknowledgements

I would like to acknowledge. . .

Dedication

to my friends and family

Foreward

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Preface

Preface content

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Chapter 1: Introduction

A wide variety of fields show consistent interest in inferring latent network structure from observed interactions, from human cognition and social infection networks, to marketing, traffic, finance, and many others. [6, 7].

However, an increasing number of authors are noting a lack of agreement in how to approach the metrology of this problem. This includes rampant disconnects between the theoretical and methodological network analysis sub-communities[1], treatment of error as purely aleatory, rather than epistemic [8], or simply ignoring measurement error in network reconstruction, entirely [6].

1.1 Intro part 1

A salient point is brought up by Torres et al. [3], in that many times our observations are more appropriately thought of as *different classes of incidence structures.*[3] The dependencies in the data generation and observation processes, as well as are assumptions are difficult to preserve when we model data as a simple graph that is better represented as, say, a hypergraph.

A common type of data used in network recovery is often called *co-occurrence* data, where nodes are observed as being in an "on" or "off" state in any given data point.

From these, we might wish to recover the latent relationships or dependencies between them. An argument could be made in the style of Torres et al. [3], that this data is fundamentally bipartite (and, thus, hypergraphical) in nature. However, in a large number of cases, we observe such co-occurrences as the result of underlying dynamical processes, like diffusion, on a carrier graph. *Further*, an increasing amount of literature is dedicated to capturing statistical properties of very large graphs, e.g. through variations on random-walk sampling. If our only snapshot of a large graph originates from samples generated on it by random walk (and other diffusive dynamic sampling strategies), then we must be able to perform *and normalize the practice of* epistemic uncertainty of edge existence from co-occurrence data.

How do we provide the needed metrological foundation to direct future research in this area? I hope that by unifying the interpretations of several classes of network recovery techniques into a single, non-parametric framework, we can re-unify methodology and theory. Much like the ubiquity of kernel density estimates for exploratory data analysis, with the right tools analysts can better reason about what they don't know, while researchers can use that reported, mutually understood experience to work on extending the things we *can know*: i.e. what they *actually want to measure.*

Chapter 2:   Background: Graph and Hypergraph Structures as Inner Product Spaces

For each, describe the meaning of

1. Observation model

2. Vector space representation

3. Inner product (linear kernel)

4. Induced Norms

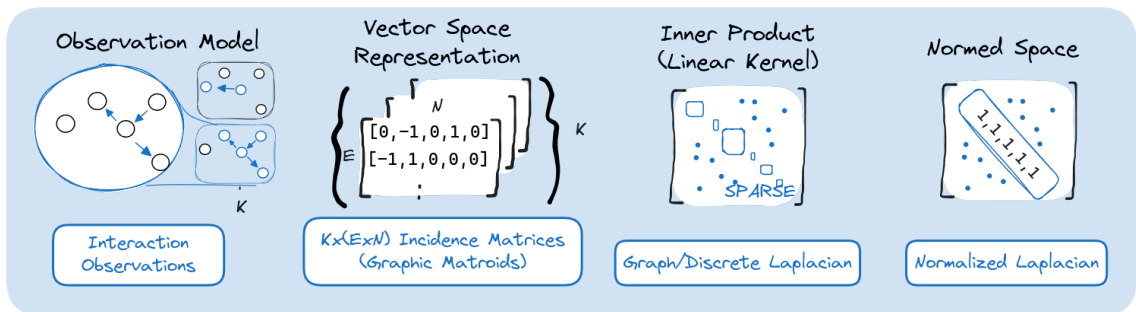## 2.1   Graphs from Relation Observations

Figure 2.1: Edge Relation Observational Model

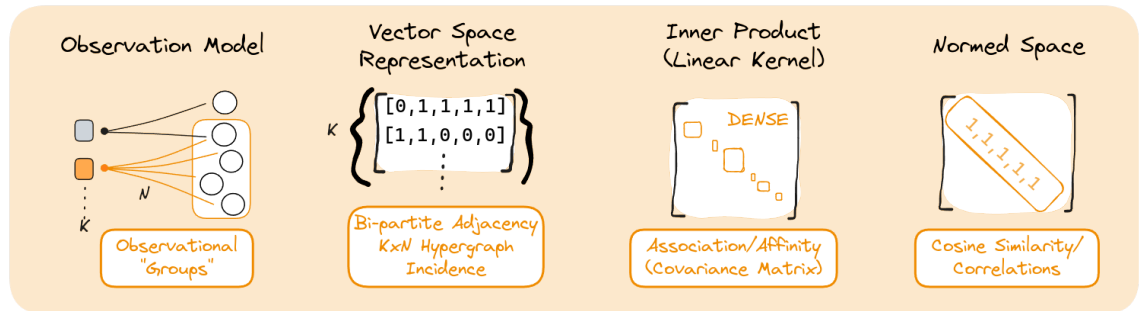## 2.2 Hypergraphs from Coocurrence Observations

Figure 2.2: Hyperedge Relation Observational Model

Chapter 3:   Review: Projections and Inverse Problems

I.e. trying to "recover" one from the other. In a way, proceduralizing the precautions described in Torres et al. [3].

