

# PARALLEL AND GPU PROGRAMMING IN PYTHON

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# Outline

- GPUs as hardware accelerator
- PyCUDA programming
  - CUDA programming and execution model
- Examples:
  - Vector (1D array) addition
  - Matrix (2D array) addition
  - Matrix multiplication
  - Reduction
- Optimization tips
- Two bugs in GPU programming

# Resources

- The slides and source code of the examples can be found at:
  - <https://github.com/sara-nl/Parallel-and-GPU-programming-in-Python>

# Jupyter Notebook

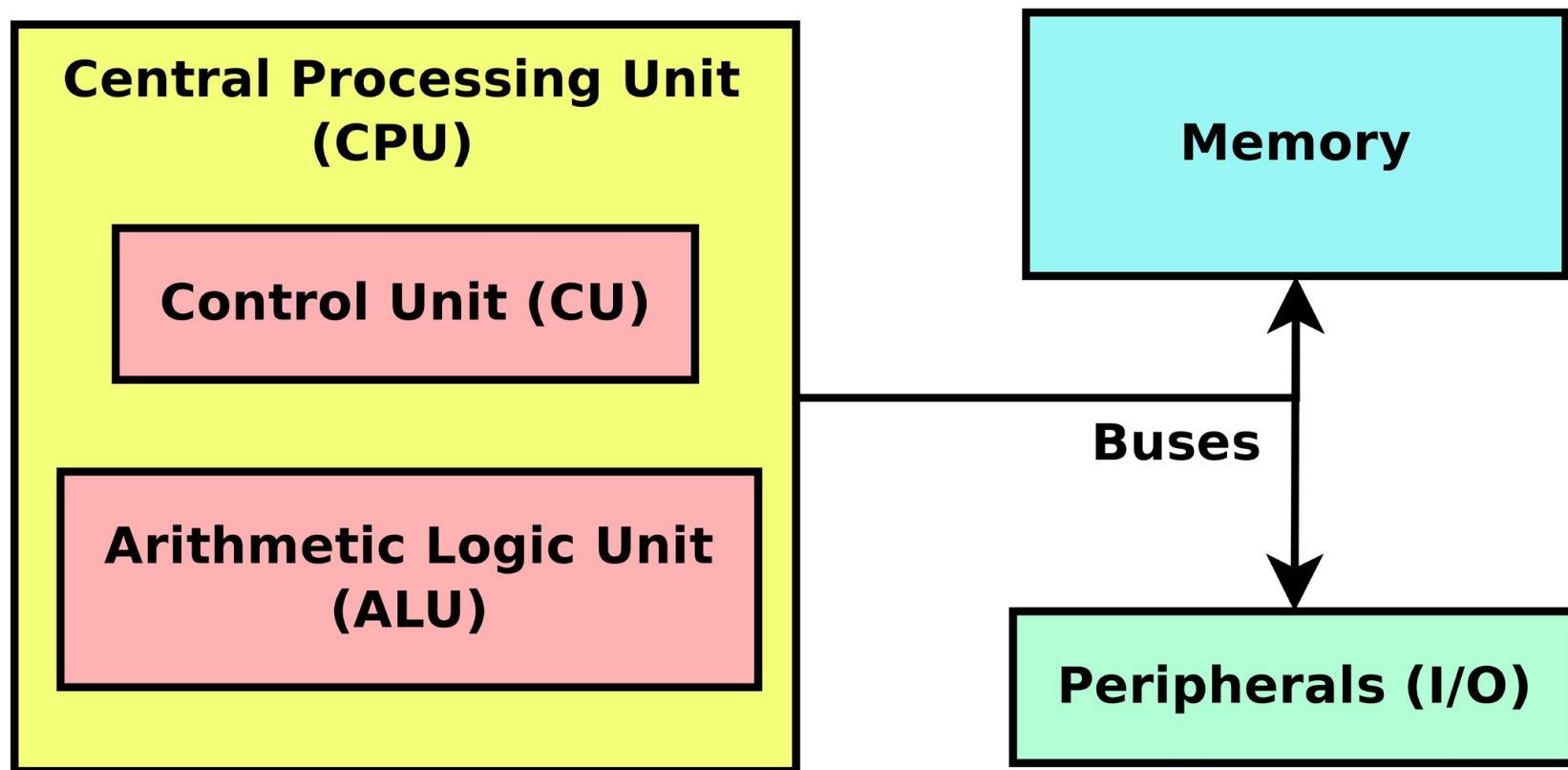
- The notebook for the GPU part of the course:
  - <https://jupyter.snellius.surf.nl/jhssrf006>

# Hardware Accelerator (e.g., GPUs)

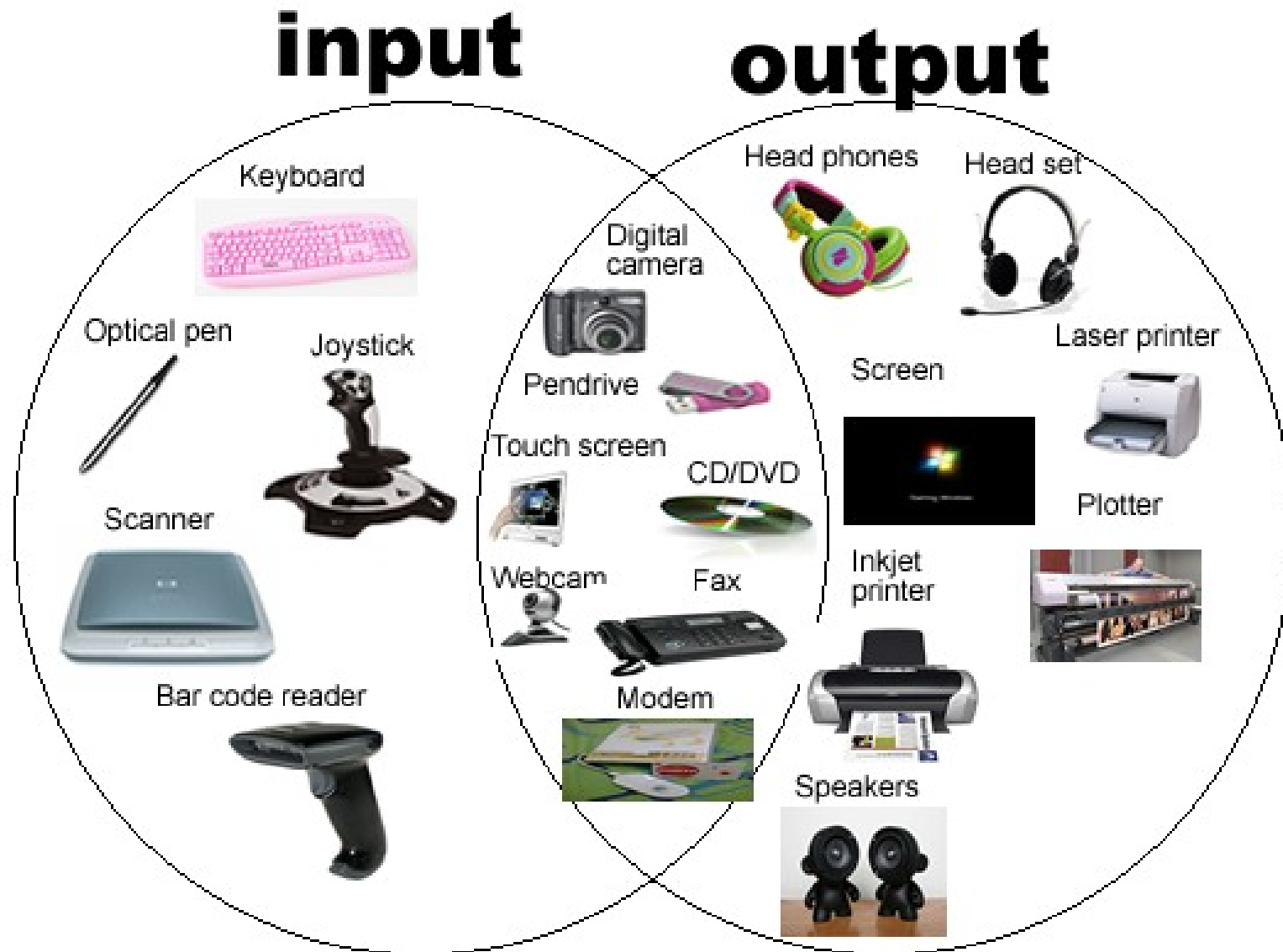
- What is it?
- Why do we need it?
- How to benefit it?
- ...



