

Keeping up with the Curve: Learning, Evolving Beliefs and the Anchoring of Expectations *

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Abstract

I explain the behavior of inflation, nominal interest rates and inflation expectations in the post-war U.S. by estimating a forward-looking model in which private agents learn about macroeconomic fundamentals and the policymakers' stabilization preferences in real-time using a *structural* model: recognizing the feedback from their expectations under imperfect knowledge to observed aggregate dynamics. Monetary policy is conducted optimally but private agents suspect that the policymakers' stabilization preferences are evolving, which they learn from observed policy behavior. This gives rise to a nonlinear filtering problem. The model provides a novel, information-theoretic explanation of how systematic monetary policy shapes expectations when agents are learning: a demonstrated emphasis on stabilizing the real economy by minimizing cyclical fluctuations in unemployment has stabilized long-run inflation expectations while at the same time rendering short-run expectations *more* susceptible to supply shocks. The model offers a new explanation for the recent post-Covid inflation surge and the “costless disinflation” that followed, shedding light on why it differed markedly from the crises of the 1970s and the 80s.

Keywords: Monetary Policy, Interest Rates, Expectation Formation, New Keynesian

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1 Introduction

Inflation surged in the United States in early 2021, reaching a forty-year high of 9.1 percent by June 2022 and catching both the private sector and policymakers off guard. Remarkably, for nearly a year, inflation continued to rise while the Federal Reserve maintained the policy rate at the effective lower bound, raising it only in March 2022, prompting widespread concern that the Fed had fallen “behind the curve.” The episode drew inevitable comparisons to the Great Inflation of the 1970s and early 1980s. Both periods were marked by sharp increases in oil prices and significant supply disruptions, yet they produced strikingly different macroeconomic outcomes: a protracted inflationary spiral culminating in a painful disinflation in the early 1980s versus the relatively swift “soft landing” that has characterized the U.S. economy’s recovery from the pandemic shock. Survey evidence (as shown in Figure 1) indicates that private agents held sharply different narratives about inflation across the two episodes: during the recent surge, even as short-run expectations rose sharply, long-run expectations remained “anchored” - a marked contrast to the 1970s and early 1980s, when both short- and long-run expectations remained elevated in unison.

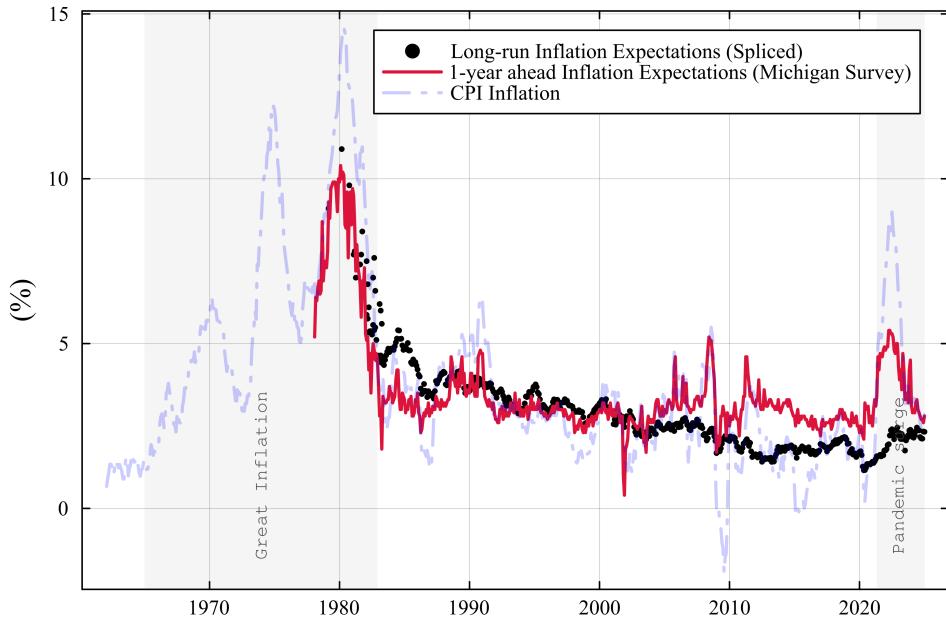


Figure 1: Growing discord between short-run and long-run inflation expectations

Note: Long-run Inflation Expectations series is constructed by splicing together inflation expectations over the 5-to-10-year horizon from Michigan Survey before 1982 and 10-year ahead inflation expectations from the Cleveland Fed afterwards (due to a shorter sample).

To explain these divergent outcomes, I develop a model with three key features. First, neither the private agents—households and firms nor central bank policymakers possess full informa-

tion - their behavior is shaped by their perceptions regarding the fundamental state of the economy; which are formed based on interpreting macroeconomic outcomes through the lens of a forward-looking structural model under perpetual learning. Second, monetary policy is conducted optimally under discretion by the central bank policymakers reflecting a dual mandate, weighing between stabilizing inflation around a target and unemployment around its “natural” level.¹ Third, agents do not know the central bank’s objectives and suspect that they evolve over time, and hence they continually update their beliefs about them based on observed policy behavior. I estimate the model using monthly data on inflation, unemployment and the federal funds rate over the postwar period in the U.S. together with 10-year ahead inflation expectations from the Survey of Professional Forecasters (SPF).

The central bank’s conduct of monetary policy is guided by the economic goals of the policymakers. In the model, monetary policy does not conform to any *instrument rule* but rather time-varying policy objectives.² Their policy decisions *reveal* information regarding their policy objectives. Hence, there is a non-trivial role for a “learning-channel” of monetary policy transmission in this environment through which policy simultaneously affects agents’ expectations by changing their beliefs about future policy behavior.

In the model, private agents’ expectations are shaped by beliefs about both the structural features of the economy and the time-varying objectives of policymakers. Hence, macroeconomic shocks by themselves do not cause agents’ expectations to de-anchor so long as policy responds the way they expect. It is the interaction between monetary policy, their perceptions about the state of the macroeconomy as well as their *ex-ante beliefs* regarding the incentives driving policymakers’ behavior that determine whether expectations are anchored and whether they remain anchored, rather than macroeconomic shocks in isolation.

Crucially, the agents make a distinction between *fundamental* inflation resulting from supply-side disturbances and *non-fundamental* inflation resulting from the policymakers’ pursuit of a nominal target. Their long-run inflation expectations are determined by their beliefs about the inflation target, while persistent supply shocks cause short-run expectations to depart from this long-run level. Given their perceptions about the policy-invariant structural state of the economy, they interpret the stance of policy. Unanticipated tilts in policy, or “policy surprises” are

¹Time-variation in policymakers’ stabilization preferences precludes commitment. The setup here is different from Kydland and Prescott (1977) where a time-invariant, commonly known social welfare function is assumed to exist. Here, policy is based on a legislative dual mandate, open to subjective interpretations by the policymakers.

²Instrument-rules such as the Taylor-rule are opaque regarding the trade-offs that policymakers actually face while deliberating about the conduct of monetary policy. It also causes an inconsistent asymmetry regarding how policy behavior is modeled, departing from the forward-looking optimizing framework modeling household and firm behavior. This critique is outlined in Svensson (2003).

partly attributed to idiosyncratic errors and partly to changes in the policymakers' stabilization preferences: their inflation target and the weight they place on stabilizing the unemployment gap - the deviation of the unemployment rate from its natural level. Anchoring or de-anchoring of expectations is an endogenous result of belief-formation under learning.

