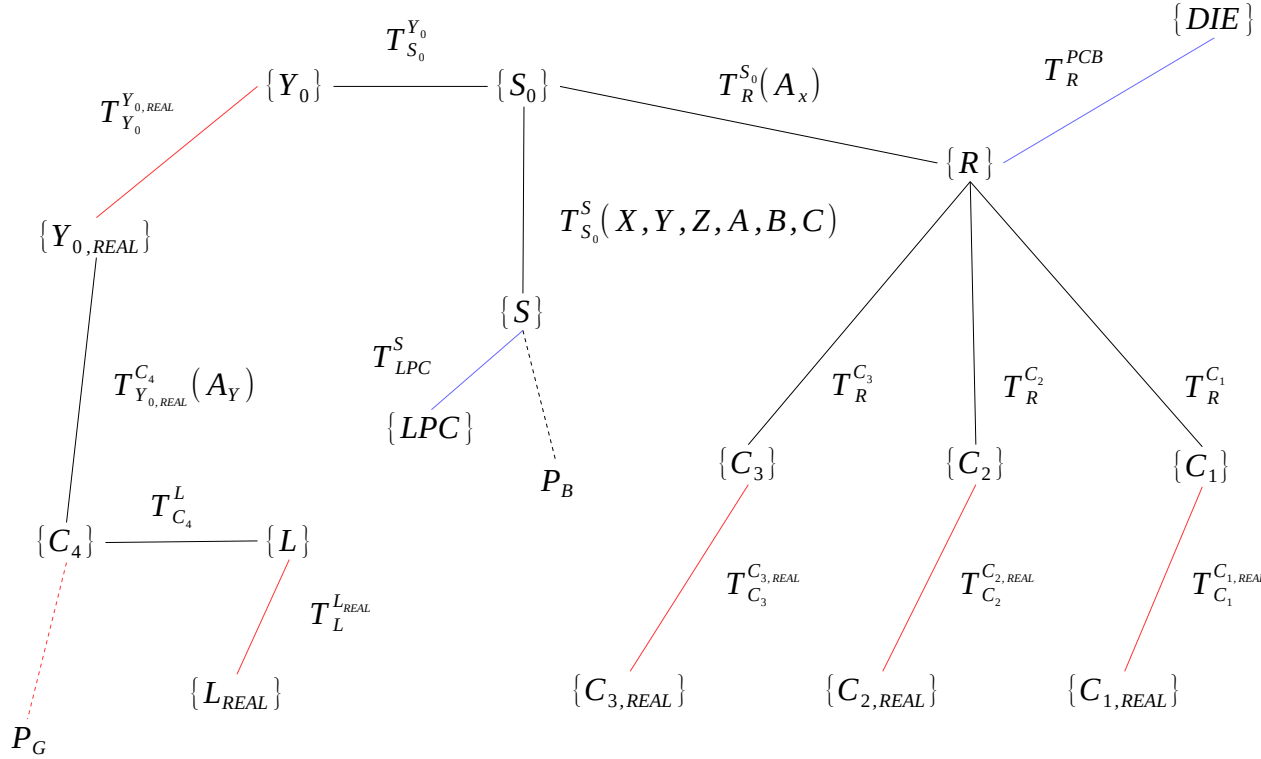


NOTATION: T_j^i represents fromFrame j toFrame i



Side/Bottom/Rear Calibration Chain

$$P_{C_i} = T_{C_i, REAL}^{C_i} T_{C_i}^R T_R^{S_0}(A_X) T_{S_0}^S(X, Y, Z, A, B, C) P_B$$

Top Calibration Chain

$$P_{C_4} = T_{C_4}^{Y_{0, REAL}}(A_Y) T_{Y_{0, REAL}}^{Y_0} T_{Y_0}^{S_0} T_{S_0}^R(A_X) P_R$$

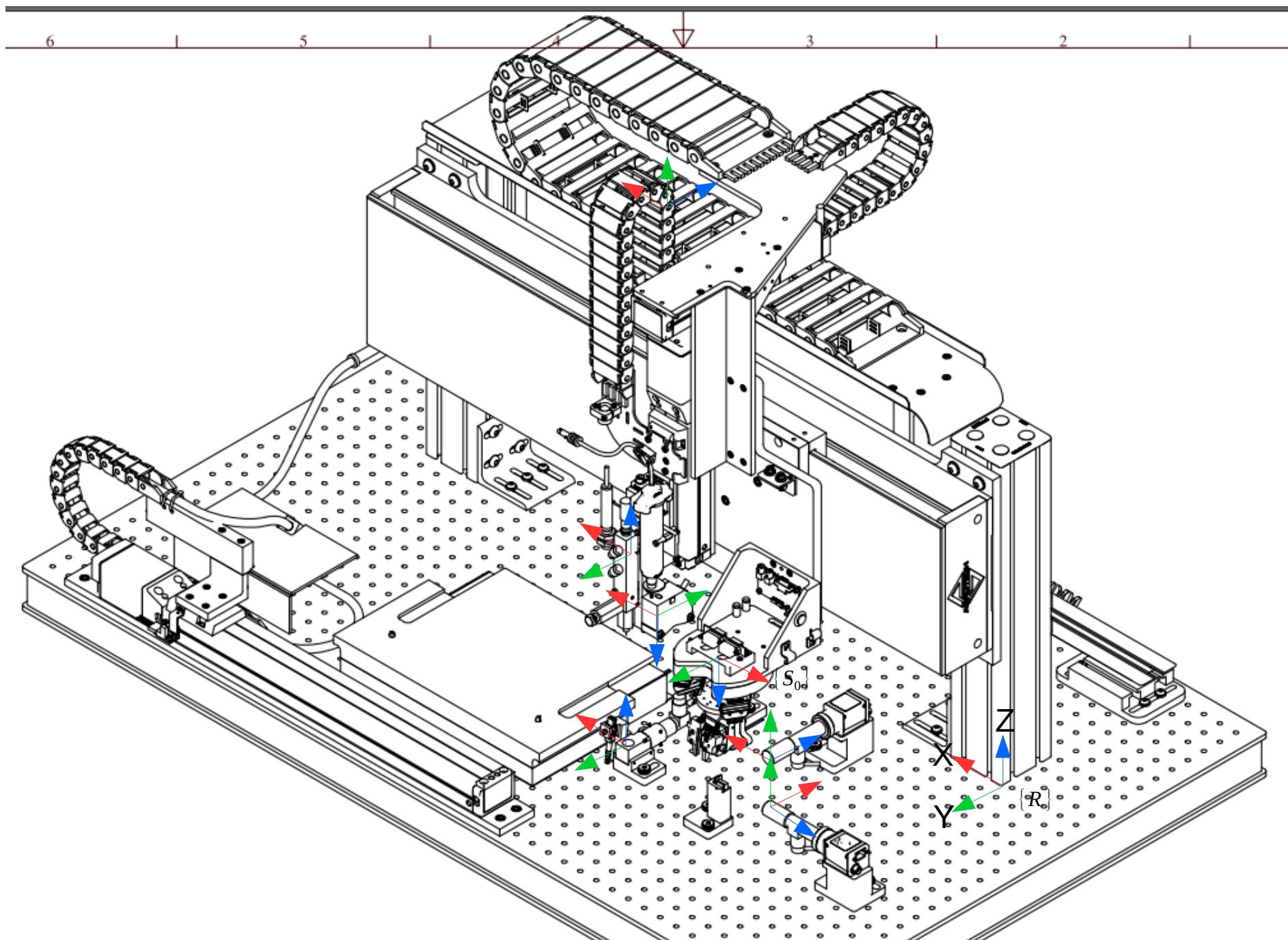
$$P_R = T_R^{C_3} T_{C_3}^{C_{3, REAL}} P_{C_{3, REAL}}$$

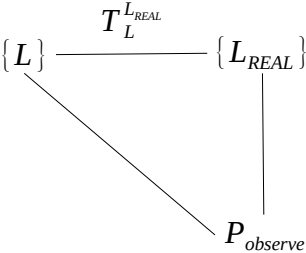
Distance Meter Calibration Chain

$$P_{L_{REAL}} = T_{L_{REAL}}^L T_L^{C_4} T_{C_4}^{Y_{0, REAL}}(A_Y) T_{Y_{0, REAL}}^{Y_0} T_{Y_0}^{S_0} T_{S_0}^R(A_X) P_R$$

$$P_R = T_R^{S_0} T_{S_0}^{Y_0} T_{Y_0}^{Y_{0, REAL}} T_{Y_{0, REAL}}^{C_4}(A_Y) P_{C_4}$$