# A computer is



# Peripherals

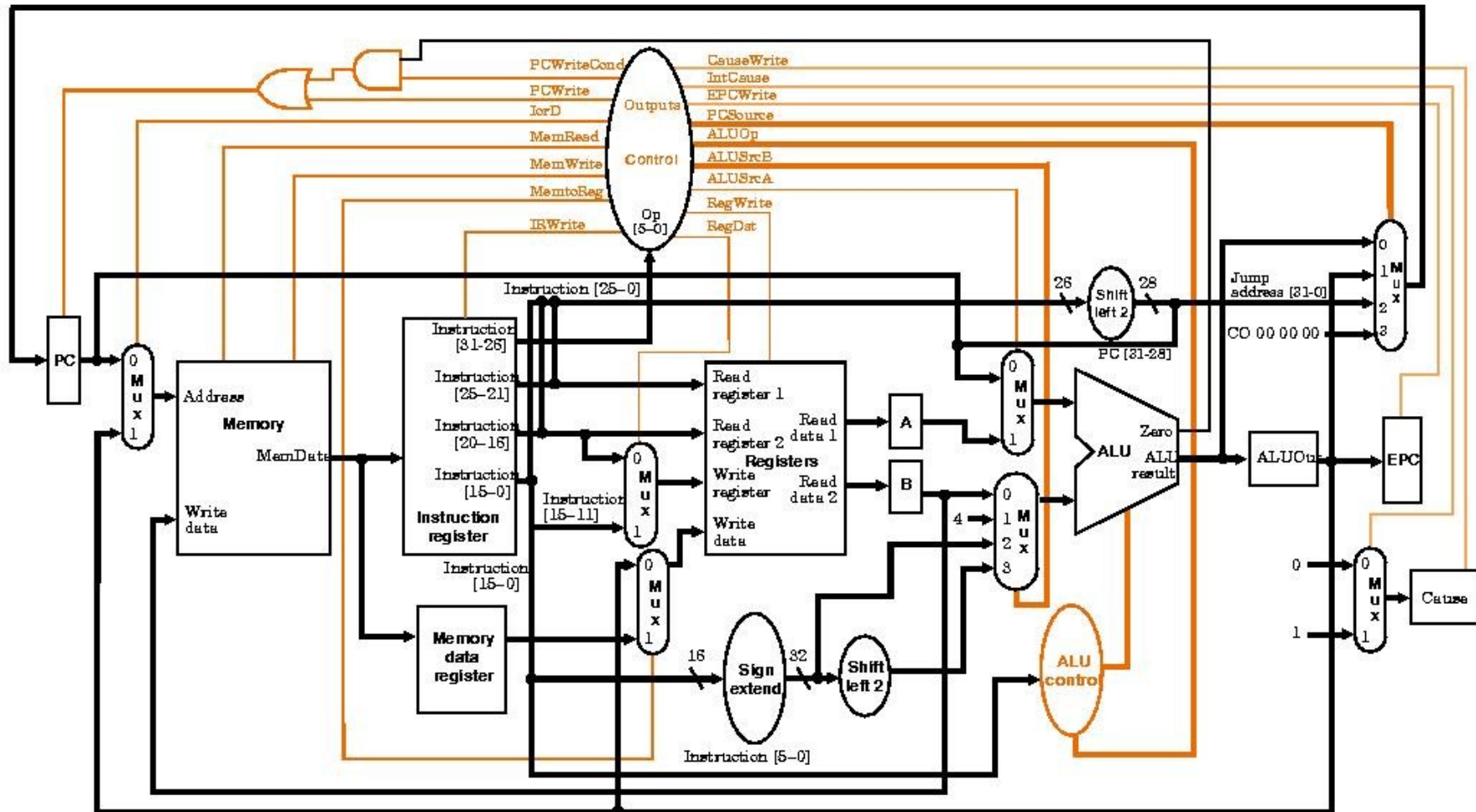




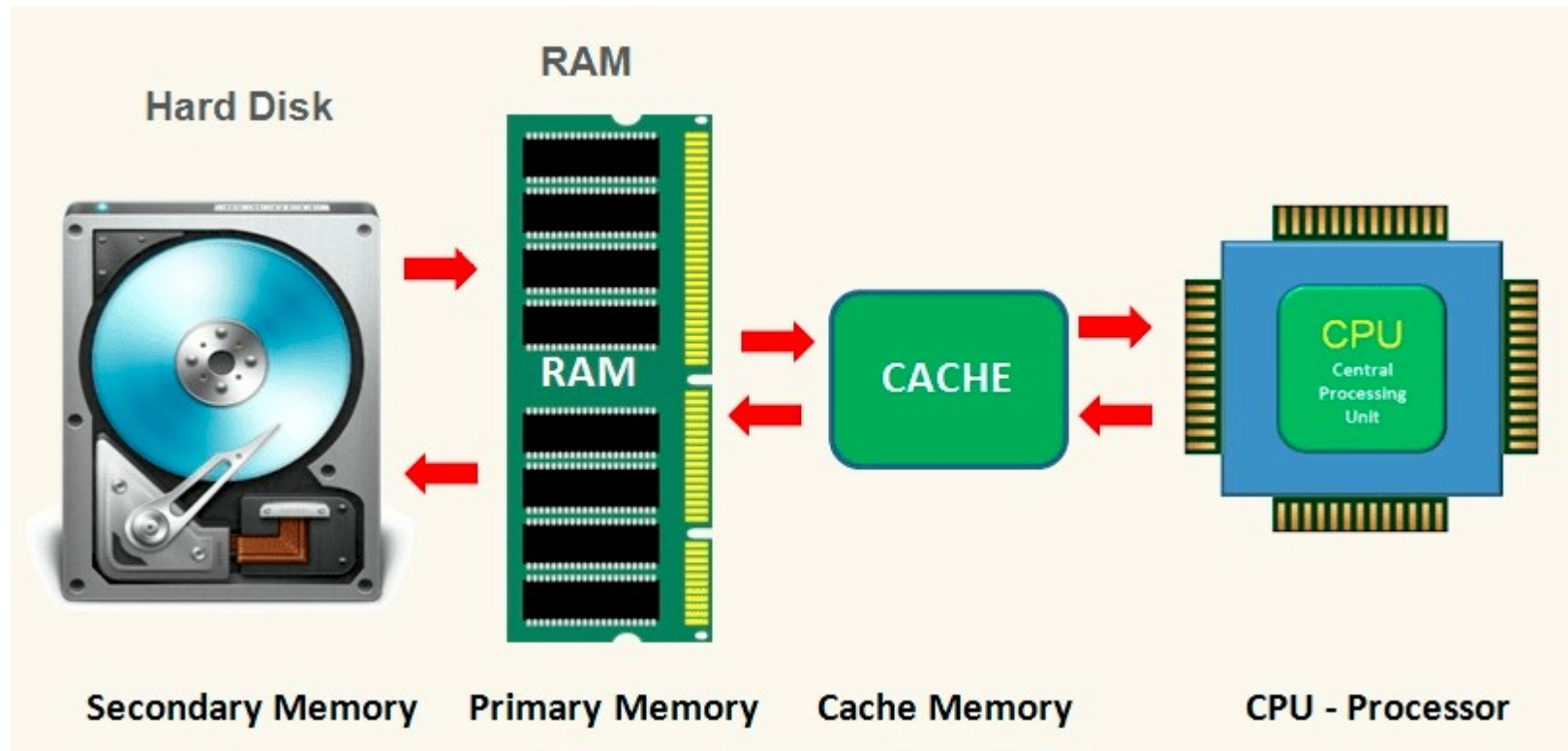
# Main Goals

- General-Purpose
- Low latency

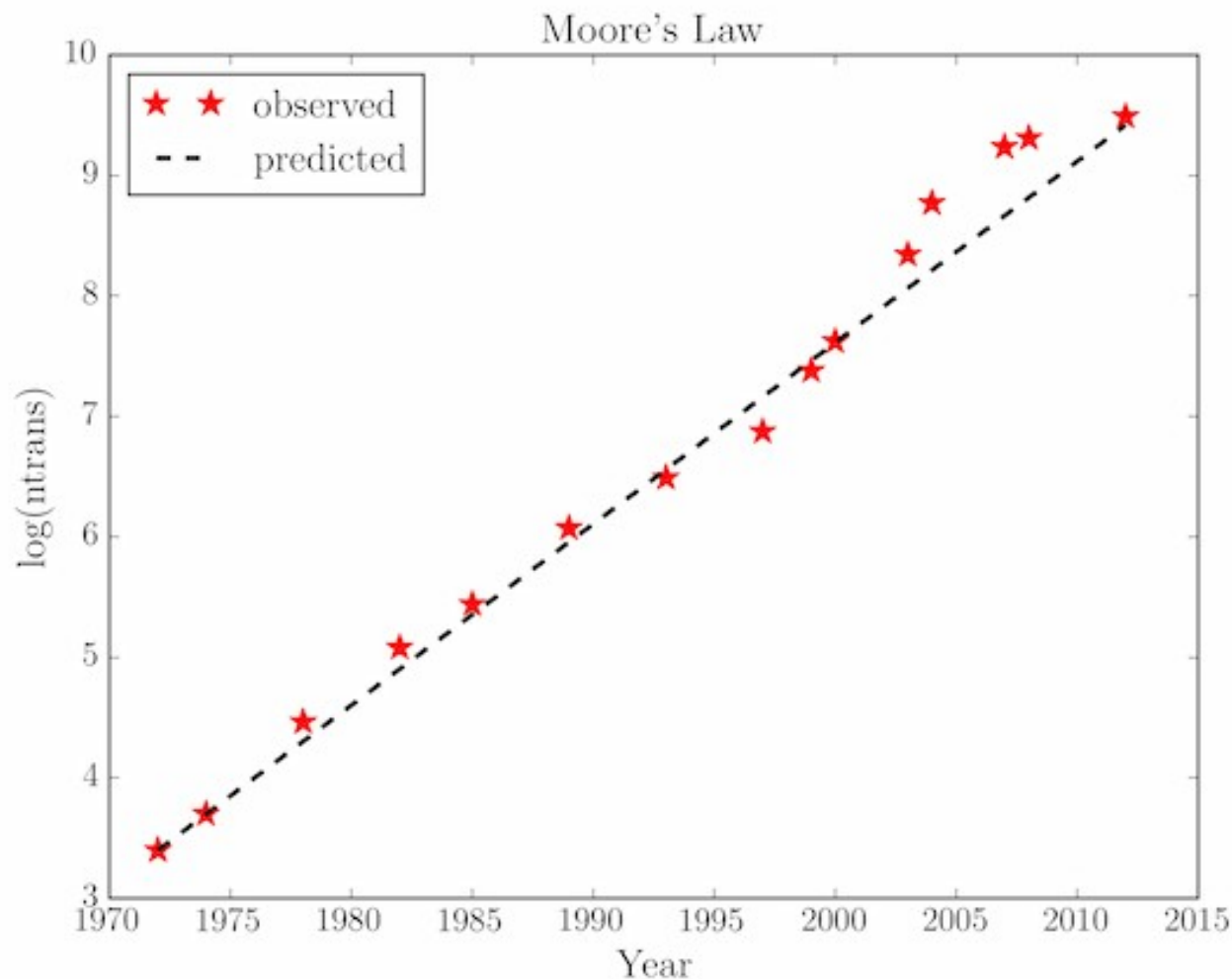
# Complicated CPUs



# Memory Hierarchy



# Moore's Law



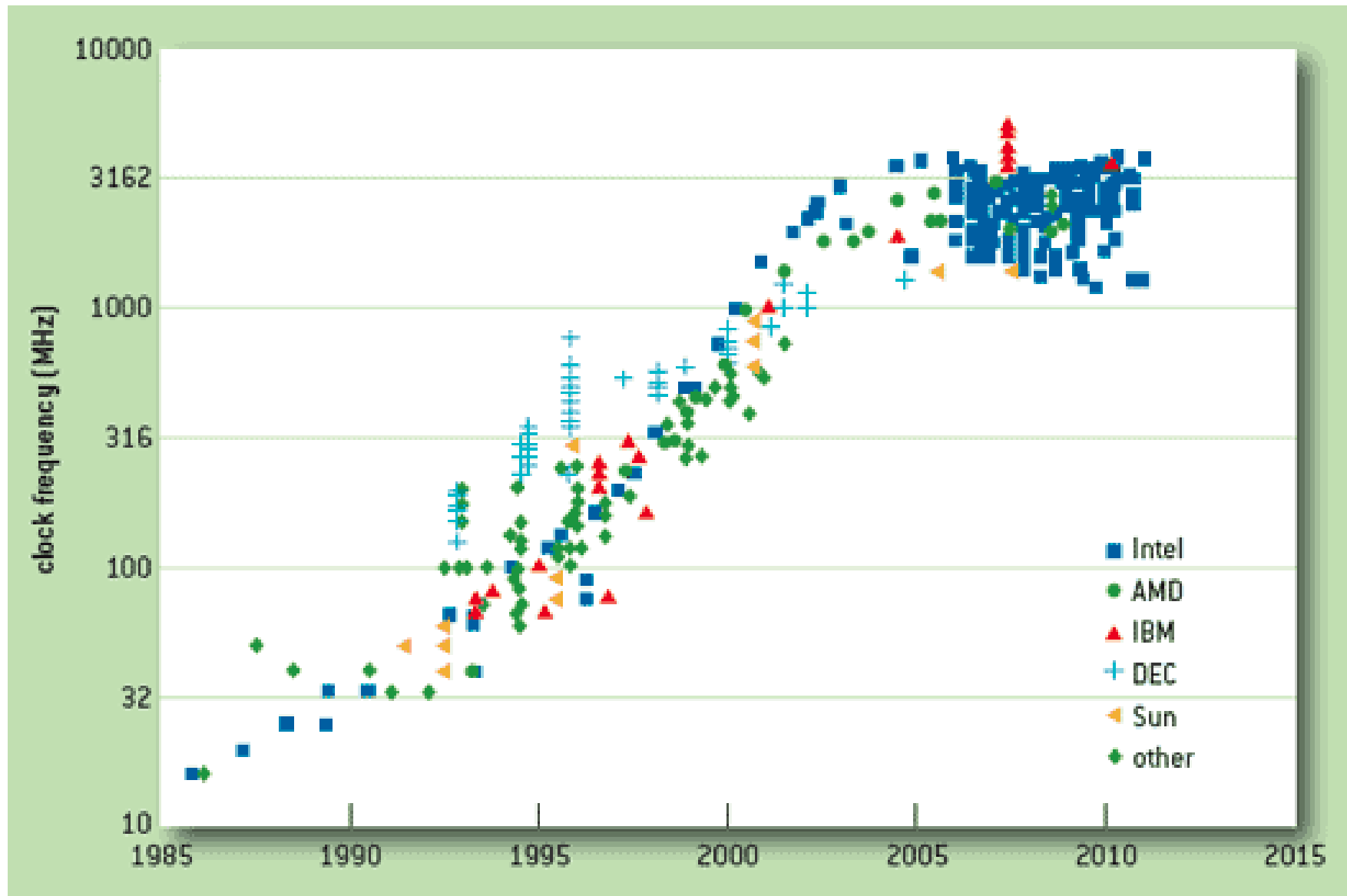
Number of transistors on a CPU chip will double every 18 months

# Dennard Scaling Law

- As transistors become smaller, their power density stays constant
- As a result of Moore's and Dennard's law:
  - **CPU manufacturers can raise clock frequency without significantly increasing overall circuit power consumption**



