

# Interpretable **and accessible** Deep Learning for single-cell data analysis

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Martin Treppner

Institute of Medical Biometry and Statistics (IMBI)

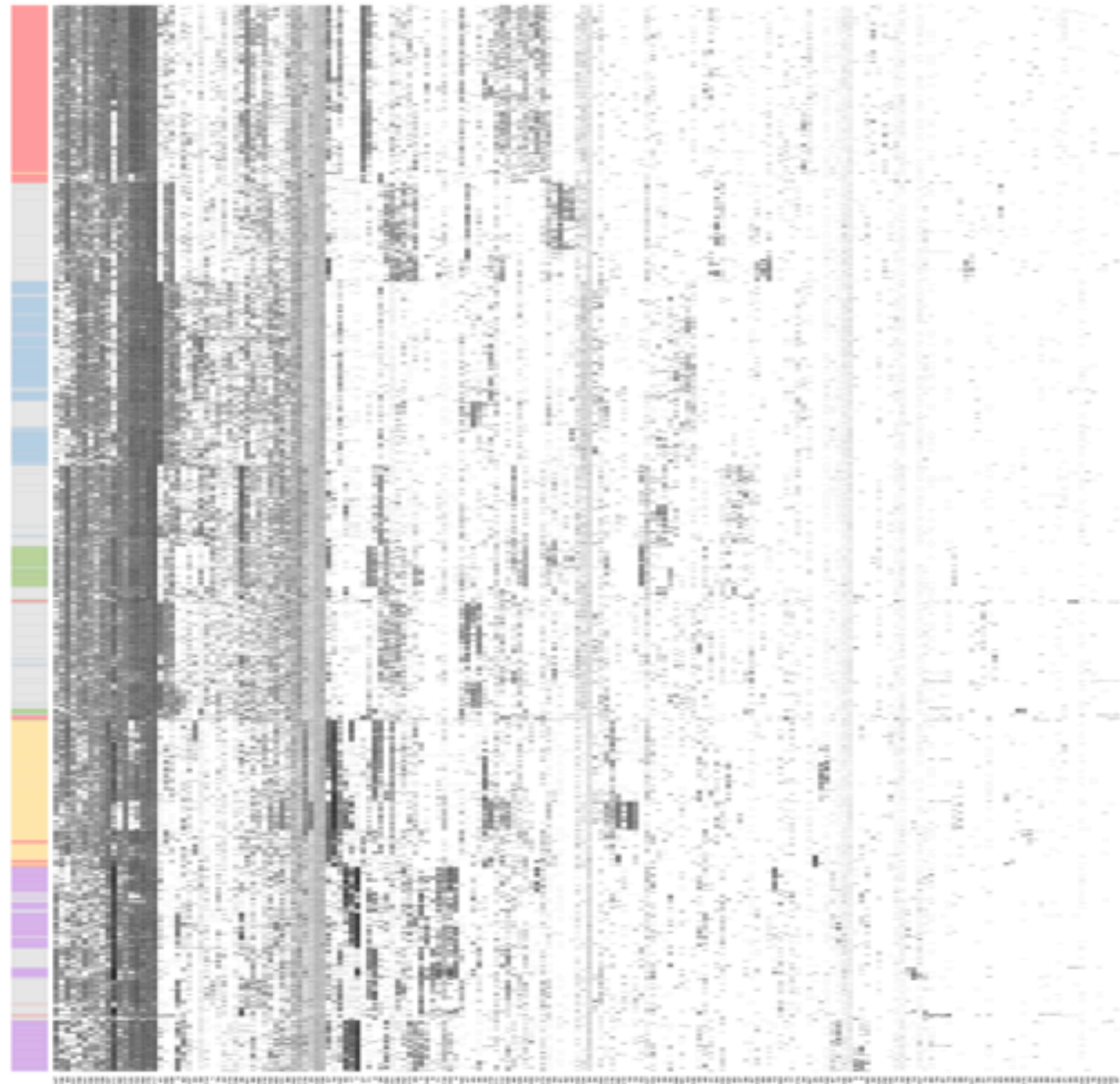
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# Gene expression - investigated in single cells

Genes



Cells

nature  
neuroscience

RESOURCE

## Adult mouse cortical cell taxonomy revealed by single cell transcriptomics

Bosiljka Tasic<sup>1,2</sup>, Vilas Menon<sup>1,2</sup>, Thuc Nghi Nguyen<sup>1</sup>, Tae Kyung Kim<sup>1</sup>, Tim Jarsky<sup>1</sup>, Zizhen Yao<sup>1</sup>, Boaz Levi<sup>1</sup>, Lucas T Gray<sup>1</sup>, Staci A Sorensen<sup>1</sup>, Tim Dolbeare<sup>1</sup>, Darren Bertagnoli<sup>1</sup>, Jeff Goldy<sup>1</sup>, Nadiya Shapovalova<sup>1</sup>, Sheana Parry<sup>1</sup>, Changkyu Lee<sup>1</sup>, Kimberly Smith<sup>1</sup>, Amy Bernard<sup>1</sup>, Linda Madisen<sup>1</sup>, Susan M Sunkin<sup>1</sup>, Michael Hawrylycz<sup>1</sup>, Christof Koch<sup>1</sup> & Hongkui Zeng<sup>1</sup>



1525 cells



100 - 200  
“interesting”  
genes

# Part I: Learning latent representations

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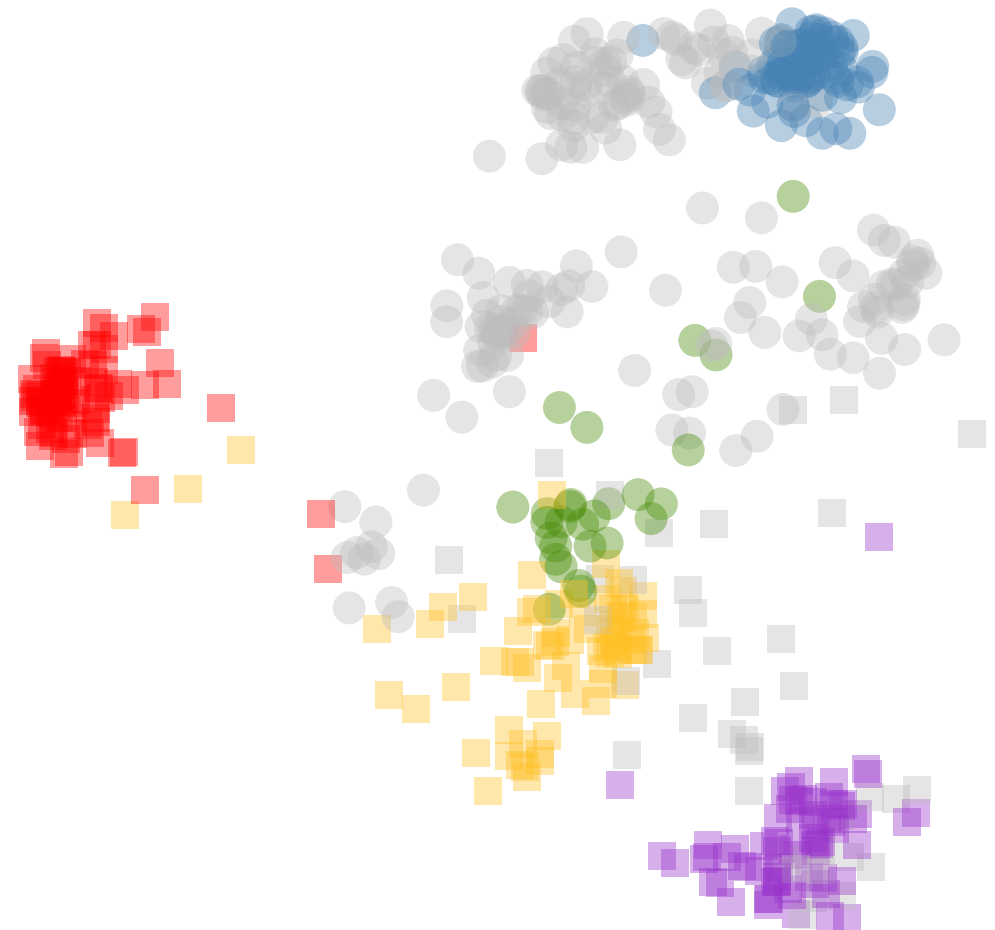


Principal components (PCs)  
computed from raw data

# Part I: Learning latent representations



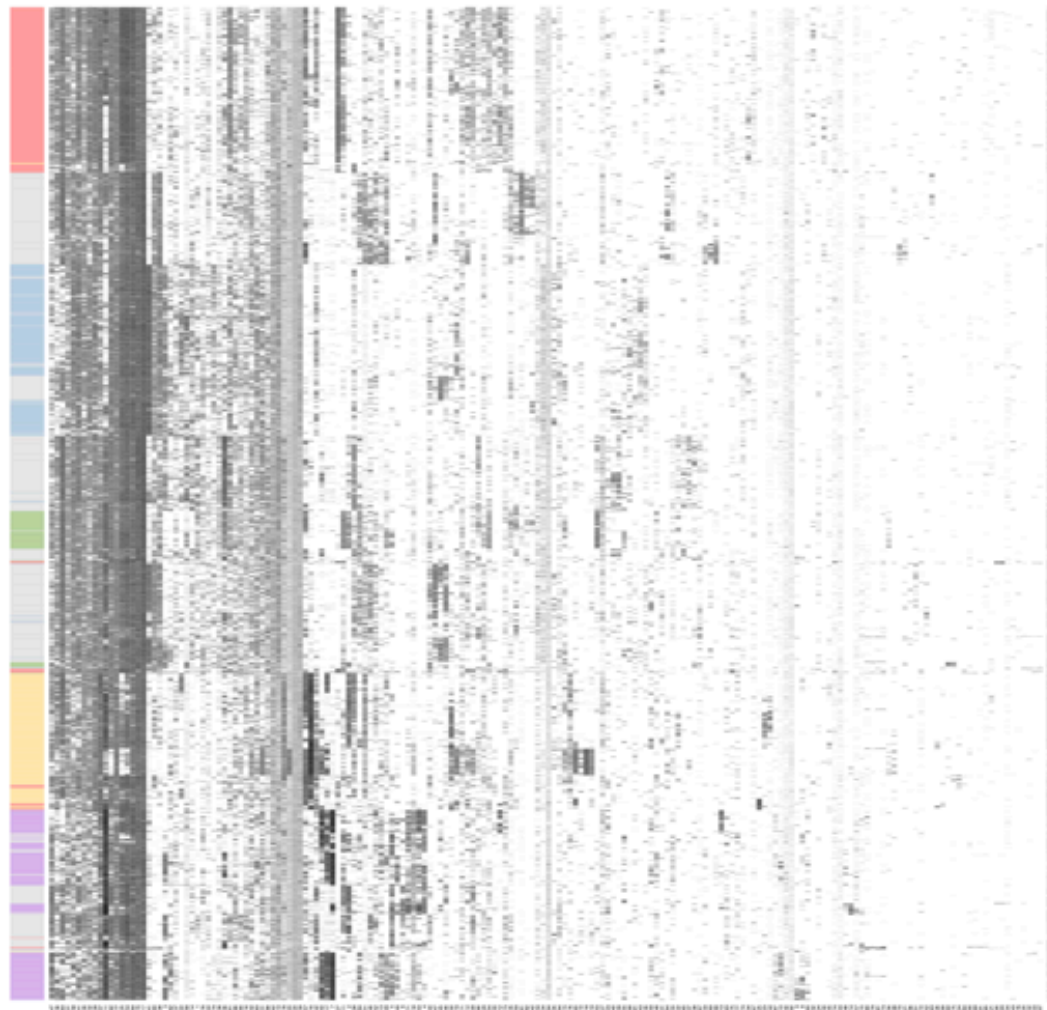
Principal components (PCs)  
computed from raw data



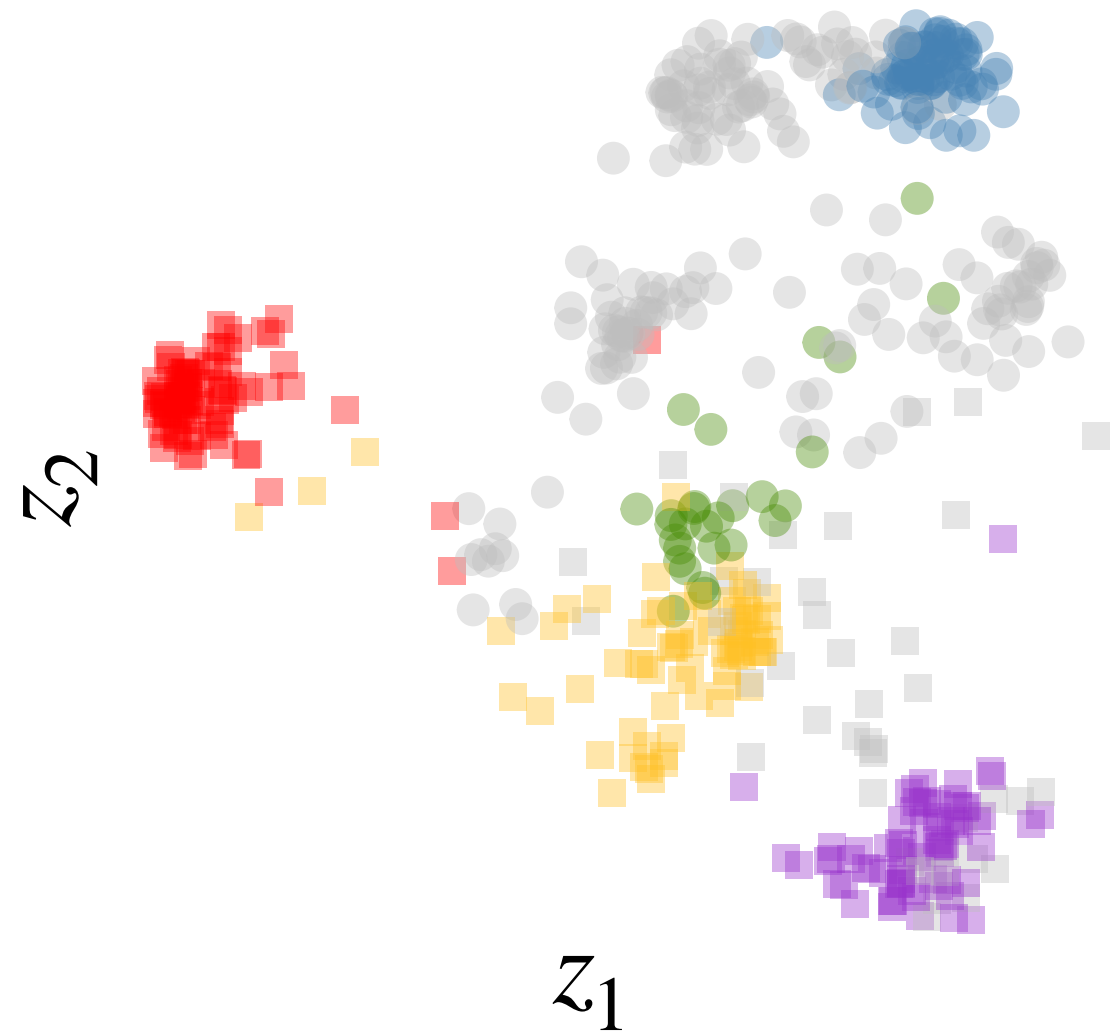
Latent representations, learned by a  
deep Boltzmann machine