The model provides an information-theoretic perspective on how the conduct of monetary policy anchors expectations: it shows that agents prior beliefs about the policymakers' incentives shape how they interpret policy behavior. Anchoring is state-dependent. When agents perceive that the central bank places substantial weight on stabilizing unemployment gaps—rather than focusing on maintaining inflation around a target—their beliefs about the target remain more firmly anchored. In such an environment, agents view interest-rate movements as less informative about changes in the inflation target, rendering policy surprises less destabilizing for long-run expectations. An incentive to limit real-side volatility serves as a natural constraint against generating non-fundamental inflation in the discretionary pursuit of shifts in the nominal target. This learning mechanism helps explain why the two most prominent inflation crises of postwar U.S. —the Great Inflation of the 1970s and the post-pandemic surge—produced such different macroeconomic outcomes.

The estimated model traces the joint evolution of the economy and the Federal Reserve's systematic conduct of monetary policy over the postwar period in the U.S. from the perspective of private agents engaged in learning. In the run up to the Great Inflation, policy was perceived by the agents to be guided almost entirely by an unobservable nominal target, with little concern for stabilizing unemployment gaps, as if the natural rates posed little concern for policy deliberations. Beginning in the late 1960s, a sustained period of expansionary monetary policy conveyed that the inflation target had begun to drift upwards. Even as supply pressures mounted in the form of two great oil shocks in the 70s and real activity softened, policy maintained and over-accommodative stance. This behavior led to the agents sharply revising their beliefs about the inflation target upwards, resulting in the de-anchoring of long-run inflation expectations. Short-run and long-run inflation expectations rose in unison.

Over the recent years, particularly after the Global Financial Crisis, the agents have perceived the Fed to put a much greater emphasis on stabilizing the unemployment gap. This development has had important implications for the recent inflation surge. Even as the Fed demonstrated an unwillingness to respond to the inflation crisis, long-run inflation expectations remained remarkably stable: agents were slower to interpret the delayed policy response as evidence of a shift in the Fed's target. They rationalized the behavior as an increase in the policymakers' concern against creating unemployment gap volatility. This however, magnified the *pass*

through from perceived supply shocks to short-run inflation expectations since they perceived little incentive from policymakers to dampen the effects through adjustments on the real side. The mechanism explains the growing discord between the behavior of short- and long-horizon inflation expectations, also shedding light on how stabilizing short-run and long-run inflation expectations can be at odds when agents are learning using structural reasoning.

Much of the existing literature on learning has focused on *adaptive learning*, where agents form expectations using reduced-form forecasting rules: agents do not internalize the general equilibrium consequences of their beliefs, treating aggregate dynamics as being exogenous to their own behavior. This paper models *structural learning* (see [Williams \(2003\)](#)): agents form expectations based on a forward-looking structural model of aggregate dynamics that would arise from their optimizing behavior. While their knowledge is imperfect, their beliefs remain model-consistent and rational at all times.

The constraints posed by the imperfect information structure of the economy can make learning about certain structural features exceptionally slow. This is particularly relevant for learning about the slope of the Phillips curve, a key variable acting as the structural link between aggregate inflation and economic slack. Only aggregate demand shocks deliver information about this parameter and hence, agents update their beliefs about the slope primarily around demand-driven recessions.

Related literature: The New-Keynesian model emphasizes the importance of expectations for understanding the structure of aggregate dynamics and individual economic behavior. The literature has highlighted the importance of explicitly accounting for agents' expectations-formation process, using survey data for understanding macroeconomic phenomena (see [Coibion et al. \(2018\)](#), [Adam and Padula \(2011\)](#), [Milani \(2023\)](#), [Del-Negro and Eusepi \(2011\)](#)). This paper models how agents form expectations in real-time, employing survey data and New-Keynesian principles to get a disciplined perspective on how their evolving beliefs have shaped the postwar U.S. economy.

This paper is closely related to the literature examining how private agents' and policymakers' learning contributed to the Great Inflation of the 1970s and 1980s (e.g., [Bullard and Eusepi \(2005\)](#); [Primiceri \(2006\)](#); [Sargent, Williams and Zha \(2006\)](#), [Orphanides and Williams \(2005\)](#)). More broadly, it connects to the literature on how the private sector learns from monetary policy behavior. For instance, [Melosi \(2016\)](#) examines the signaling role of policy in a DSGE framework, where monetary policy is informative about aggregate shocks. By contrast, in this paper, the only source of information asymmetry arises from the private sector's inability to observe

the central bank’s possibly time-varying stabilization preferences.³ Other empirical papers have explored how agents infer policy targets from macroeconomic data (e.g., [Kozicki and Tinsley \(2005\)](#); [Erceg and Levin \(2003\)](#); [Orphanides and Williams \(2006\)](#)).⁴ However, much of this literature relies on adaptive learning, in which agents form beliefs using reduced-form forecasting rules based on historical correlations. In contrast, the learning behavior in this paper is grounded in a structural, forward-looking framework rooted in New Keynesian principles, where agents understand and internalize the effects of their expectations on macroeconomic outcomes.

The causes of the Great Inflation and the subsequent Great Moderation have been the subject of long-standing debate. One school attributes the volatility of the 1970s–80s era to “bad luck”: a sequence of large, adverse non-policy shocks (e.g., [Sims and Zha \(2006\)](#); [Bernanke and Mihov \(1998\)](#)). Under this view, the structure of the economy and policy rules remained largely stable; it was the volatility of exogenous shocks that changed. This view implies that monetary policy made little fundamental progress—if similar shocks were to recur, so would similar outcomes. However, I find that systematic monetary policy has shaped agents’ expectations in important ways, making their long-run inflation expectations more resilient.

An alternative view emphasizes policy errors. [Clarida, Gali and Gertler \(2000\)](#), [Taylor \(1993\)](#) and [Lubik and Schorfheide \(2004\)](#) argue that the shift to systematic anti-inflation policy by the Fed under the chairmanship of Paul Volcker was central to the subsequent stability. [DeLong \(1996\)](#) and [Romer and Romer \(2002\)](#) provide narrative evidence that policymakers in the 1970s were misled by a perceived long-run tradeoff between inflation and unemployment. Some papers study whether these policy mis-steps by the Fed were a result of “wrong” incentives. For example [Christiano and Gust \(2000\)](#) contend that the Fed fell into an “expectations trap”, lacking the incentives to take decisive action to rein in inflation expectations during the 70s. [Bianchi and Ilut \(2017\)](#) instead find that inflation during this period was fiscally led: Fed policy accommodated expansionary fiscal policy by remaining passive. In this paper, the focus is on whether private agents perceived policy surprises and to what extent these affected their beliefs rather than an ex-post evaluation of policy behavior.

A related strand of literature has studied the state-dependent nature of anchoring. [Carvalho, Eusepi, Moench and Preston \(2023\)](#) and [Gati \(2023\)](#) describe anchoring in terms of how agents

³Hence this paper is also broadly related to the literature examining time-variation in the Fed’s policy targets such as [Ireland \(2007\)](#), [Cogley, Primiceri and Sargent \(2010\)](#), [Del-Negro and Eusepi \(2011\)](#), and [Lakdawala \(2016\)](#). However, the focus in this paper is on private agents’ beliefs about the Fed’s objectives rather than the true policy objectives themselves.