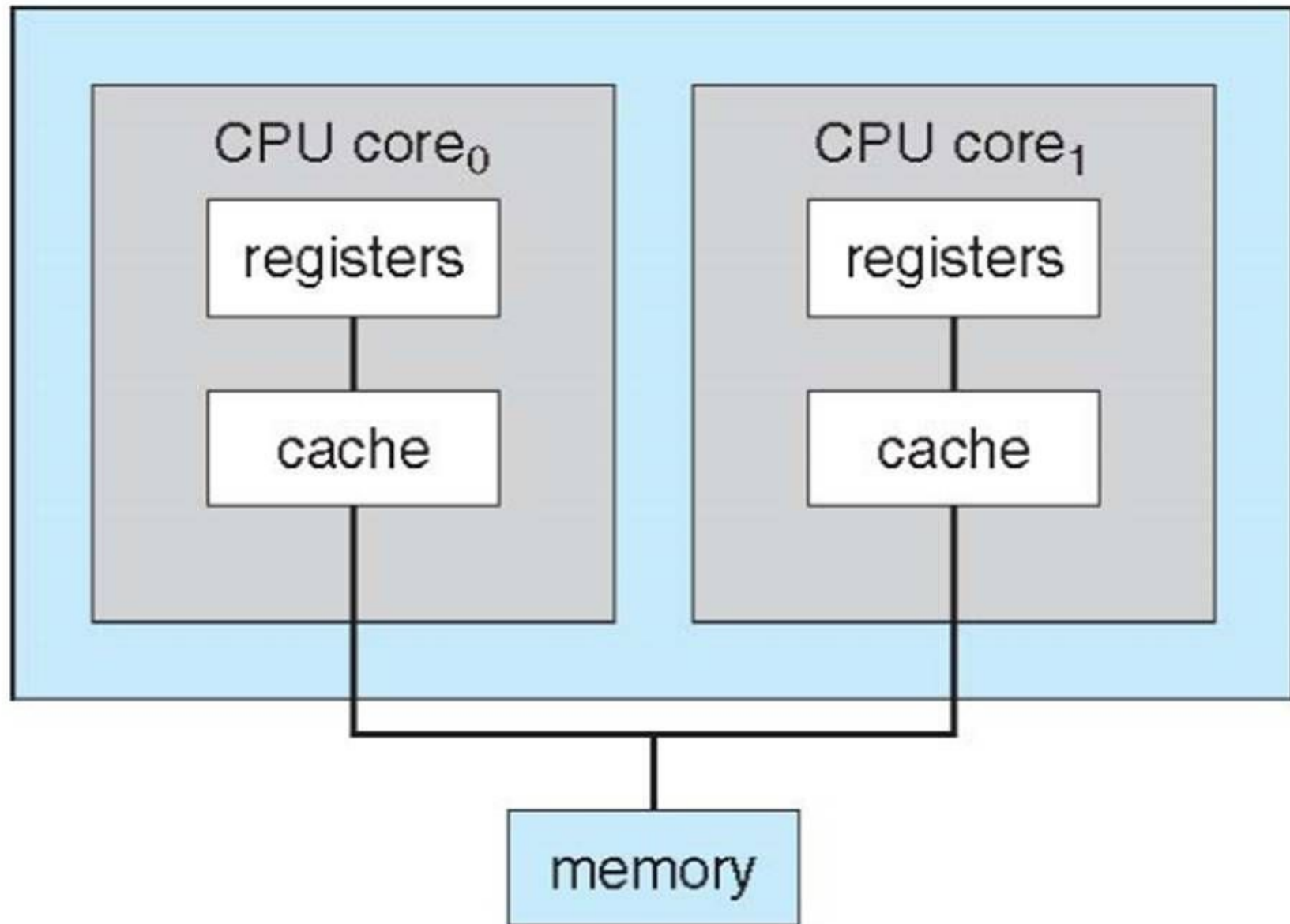
# Clock Frequency



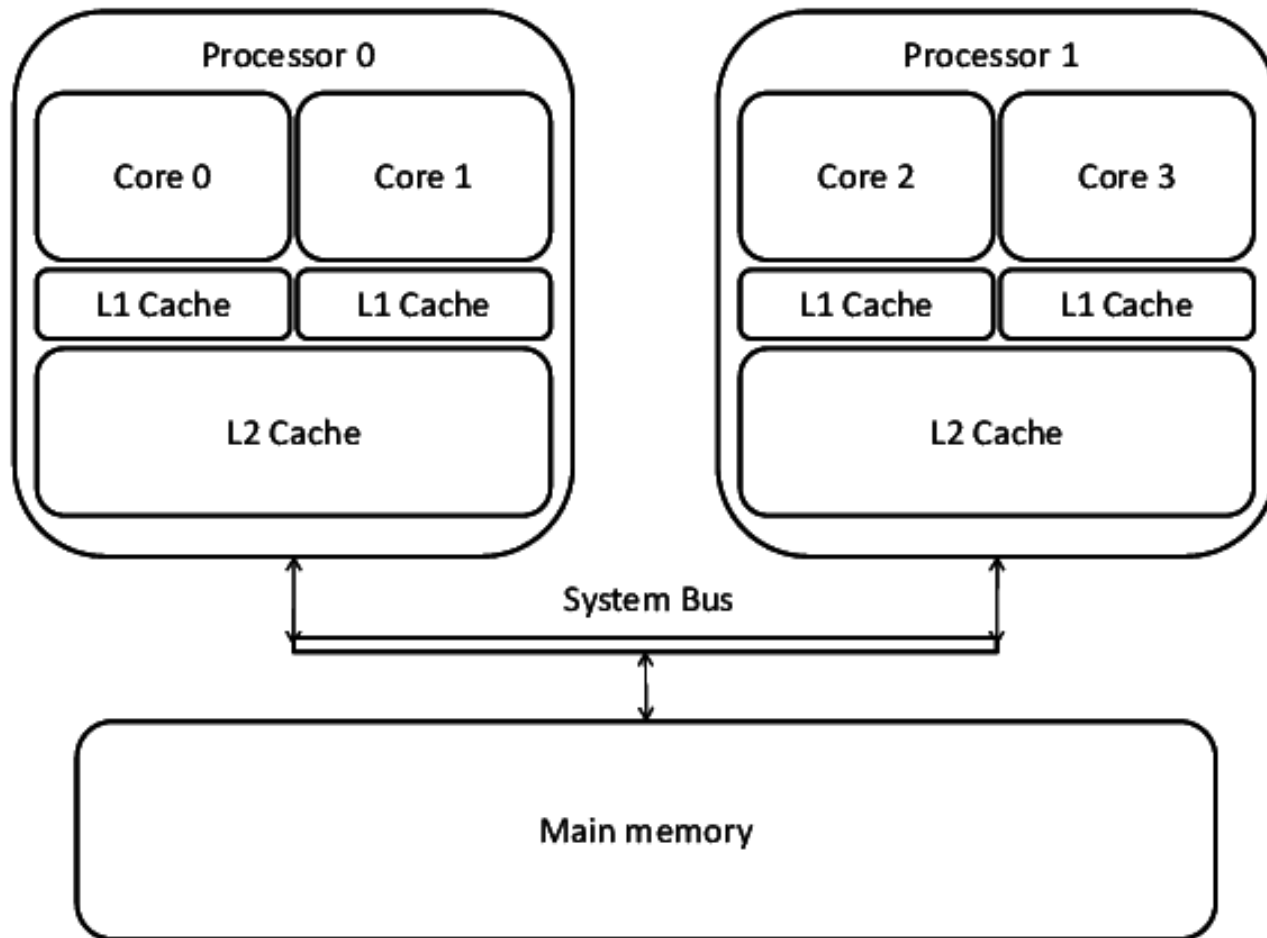
# End of Moore's/Dennard's Law

- The prediction had been true for a long time
- We observe that #transistors does not increase in the scale of Moore's law
- We reach the end of Dennard scaling law

# Multi-core CPUs



# Multi-processors

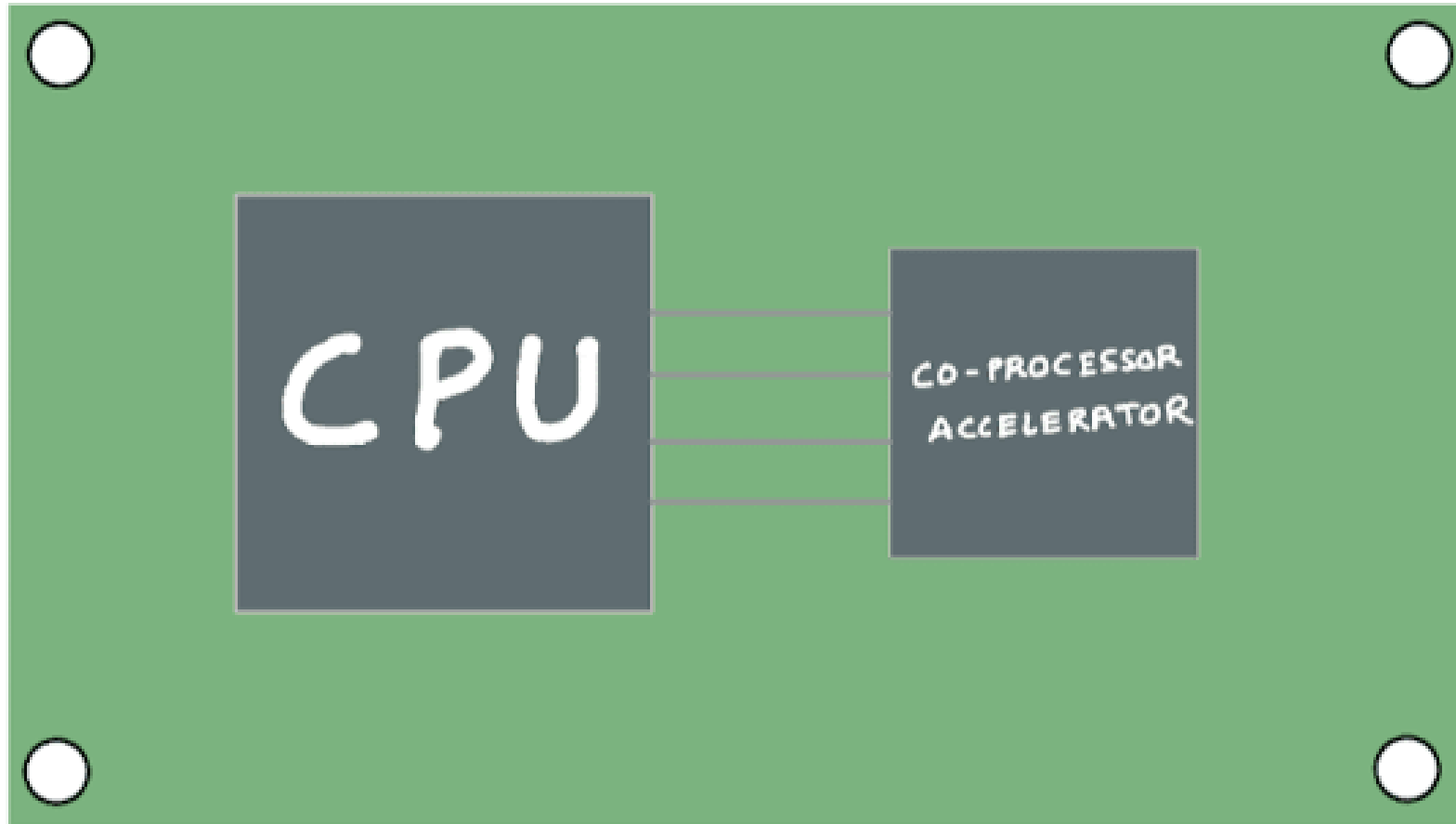


# New requirements

- Big data
- New applications:
  - Massively parallel
  - Certain operations
- Faster computation



# Accelerator



# Accelerators/Co-processors

- Graphics Processing Units (GPUs)
- Field Programmable Gate Arrays (FPGAs)
- Tensor Processing Units (TPUs)
- ...

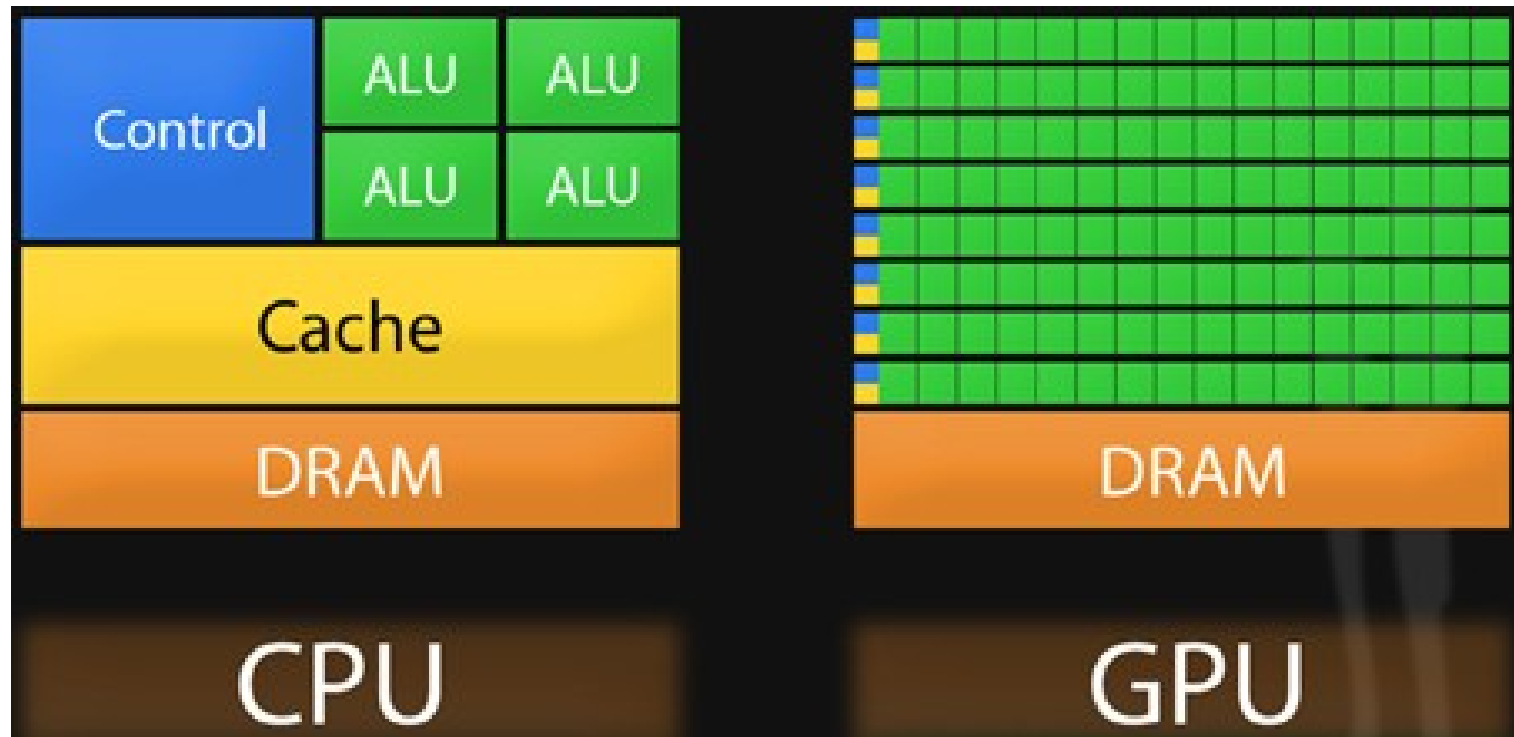
# Simplere many cores

- Simpler cores (i.e., simplified ALUs and CUs)
- Replicate many of them
- As a co-processor

# GPUs

- Initially invented for image rendering purposes
- Gradually evolved to be used as General Purpose GPU

# GPUs vs CPUs





# Two Metrics

- Latency: the time it takes an instruction to be processed
- Throughput: the number of instructions that can be processed in a certain amount of time

# Two Metrics

- CPUs are latency-optimized processors
- GPUs are throughput-optimized (co-)processors

# GPU Manufacturers



# Supercomputers

Rank	System	Cores	Rmax (PFlop/s)	Rpeak (PFlop/s)	Power (kW)
1	<b>Frontier</b> - HPE Cray EX235a, AMD Optimized 3rd Generation EPYC 64C 2GHz, AMD Instinct MI250X, Slingshot-11, HPE DOE/SC/Oak Ridge National Laboratory United States	8,730,112	1,102.00	1,685.65	21,100
2	<b>Supercomputer Fugaku</b> - Supercomputer Fugaku, A64FX 48C 2.2GHz, Tofu interconnect D, Fujitsu RIKEN Center for Computational Science Japan	7,630,848	442.01	537.21	29,899
3	<b>LUMI</b> - HPE Cray EX235a, AMD Optimized 3rd Generation EPYC 64C 2GHz, AMD Instinct MI250X, Slingshot-11, HPE EuroHPC/CSC Finland	1,110,144	151.90	214.35	2,942
4	<b>Summit</b> - IBM Power System AC922, IBM POWER9 22C 3.07GHz, NVIDIA Volta GV100, Dual-rail Mellanox EDR Infiniband, IBM DOE/SC/Oak Ridge National Laboratory United States	2,414,592	148.60	200.79	10,096
5	<b>Sierra</b> - IBM Power System AC922, IBM POWER9 22C 3.1GHz, NVIDIA Volta GV100, Dual-rail Mellanox EDR Infiniband, IBM / NVIDIA / Mellanox DOE/NNSA/LLNL United States	1,572,480	94.64	125.71	7,438