> Takeaway: a way to organize existing algorithms, AND highlight unique
>
> set of problems we set out to solve

3.1   Connecting Graphs & Hypergraphs as Adjoint

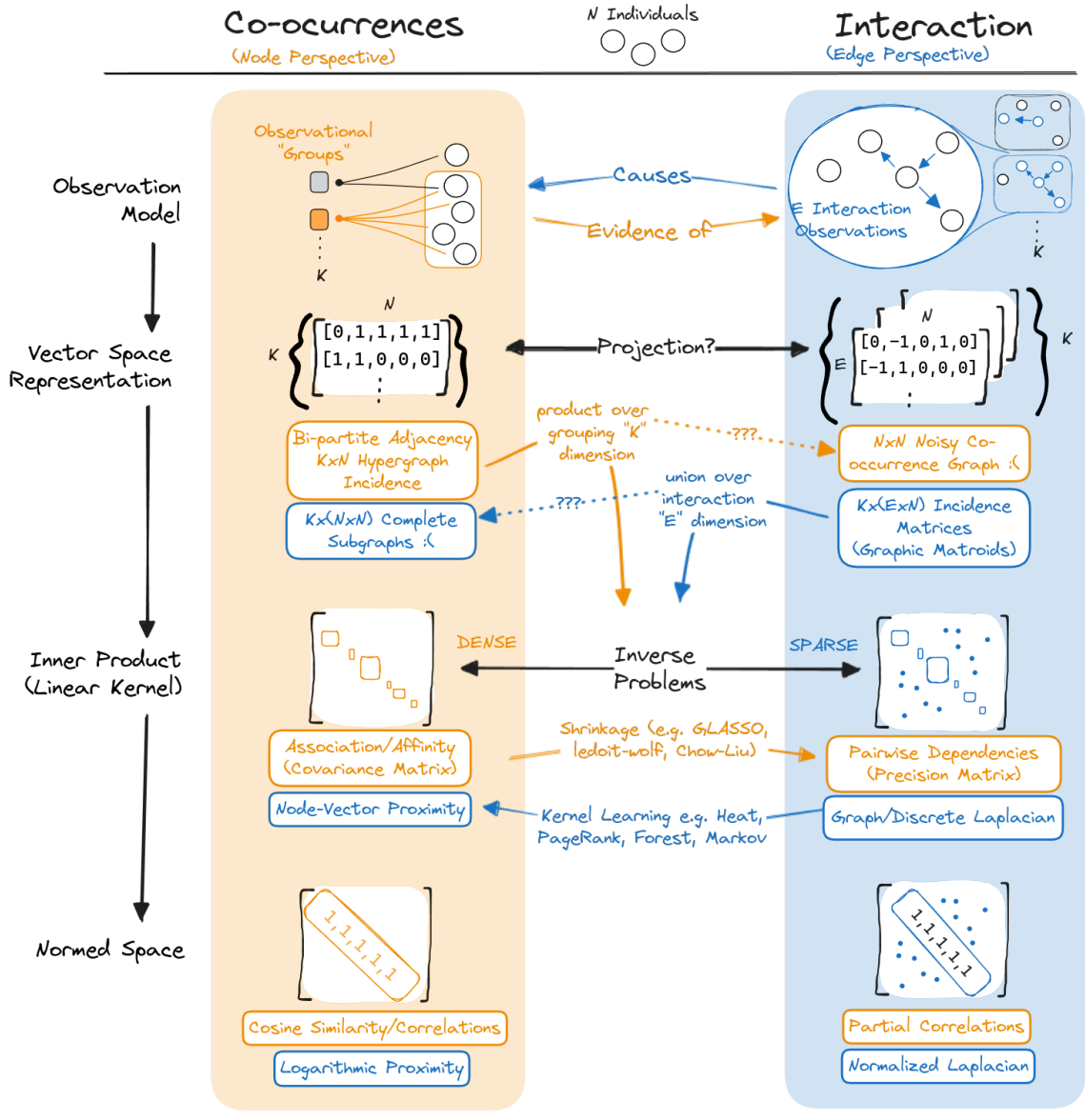i.e. Network Recovery as an Inverse Problem

Figure 3.1: Relating Graphs and Hypergraph/bipartite structures as adjoint operators

3.2 Algorithmic Information Loss in Literature

- Observation-level loss (starting with the inner product or kernel)

- Non-generative model loss (no projection of data into model space)