## Part II: Understanding the relationship between latent representations and the observed variables (genes).

Genes

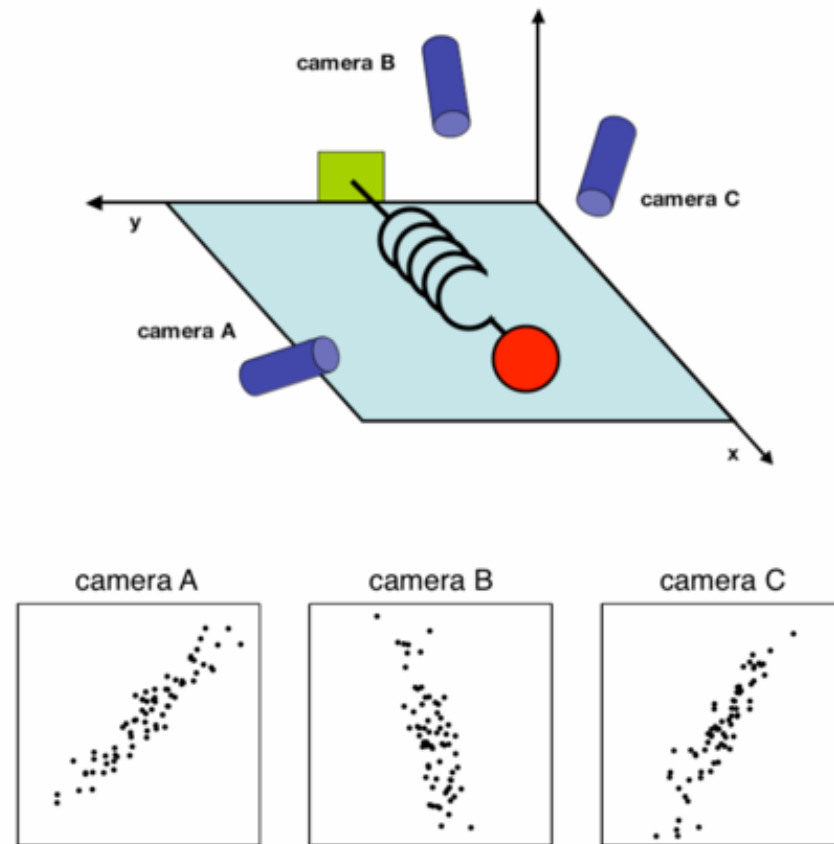


Cells



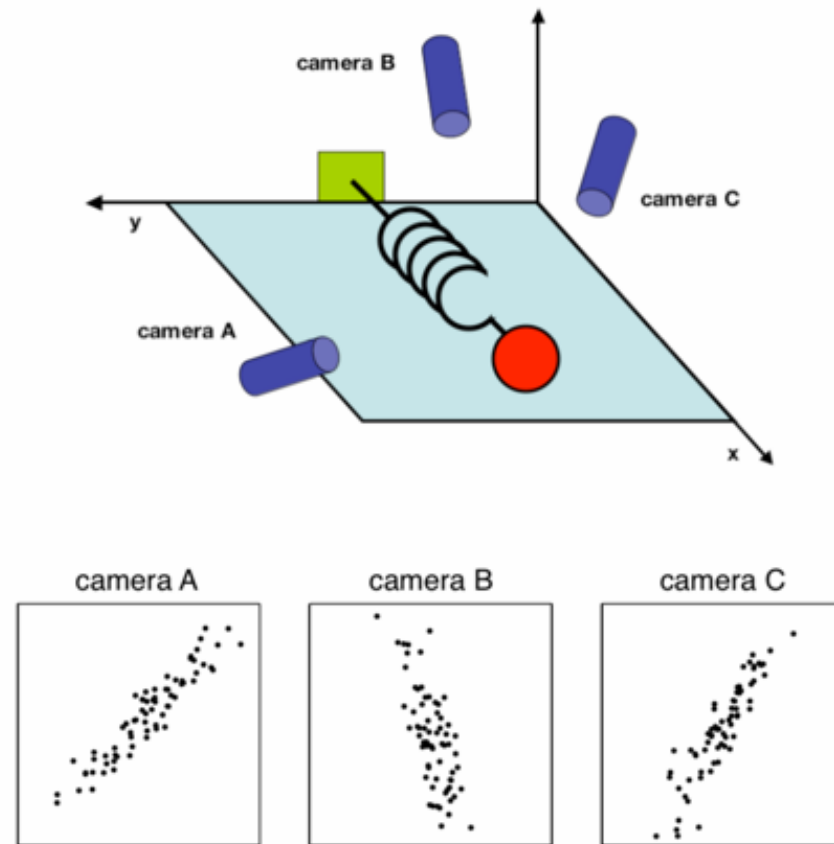


# Principal component analysis (PCA)

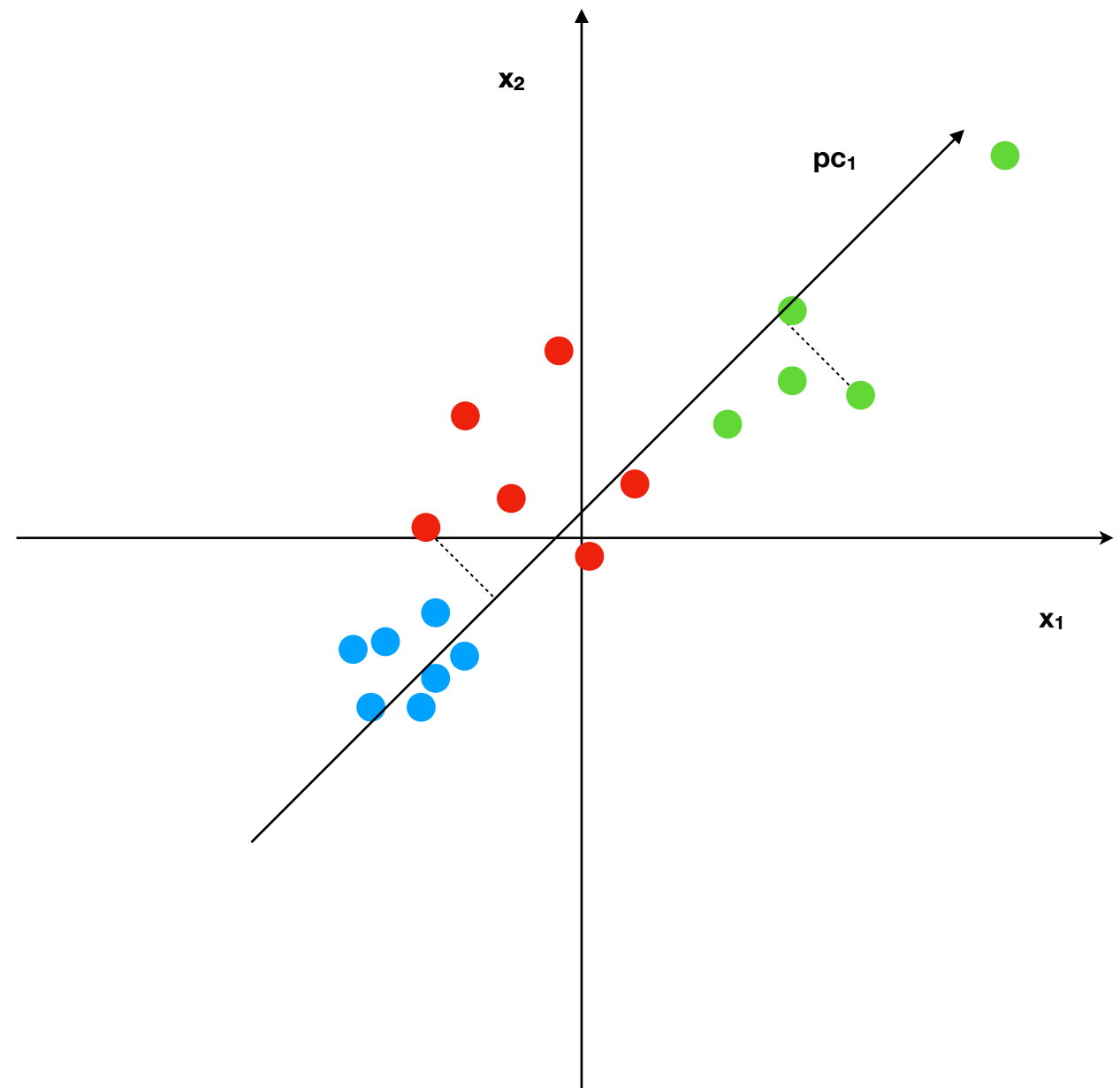


Shlens et al. 2014

# Principal component analysis (PCA)



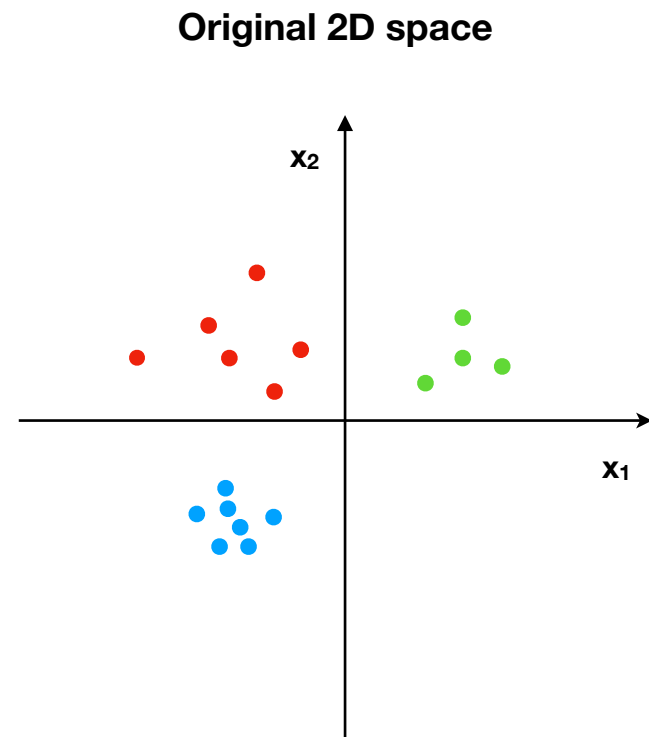
Shlens et al. 2014





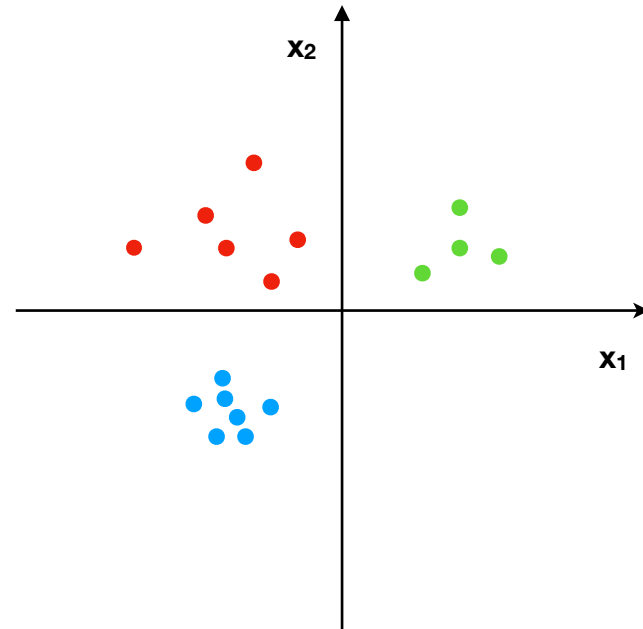
# t-SNE and UMAP

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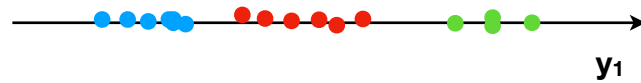


