## **SPRING Summary**

Hercy saves money as follows:

- On Monday, he deposits \$1.
- Each next day (Tue-Sun), he deposits \$1 more than the previous day.
- Every next Monday, he starts with \$1 more than the previous Monday.

Find the total money in the bank after n days.

### **IIII** Mathematical Concept Used → Arithmetic Progression (AP)

Each week forms an AP (Arithmetic Progression):

Monday to Sunday → difference = 1

Example week pattern:

Week	Monday	Tuesday	Wednesday	Thursday	Friday	Saturday	Sunday	Weekly To
1	1	2	3	4	5	6	7	28
2	2	3	4	5	6	7	8	35
3	3	4	5	6	7	8	9	42

# Formula Derivation

Let

- n = total number of days
- w = n//7 (full weeks)
- d = n%7 (remaining days)

#### 1 Total of full weeks:

Each week increases its base deposit by 1.

Sum of full weeks = 
$$7 \times \frac{w(w-1)}{2} + 28w$$

#### Remaining days:

Start of next week deposit = w + 1

Sum of remaining days = 
$$d \times (w+1) + \frac{d(d-1)}{2}$$

3 Final Total:

Total = 
$$[7 \times \frac{w(w-1)}{2} + 28w] + [d \times (w+1) + \frac{d(d-1)}{2}]$$

#### Python Code Implementation

```
class Solution(object): def totalMoney(self, n): """ :type n: int :rtype: int """ # Full weeks and remaining days weeks = n // \frac{7}{7} days = n % \frac{7}{7} # Formula for full weeks total = \frac{7}{7} * weeks * (weeks - \frac{1}{7}) // \frac{2}{7} + \frac{28}{7} * weeks # Add remaining days total += days * (weeks + \frac{1}{7}) + (days * (days - \frac{1}{7})) // \frac{2}{7} return total
```

## $\blacksquare$ Example: n = 20

Week	Days Deposited	Deposits Each Day	Weekly Total
1	7	1, 2, 3, 4, 5, 6, 7	28
2	7	2, 3, 4, 5, 6, 7, 8	35

Week	Days Deposited	Deposits Each Day	Weekly Total
3	6	3, 4, 5, 6, 7, 8	33
Total	20 days		96



# Summary

Concept	Description
Туре	Arithmetic Progression (AP)
Formula Used	$S_n = \frac{n}{2}(2a + (n-1)d)$
Math Operations	Division, modulus, summation
Time Complexity	O(1) (no loops)
Space Complexity	O(1)