# Supercomputers

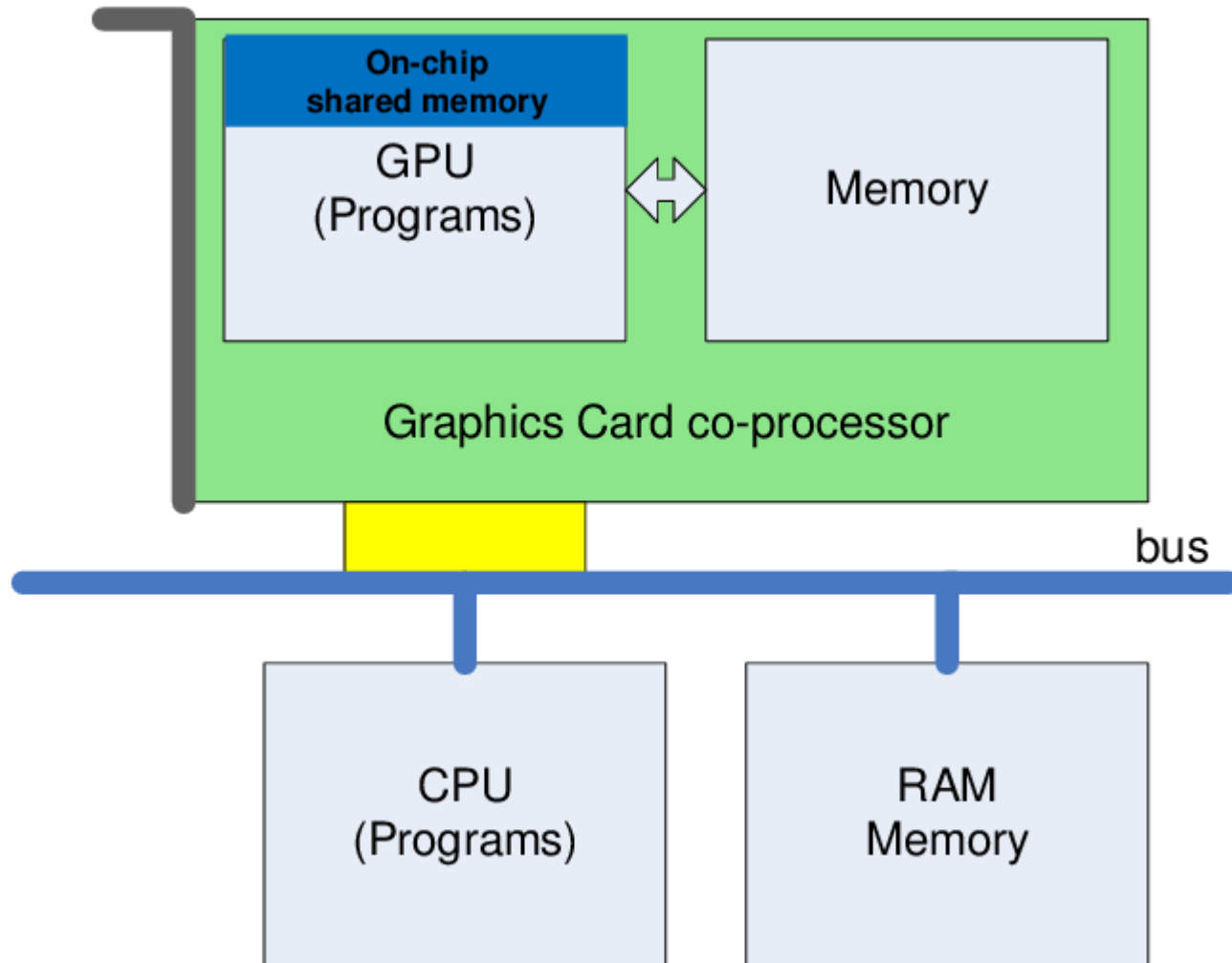
6	<b>Sunway TaihuLight</b> - Sunway MPP, Sunway SW26010 260C 1.45GHz, Sunway, NRCPC National Supercomputing Center in Wuxi China	10,649,600	93.01	125.44	15,371
7	<b>Perlmutter</b> - HPE Cray EX235n, AMD EPYC 7763 64C 2.45GHz, NVIDIA A100 SXM4 40 GB, Slingshot-10, HPE DOE/SC/LBNL/NERSC United States	761,856	70.87	93.75	2,589
8	<b>Selene</b> - NVIDIA DGX A100, AMD EPYC 7742 64C 2.25GHz, NVIDIA A100, Mellanox HDR Infiniband, Nvidia NVIDIA Corporation United States	555,520	63.46	79.22	2,646
9	<b>Tianhe-2A</b> - TH-IVB-FEP Cluster, Intel Xeon E5-2692v2 12C 2.2GHz, TH Express-2, Matrix-2000, NUDT National Super Computer Center in Guangzhou China	4,981,760	61.44	100.68	18,482
10	<b>Adastra</b> - HPE Cray EX235a, AMD Optimized 3rd Generation EPYC 64C 2GHz, AMD Instinct MI250X, Slingshot-11, HPE Grand Equipement National de Calcul Intensif - Centre Informatique National de l'Enseignement Suprieur (GENCI-CINES) France	319,072	46.10	61.61	921



# Snellius Supercomputer

- 72 GPU nodes
- Each node has 4 A100 NVIDIA GPU devices
- In total 288 GPUs

# GPU CPU Connectivity



# GPU Usability

- How to Use GPUs?

# GPU Usability

## 3 Ways to Accelerate Applications

Applications

Libraries

OpenACC  
Directives

Programming  
Languages

“Drop-in”  
Acceleration

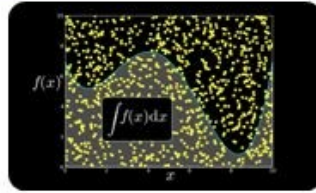
Easily Accelerate  
Applications

Maximum  
Flexibility

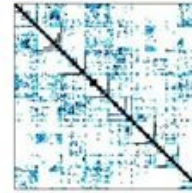
# GPU Libraries



NVIDIA cuBLAS



NVIDIA cuRAND



NVIDIA cuSPARSE



NVIDIA NPP

**GPU VSIPL**

Vector Signal  
Image Processing

**CULA** | tools

GPU Accelerated  
Linear Algebra



Matrix Algebra on  
GPU and Multicore



NVIDIA cuFFT



IMSL Library



Building-block  
Algorithms for CUDA

**CUSP**

Sparse Linear  
Algebra



C++ STL Features  
for CUDA



**GPU Accelerated Libraries**

"Drop-in" Acceleration for Your Applications

# GPU Usability

## 3 Ways to Accelerate Applications

Applications

Libraries

OpenACC  
Directives

Programming  
Languages

“Drop-in”  
Acceleration

Easily Accelerate  
Applications

Maximum  
Flexibility

# OpenACC/OpenMP

- OpenACC stands for Open Accelerators
- OpenMP stands for Open Multi-Processing
- Directive-based APIs
- Simple compiler hints to parallelize the code

# GPU Usability

## 3 Ways to Accelerate Applications

Applications

Libraries

“Drop-in”  
Acceleration

OpenACC  
Directives

Easily Accelerate  
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Maximum  
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# GPU Programming Languages

**Numerical analytics** ▶

MATLAB, Mathematica, LabVIEW

**Fortran** ▶

CUDA Fortran, OpenACC,  
OpenMP4.5

**C** ▶

CUDA C, OpenCL, OpenACC,  
OpenMP4.5

**C++** ▶

CUDA C++, Thrust, OpenCL,  
OpenACC/OpenMP4.5

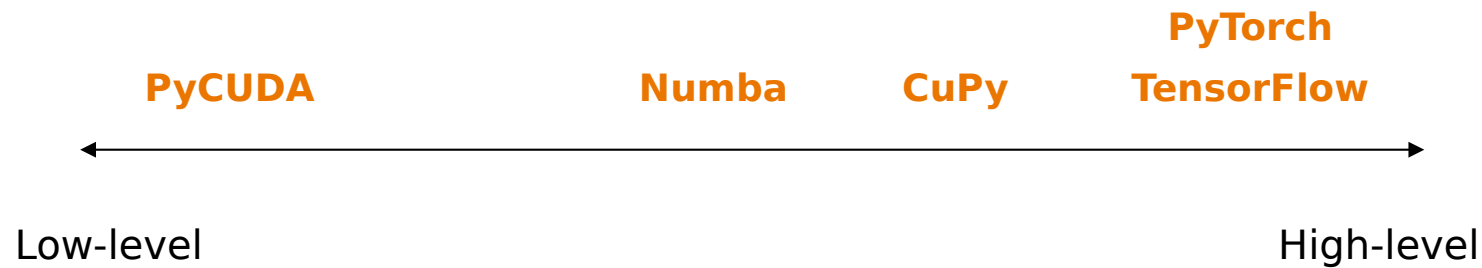
**Python** ▶

PyCUDA/PyOpenCL, Numba, ...

# Core GPU Programming

- Nvidia GPUs:
  - CUDA, OpenCL, HIP
- AMD GPUs:
  - OpenCL, HIP
- Intel GPUs:
  - OpenCL

# Accessing to GPUs in Python



# PyTorch/TensorFlow

- They are powerful and mature deep learning libraries
- They benefit from GPUs without knowing GPU programming knowledge
- They are open sources
- They are taught in machine learning courses

# CuPy vs NumPy



```
import numpy as np
X_cpu = np.zeros((10,))
W_cpu = np.zeros((10, 5))
y_cpu = np.dot(x_cpu, W_cpu)
```



```
import cupy as cp
x_gpu = cp.zeros((10,))
W_gpu = cp.zeros((10, 5))
y_gpu = cp.dot(x_gpu, W_gpu)
```

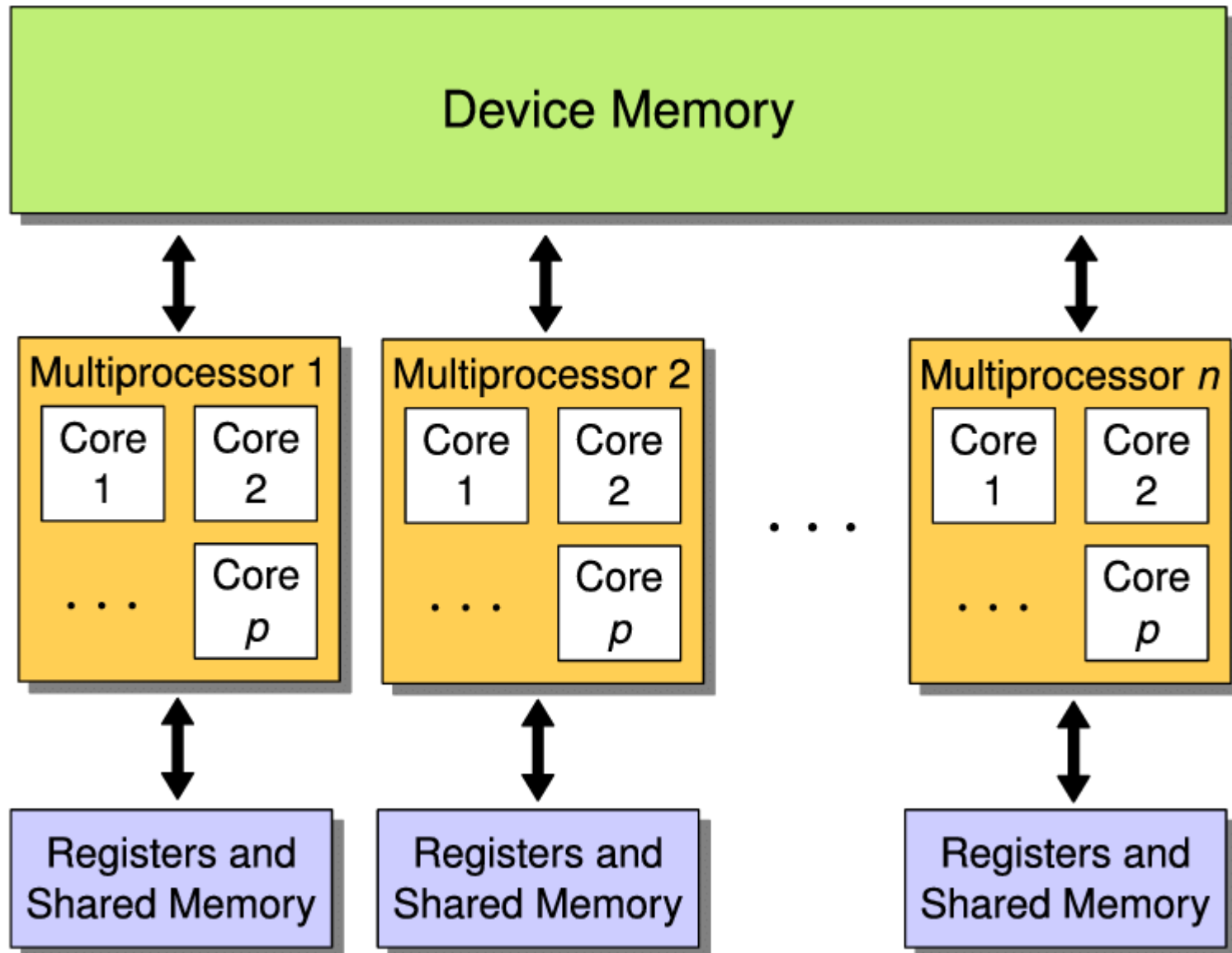
# Numba

- It is an open-source Just-In Time (JIT) compiler that translates a subset of Python and Numpy into GPU machine code.
- It uses a collection of decorators that can be applied to your functions to instruct Numba to compile them.
- For more information: <https://numba.pydata.org/>

# PyCUDA

- It gives you easy, Pythonic access to NVIDIA's CUDA parallel computation API.
- There is more flexibility to write custom CUDA kernels
- For more information: <https://documen.tician.de/pycuda/>

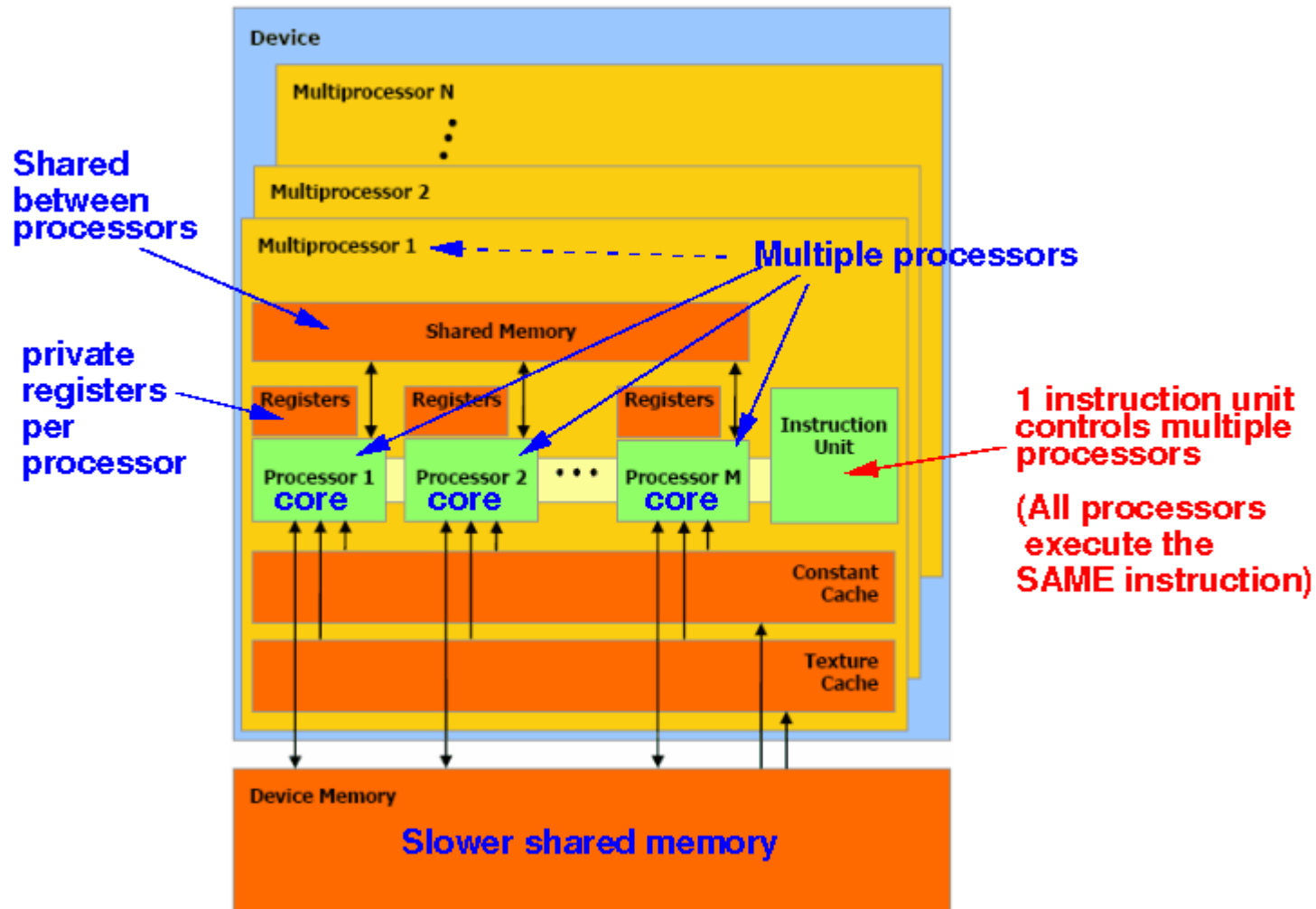
# NVIDIA GPU Hardware





# NVIDIA GPU Hardware

GPU device:



# Flynn's classical taxonomy

		Instruction stream	
		Single	Multiple
Data stream	Single	SISD	MISD
	Multiple	SIMD	MIMD

# CUDA Programming Model

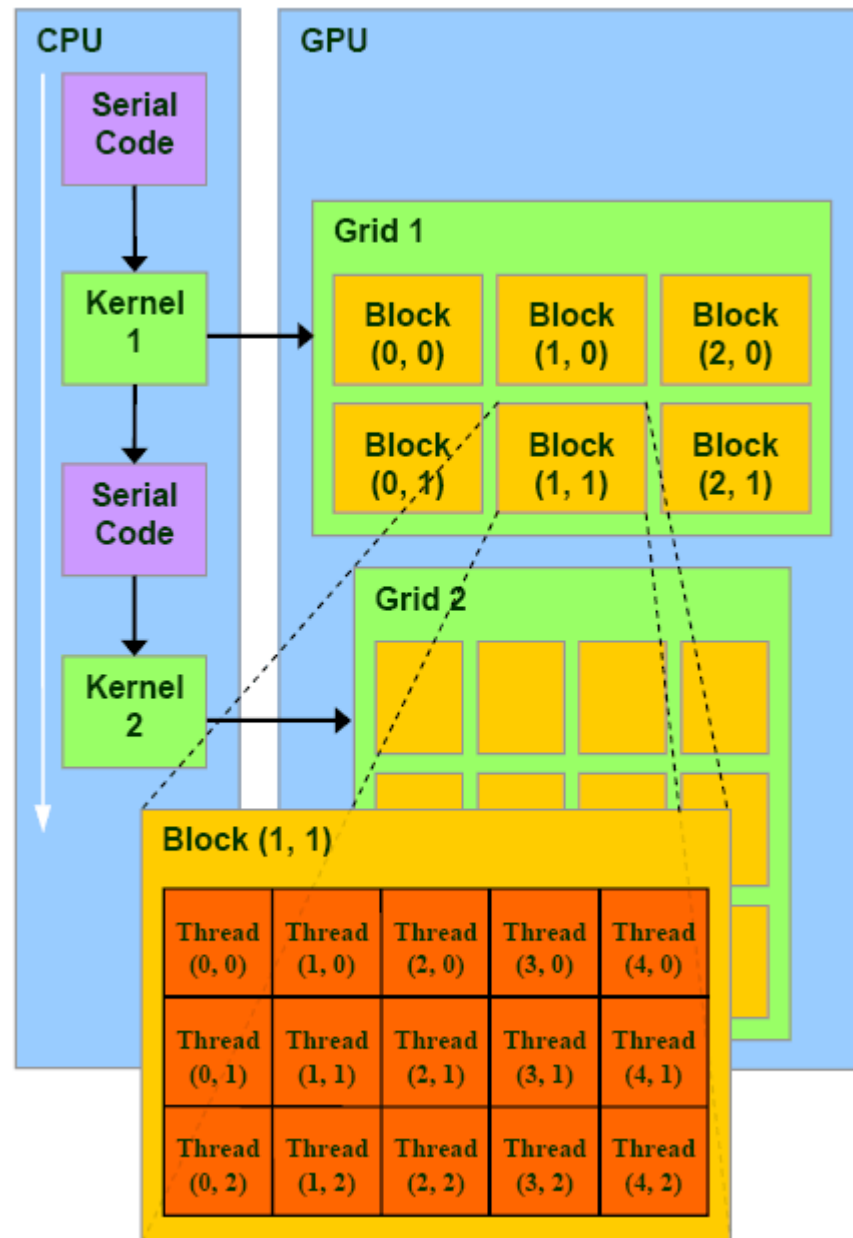
- Introduced by NVIDIA in 2006, Compute Unified Device Architecture
- General purpose programming model that leverages the parallel compute engine in NVIDIA GPUs
- An extension of C language
- CUDA programs are CPU-GPU programs:
  - CPU part is called *host*
  - GPU part is called *kernel*

# CUDA Programming Model

To execute any CUDA program, there are three main steps:

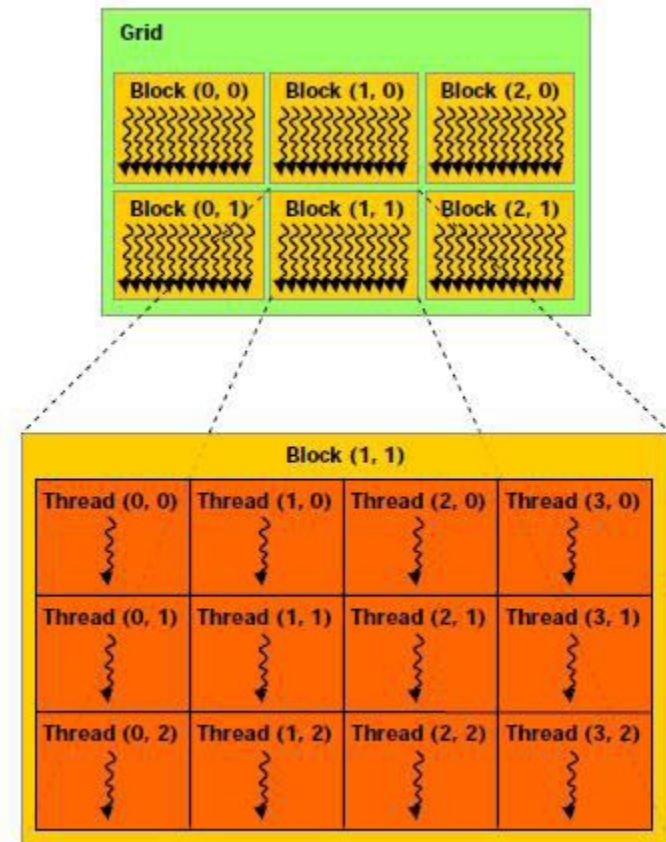
- Copy the input data from host memory to device memory, also known as host-to-device transfer
- Call the kernel from host and execute the GPU program
- Copy the results from device memory to host memory, also called device-to-host transfer

# CUDA Programming Model



# CUDA Programming Model

- Threads are organized into two hierarchical levels:
  - Threads are grouped into *blocks*
  - Blocks are grouped into *grids*
- Blocks and grids can be 1D, 2D and 3D



# CUDA Programming Model

- Built-in functions:

- Dimension:

- `gridDim.x`, `gridDim.y`, `gridDim.z`
    - `blockDim.x`, `blockDim.y`, `blockDim.z`

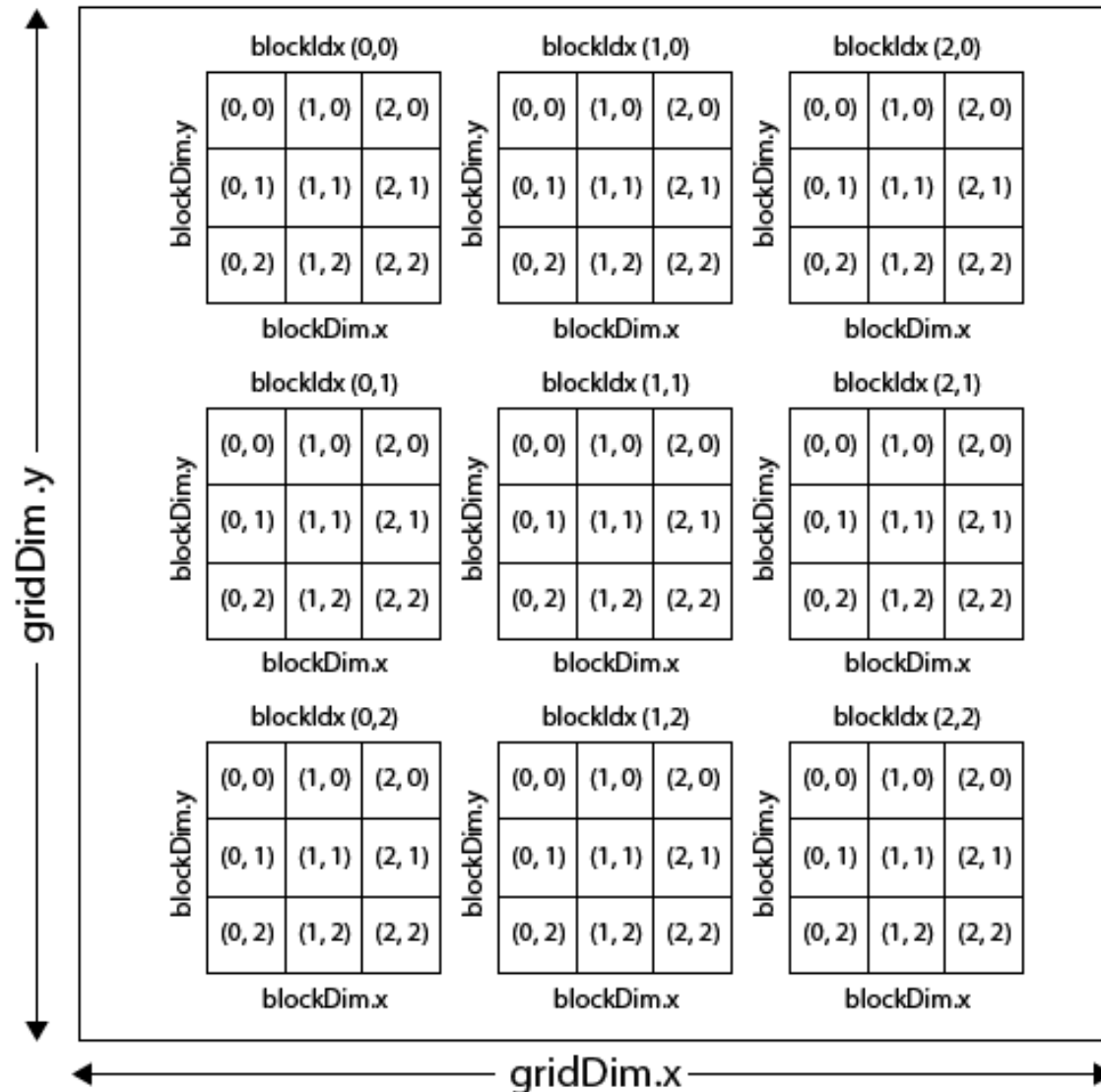
- Index:

- `blockIdx.x`, `blockIdx.y`, `blockIdx.z`
    - `threadIdx.x`, `threadIdx.y`, `threadIdx.z`