# t-SNE and UMAP

Original 2D space

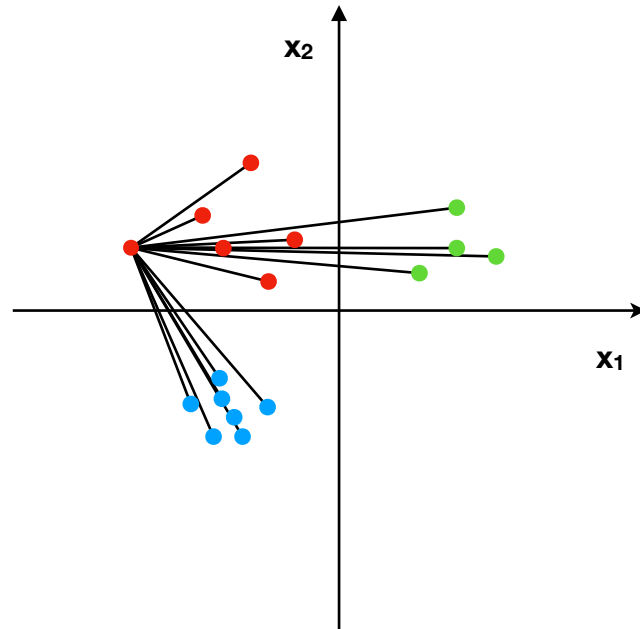


Dimension reduced 1D space

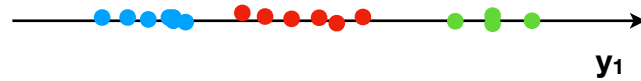


# t-SNE and UMAP

Original 2D space

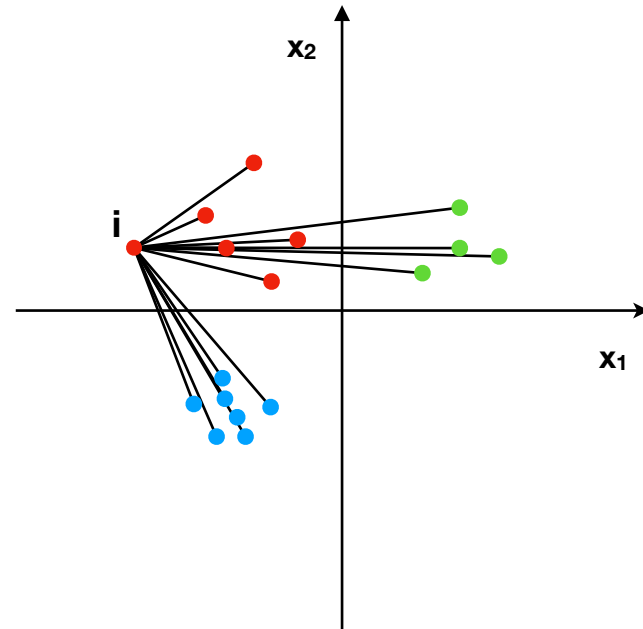


Dimension reduced 1D space

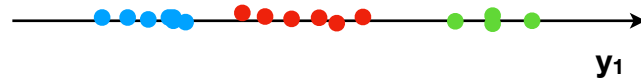


# t-SNE and UMAP

Original 2D space

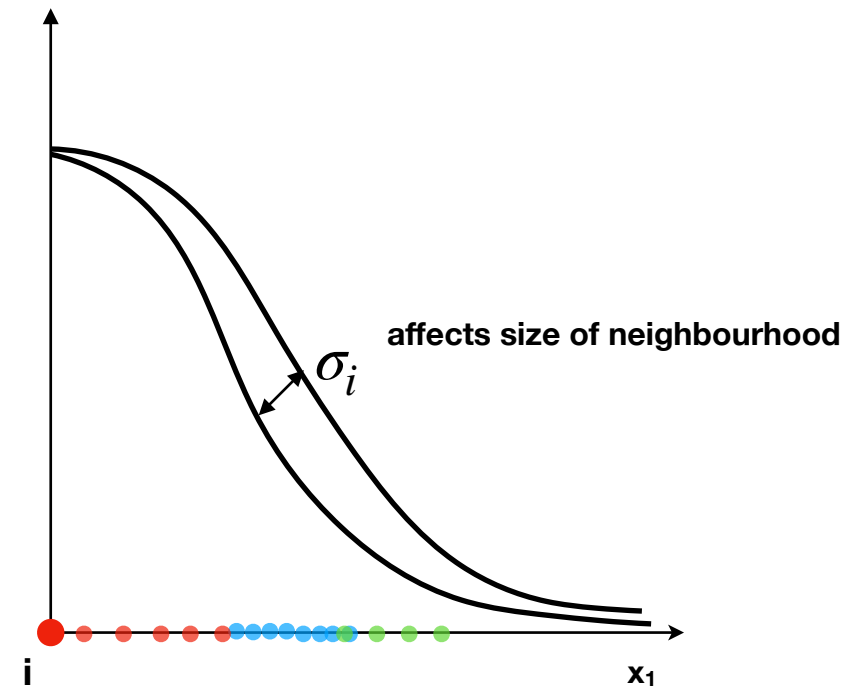
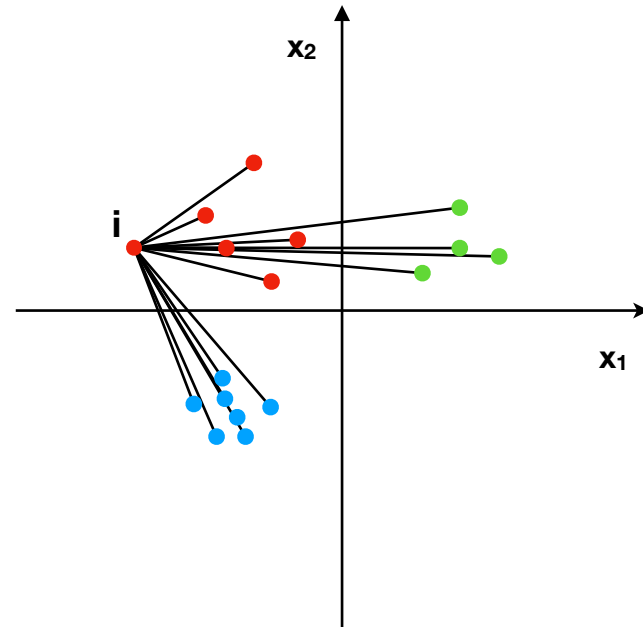


Dimension reduced 1D space

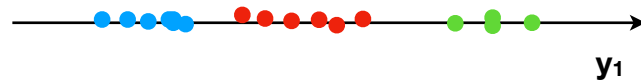


# t-SNE and UMAP

Original 2D space

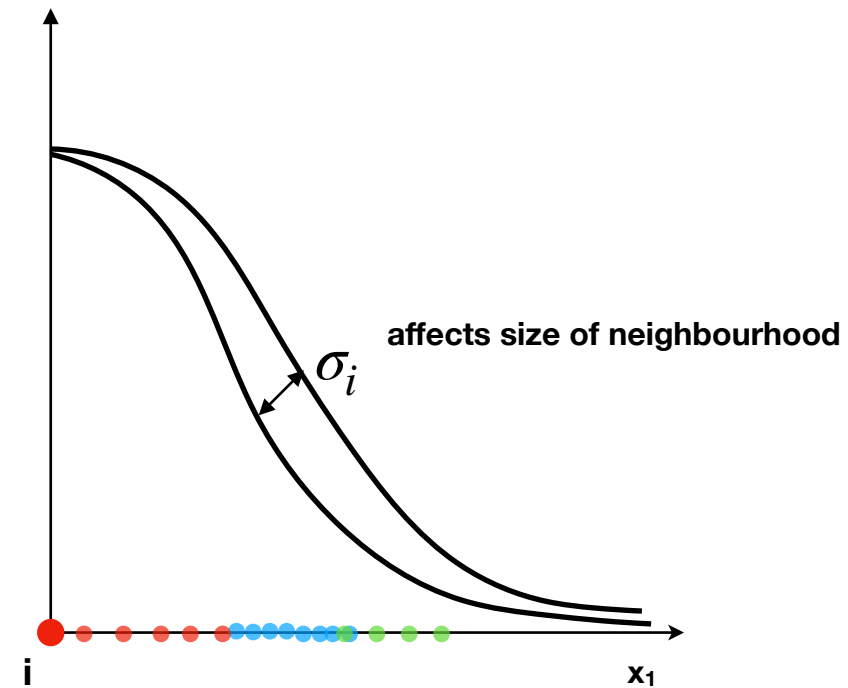
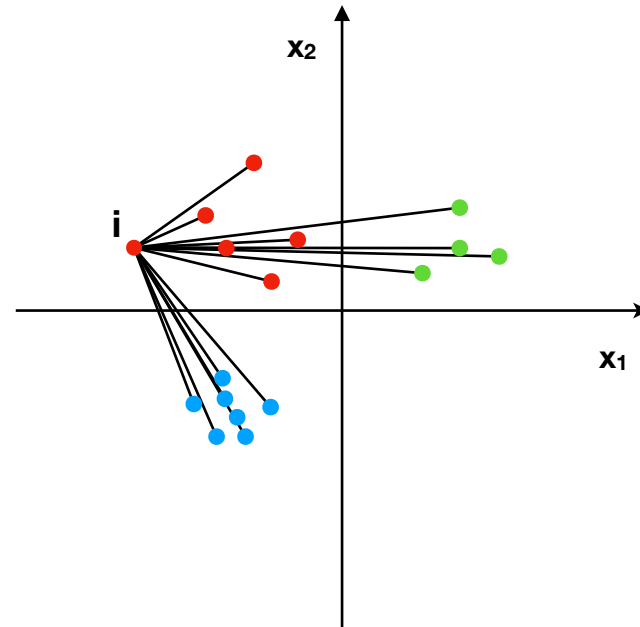


Dimension reduced 1D space



# t-SNE and UMAP

Original 2D space



Dimension reduced 1D space



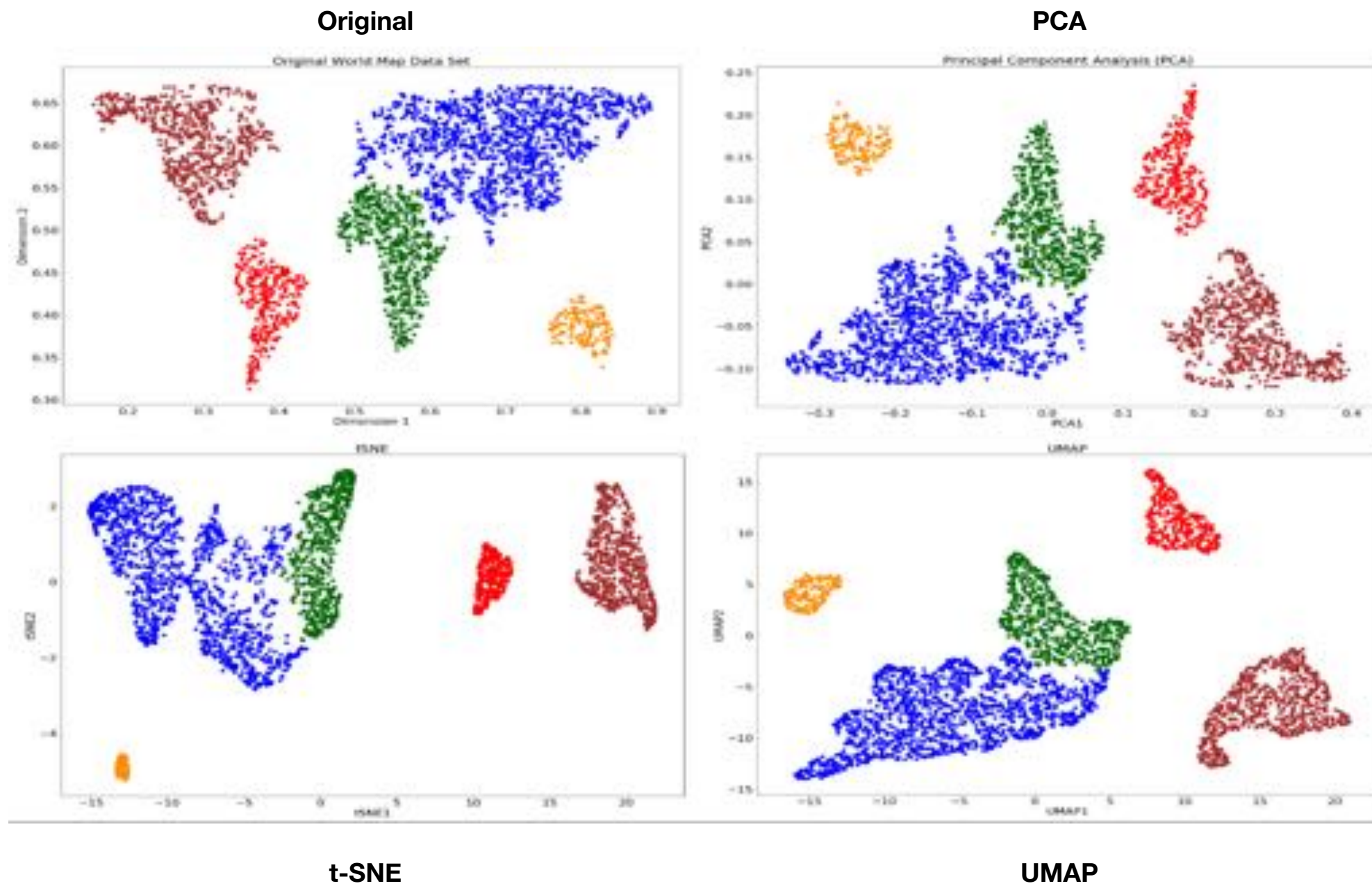
Objective function

$$C = D_{KL}(P || Q) = \sum_{x \in X} P(x) \log \left( \frac{P(x)}{Q(x)} \right)$$

$$\frac{\delta C}{\delta y_i} = 4 \sum_j (p_{ij} - q_{ij})(y_i - y_j)(1 + ||y_i - y_j||^2)^{-1}$$



