## Hashing for Machine Learning

Hashing Summer School, University of Copenhagen

To follow along: git clone git://github.com/JohnLangford/vowpal\_wabbit.git wget http://hunch.net/~jl/rcv1.tar.gz



John Langford, Microsoft Resarch, NYC

# Simple Machine Learning: Linear Learning

Features: a vector  $x \in \mathbb{R}^n$ 

Label:  $y \in \mathbb{R}$ 

Goal: Learn  $w \in \mathbb{R}^n$  such that  $\hat{y}_w(x) = \sum_i w_i x_i$  is close to y.

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Dataset size:

781K examples

60M nonzero features

1.1G bytes

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Progressive validation loss  $0.0513~(\simeq best)$  in 1~second.~(best)

Performance real, but timing not: TFIDF transform >2 minutes.



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 $1 \mid$  tuesday year million short compan vehicl line stat financ commit exchang plan corp subsid credit issu debt pay gold bureau prelimin refin billion telephon time draw

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```
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```
vw -b 24 -c rcv1.train.raw.txt --binary
Progressive validation loss 0.0572 in 1.3s
vw -b 24 -c rcv1.train.raw.txt --binary --ngram 2
Progressive validation loss 0.0500 in 3.4s
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vw -b 24 -c rcv1.train.raw.txt --binary --ngram 2 --skips 4
Progressive validation loss 0.0454 in 11s
vw -b 24 -c rcv1.train.raw.txt --binary --ngram 2 --skips 4 -l 0.25
Progressive validation loss 0.0449 in 11s
+Better error rate
+1/10th traing time!
+faster/easier testing
```

### Outline

- A bit more about machine Learning
- Use of Hash
- Hashing applications

# Algorithm used: Online Linear Learning

```
Start with \forall i: w_i = 0
Repeatedly:
```

- Get features  $x \in \mathbb{R}^n$ .
- ② Make linear prediction  $\hat{y}_w(x) = \sum_i w_i x_i$ .
- Observe label y.
- **1** Record loss  $\ell(y, \hat{y}_w(x))$ .
- **1** Update weights so  $\hat{y}_w(x)$  is closer to y.

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(many more details that matter in practice)

### Features in Practice: Engineered Features

Hand crafted features, built up iteratively over time, each new feature fixing a discovered problem.

- +Good understanding of what's happening.
- 2 +Never fail to learn the obvious.
- +Small RAM usage.
- Slow at test time. Intuitive features for humans can be hard
- -Low Capacity. A poor fit for large datasets. (Boosted)
   Decision trees are a good compensation on smaller datasets.
- High persontime.

### Features in Practice: Learned Features

Use a nonlinear/nonconvex possibly deep learning algorithm.

- +Good results in Speech & Vision.
- 2 +Fast at test time.
- 4 + High capacity. Useful on large datasets.
- Slow training. Days to weeks are common.
- -Wizardry may be required.

### Features in Practice: sparse words

Generate a feature for every word.

- +High capacity.
- 4-fast test time. Lookup some numbers, then compute an easy prediction.
- 4 +fast learning Linear faster than decision tree, but parallel is tricky.
- -High RAM usage

### Features in Practice: sparse words

Generate a feature for every word.

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Hash function: string  $\rightarrow \{0,1\}^b$ 

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Hash table = Hash function + Array< Pair<string, int> > of length  $\{0,1\}^b$ 

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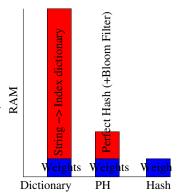
Hash function: string  $\rightarrow \{0,1\}^b$ 

Hash table = Hash function + Array< Pair<string, int> > of length  $\{0,1\}^b$ 

Perfect hash = mapping of n fixed (and known in advance) strings to integers  $\{1, n\}$ .

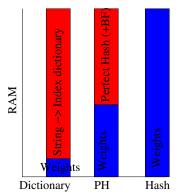
### How does feature address parameter?

- Hash Table (aka Dictionary): Store hash function + Every string + Index.
- Perfect Hash (+Bloom Filter): Store Custom Hash function (+ bit array).
- 3 Hash function: Store Hash function.



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## A variation: unbiased hashing

Multiply feature value by  $(-1)^s$  where s is a 1 bit hash.

Advantage: Feature values have expectation 0 for a random  $s \Rightarrow$  better performance in the high collision regime.

## Objection: Collisions!

Valid sometimes: particularly with low dimensional hand engineered features.

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Theorem: If a feature is duplicated  $O(\log n)$  times when there are O(n) features, at least one version of the feature is uncollided when hashing with  $\log(n \log n)$  bits.

Proof: Essentially Bloom filter logic. See Michael Mitzenmacher's talk Monday.

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Use --audit to decode.

Keep your own dictionary on the side --invert\_hash if needed.

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## Use of Hash: Ngrams