# CUDA Programming Model

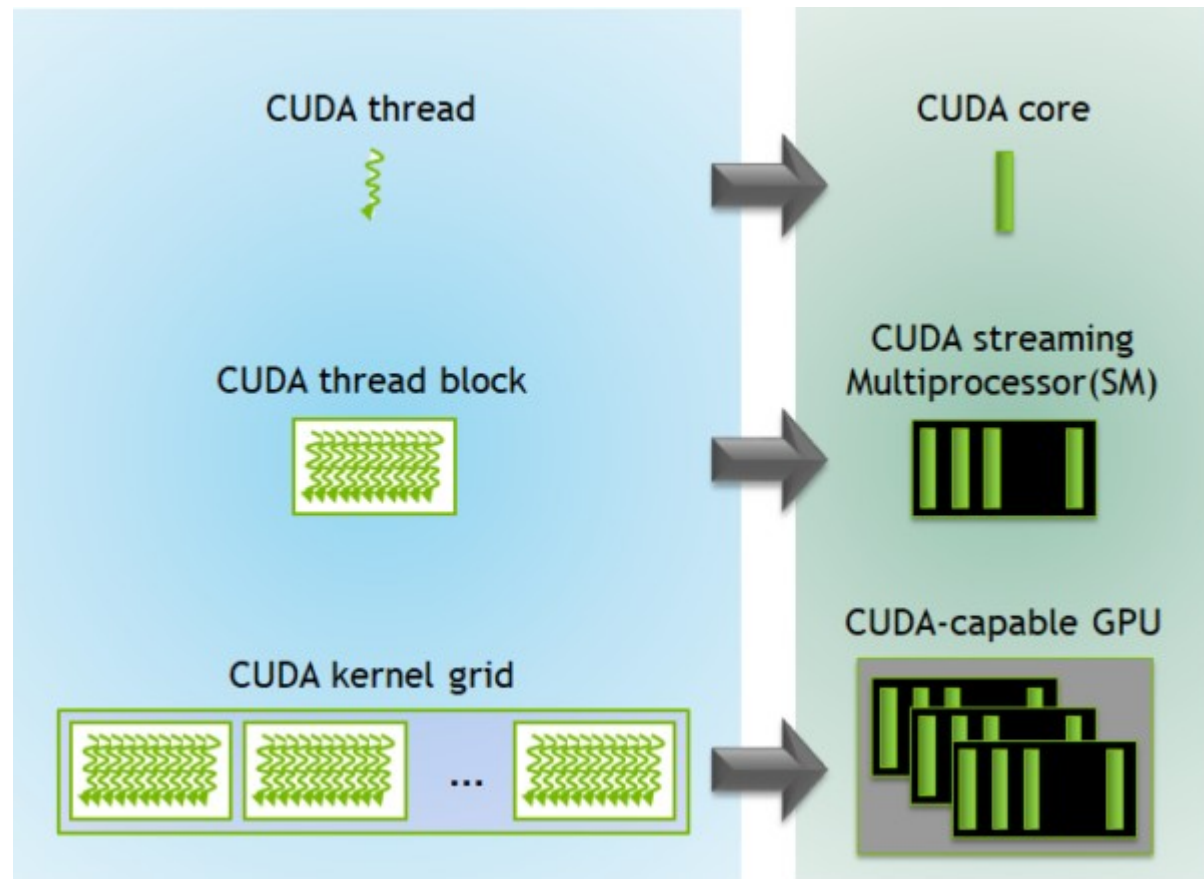
## CUDA Grid

- gridDim.x = 3
- gridDim.y = 3
- blockDim.x = 3
- blockDim.y = 3

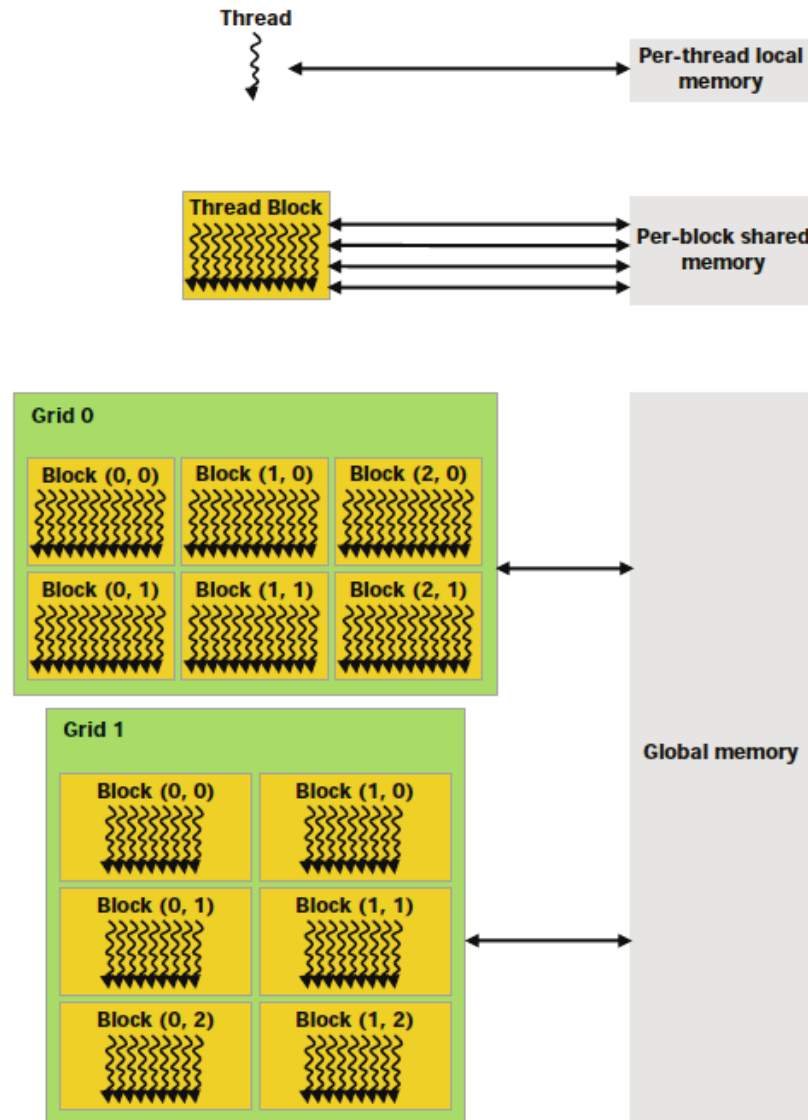




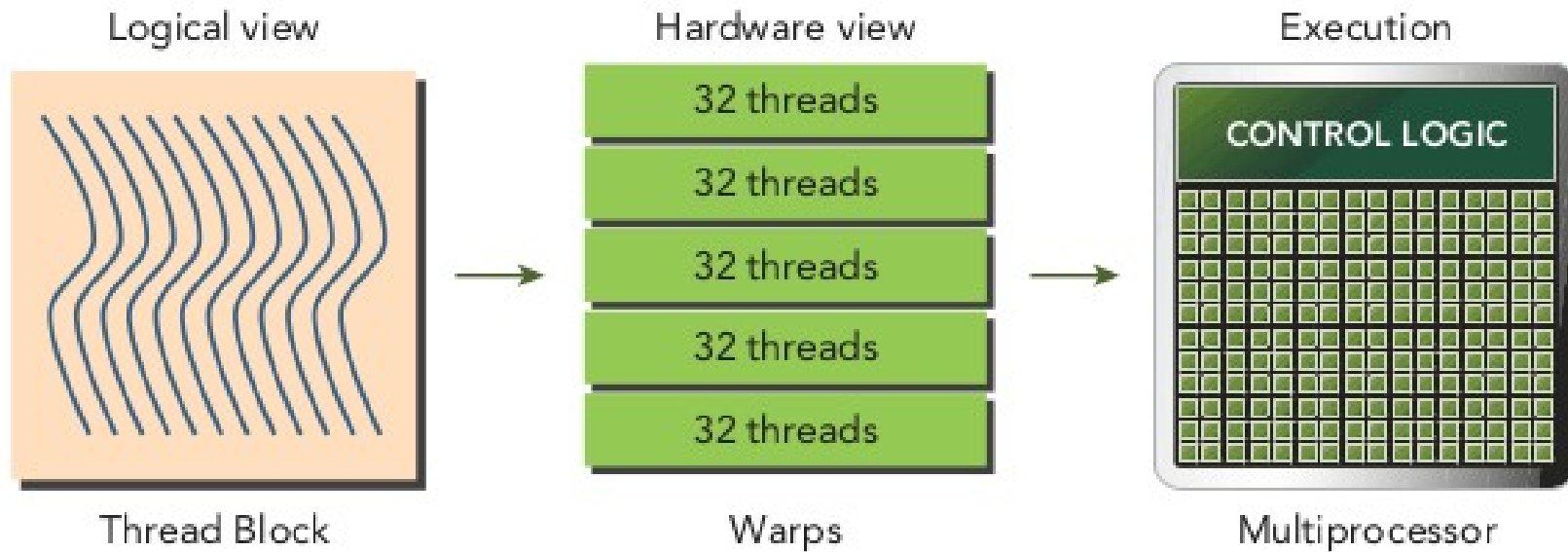
# CUDA Execution Model



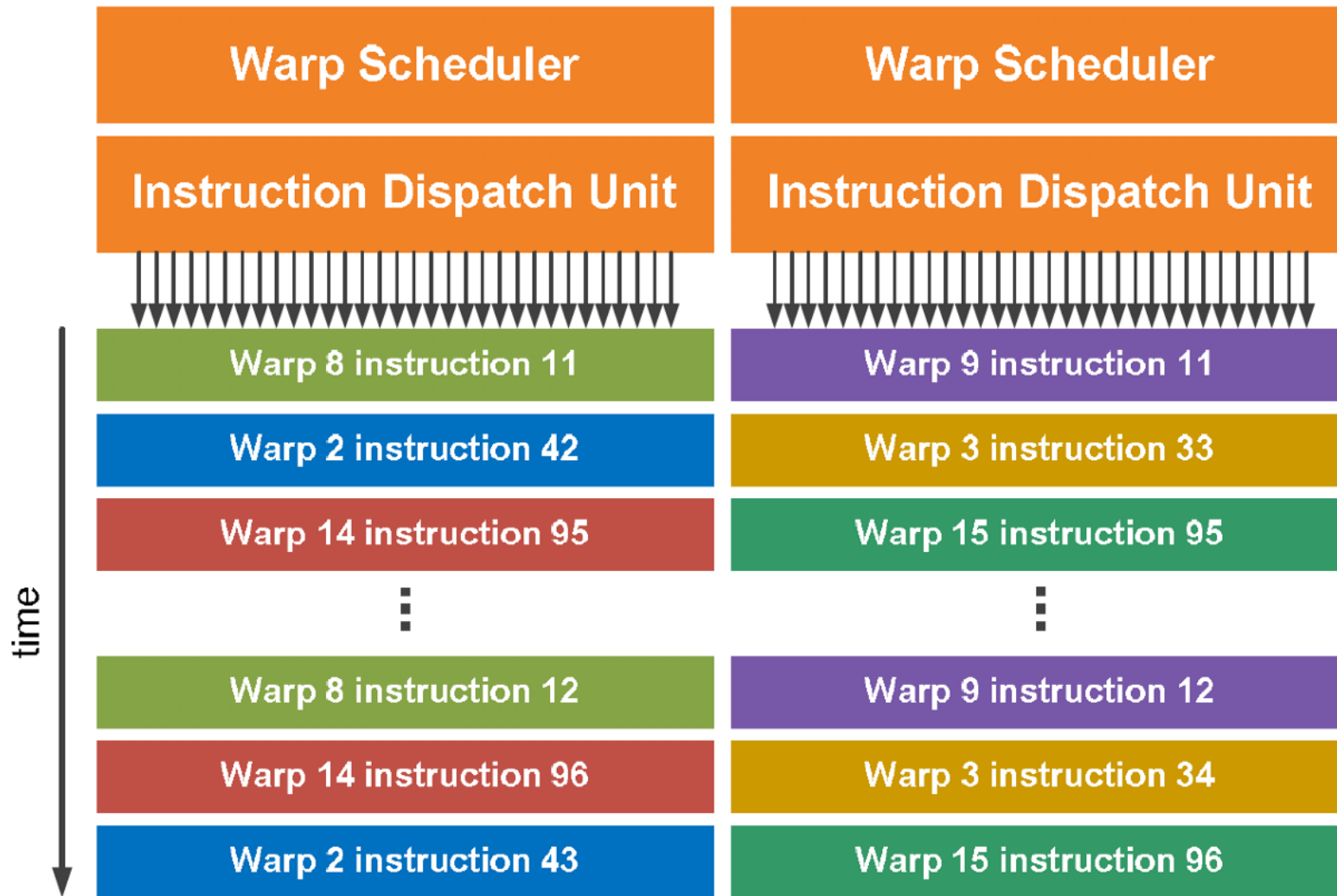
# CUDA Execution Model



# CUDA Execution Model



# CUDA Execution Model



# Synchronization in CUDA

- There is a mechanism to synchronize all threads in a block:
  - Built-in function `__syncthreads()`
- There is no mechanism to synchronize all threads across all blocks
  - Decouple the kernel into two separate kernels

# GPU Node

- 4 NVIDIA A100 GPUs per node
  - Multiprocessors: 108
  - Streaming cores: 6912
  - Tensor Cores: 432
  - Global memory: 40 GB
- MIG partitions: 1/7th of A100 GPUs
- One GPU is shared among 7 people
- Note that you have around 5 GB memory:
  - Matrix  $(35,000 * 35,000) = 35,000 * 35,000 * 4 \approx 5 \text{ GB}$

First Example:

Parallel Vector (1D array) Addition in  
PyCUDA

# Calculate Global Index (1D grid, 1D block)

Global Thread ID

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
threadIdx.x								threadIdx.x								threadIdx.x								threadIdx.x							
0	1	2	3	4	5	6	7	0	1	2	3	4	5	6	7	0	1	2	3	4	5	6	7	0	1	2	3	4	5	6	7
blockIdx.x = 0								blockIdx.x = 1								blockIdx.x = 2								blockIdx.x = 3							

- Global Thread ID:  $\text{blockIdx.x} * \text{blockDim.x} + \text{threadIdx.x}$
- For global thread ID 26:
  - $\text{blockIdx.x} = 3$
  - $\text{blockDim.x} = 8$
  - $\text{threadIdx.x} = 2$
  - Global thread ID =  $3 * 8 + 2 = 26$



# PyCUDA Implementation

- Implement vector addition in PyCUDA
- Compare its execution time to the sequential version

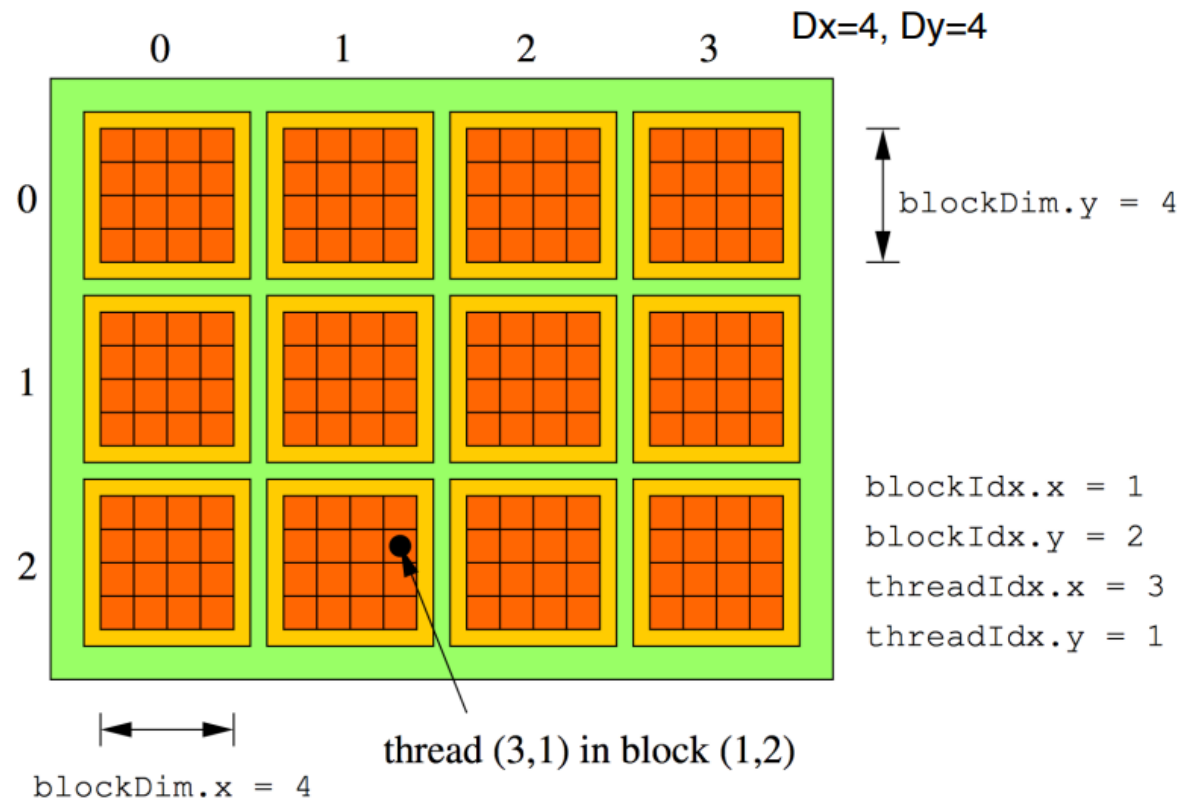
# Automatic Data Transfer

- Automatic data transfer using PyCUDA driver:
  - In()
  - Out()
  - InOut()
- PyCUDA programs become simpler