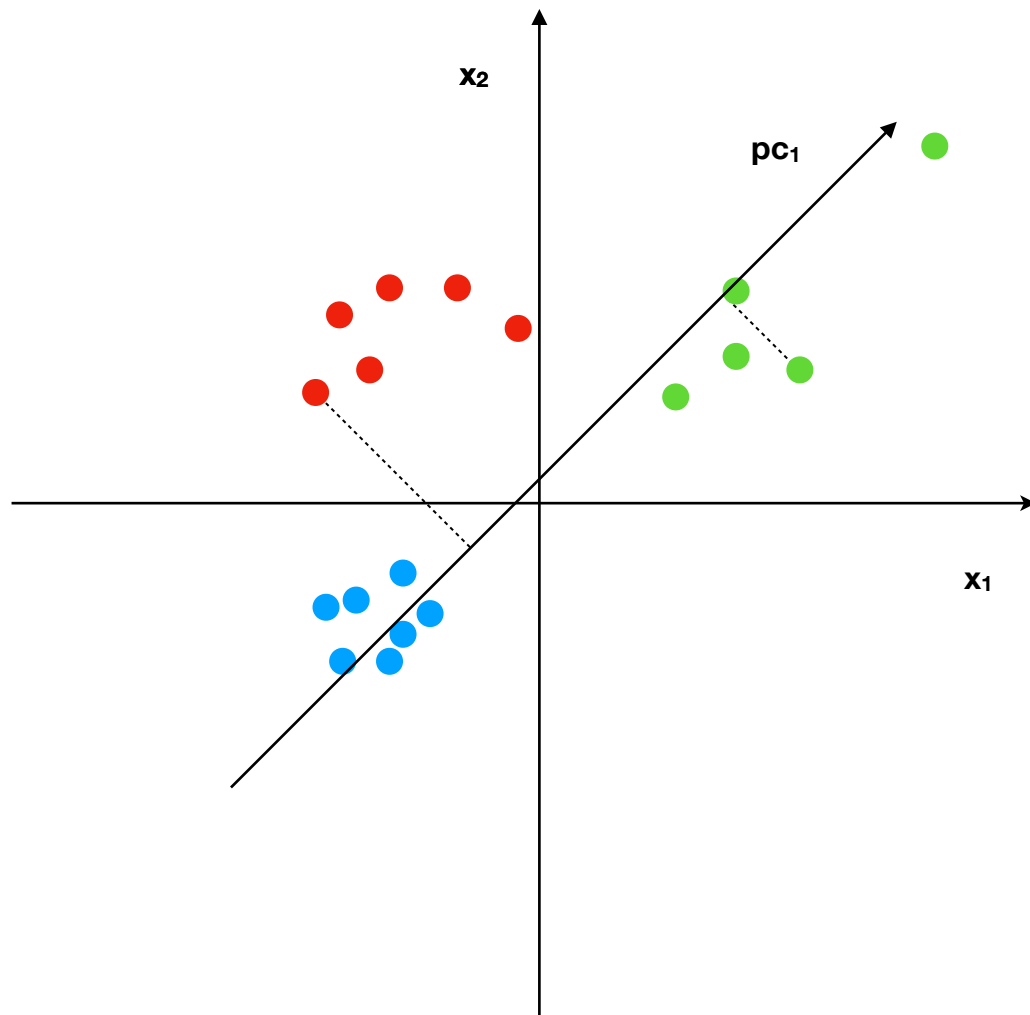
# t-SNE and UMAP



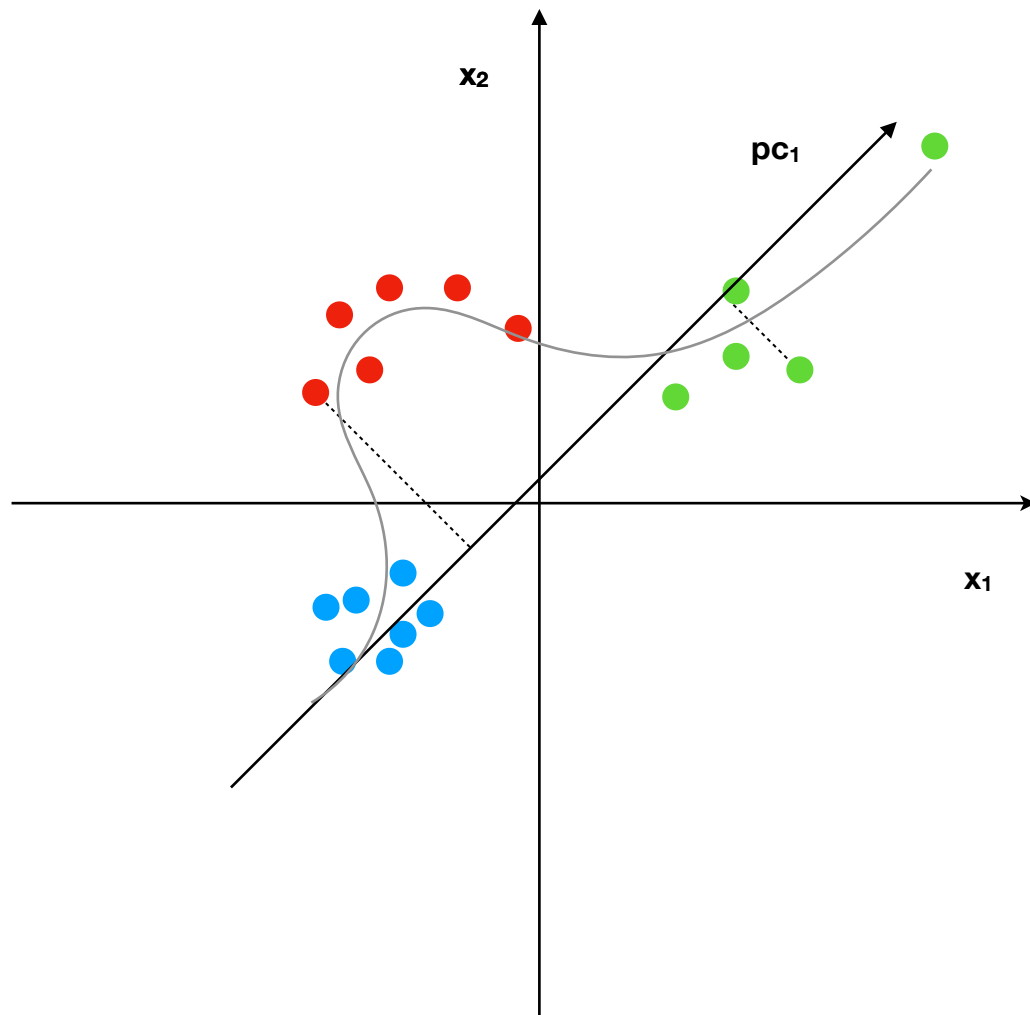
<https://towardsdatascience.com/tsne-vs-umap-global-structure-4d8045acba17>

# Autoencoder

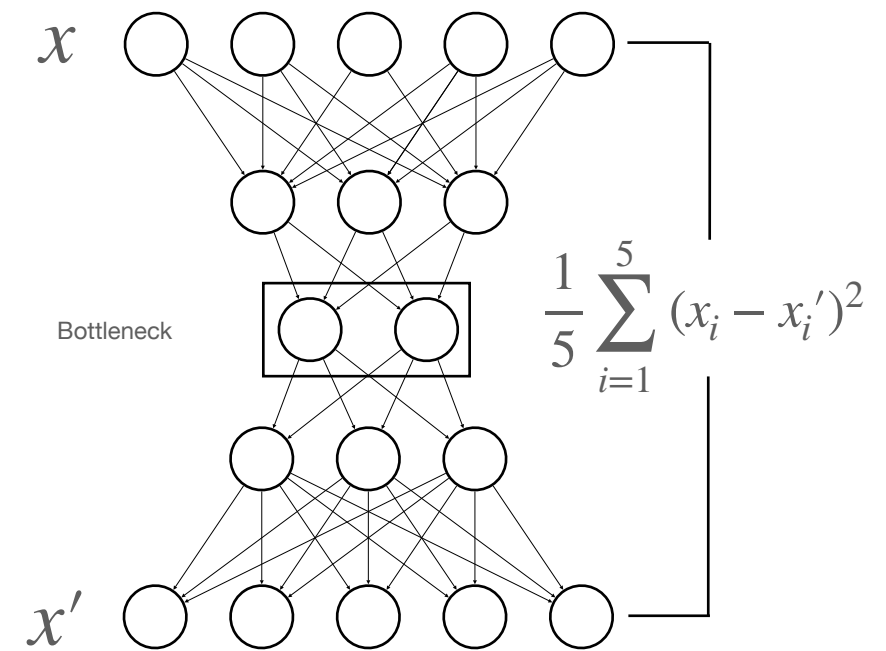
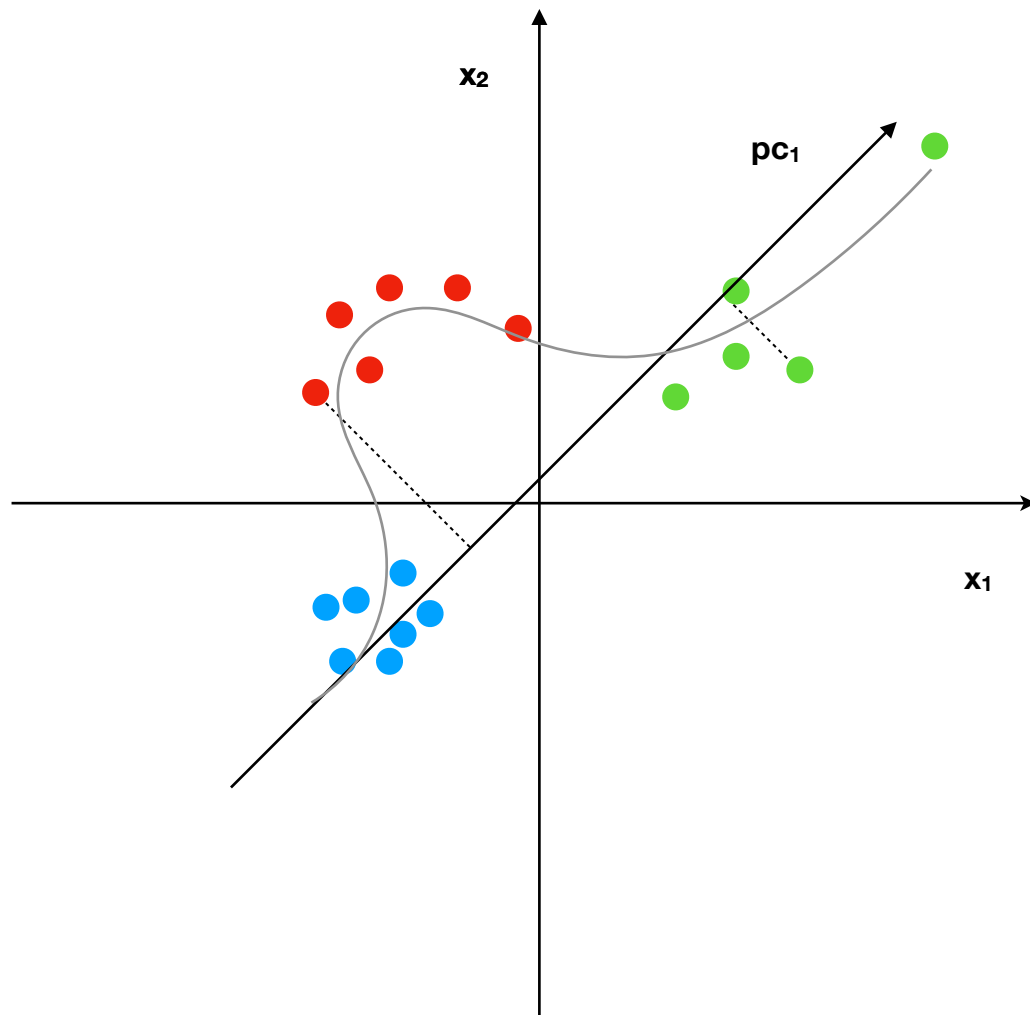
# Autoencoder