⁴This paper is similar in spirit to [Bianchi \(2012\)](#) where agents learn about the active policy regime within a regime-switching model.

weight recent inflation data when updating their beliefs about the long-run mean of inflation based on past forecast errors (forecast-switching).⁵ In this paper, anchoring directly results from agents learning about the central bank’s stabilization preferences based on the policy response to inflation rather than the behavior of inflation itself.

This paper contributes to the debate by offering a framework that disentangles these explanations and sheds light on how each of these contributed to shaping the two prominent inflationary episodes in the post-war period in the U.S.

Outline: In Section 2, I motivate the agents’ perceived structural model describing the economy as perceived by private agents which they use to reason about the macroeconomic environment that they face. In Section 3, I describe how agents recursively update their beliefs regarding the policy-invariant structural variables in their model conditional on macroeconomic observations. In Section 4, I describe the conduct of monetary policy from the perspective of the agents and describe how they update beliefs regarding the policymakers’ stabilization preferences conditional on observed nominal interest rates. In Section 5, I describe the estimation methodology and the data. In Section 6, I discuss how the agents’ beliefs have evolved during the postwar period in the U.S. under learning followed by concluding remarks.

2 A forward looking model under imperfect knowledge

Here I begin by describing the information structure of the economy, defining the set of signals that agents observe at any time, based on which they form their beliefs and make decisions. Then, I derive the agents’ perceived law of motion describing the structural dynamics of the macroeconomic aggregates under imperfect knowledge.

2.1 Information structure and learning

Time is discrete ($t = 0, 1, 2, 3, \dots$). Under the information structure in the model, neither the latent structural parameters or the structural shocks are directly observed by the agents. The only relevant signals available to them comes in the form of the realizations of the aggregate inflation rate, unemployment rate and the nominal interest rate. At the beginning of each period

⁵A related line of research (King and Lu (2022) and Debortoli and Lakdawala (2016)) models anchoring in the context of the ability of the policymakers to commit.

t , firms and households make their decisions conditional on the history of signals observed until that point. The period- t inflation π_t and unemployment rate u_t then realize and are observed by the agents. The central bank then sets the interest rate i_{t+1} in anticipation of future outcomes. The agents interpret the policy decision and form beliefs regarding the policymakers' stabilization preferences. Thus, at the end of period- t , π_t , u_t and i_{t+1} are realized and observed by all agents.

The entire history of aggregate signals observed by agents up to (and including) period t_0 is denoted by:

$$\mathcal{H}^{t_0} = \{i_{t+1}\}_{t=-\infty}^{t_0} \cup \{z_t\}_{t=-\infty}^{t_0}$$

where $z_t = [\pi_t, u_t]'$ is the vector of realizations of inflation and unemployment, and i_{t+1} denotes the interest-rate policy set in period- t .

2.2 The agents' perceived model of aggregate dynamics

Following New Keynesian principles, I derive the log-linearized equations describing the structural dynamics of the economy from the perspective of the agents, based on a model of optimizing behavior by firms and households under imperfect knowledge. I assume that all private agents have common beliefs, formed conditional on the same data and model.⁶ I denote the private agents' expectations, formed conditional on history \mathcal{H}^t as E_t^P .

2.2.1 Aggregate demand: Households' consumption smoothing problem

Consider the problem of a representative household, deriving utility from consumption of an aggregate good and saving in nominal bonds every period conditional on their beliefs formed based on the history of signals observed in the past. In period- t , the household solves:

$$\max_{\{C_{t+k}\}_{k=0}^{\infty}} E^P \left[\sum_{k=0}^{\infty} \beta^k \frac{C_{t+k}^{1-\sigma}}{1-\sigma} \middle| \mathcal{H}^{t-1} \right] \quad (1)$$

where C_t is consumption, β is a discount factor, $\sigma > 0$ is the inverse of the intertemporal elasticity of substitution and E^P denotes the representative household's expectations, formed conditional on its model.

⁶I abstract from any distinction in firms and households' belief-formation process.

The household's budget constraint in nominal terms is:

$$P_t C_t + B_t = (1 + i_{t-1}) B_{t-1} + W_t + T_t + \Pi_t \quad (2)$$

where P_t is the aggregate price level, B_t are nominal bond holdings, i_{t-1} is the nominal interest rate in period $t - 1$, W_t denotes their nominal wage-income, T_t denote lump-sum government transfers and Π_t denotes profits from the ownership of firms.

In this setting, the only dynamic decision that the representative household makes is the savings decision, which leads to the following Euler equation:

$$C_t^{-\sigma} = \beta E^P \left[C_{t+1}^{-\sigma} \frac{1 + i_t}{1 + \pi_{t+1}} \middle| \mathcal{H}^{t-1} \right] \quad (3)$$

where $1 + \pi_{t+1} = P_{t+1}/P_t$ is the aggregate inflation rate.

Since there is no investment or government expenditure in the model, all output is consumed every period $Y_t = C_t$, log-linearizing around the steady state, we get the aggregate-demand IS-curve:

$$\hat{y}_t = E_{t-1}^P[\hat{y}_{t+1}] - \frac{1}{\sigma}(i_t - E_{t-1}^P[\pi_{t+1}] - \rho) \quad (4)$$

where \hat{y}_t denotes the log-deviation of output from its steady-state. $\rho = -\log \beta$. Defining the *ex-ante* real interest rate as $r_t = i_t - E_{t-1}^P[\pi_{t+1}]$, the IS curve may be more compactly written as:

$$\hat{y}_t = E_{t-1}^P[\hat{y}_{t+1}] - \frac{1}{\sigma}(r_t - \rho) \quad (5)$$

At some hypothetical real interest rate, output would continue along the trend path, y_t^n (or the “natural” level of output) absent cyclical fluctuations. We call this the natural rate of interest and denote it by r_t^n . Log-deviations in the natural level of output \hat{y}_t^n follow:

$$\hat{y}_t^n = E_{t-1}^P[\hat{y}_{t+1}^n] - \frac{1}{\sigma}(r_t^n - \rho) \quad (6)$$

Subtracting Equation 6 from Equation 5 yields:

$$\hat{y}_t - \hat{y}_t^n = E_{t-1}^P[\hat{y}_{t+1} - \hat{y}_{t+1}^n] - \frac{1}{\sigma}(r_t - r_t^n) \quad (7)$$

Denoting $\hat{y}_t - \hat{y}_t^n$ as output gap \tilde{y}_t , we may re-write the dynamic IS curve in terms of output

gap as:

$$\tilde{y}_t = E_{t-1}^P[\tilde{y}_{t+1}] - \frac{1}{\sigma}(i_t - E_{t-1}^P[\pi_{t+1}] - r_t^n) \quad (8)$$

2.2.2 Aggregate supply: Firms' pricing problem

Firm price-setting under dispersed information Every period t , all firms automatically adjust their prices by the perceived trend inflation rate conditional on their $t-1$ information set, given by π_{t-1}^{*P} .⁷ The perceived level of trend inflation does not enter firms' pricing problem since all firms have the same beliefs and adjust to the same perceived trend rate every period. However, relative price adjustments are subject to Calvo frictions. Only a constant fraction $(1-\theta)$ of firms are able to adjust their price every period (adjustment frequency θ is common knowledge). All firms set prices in order to earn a constant markup over their nominal marginal cost. The steady-state relative price of each firm is unity. For concision, we express their optimal price setting problem in terms of log-deviations from steady-state.