Second Example:

Parallel Matrix (2D array) Addition in  
PyCUDA

# Calculate Global Index (2D grid, 2D block)



Matrix 12\*16

Global Thread ID:

- $\text{row} = \text{blockIdx.y} * \text{blockDim.y} + \text{threadIdx.y} = 2 * 4 + 1 = 9$
- $\text{column} = \text{blockIdx.x} * \text{blockDim.x} + \text{threadIdx.x} = 1 * 4 + 3 = 7$

# Row-Major Flattening of a Matrix

- Matrix 3\*3
- For each element (row, col):
  - New ID = row \* (No of col) + col
- For instance element “5” in location (1, 2):
  - New ID =  $1 * 3 + 2 = 5$

How we see a 2D array

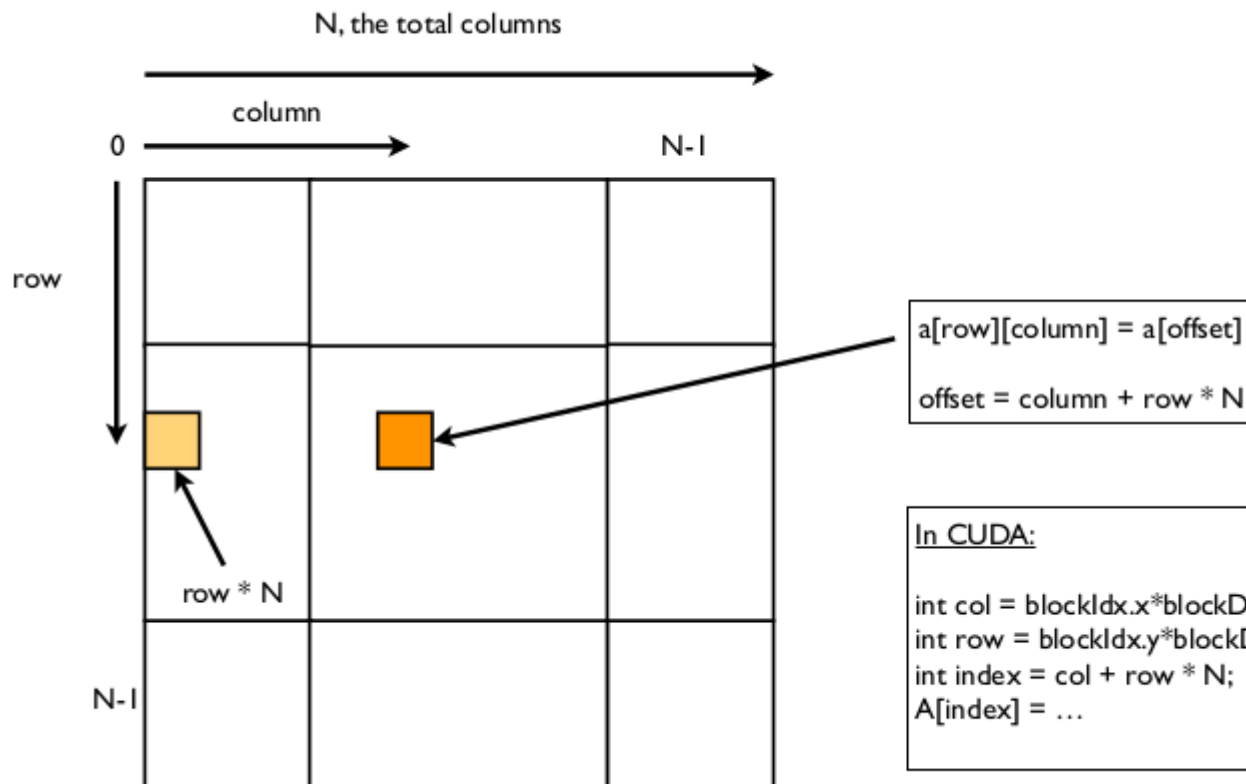
0	1	2
3	4	5
6	7	8



How it's stored in memory

0	1	2	3	4	5	6	7	8
---	---	---	---	---	---	---	---	---

# Row-Major Flattening of a Matrix



# PyCUDA Implementation

- Implement matrix addition in PyCUDA
- Compare its execution time to the sequential version

# Exercise 1

- Try to transpose a matrix in parallel using PyCUDA
- Compare its execution time to the sequential version



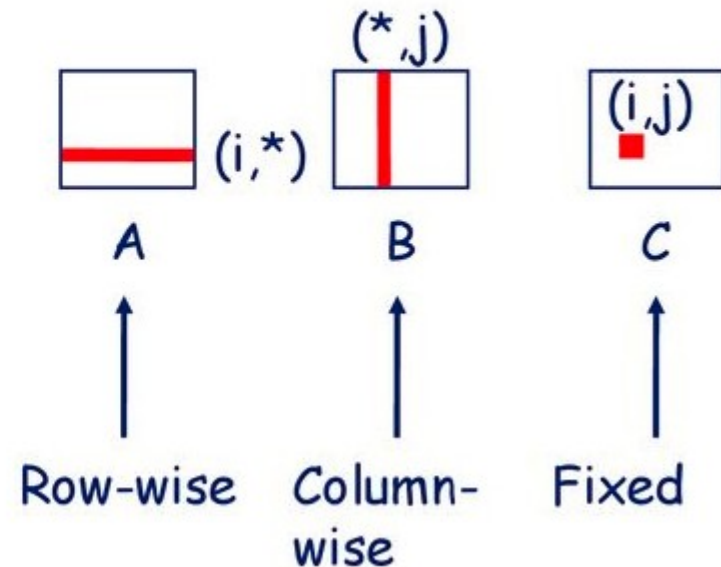
Third Example:

Parallel Matrix (2D array) Multiplication  
in PyCUDA

# Sequential Matrix Multiplication

```
/* ijk */
for (i=0; i<n; i++) {
  for (j=0; j<n; j++) {
    sum = 0.0;
    for (k=0; k<n; k++)
      sum += a[i][k] * b[k][j];
    c[i][j] = sum;
  }
}
```

Inner loop:



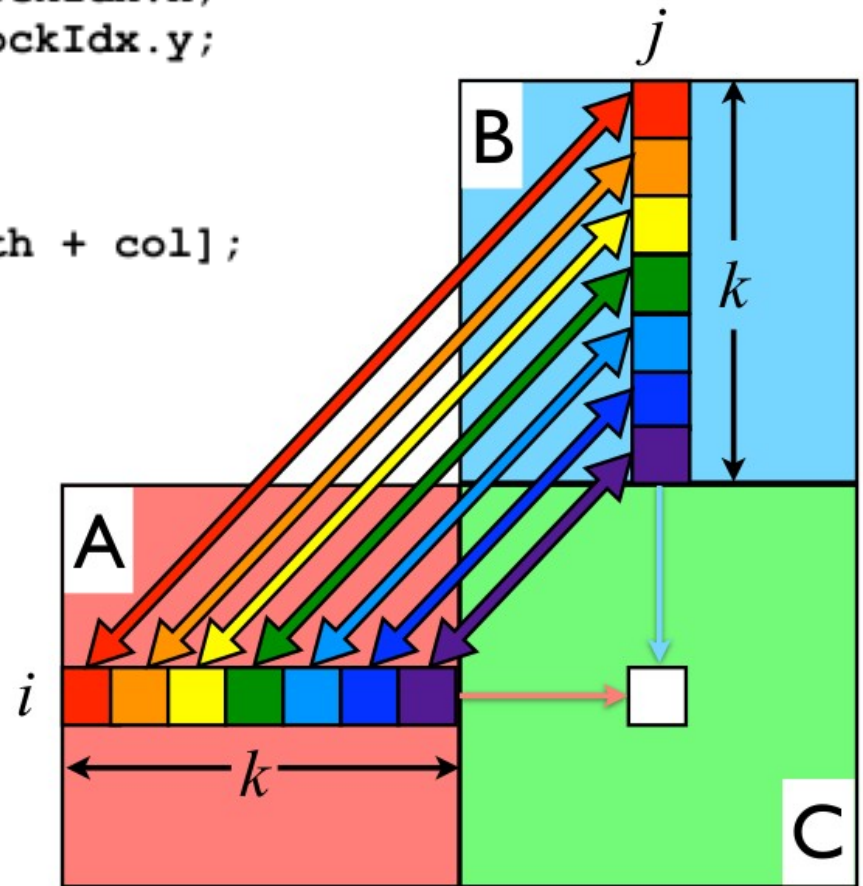
$$\begin{bmatrix} a & b \\ c & d \end{bmatrix}_A \times \begin{bmatrix} e & f \\ g & h \end{bmatrix}_B = \begin{bmatrix} ae + bg & af + bh \\ ce + dg & cf + dh \end{bmatrix}_C$$

# Parallel Matrix Multiplication

```
int k, sum = 0;

int col = threadIdx.x + blockDim.x * blockIdx.x;
int row = threadIdx.y + blockDim.y * blockIdx.y;

if(col < width && row < width) {
    for (k = 0; k < width; k++)
        sum += a[row * width + k] * b[k * width + col];
    c[row * width + col] = sum;
}
```

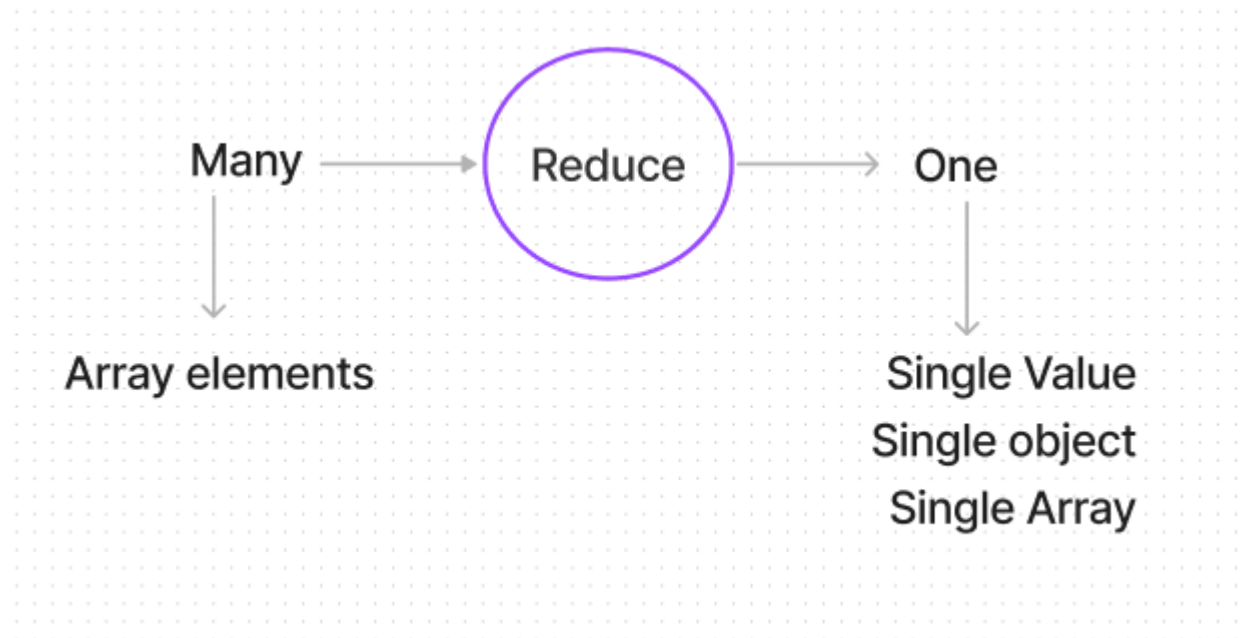


# PyCUDA Implementation

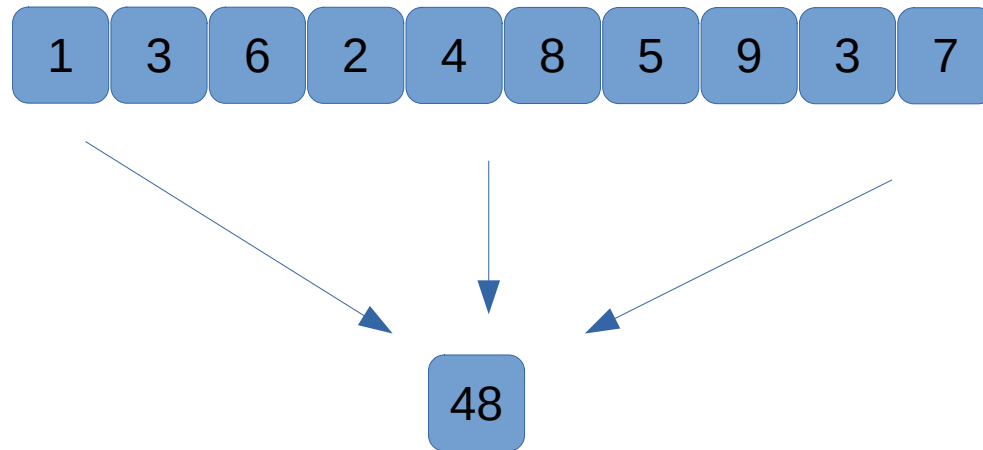
- Implement matrix multiplication in PyCUDA
- Compare its execution time to
  - Sequential CPU-based
  - Numpy.matmul()
  - @ operator