# Autoencoder

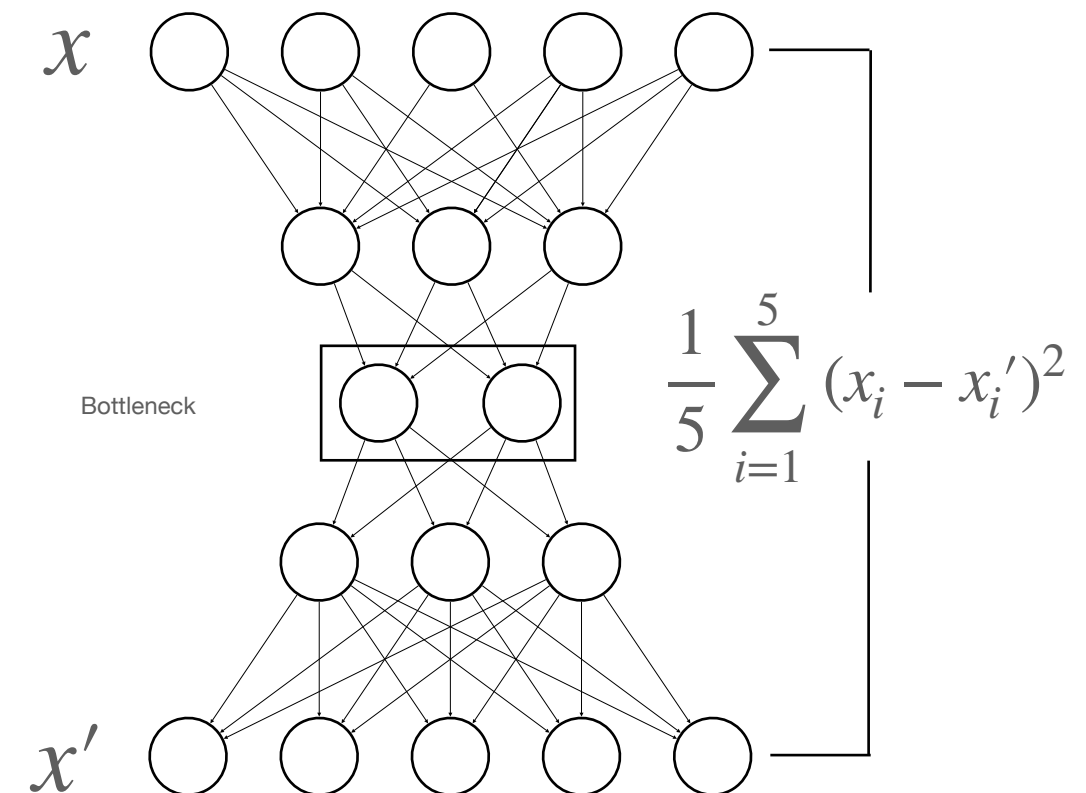
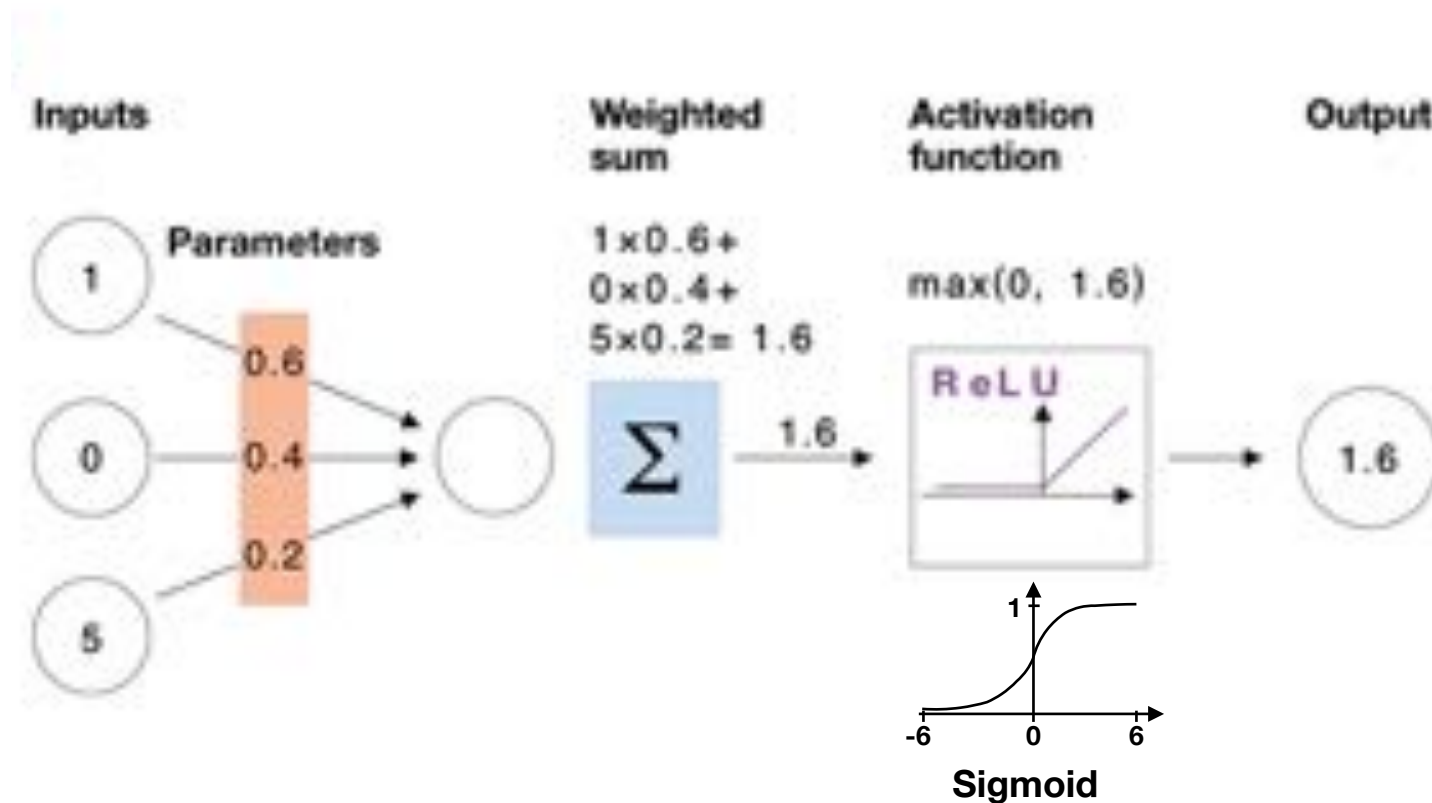


# Autoencoder

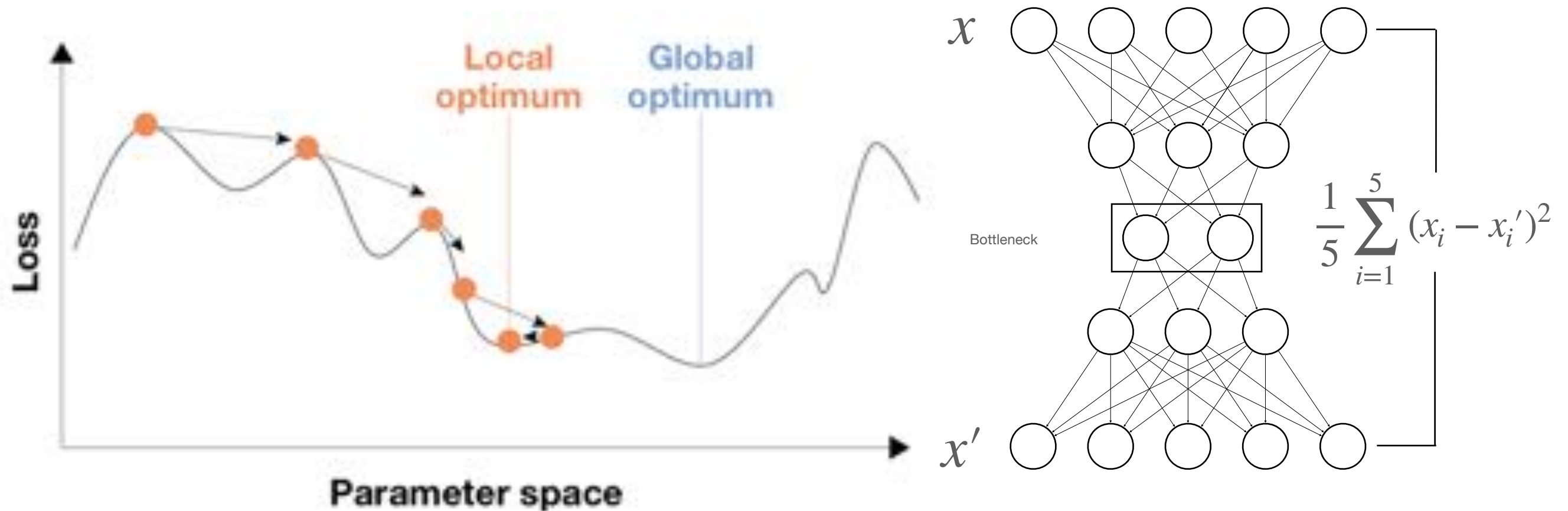


$x_1 =$	25	9	26	300	1
$x'_1, \hat{x}_1 =$	20	4	20	310	1

# Learning non-linearities with deep neural networks

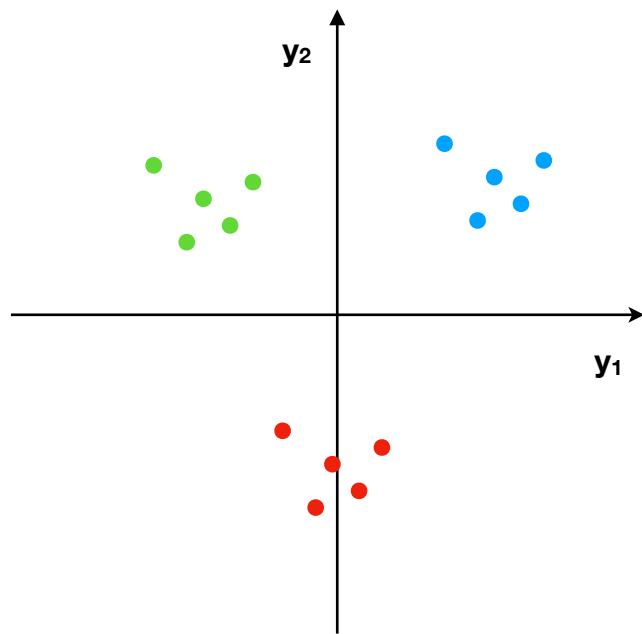


# (Stochastic) gradient descent / Back-propagation

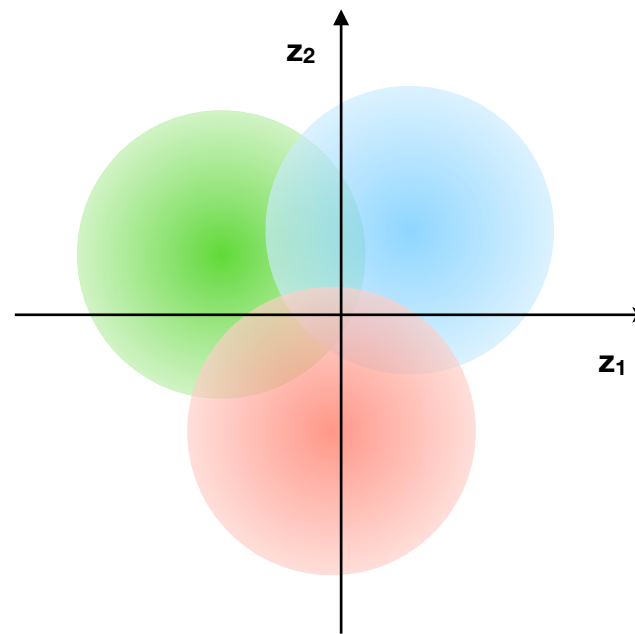




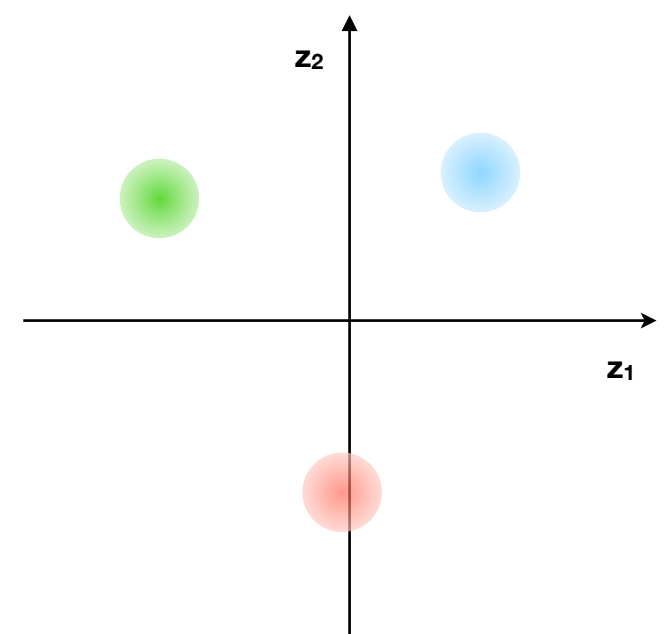
# What is a good latent space ?



Ground truth

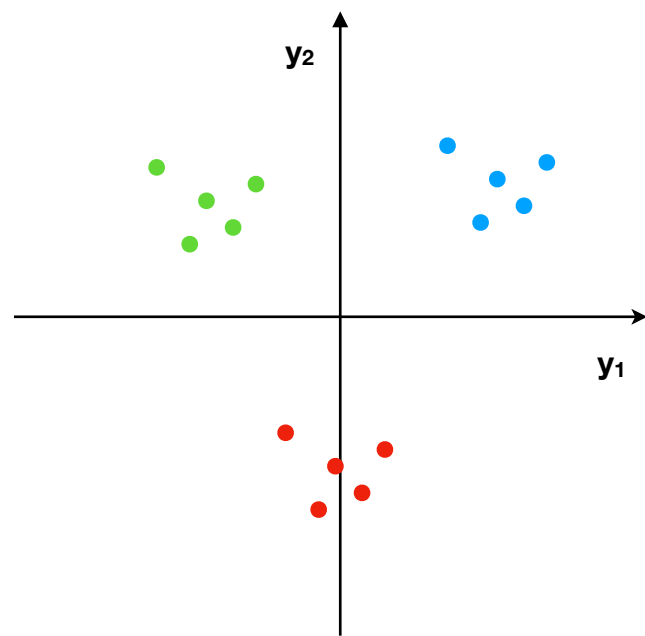


Latent space 1

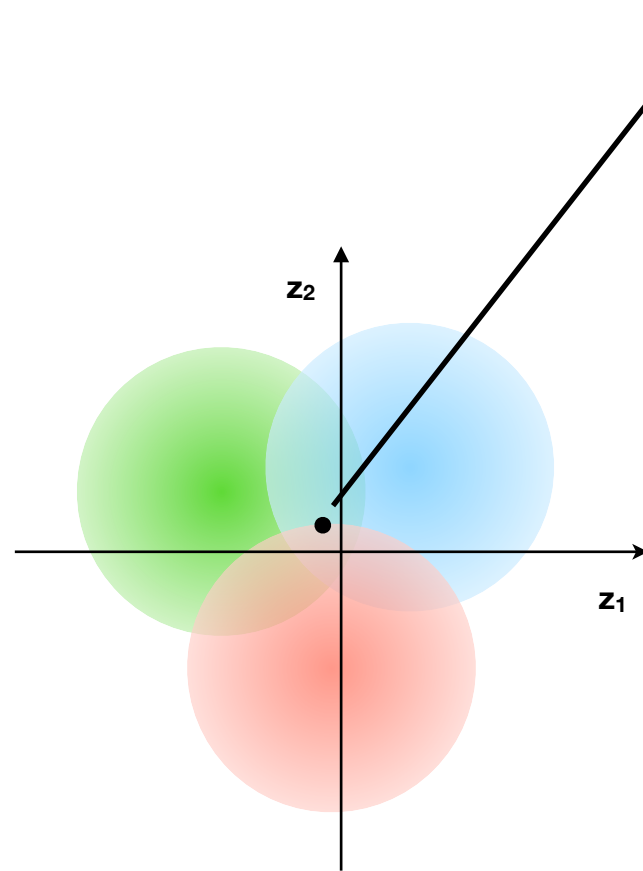


Latent space 2

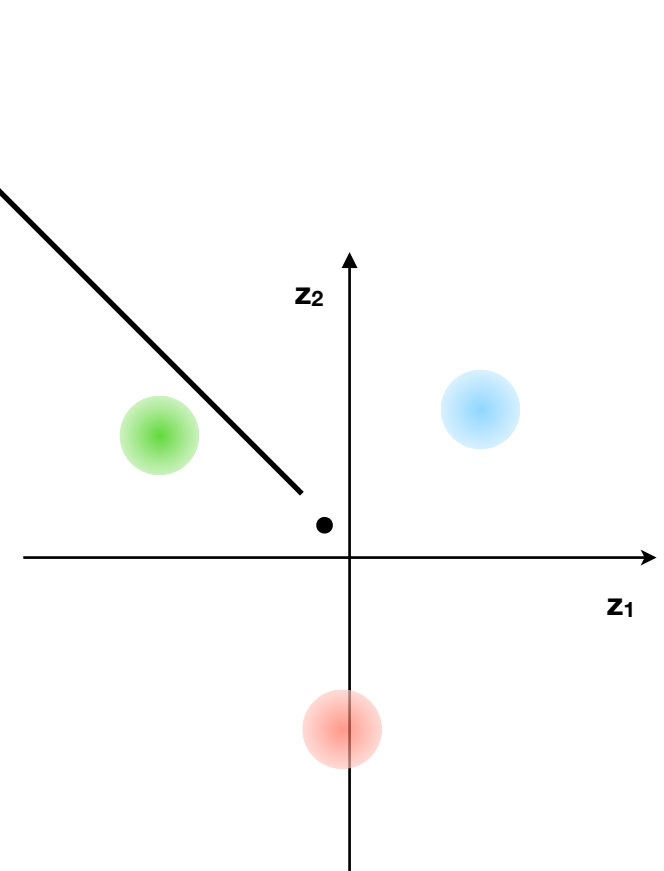
# What is a good latent space ?