In the absence of Calvo frictions, log-deviation in firm j 's optimal price is equal to the sum of log-deviations in the aggregate price-level, denoted as \hat{p}_t and log-deviations in their real marginal cost, $\hat{m}c_t(j)$.

$$\hat{p}_t^*(j) = \hat{p}_t + \hat{m}c_t(j)$$

Under Calvo frictions, firms cannot set prices flexibly, so that each firm must set prices in order to receive a constant markup *in expectation*. Their optimal price is given by:

$$\hat{p}_t^*(j) = (1-\beta\theta)E^j\left[\sum_{k=0}^{\infty}(\beta\theta)^k(\hat{p}_{t+k} + \hat{m}c_{t+k}(j))|\mathcal{H}^{t-1}\right] \quad (9)$$

where $E^j[\cdot]$ denotes the expectation operator conditional on firm j 's information set. The firms' information set is the same as that of the representative households, and is denoted by \mathcal{H}^{t-1}

Additionally, each firm observes its own real marginal cost $\hat{m}c_t(j)$ at the beginning of the period. $\hat{m}c_t(j)$ is composed of an economy-wide component $\hat{m}c_t$ plus an idiosyncratic firm-specific *i.i.d* (across firms and across time) component, $\varepsilon_t(j)$ with *large* variance.⁸

$$\hat{m}c_t(j) = \hat{m}c_t + \varepsilon_t(j) \quad \varepsilon_t(j) \sim N(0, \sigma_\varepsilon^2) \quad \forall j \in (0, 1) \quad (10)$$

⁷This assumption permits the model to be log-linearized around the zero inflation steady state despite non-zero trend inflation. Inflation here refers to inflation beyond this "normal" level.

⁸This assumption is motivated by the observation that firm-specific price changes are much more volatile as compared to fluctuations in the aggregate price-level. This modeling framework is based on [Nimark \(2008\)](#).

Under knowledge that it can only reset with probability $1 - \theta$ any period in the future would, the optimal price is given by:

$$\hat{p}_t^*(j) = (1 - \beta\theta)E^j \left[\sum_{k=0}^{\infty} (\beta\theta)^k (\hat{p}_{t+k} + \hat{m}c_{t+k}(j)) | \mathcal{H}^{t-1} \cup \hat{m}c_t(j) \right] \quad (11)$$

Dispersed information assumption: The firm is atomistic, its own marginal cost reveals negligible information about innovations to the economy-wide real marginal costs or changes in the aggregate price level p_t . Thus, their expectations regarding these variables are unchanged upon observing $\hat{m}c_t(j)$ and common across all firms, denoted as E_{t-1}^P . Hence:

$$E^j[\hat{p}_t + \hat{m}c_t(j) | \mathcal{H}^{t-1} \cup \hat{m}c_t(j)] = E_{t-1}^P \hat{p}_t + \hat{m}c_t(j) \quad (12)$$

$$E^j[\hat{p}_{t+k} + \hat{m}c_{t+k} | \mathcal{H}^{t-1} \cup \hat{m}c_t(j)] \approx E_{t-1}^P \hat{p}_{t+k} + E_{t-1}^P \hat{m}c_{t+k} \quad \forall k \geq 0 \quad (13)$$

Log-deviations in firm j's optimal reset price may be written as:

$$\hat{p}_t^*(j) = (1 - \beta\theta)(E_{t-1}^P \hat{p}_t + \hat{m}c_t(j)) + \beta\theta E_{t-1}^P \hat{p}_{t+1}^* \quad (14)$$

All firms face the same price-setting problem, just observe a different marginal cost signal. Aggregating across firms yields:

$$\hat{p}_t^* = (1 - \beta\theta)(E_{t-1}^P \hat{p}_t + \hat{m}c_t) + \beta\theta E_{t-1}^P \hat{p}_{t+1}^* \quad (15)$$

Under a Calvo-probability of price adjustment of $(1 - \theta)$, evolution of the aggregate price index satisfies:

$$\hat{p}_t = \theta \hat{p}_{t-1} + (1 - \theta) \hat{p}_t^* \quad (16)$$

Combining Equation 15 and Equation 16 yields the aggregate supply condition in terms of the aggregate inflation rate $\pi_t = \hat{p}_t - \hat{p}_{t-1}$:

$$\pi_t = \beta E_{t-1}^P \pi_{t+1} + \frac{(1 - \theta)(1 - \beta\theta)}{\theta} \hat{m}c_t + \frac{(1 - \theta)^2(1 - \beta\theta)}{\theta} (E_{t-1}^P \hat{m}c_t - \hat{m}c_t) \quad (17)$$

The expectational errors manifest due to the fact that the economy-wide real marginal cost is

not perfectly forecast-able. If the firms' private signal revealed \hat{mc}_t perfectly, we would go back to the standard New-Keynesian Phillips curve formulation and the expectational error term goes away. Also, it can be seen that the smaller the degree of price-stickiness (θ), the larger the contribution of these errors to actual inflation.

Pro-cyclicality of marginal cost The economy-wide real marginal cost mc_t is unobservable. Agents can only infer it from the realizations of macroeconomic aggregates. The structural dynamics driving the economy-wide component of real-marginal costs are unknown, but agents posit a pro-cyclical relationship: when output is above the flex-price level, it puts upward pressure on real marginal costs across all firms. Variation in \hat{mc}_t above and beyond this pro-cyclical channel are attributed to economy-wide supply shocks, s_t . Hence, they perceive the following structural relationship:

$$\hat{mc}_t = \gamma \tilde{y}_t + s_t$$

where s_t denotes the supply shock, assumed to follow a mean-zero stationary process and independent of the unemployment-gap \tilde{y}_t . $\gamma > 0$ represents the link between economy-wide real marginal cost and the cyclical fluctuations in unemployment. It is assumed to be constant, but unknown.

The agents' reasoning motivates the following forward-looking Phillips curve:

$$\pi_t = \beta E_{t-1}^P[\pi_{t+1}] + \psi \tilde{y}_t + \xi_t \quad (18)$$

where (i) $E_{t-1}^P[\pi_{t+1}]$ denotes the private-sector's expectation of inflation in period $t+1$ conditional on history of signals \mathcal{H}^{t-1} (ii) ψ represents the sensitivity of inflation to current output-gap. Agents assume ψ is constant but unknown and hence learn about it every period. (iii) ξ_t is a cost-push shock composed of the supply-shock s_t and the expectational error.