$$V_R = T_R^{S_0}(A_{X,1}) T_{S_0}^{Y_0} T_{Y_0}^{Y_{0, REAL}} T_{Y_{0, REAL}}^{C_4}(A_{Y,1}) T_{C_4}^L T_L^{L_{REAL}} P_{L_{REAL,1}} - T_R^{S_0}(A_{X,2}) T_{S_0}^{Y_0} T_{Y_0}^{Y_{0, REAL}} T_{Y_{0, REAL}}^{C_4}(A_{Y,2}) T_{C_4}^L T_L^{L_{REAL}} P_{L_{REAL,2}}$$





$$P_{observer_l} = \begin{bmatrix} C_x \\ C_y \\ C_z \\ 1 \end{bmatrix} = T_L^{L_{REAL}} P_{observer_{real}} = \begin{bmatrix} 1 & -e_z & e_y & s_x \\ e_z & 1 & -e_x & s_y \\ -e_y & e_x & 1 & s_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ M_z \\ 1 \end{bmatrix}$$

$$P_r=\begin{bmatrix} Ax+Ay\,C_1+C_2\,Mz+C_3\\ Ay+C_4\,Mz+C_5\\ Ay\,C_9+C_6\,Mz+C_7 \end{bmatrix}$$

$$r^2=\big(Ay+C_4\,Mz+C_5\big)^2+\big(Ay\,C_9+C_6\,Mz+C_7\big)^2+\big(Ax+AyC_1+C_2\,Mz+C_3\big)^2$$

$$=\begin{bmatrix} A_x & A_y & Mz \end{bmatrix} \begin{bmatrix} 1 & C_1 & C_2 \\ C_1 & C_1^2+C_3^2+1 & C_1C_2+C_3C_6+C_4 \\ C_2 & C_1C_2+C_3C_6+C_4 & C_2^2+C_4^2+C_6^2 \end{bmatrix} \begin{bmatrix} A_x \\ A_y \\ Mz \end{bmatrix}$$