Ground truth



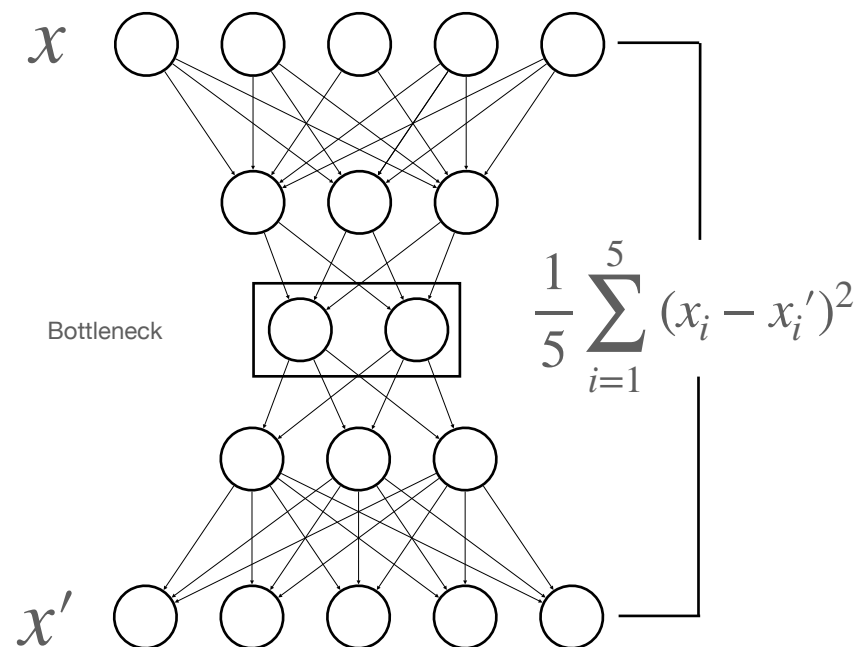
Latent space 1



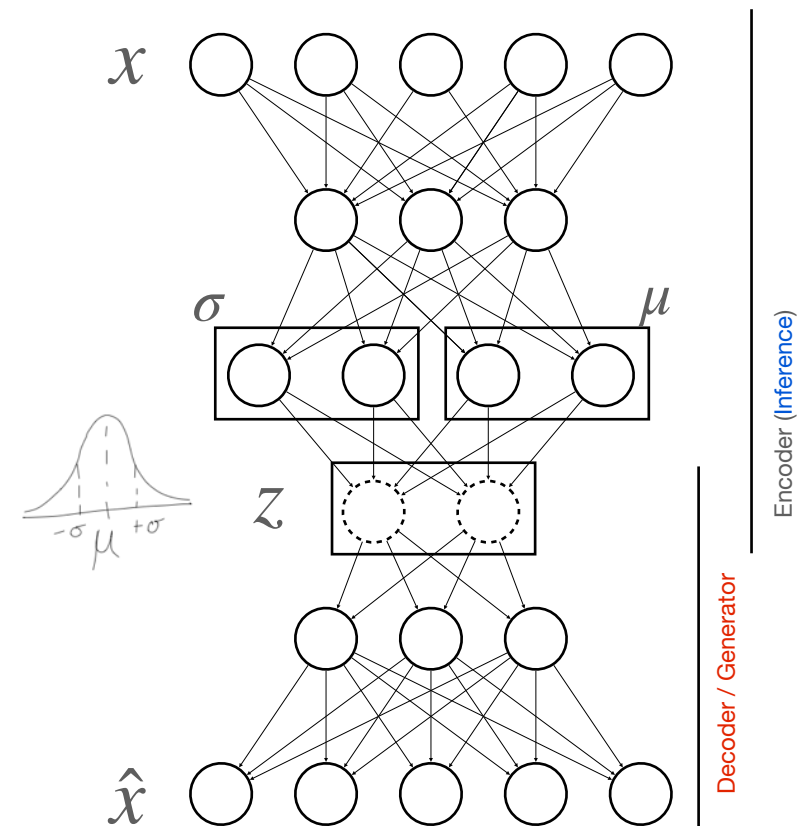
Latent space 2

# Variational Autoencoder (VAE)

Autoencoder



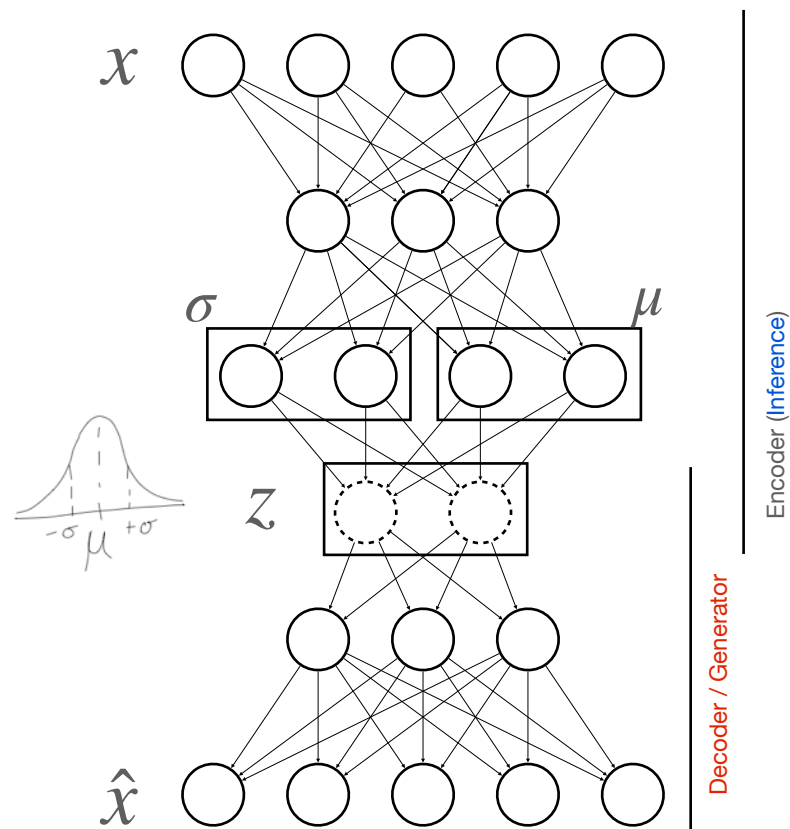
Variational Autoencoder



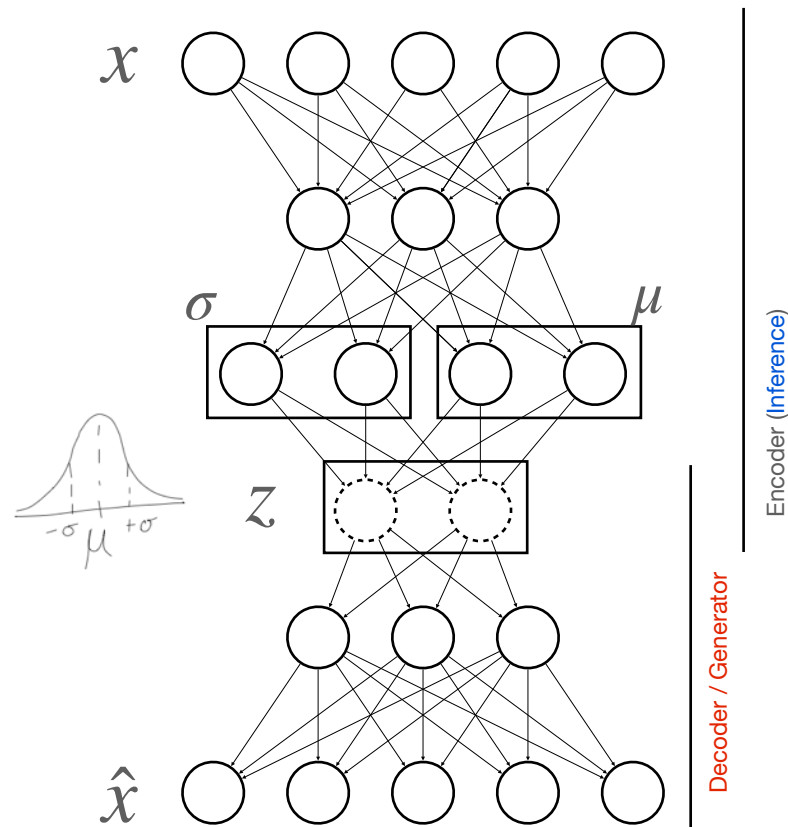
- random
- deterministic

$x_1 =$	25	9	26	300	1
$x'_1, \hat{x}_1 =$	20	4	20	310	1

# VAE viewed as a probabilistic random variable model



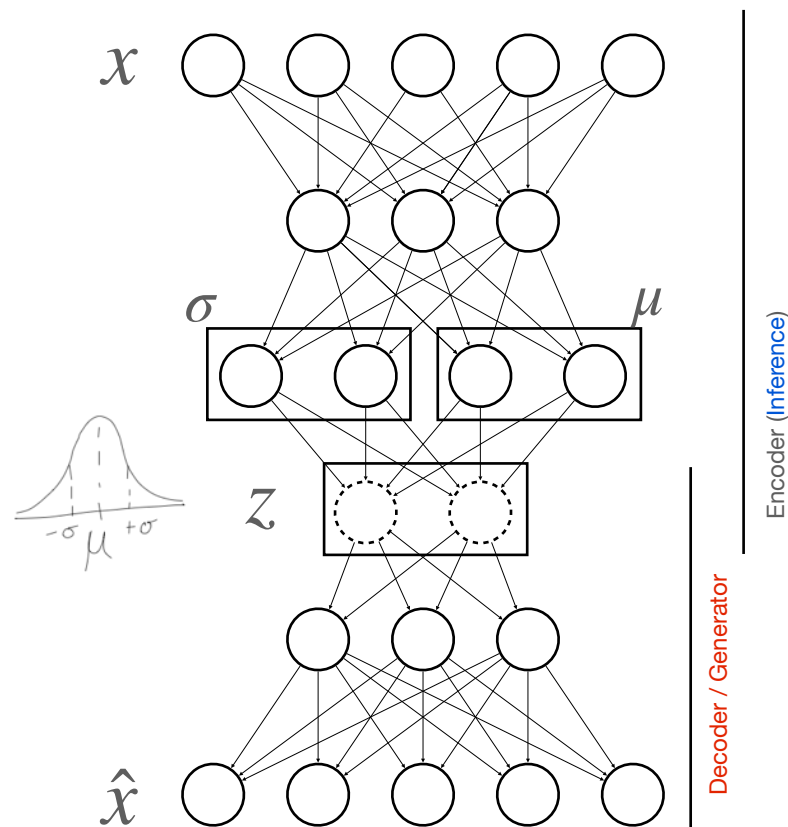
# VAE viewed as a probabilistic random variable model



We want to learn the posterior distribution over the latent variables, given the data.

$$p(z|x) = \frac{\overset{\text{likelihood}}{p(x|z)} * \overset{\text{prior}}{p(z)}}{\underset{\text{evidence}}{p(x)}}$$