The cost-push shock ξ_t captures the component of inflationary pressures arising from factors over and beyond the output gap. Agents allow for the possibility that the cost-push shocks have a persistent component. Hence they decompose the cost-push shock, ξ_t into a *persistent* AR(1) component denoted by ξ_t^p , with large persistence ρ and a *transitory* i.i.d normal component ξ_t^T .

$$\xi_t = \xi_t^p + \xi_t^T, \quad \xi_t^T \sim iid N(0, \sigma_{\xi,T}^2)$$

The persistent component is perceived to evolve as:

$$\xi_t^p = \rho \xi_{t-1}^P + \varepsilon_t^P, \quad \varepsilon_t^P \sim iid N(0, \sigma_{\xi,P}^2)$$

Only the persistent component ξ_t^p affects future outcomes. Agents must learn about this shock to form expectations about the future. ξ_t^T functions as observation noise.

Natural rate hypothesis: Agents in the model a-priori assume that monetary policy cannot systematically drive real variables once prices and expectations fully adjust. Under the natural rate hypothesis, the output and the real interest rate attain their natural levels in the long-run, beyond the control of monetary policy. This is equivalent to agents assuming that the discount-factor $\beta \rightarrow 1$ so that expectations-augmented Phillips curve is vertical in the long-run.⁹ Agents reason that in the long run, monetary policy can only sustain non-zero inflation, not output gap.

2.2.3 Measuring real-economic activity

Economic slack, as measured by the *output gap* is an important variable driving aggregate inflation and forms the important structural link between interest-rate policy and aggregate inflation. However, it is not directly observable. It must be inferred based on real time indicators of economic activity. I assume that the only real indicator in this economy, informing agents about the state of aggregate demand is the unemployment rate. This is due to the unemployment rate being a salient variable, directly part of the dual mandate that most modern central banks in the world, including the Fed follow. For this reason, it is useful to re-frame the analysis in terms of unemployment gaps, defined as the difference between the realized unemployment rate and the one that would prevail under flexible prices, or the “natural” rate of unemployment.

In the model, the agents posit a linear relationship between the output gap and the unemployment gap¹⁰ defined as the difference between the unemployment rate and the natural rate of unemployment (empirically, the “trend” component of unemployment rate): $x_t = u_t - u_t^n$, we have

$$\tilde{y}_t = -\eta x_t$$

where η is referred to as the Okun’s law coefficient.

This yields the following dynamic IS-curve representing the law of motion of the unemployment-gap:

$$x_t = E_{t-1}^P x_{t+1} + \tau(i_t - E_{t-1}^P \pi_{t+1} - r_t^n) \quad (19)$$

where $\tau = \frac{1}{\sigma\eta}$ represents the ratio of the intertemporal elasticity of substitution and the Okun’s

⁹Since otherwise, the long-run unemployment-gap must be non-zero from [Equation 20](#).

¹⁰This relationship is sometimes referred to as Okun’s law. [Ball et al. \(2017\)](#) find that it has been relatively stable across time.

law coefficient. τ is assumed to be constant and known to all agents.

Similarly, the expectations-augmented Phillips curve in terms of unemployment gap becomes:

$$\pi_t = E_{t-1}^P \pi_{t+1} - \kappa x_t + \xi_t \quad (20)$$

where $\kappa = \psi\eta$ is assumed to be a constant that the agents learn about.

3 Learning: Latent structure of the economy

Every period, conditional on the observed unemployment rate u_t , all agents infer the contemporaneous unemployment gap, x_t and update their beliefs about the natural rate of interest r_t^n . Conditional on these, agents update their beliefs about the slope of the Phillips curve κ , and the persistent supply shock ξ_t^p based on the observed aggregate inflation rate π_t . Thus, they inform themselves regarding all the latent structural variables describing economic dynamics in their model, every period. The rest of the section discusses the mechanics of their learning behavior.

3.1 Learning and the Anticipated Utility assumption

This paper takes the anticipated utility approach to learning described in [Kreps \(1998\)](#). Under this assumption, agents form “certainty-equivalent” estimates of the relevant state-variables every period and treat their best estimates as if they were constants known with certainty when making decisions. Agents disregard the possibility of updating their current estimates in the future. This assumption is widely used in the literature on learning in macroeconomics (see [Evans and Honkapohja \(2001\)](#)). It allows us to surmount the computational challenges associated with solving the dynamic problem in the full Bayesian setting. [Cogley and Sargent \(2008\)](#) demonstrate how the anticipated utility assumption provides an excellent approximation to Bayesian decision-making in a wide class of problems.

3.2 Inferring unemployment gap x_t

Conditional on the observed unemployment rate u_t , agents update their estimate of the natural rate u_t^n according to the univariate smoothing algorithm:

$$u_t^n = u_{t-1}^n + g_u(u_t - u_{t-1}^n) \quad (21)$$

The natural rate is inferred from a backward-looking filter based on the unemployment rate, putting more weight on recent observations. The gain coefficient g_u determines the degree to which shifts in the unemployment rate are attributed to shifts in the natural rate of unemployment. g_u is constant and known to all agents.

From the natural rate hypothesis, $\lim_{h \rightarrow \infty} x_{t+h} = 0$. Hence, the unemployment rate is always expected to converge to the natural rate u_t^n in the long-run equilibrium, consistent with the update-rule [Equation 21](#).¹¹

Agents' estimate of the contemporaneous unemployment gap is:

$$x_t = u_t - u_t^n$$

I abstract from issues of real-time mis-measurement and data revisions. I do however find that the agents' real-time measure inferred from data lines up quite well with series that are revised retroactively (the CFNAI index as an example, see [Appendix D](#)) suggesting that these issues are not of large consequence over the sample period.

¹¹ [Staiger, Stock and Watson \(1997\)](#) and [Orphanides and van Norden \(2002\)](#) show that such univariate algorithms deliver estimates that are essentially indistinguishable from the ones derived under more sophisticated procedures. Similarly, [Kamber, Morley and Wong \(2018\)](#) demonstrate that economic slack-measures derived from similar univariate procedures can be robust to revisions and are found to be in line with more refined measures of real-time economic activity (such as the Chicago Fed National Economic Activity Index).

3.3 Recursive updating

Agents' perceived model of aggregate dynamics: The equations describing the aggregate laws of motion of the economy from the perspective of the private agents are:

$$x_t = E_{t-1}^P[x_{t+1}] + \tau(i_t - E_{t-1}^P[\pi_{t+1}] - r_t^n)$$

$$\pi_t = E_{t-1}^P[\pi_{t+1}] - \kappa x_t + \xi_t^p + \xi_t^T, \quad \xi_t^T \sim iid N(0, \sigma_{\xi,T}^2)$$

$$\xi_t^p = \rho \xi_{t-1}^P + \varepsilon_t^P, \quad \varepsilon_t^P \sim iid N(0, \sigma_{\xi,P}^2)$$

Conditional on the observed aggregate inflation rate π_t and the unemployment gap x_t inferred from u_t based on the de-trending procedure, agents update their beliefs regarding κ , ξ_t^p and r_t^n recursively every period treating $[\sigma_{\xi,T}^2, \sigma_{\xi,P}^2, \tau, \rho]$ as known constants.