```
2-gram = a feature for every pair of adjacent words.
3-gram = a feature for every triple of adjacent words, etc...
n-gram = ...
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\begin{array}{l} \hbox{2-gram} = \hbox{a feature for every pair of adjacent words.} \\ \hbox{3-gram} = \hbox{a feature for every triple of adjacent words, etc...} \\ \hbox{n-gram} = ... \\ \\ \hbox{lnput:} \\ \hbox{(index}_1, \hbox{value}_1) \\ \hbox{(index}_2, \hbox{value}_2) \\ \hbox{Output:} \end{array}
```

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2-gram = a feature for every pair of adjacent words.
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n-gram = ...
Input:
(index<sub>1</sub>, value<sub>1</sub>)
(index2, value2)
Output:
((index_1 magic + index_2)\&mask, value_1 value_2)
(linear hash, value multiplication)
```

### Use of Hash: Outer Products

```
Input: Feature sets F_1, F_2 Output: Outer product set F_1 \times F_2 Use linear hash again.
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Input: Feature sets F_1, F_2 Output: Outer product set F_1 \times F_2 Use linear hash again. Implemented via -q in VW.
```

# Example 2: Mass Personalized Spam Filtering

- $0.3.2 * 10^6$  labeled emails.
- **2** 433167 users.
- $3 \sim 40 * 10^6$  unique tokens.

How do we construct a spam filter which is personalized, yet uses global information?

## Example 2: Mass Personalized Spam Filtering

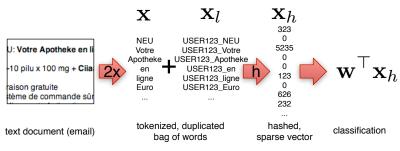
- $3.2 * 10^6$  labeled emails.
- **2** 433167 users.

How do we construct a spam filter which is personalized, yet uses global information?

Bad answer: Construct a global filter + 433167 personalized filters using a conventional hashmap to specify features. This might require 433167 \* 40 \*  $10^6$  \* 4  $\sim$  70Terabytes of RAM.

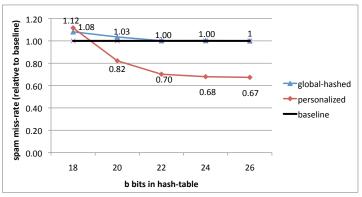
### Using Hashing

Use hashing to predict according to:  $\langle w, \phi(x) \rangle + \langle w, \phi_u(x) \rangle$ 



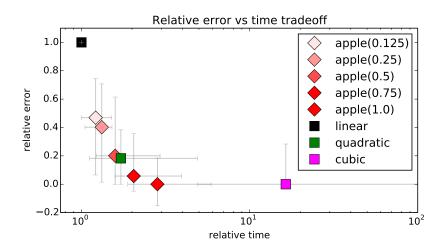
(in VW: specify the userid as a feature and use -q)

#### Results



 $2^{26}$  parameters = 64M parameters = 256MB of RAM. An  $\times 270 \, \text{K}$  savings in RAM requirements.

# Another Application: Efficient Sparse Polynomial learning



# Features sometimes collide, which is scary, but then you love it

Generate a feature for every word, ngram, skipgram, pair of (ad word, query word), etc... and use high dimensional representation.

- +High capacity.
- +Correlation effects nailed
- 4 +Fast test time. Compute an easy prediction.
- +Fast Learning (with Online + parallel techniques. See talks.)
- +/-Variable RAM usage. Highly problem dependent but fully controlled.

Another cool observation: Online learning + Hashing = learning algorithm with fully controlled memory footprint  $\Rightarrow$  Robustness.

## References, prequels

- Reinforcement Learning: An Introduction, Richard S. Sutton and Andrew G. Barto, MIT Press, Cambridge, MA, 1998. Chapter 8.3.1 hashes states.
- 2 CRM114 http://crm114.sourceforge.net/, 2002. Uses hashing of grams for spam detection.
- Apparently used by others as well, internally.
- Many use hashtables which store the original item or a 64+ bit hash of the original item.

# References, "modern" hashing trick

- 1 2007, Langford, Li, Strehl, Vowpal Wabbit released.
- 2008, Ganchev & Dredze, ACL workshop: A hash function is as good as a hashmap empirically.
- 2008/2009, VW Reimplementation/Reimagination/Integration in Stream (James Patterson & Alex Smola) and Torch (Jason Weston, Olivier Chapelle, Kilian).
- 2009, AlStat Qinfeng Shi et al, Hash kernel definition, Asymptopia Redundancy analysis
- 2009, ICML Kilian et al, Unbiased Hash Kernel, Length Deviation Bound, Mass Personalization Example and Multiuse Bound.

### Question 1

Hashing is applied to features before learning. Is it better to apply to parameters after learning?

### Question 2

A commonly proposed alternative to hashing is random projection as per Johnson-Lindenstrauss (see Alex Andoni's lecture yesterday). Is that a better approach?

### Question 3

How do you compute the n-grams for k elements in time O(k)?