# VAE viewed as a probabilistic random variable model



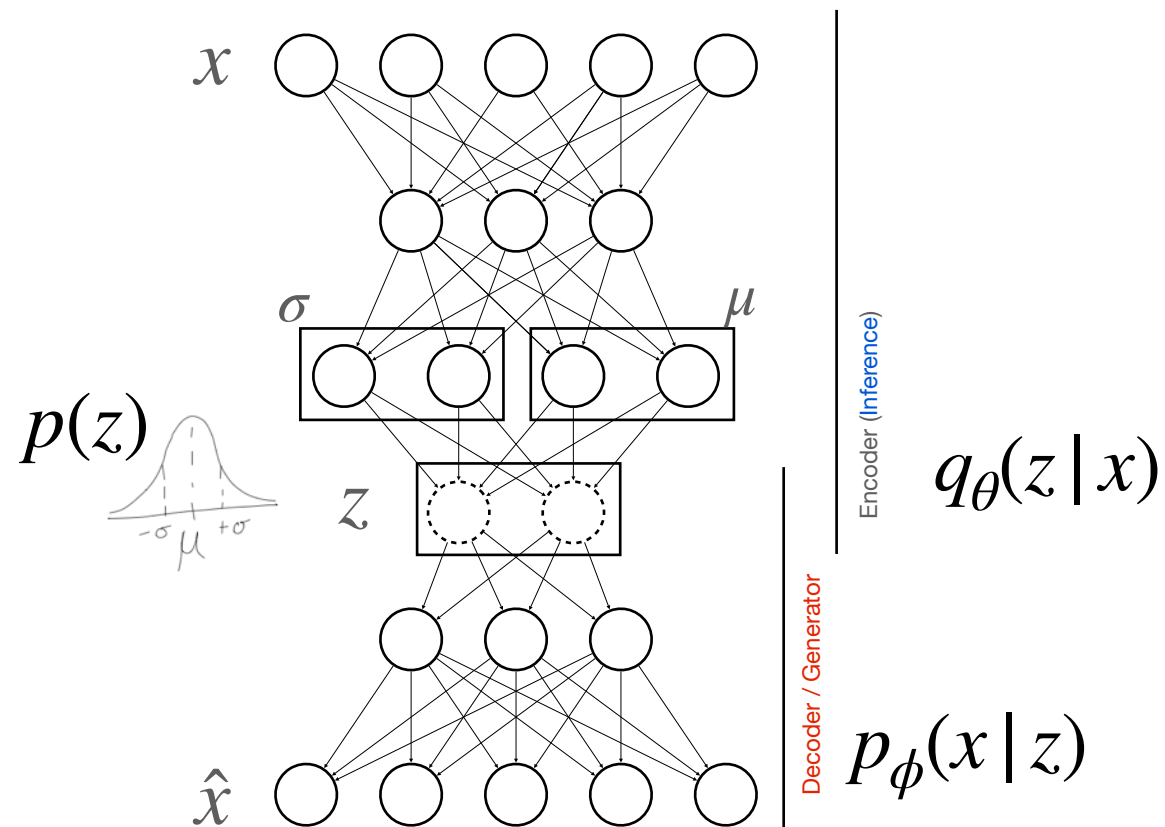
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$$p(z|x) = \frac{\overset{\text{likelihood}}{p(x|z)} * \overset{\text{prior}}{p(z)}}{\underset{\text{evidence}}{p(x)}}$$

**Objective function: Evidence Lower Bound**

$$\log p_{\theta}(x_i) \geq \mathbb{E}_{q_{\theta}(z|x_i)}[\log p_{\phi}(x_i|z)] - \mathbb{KL}(q_{\theta}(z|x_i) || p(z))$$

# VAE viewed as a probabilistic random variable model



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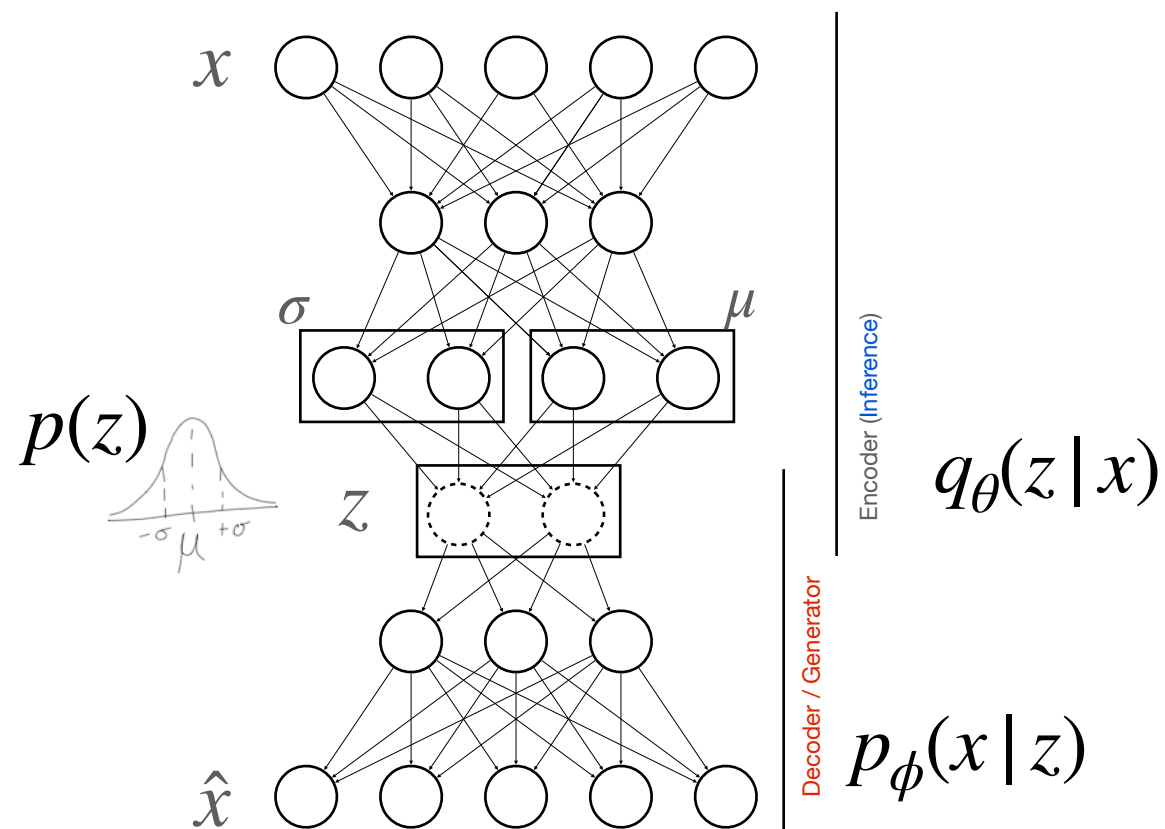
$$p(z|x) = \frac{\overset{\text{likelihood}}{p(x|z)} * \overset{\text{prior}}{p(z)}}{\underset{\text{evidence}}{p(x)}}$$

**Objective function: Evidence Lower Bound**

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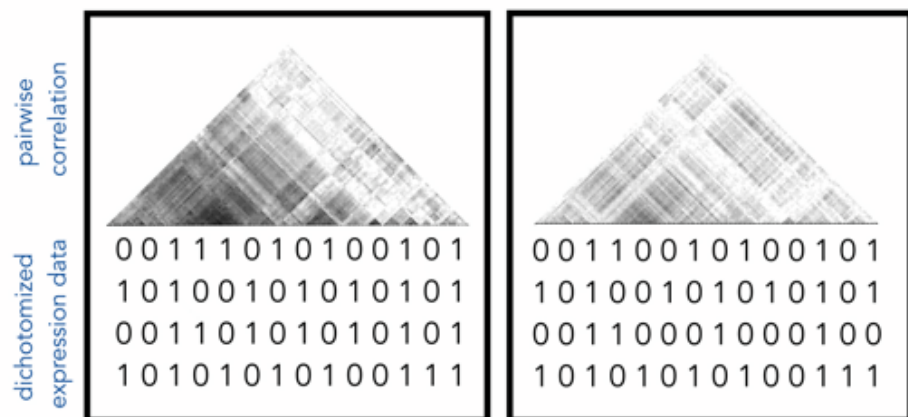
# VAE viewed as a probabilistic random variable model



We want to learn the posterior distribution over the latent variables, given the data.

$$p(z|x) = \frac{\text{likelihood} \cdot \text{prior}}{\text{evidence}} = \frac{p(x|z) * p(z)}{p(x)}$$

Training ↑ Sampling ↓

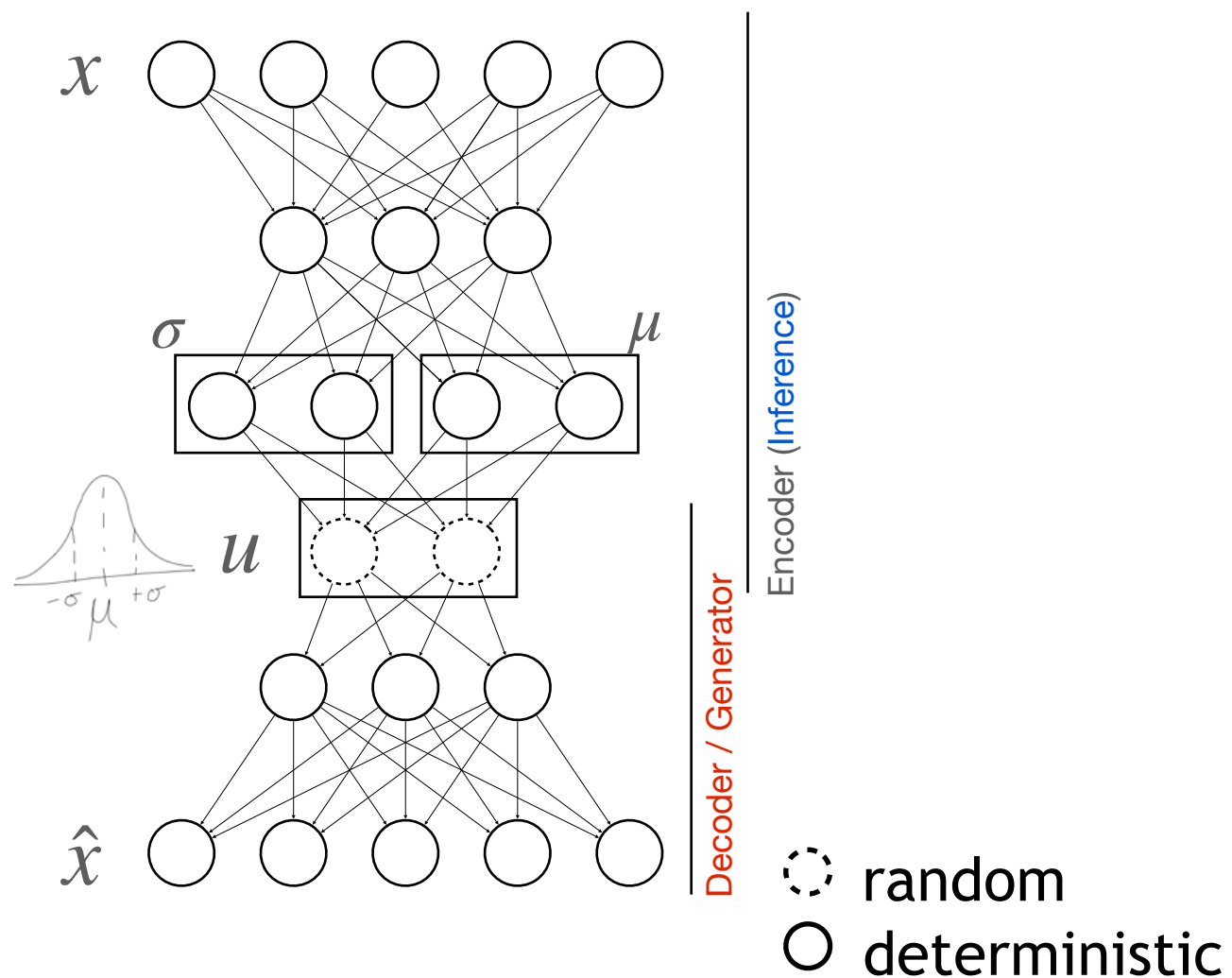


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$$\log p_{\theta}(x_i) \geq \mathbb{E}_{q_{\theta}(z|x_i)}[\log p_{\phi}(x_i|z)] - \mathbb{KL}(q_{\theta}(z|x_i) || p(z))$$

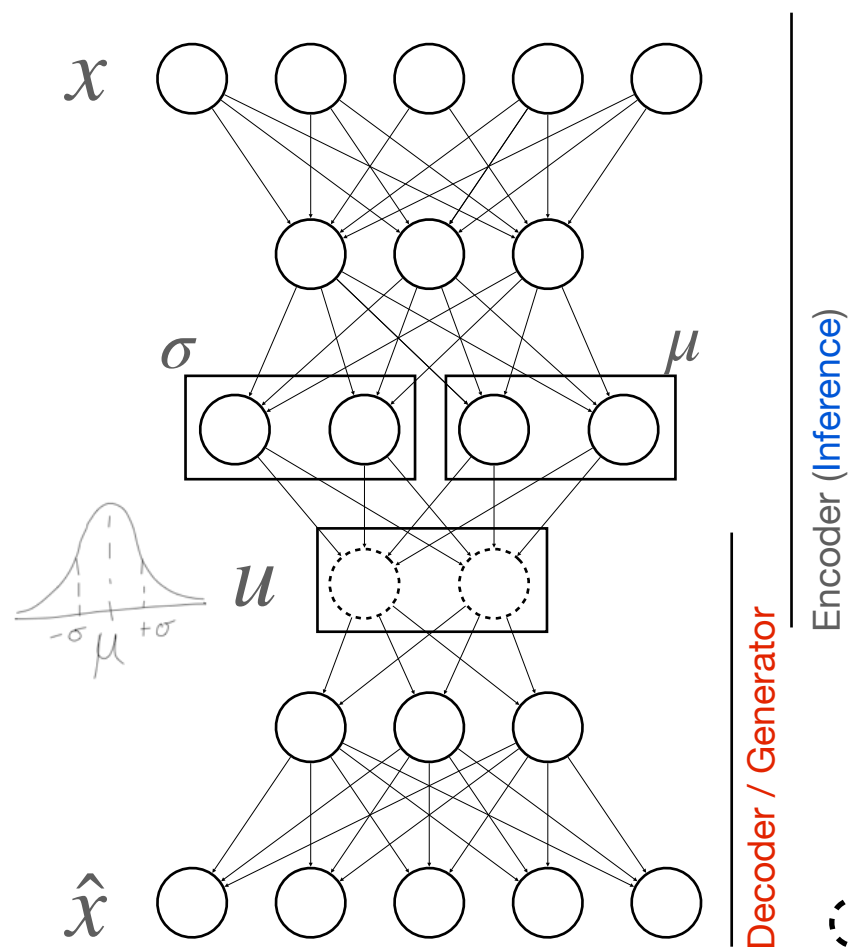
# Other deep generative approaches ...