Learning the natural rate of interest r_t^n : Conditional on the inferred unemployment-gap x_t , the contemporaneous estimate of the natural rate of interest $r_{t|t}^n$ is given by the dynamic IS curve ([Equation 19](#)):

$$r_{t|t}^n = \tau^{-1}(E_{t-1}^P x_{t+1} - x_t) + i_t - E_{t-1}^P \pi_{t+1}$$

Further, agents assume that r_t^n follows a Martingale, so that $r_{t+1|t}^n = r_{t|t}^n$

Learning ξ_t^p and κ : Given the unemployment-gap x_t , beliefs about the persistent component of the cost-push shock ($\xi_{t|t}^p$) and the slope of the Phillips curve ($\kappa_{t|t}$) are recursively updated every period based on observed aggregate inflation rate π_t .

Agents face a signal-extraction problem in real time: they cannot immediately distinguish whether an inflation surprise was driven by the unemployment-gap (due to mis-perception of the slope κ), persistent supply shocks—relevant for dynamics—or transitory supply shocks, irrelevant for dynamics.

The observation equation, relating aggregate inflation to ξ_t^p and κ in the agents' perceived model is given by:

$$\pi_t - E_{t-1}^P \pi_{t+1} = \begin{pmatrix} -x_t & 1 \end{pmatrix} \begin{pmatrix} \kappa \\ \xi_t^p \end{pmatrix} + \xi_t^T, \quad \xi_t^T \sim N(0, \sigma_{\xi,T}^2).$$

The state-transition equation specifying the agents' prior regarding how the state variables κ and ξ_t^p evolve over time is given by:

$$\begin{pmatrix} \kappa \\ \xi_t^p \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & \rho \end{pmatrix} \begin{pmatrix} \kappa \\ \xi_{t-1}^p \end{pmatrix} + \begin{pmatrix} 0 \\ \epsilon_t^P \end{pmatrix}, \quad \epsilon_t^P \sim N(0, \sigma_{\xi, P}^2)$$

Note that the state-transition equation reflects the agents' prior that the true slope κ is time-invariant.

4 Learning: Policymakers' stabilization preferences

Given their beliefs regarding the latent structural variables - the slope of the Phillips curve $\kappa_{t|t}$, the persistent supply shock $\xi_{t|t}^p$ and the natural rate of interest $r_{t|t}^n$, the agents interpret the period- t policy decision i_{t+1} and learn about the policymakers' stabilization preferences underlying policy behavior. The next subsection describes the policymakers' optimal policy problem under a dual mandate, based on [Svensson and Woodford \(2004\)](#).

4.1 Monetary policy

The private-agents assume that the central bank conducts monetary policy optimally under discretion, having the same beliefs about the policy-invariant latent structural variables as them formed based on the same economic model and data. The central bank's *dual mandate* characterized by the following loss function¹²:

$$\mathcal{L}_t = \sum_{j=1}^{\infty} [(\pi_{t+j|t} - \pi_t^*)^2 + \lambda_t x_{t+j|t}^2] \quad (22)$$

where $\pi_{t+j|t}$ and $x_{t+j|t}$ denote the central bank's forecasts of inflation and the unemployment gap for period $t + j$ formed in period- t after the contemporaneous π_t, x_t have been realized. Here, π_t^* and λ_t represent the policymakers' period- t stabilization preferences: their inflation target and the relative weight they place on unemployment-gap stabilization. Private agents do not observe these and assume that they are subject to slow innovations over time. Their beliefs

¹²Agents assume that the central bank's policy preferences are not fundamentally incompatible. There is no stabilization bias.

regarding these parameters conditional on \mathcal{H}^t are denoted by π_t^{*P} and λ_t^P .

The central bank in its period- t decision cycle chooses the one-period ahead unemployment gap plan $x_{t+1|t}$. Private agents' period- t expectations regarding future inflation and unemployment gaps formed prior to observing the policy decision (denoted by $E_t^{P-}\pi_{t+j}$ and $E_t^{P-}x_{t+j}$) are observed by the central bank.¹³ Every period, the central bank chooses $x_{t+1|t}$ which solves its period- t static optimization problem taking the observed private-sector expectations as given, conditional on the following structural constraint implied by the Phillips curve:

$$\pi_{t+1|t} = E_t^{P-}\pi_{t+2} - \kappa_{t|t}x_{t+1|t} + \xi_{t+1|t} \quad (23)$$

The optimal unemployment gap plan $x_{t+1|t}$ is given by the targeting rule:

$$x_{t+1|t} = \frac{\kappa_{t|t}}{\lambda_t}(\pi_{t+1|t} - \pi_t^*) \quad (24)$$

[Equation 24](#) describes the textbook “lean against the wind” policy solution where the central bank reacts by creating a positive unemployment gap if it expects inflation to be above its target in the following period.

Using [Equation 23](#) and [Equation 24](#), the central bank's one-period ahead inflation and unemployment gap plan must satisfy:

$$\pi_{t+1|t} = \pi_t^* + \frac{\lambda_t}{\lambda_t + \kappa_{t|t}^2}(E_t^{P-}\pi_{t+2} + \xi_{t+1|t} - \pi_t^*) \quad (25)$$

$$x_{t+1|t} = \frac{\kappa_{t|t}}{\lambda_t + \kappa_{t|t}^2}(E_t^{P-}\pi_{t+2} + \xi_{t+1|t} - \pi_t^*) \quad (26)$$

[Equation 25](#) shows that when $\lambda_t > 0$, the central bank allows inflation to rise above its target when faced with a persistent cost-push shock. Deviations of inflation from the target, arising from private agents' inflation expectations and persistent cost-push shocks are accommodated to an extent. The larger λ_t is, the greater the accommodation, with $\lambda_t \rightarrow \infty$ characterized by the scenario where the central bank can no longer push back against private agents' expectations anymore. This represents an “expectations-trap” in the sense of [Christiano and Gust \(2000\)](#) that policymakers fall into where any real-side adjustment is deemed too costly. In the same vein, [Equation 26](#) shows that the extent of unemployment gap adjustments that policymakers

¹³ E_t^{P-} denote expectations formed after the realization of the contemporaneous aggregates $z_t = [\pi_t, u_t]$ but before the period- t policy decision, and are thus conditional on beliefs $\kappa_{t|t}, \xi_{t|t}^P, \pi_{t-1}^{*P}, \lambda_{t-1}^P$.

will engage in, is decreasing in λ_t .¹⁴

4.2 Private sector expectations in a learning equilibrium

Under rationality, private-agents' expectations for all future horizons must be consistent with their structural model of inflation dynamics¹⁵:

$$E^P[\pi_{t+j}] = E^P[\pi_{t+j+1}] - E^P[\kappa x_{t+j}] + E^P[\xi_{t+j}] \quad \forall j \geq 1$$

The constraint above yields the following forward looking system of equations that their expectations at any period t must satisfy:

$$E_t^P \pi_{t+j} = E_t^P \pi_{t+j+1} - \kappa_{t|t} E_t^P x_{t+j} + \rho^j \xi_{t|t}^p$$

From the “lean against the wind” targeting rule, their unemployment gap expectations are:

$$E_t^P x_{t+j} = \frac{\kappa_{t|t}}{\lambda_t^P + \kappa_{t|t}^2} (E_t^P \pi_{t+j+1} + \rho^j \xi_{t|t}^p - \pi_t^{*P}) \quad (27)$$