- no uncertainty quantification

Sorting algorithms... *none address all three!*

i.e. MOTIVATES FOREST PURSUIT

Chapter 4: Nonparametric Network Recovery With Random Spanning Forests

filling the gap we saw in the literature
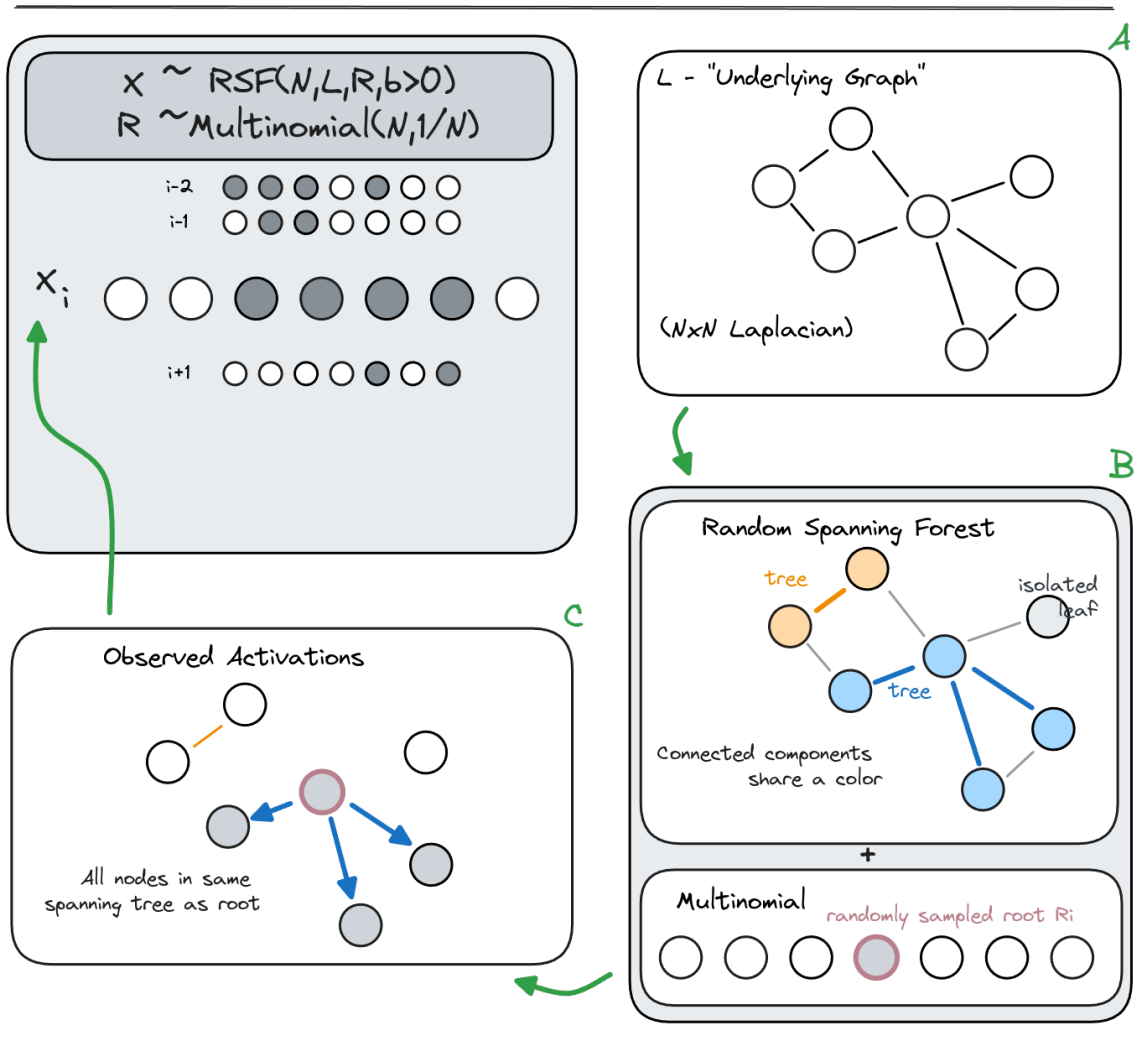
4.1 Generative Model Specification

Figure 4.1: Explanation of the Random Spanning Forest generative model for binary activation observations

4.2 Forest Pursuit: Approximate Recovery in Near-linear Time

I.e. the PLOS paper (modified basis-pursuit via MSTs)

4.3   Bayesian Estimation by Gibbs Sampling

I.e. the unwritten paper, modifying technique by Duan and Dunson [2] for RSF instead of RSTs

Chapter 5: Recovery from Ordered Random-Walk Observation Sets

Like before, but with the added twist of *knowing* our nodes were activated with a particular partial order.

insert from [4, 5]

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