## Variational Autoencoder

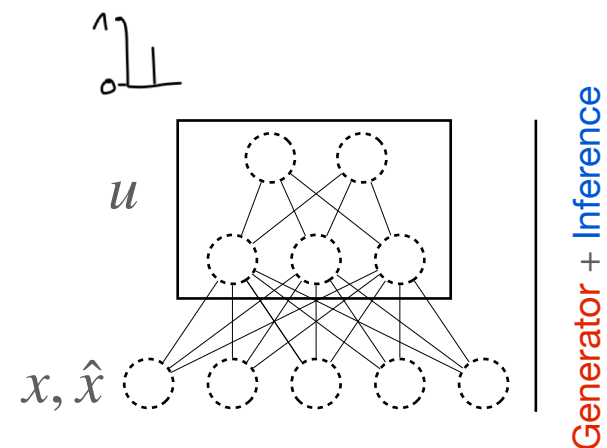


# Other deep generative approaches ...

## Variational Autoencoder



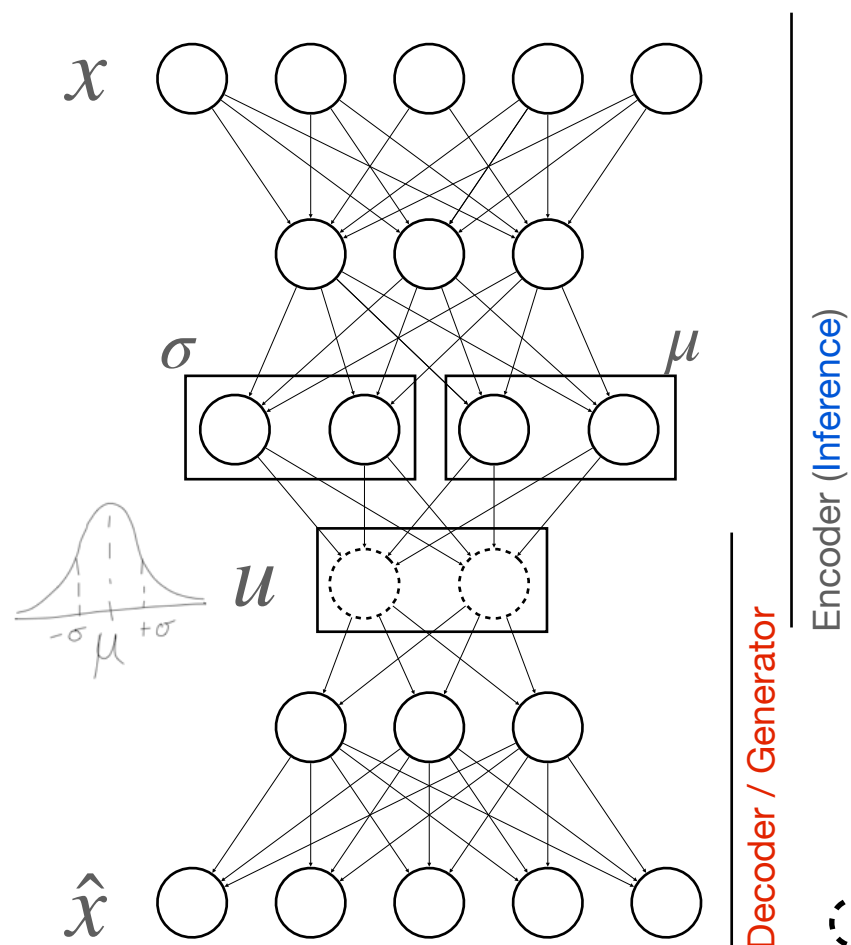
○ random  
○ deterministic



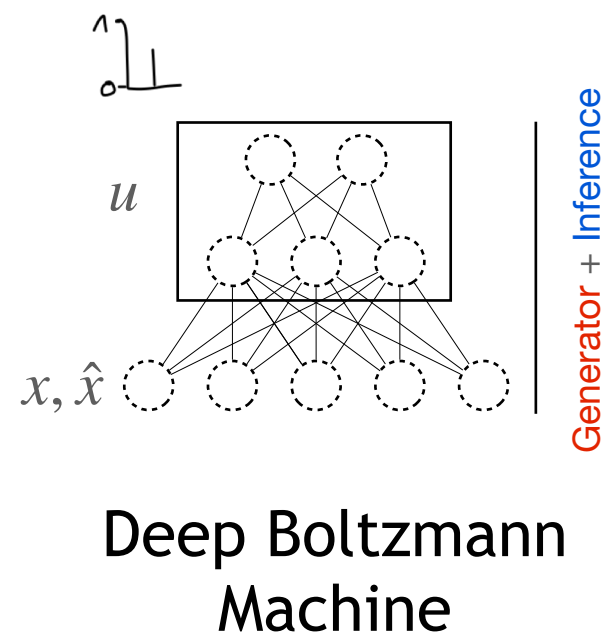
## Deep Boltzmann Machine

# Other deep generative approaches ...

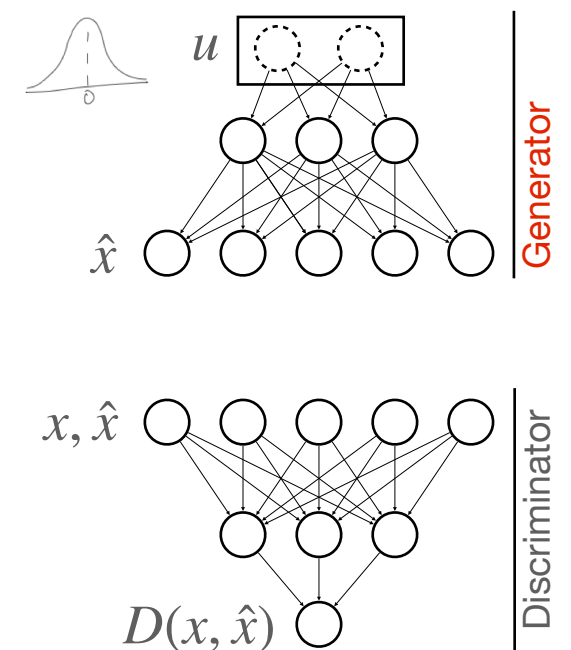
## Variational Autoencoder



○ random  
○ deterministic

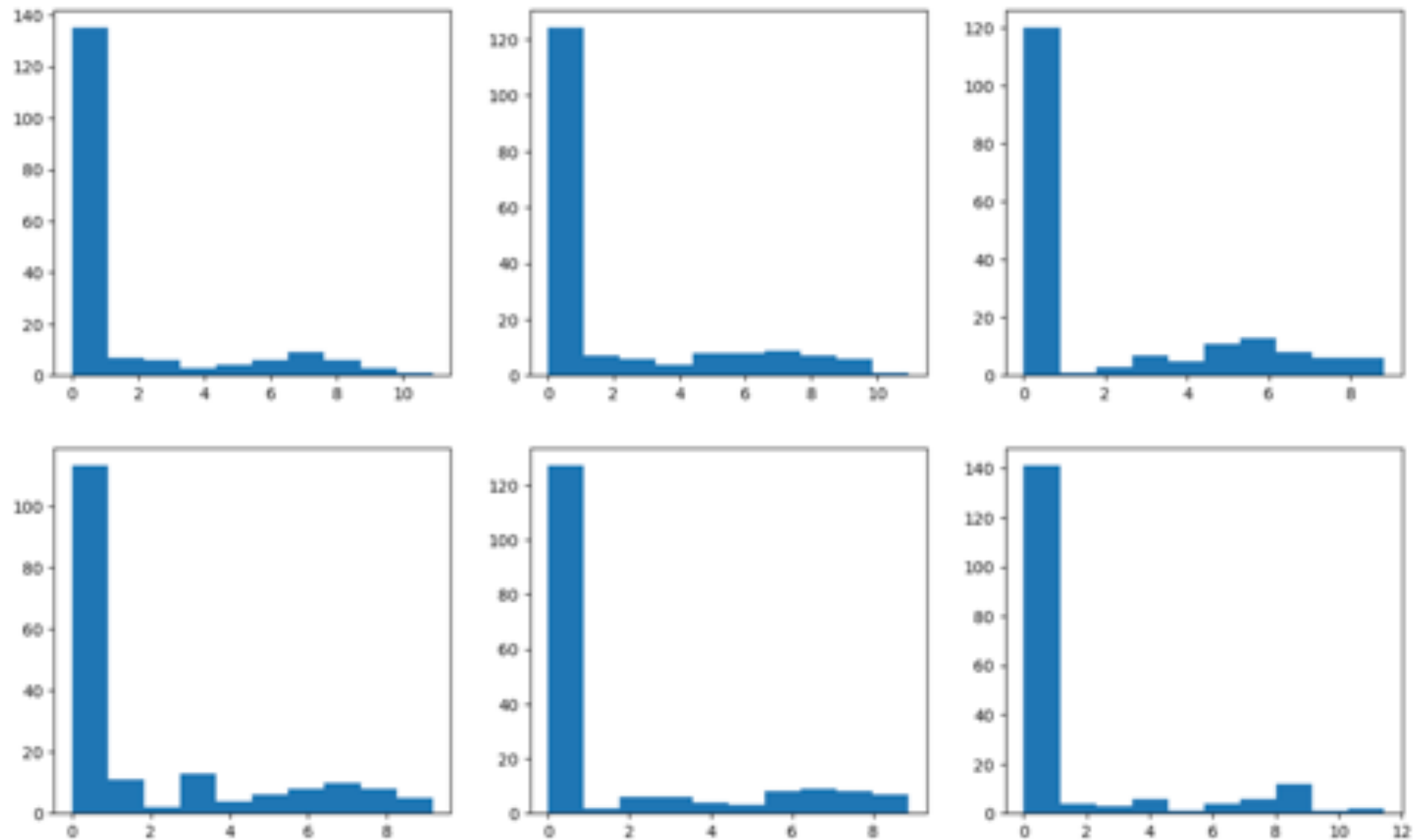


## Deep Boltzmann Machine



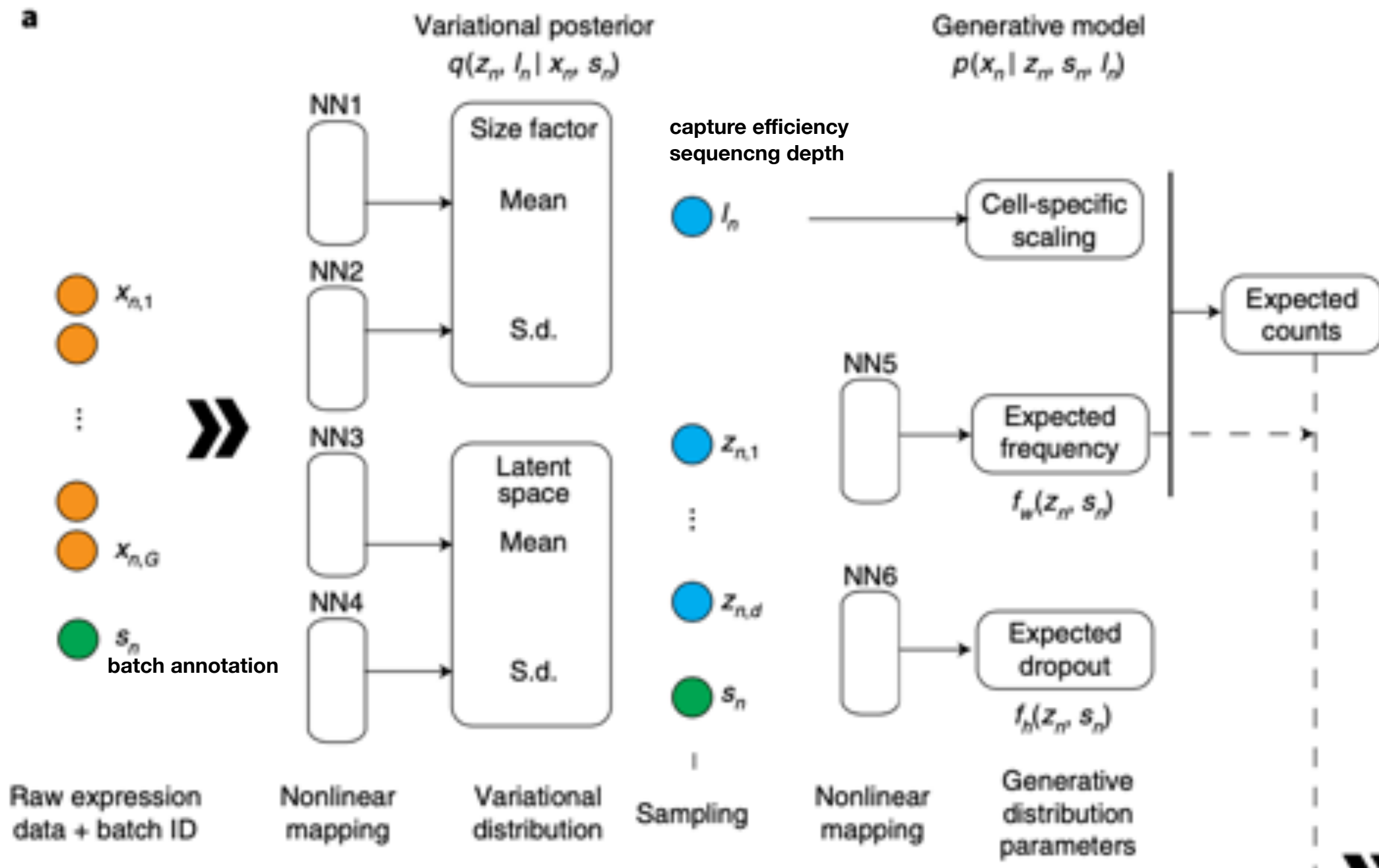
## Generative Adversarial Network

# Adaptations to single cell RNA-Seq data



**Exemplary gene expression (log transformed) of six random genes from Tasic et al. (2016) data**

# Adaptations to single cell RNA-Seq data



From Lopez et al. 2018: “Deep generative modeling for single-cell transcriptomics”