Solving forward, we get an analytical expressions describing their inflation and unemployment gap expectations for all future horizons in terms of their beliefs $\kappa_{t|t}$, $\xi_{t|t}^p$, π_t^{*P} , λ_t^P formed conditional on \mathcal{H}^t :

$$E_t^P \pi_{t+j} = \underbrace{\pi_t^{*P}}_{\text{perceived target}} + \underbrace{\frac{\lambda_t^P}{\lambda_t^P(1-\rho) + \kappa_{t|t}^2} \rho^j \xi_{t|t}^p}_{\text{cost-push inflation}} \quad (28)$$

$$E_t^P x_{t+j} = \frac{\kappa_{t|t}}{\lambda_t^P(1-\rho) + \kappa_{t|t}^2} \rho^j \xi_{t|t}^p \quad (29)$$

Their expectations reflect simple economic intuition. According to Equation 28, from the private-agents' perspective, the path of inflation is ultimately determined by two forces: (i) π_t^{*P} , representing their beliefs about the central bank's inflation target, defines the level that the agents expect inflation to converge to in the long run. Inflation expectations at all horizons move one-for-one with π_t^{*P} . Hence this belief is a crucial determinant of the low-frequency (slow-moving) dynamics of inflation; and (ii) persistent supply shocks $\xi_{t|t}^p$, which create involuntary inflation above and beyond this voluntary level in the short-run: the extent of their *pass-through*

¹⁴The expression $\frac{\kappa_{t|t}}{\lambda_t^P + \kappa_{t|t}^2}$ is bounded above by $\frac{1}{2\sqrt{\lambda_t}}$. So even though it also depends on κ_t , its limiting behavior is determined by λ_t .

¹⁵Here, I implicitly assume that agents' beliefs are consistent with the law of iterated expectations.

to short-run inflation expectations is *decreasing* in the perceived slope of the Phillips curve $\kappa_{t|t}$ but *increasing* in λ_t^P , the perceived weight that the central bank puts on unemployment-gap stabilization. Thus, when agents perceive the central bank to prioritize real-side stabilization (λ_t^P is large), their short-run inflation expectations respond to persistent supply shocks strongly and causes them to depart further away from the long-run level, π_t^{*P} .

Perceived policy rule: The interest-rate i_{t+1}^* that implements the optimal unemployment gap plan is given by the IS-curve:

$$i_{t+1}^* = \tau^{-1}(x_{t+1|t} - E_t^{P-}x_{t+2}) + E_t^{P-}\pi_{t+2} + r_{t+1|t}^n$$

The agents' expectations $E_t^{P-}\pi_{t+j}$ and $E_t^{P-}x_{t+j}$, given their ex-ante beliefs about policymakers' preferences are given by:

$$\begin{aligned} E_t^{P-}\pi_{t+j} &= \pi_{t-1}^{*P} + \frac{\lambda_{t-1}^P}{\lambda_{t-1}^P(1-\rho) + \kappa_{t|t}^2} \rho^j \xi_{t|t}^p \\ E_t^{P-}x_{t+j} &= \frac{\kappa_{t|t}}{\lambda_{t-1}^P(1-\rho) + \kappa_{t|t}^2} \rho^j \xi_{t|t}^p \end{aligned}$$

We obtain the following expression mapping the policymakers' period- t preferences to the optimal nominal interest rate:

$$i_{t+1}^*(\pi_t^*, \lambda_t) = \underbrace{-\tau^{-1}E_t^{P-}x_{t+2} + r_{t|t}^n + E_t^{P-}\pi_{t+2}}_{\text{ex-ante known}} + \underbrace{\frac{\tau^{-1}\kappa_{t|t}}{\lambda_t + \kappa_{t|t}^2} (E_t^{P-}\pi_{t+2} + \rho\xi_{t|t}^p - \pi_t^*)}_{\text{contains information about Fed objectives}}$$

When the central bank sets interest rates, it reveals information regarding its policy preferences. This is the only relevant information that interest rates reveal, since all the other variables in [Equation 4.2](#) are known ex-ante. Only the last term depends on the policymakers' true policy preferences π_t^* and λ_t and therefore contains new information. The coefficient $\frac{\tau^{-1}\kappa_{t|t}}{\lambda_t + \kappa_{t|t}^2}$ partly controls the strength of the signaling channel. Observe that as λ_t increases, this term shrinks and the signal becomes weak.

In the limiting case of $\lambda_t \rightarrow \infty$, interest rates carry no independent information: systematic policy is entirely determined by the private agents' ex-ante expectations and the perceived natural rate of interest. As a result, the "learning channel" of policy completely dies out. Consequently, when agents perceive the central bank to only care about unemployment gap stabilization, they

expect the unemployment gap to be zero at all future horizons and the central bank is seen to implement a Wicksellian policy: with the ex-ante real interest rate $i_{t+1}^* - E_t^{P-} \pi_{t+2}$ tracking the perceived natural rate of interest $r_{t|t}^n$ closely. In this case, policymakers are expected to tolerate arbitrary deviations in inflation: there is no inflation-target and policy contains no information about the long-run level of inflation, leading to self-fulfilling dynamics. Note that policy response to $E_t^{P-} x_{t+2}$ and $r_{t|t}^n$ does not depend on λ_t - since they don't pose a trade-off.

4.3 Monetary policy surprises

The agents assume that the central bank sets interest rates optimally every period up to some idiosyncratic policy error of constant variance so that¹⁶:

$$i_{t+1} = i_{t+1}^* + \epsilon_t^i, \quad \epsilon_t^i \sim N(0, \sigma_i^2)$$

Whenever the nominal interest rate is different from what the private agents expect from systematic policy, given their beliefs about prevailing macroeconomic conditions, it constitutes a monetary policy surprise:

$$\underbrace{i_{t+1} - E^{P-} i_{t+1}}_{\text{monetary policy surprise}} = \underbrace{(i_{t+1}^* - E^{P-} i_{t+1}^*)}_{\text{shift in systematic policy}} + \underbrace{\epsilon_t^i}_{\text{idiosyncratic policy error}}$$

Agents interpret policy surprises as stemming from two sources: shifts in policymakers' preferences, which they must learn about, or a idiosyncratic policy errors carrying no information about future policy behavior. But they cannot tell whether a given surprise reflects a goal-oriented shift in policy or an unintended error.

4.4 The nonlinear filter

The observed nominal interest rate functions as a noisy signal about the central bank's preferences $[\pi_t^*, \lambda_t]$, which describe the relevant state that the agents learn about:

$$i_{t+1} = i_{t+1}^*(\pi_t^*, \lambda_t) + \epsilon_t^i, \quad \epsilon_t^i \sim N(0, \sigma_i^2)$$

¹⁶The source of this error could be motivated as coming from cognitive noise in decision-making. It could also be thought of as a "control error". The main idea being that the private agents allow for idiosyncratic deviations from optimal policy arising from factors unrelated to changes in the policymakers' stabilization preferences.