## Fourth Example: Reduction in PyCUDA

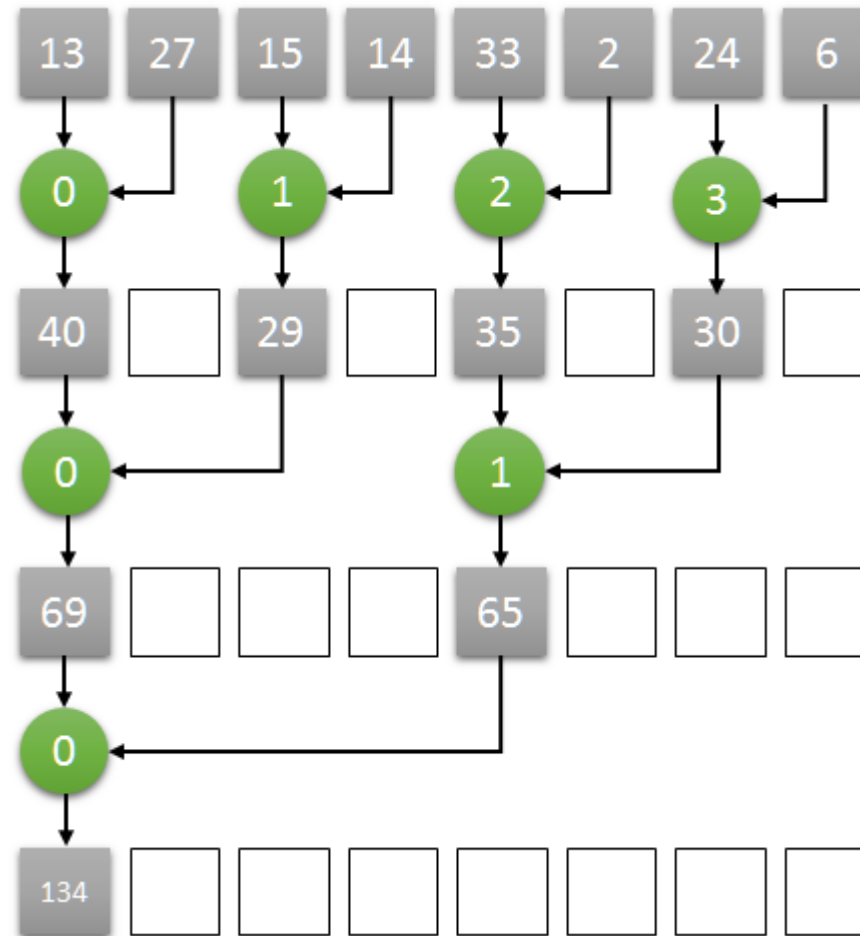
# Reduction



# Reduction (addition)

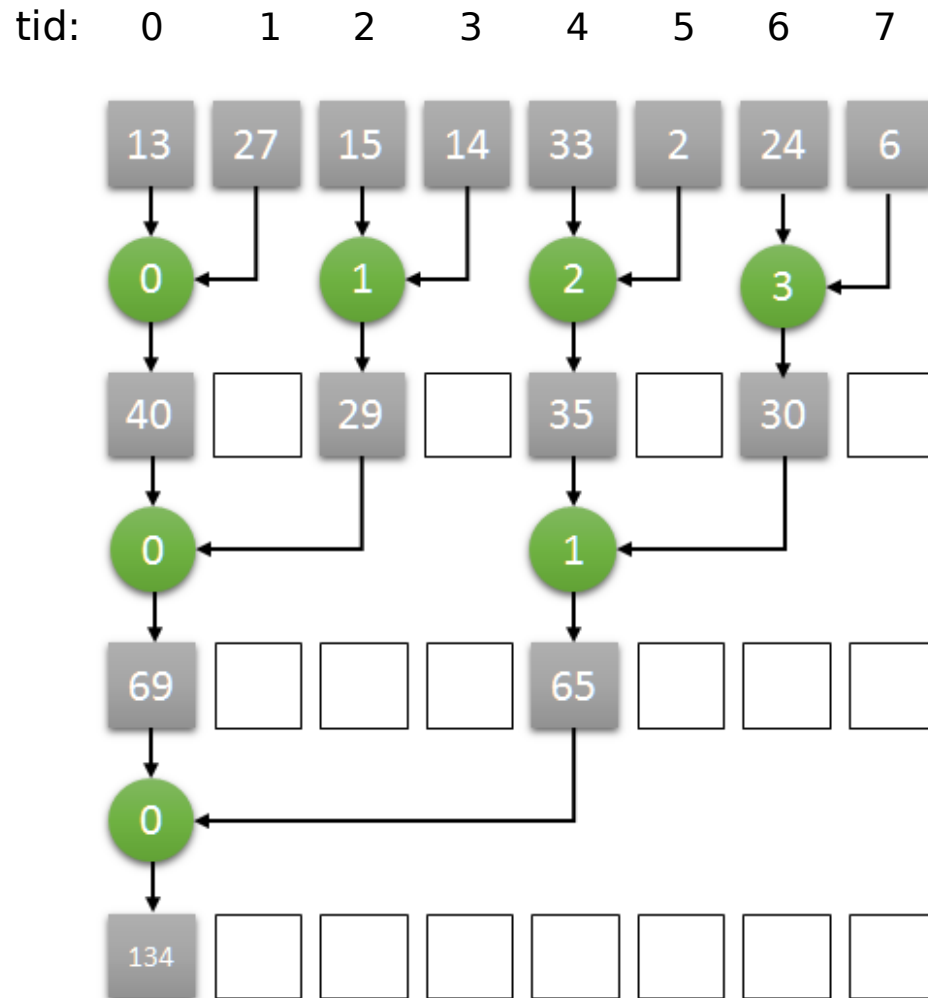


# Reduction (addition)





# Reduction (addition)



level

1  $(tid \% 2 == 0) ==> a[tid] += a[tid+1]$

2  $(tid \% 4 == 0) ==> a[tid] += a[tid+2]$

3  $(tid \% 8 == 0) ==> a[tid] += a[tid+4]$

4  $(tid \% 16 == 0) ==> a[tid] += a[tid+8]$

$(tid \% (2^{\text{level}}) == 0) ==> a[tid] += a[tid + 2^{(\text{level}-1)}]$

# PyCUDA Implementation

- Implement reduction in PyCUDA using one thread block
- Compare its execution time to the sequential version and Python reduce operator

# PyCUDA Implementation

- Extend it to use arbitrary size (i.e., multiple thread blocks)
- Compare its execution time to the sequential version and Python reduce operator

# PyCUDA Implementation

- How to use shared memory in reduction?
- Compare its execution time to the sequential version and Python reduce operator

# Exercise 2

- Reduce an array using other operators (subtraction, multiplication, etc.)

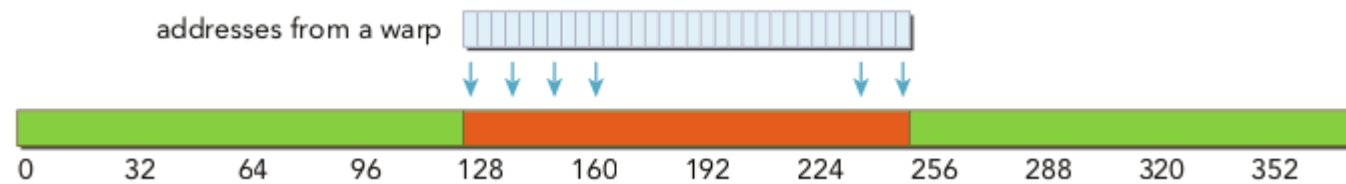
# Optimization

There are different ways to optimize CUDA codes:

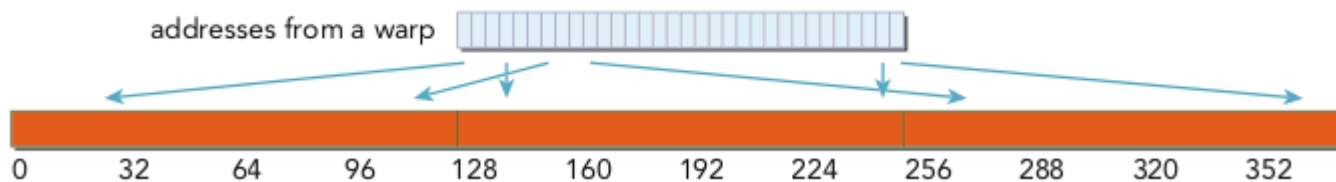
- Number of threads per block
- Workload per thread
- Total work per thread block
- Correct memory access and data locality
- ...

# Tips for Optimization

- Global Memory Access:



Coalesced

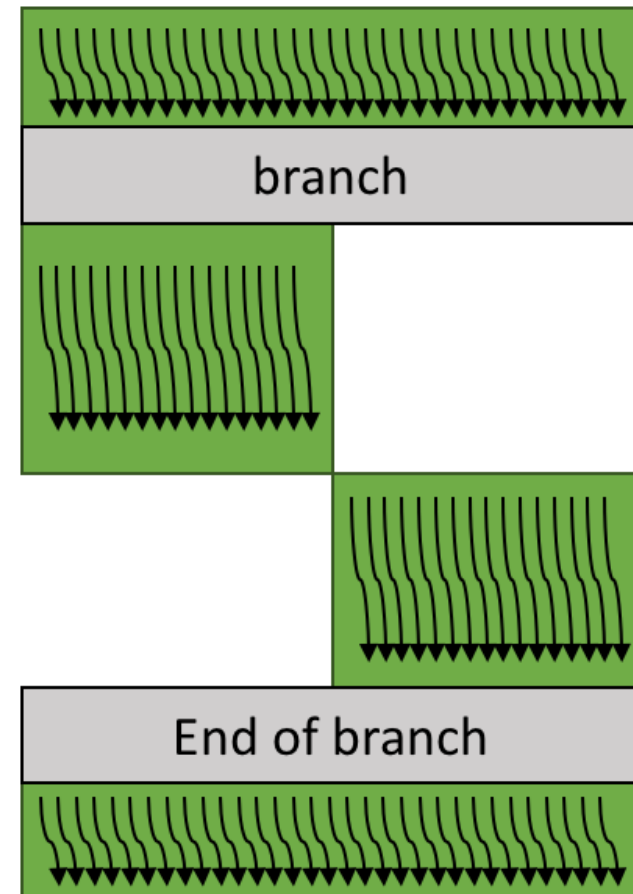


Non-coalesced

# Tips for Optimization

- Avoid Warp Divergence:

```
...  
if ( threadIdx.x < 16 )  
{  
    ... A ...  
}  
else  
{  
    ... B ...  
}  
...
```



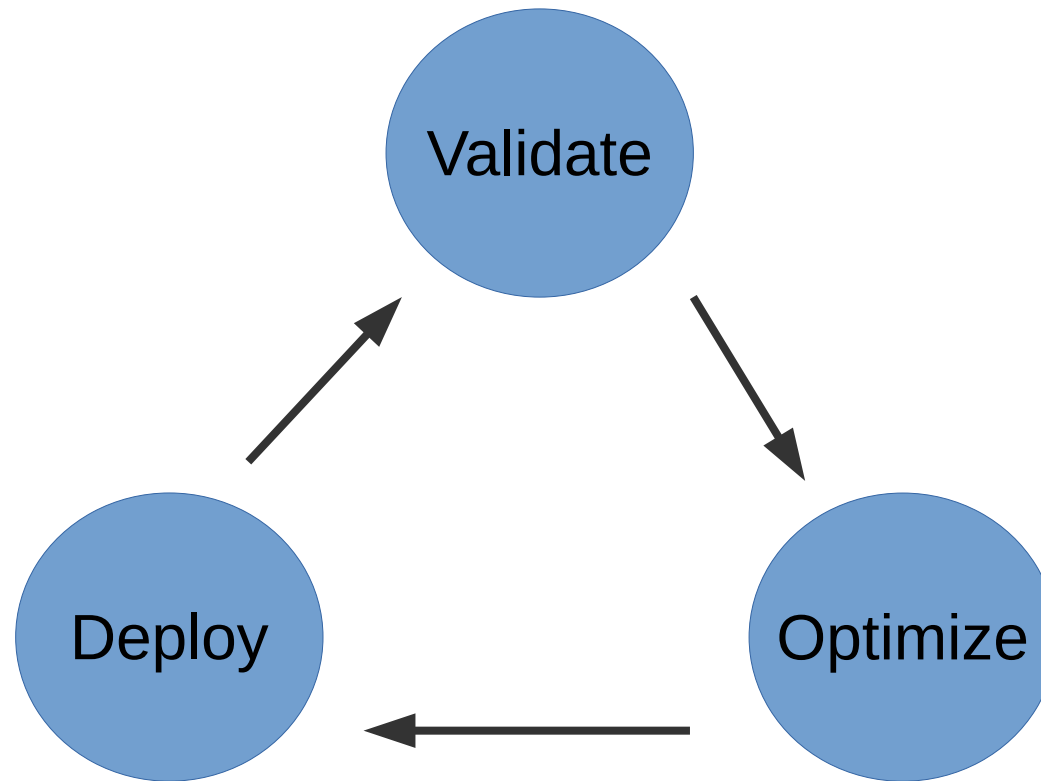


# Tips for Optimization

- Use shared memory in two cases:

- When threads in a block need to shared data
- When there are repeated accesses to one location in global memory
  - In this case, it is possible to use registers as local memory to each thread

# GPU Development Cycle



# Data Races

- A data race is a situation where two or more threads may access the same memory location simultaneously and at least one of them is a write
- It causes undefined behavior of programs

# Data Race Example

```
__global__ void kernel(int *arr)
{
    arr += 1;
}
```

- One solution is to use built-in atomic operations in GPU programming languages

# Data Race Example

```
__global__ void kernel(int *arr, int size)
{
    if (tid < size-1)
    {
        arr[tid] += arr[tid+1];
    }
}
```

- One solution is to use synchronization methods in GPU programming

# Barrier Divergence

- A barrier divergence happens when threads from the same thread block diverge and hit different (syntactical) barriers

# Barrier Divergence Example

```
__global__ void kernel(...){  
    if (tid % 2 == 0){  
        ....  
        syncthreads();  
        ....  
    } else{  
        ...  
        syncthreads(); }  
}
```

# Questions

Thank you for participating! Any questions?