Linearizing around agents' prior estimates $\pi_{t-1}^P, \lambda_{t-1}^P$ assuming $\pi_t^* \approx \pi_{t-1}^P, \lambda_t \approx \lambda_{t-1}^P$ ¹⁷

$$i_{t+1}^*(\pi_t^*, \lambda_t) \approx i_{t+1}^*(\pi_{t-1}^{*P}, \lambda_{t-1}^P) + \frac{\partial i_{t+1}^*}{\partial \pi_t^*}|_{\pi_{t-1}^{*P}, \lambda_{t-1}^P} (\pi_t^* - \pi_{t-1}^{*P}) + \frac{\partial i_{t+1}^*}{\partial \lambda_t}|_{\pi_{t-1}^{*P}, \lambda_{t-1}^P} (\lambda_t - \lambda_{t-1}^P)$$

The monetary policy surprise, $\Delta_t = i_{t+1} - i_{t+1}^*(\pi_{t-1}^{*P}, \lambda_{t-1}^P)$ is:

$$\Delta_t = \frac{\partial i_{t+1}^*}{\partial \pi_t^*}|_{\pi_{t-1}^{*P}, \lambda_{t-1}^P} (\pi_t^* - \pi_{t-1}^{*P}) + \frac{\partial i_{t+1}^*}{\partial \lambda_t}|_{\pi_{t-1}^{*P}, \lambda_{t-1}^P} (\lambda_t - \lambda_{t-1}^P) + \epsilon_t^i, \quad \epsilon_t^i \sim N(0, \sigma_i^2)$$

The approximation above (called the Extended Kalman Filter) yields an expression for i_{t+1}^* that is linear in the latent states π_t^* and λ_t much like the simple Kalman filter. The key difference is that the coefficients mapping the observable i_{t+1}^* to the latent states are not constant, but state-dependent. They are determined by the partial derivatives of the interest rate rule with respect to π_t^* and λ_t evaluated at the agents' prior estimates π_{t-1}^{*P} and λ_{t-1}^P . These determine how "informative" interest rates are perceived to be regarding the policymakers' stabilization preferences.

The agents perceive that $\log \pi_t^*$ and $\log \lambda_t$ evolve exogenously as independent random walks, so that¹⁸:

$$\begin{pmatrix} \log \pi_t^* \\ \log \lambda_t \end{pmatrix} = \begin{pmatrix} \log \pi_{t-1}^* \\ \log \lambda_{t-1} \end{pmatrix} + \begin{pmatrix} \epsilon_t^{\pi^*} \\ \epsilon_t^\lambda \end{pmatrix}, \quad \begin{pmatrix} \epsilon_t^{\pi^*} \\ \epsilon_t^\lambda \end{pmatrix} \sim N(\mathbf{0}, \begin{pmatrix} \sigma_{\pi^*}^2 & 0 \\ 0 & \sigma_\lambda^2 \end{pmatrix})$$

Every period, agents update their beliefs π_t^{*P} and λ_t^P based on their best-estimates as:

$$\pi_t^{*P} = \pi_{t|t}^*, \quad \lambda_t^P = \lambda_{t|t}$$

4.5 What anchors long-run beliefs?

Anchoring reflects the entrenchment of expectations, where beliefs about the future remain resilient to surprises. The following quote by Ben Bernanke summarizes what anchoring means in the context of monetary policy:

¹⁷This assumption is important for the filtering problem to be well-specified. Since interest-rate dynamics would be state-dependent due to the nonlinearity of i_{t+1}^* , large discrepancies can cause the filter to diverge. The assumption implies that under their own beliefs, the agents track changes in the policymakers' preferences efficiently at all times. In Appendix G, I report evidence in support of this assumption based on the Fed's Greenbook forecasts.

¹⁸The perceived dynamics reflect agents' beliefs that π_t^* and λ_t are non-negative.

“...I use the term “anchored” to mean relatively insensitive to incoming data. So, for example, if the public experiences a spell of inflation higher than their long-run expectation, but their long-run expectation of inflation changes little as a result, then inflation expectations are well anchored...”

According to [Equation 28](#), agents’ long-run inflation expectations are completely pinned down by their beliefs regarding the central bank’s inflation target. For inflation expectations to be “well-anchored” according to this definition, agents should not revise their beliefs regarding the target by much even as they anticipate inflation to remain elevated in the short-run on account of persistent supply shocks. In the model, revisions to agents’ long-run inflation expectations occur only in response to interest rate surprises. The degree of *pass-through* from these surprises to their perceived inflation target depends on how informative they perceive policy actions to be regarding shifts in the central bank’s inflation target π_t^* .

4.5.1 Anchoring: An information-theoretic perspective

Based on their views about how policymakers operate, the volume of information regarding these parameters contained in a signal i_{t+1} would be given by its Fisher information which is a measure of the curvature of the log-likelihood function. Fisher information tells us how well an observation is able to “locate” a parameter. The marginal increase in the Fisher information upon receiving a signal is the Fisher information increment, \mathcal{I}_t . It is given by:

$$\mathcal{I}_t = \frac{1}{\sigma_i^2} \mathbf{H}_t^\top \mathbf{H}_t, \quad \mathbf{H}_t = \left[\frac{\partial i_{t+1}^*(\pi_t^*, \lambda_t)}{\partial \pi_t^*}, \frac{\partial i_{t+1}^*(\pi_t^*, \lambda_t)}{\partial \lambda_t} \right]_{\pi_{t-1}^{*P}, \lambda_{t-1}^P}$$

\mathbf{H}_t is the Jacobian of i_{t+1}^* , evaluated at their ex-ante beliefs. \mathcal{I}_t is decreasing in σ_i^2 , the variance of the idiosyncratic noise term. Clearly, the larger the noise, the less informative the signal is. Also, if private agents expect interest rates to be sensitive to changes in the underlying preferences, they would perceive interest rates to be more informative. This sensitivity is given by the Jacobian \mathbf{H}_t . Since σ_i^2 is constant, the Jacobian determines the perceived informativeness of the interest rate signal. Consider the partial derivative with respect to π_t^* :

$$\frac{\partial i_{t+1}^*}{\partial \pi_t^*} \Big|_{(\pi_{t-1}^{*P}, \lambda_{t-1}^P)} = -\frac{\tau^{-1} \kappa_{t|t}}{\lambda_{t-1}^P + \kappa_{t|t}^2} \tag{30}$$

[Equation 30](#) implies that interest rates fall in response to an exogenous increase in the policy-makers’ inflation target. Thus when interest rates undershoot expectations, agents revise their

beliefs regarding the inflation target upwards.

$$\frac{\partial i_{t+1}^*}{\partial \lambda_t}|_{(\pi_{t-1}^{*P}, \lambda_{t-1}^P)} = -\frac{\tau^{-1} \kappa_{t|t}}{\lambda_{t-1}^P + \kappa_{t|t}^2} \underbrace{(E_t^P - \pi_{t+2} + \rho \xi_{t|t}^p - \pi_{t-1}^{*P})}_{\chi_t} \quad (31)$$

The factor in parenthesis denotes the perceived distortion wedge created by the private agents' inflation expectations and the persistent supply shock. Clearly, interest rates only reflect λ_t to the extent that such a wedge is present. Thus the larger they are in magnitude, the more information interest rates reveal about how it resolves policy trade-offs i.e, about λ_t .

[Equation 31](#) and [Equation 32](#) together tell us that the degree to which interest rates respond to persistent supply shocks is decreasing in λ_t . When interest rates are seen to offset supply shocks more strongly than agents anticipate, they lower their beliefs about λ_t .

The magnitude of information: The coefficient $-\tau^{-1} \kappa_{t|t}/(\lambda_{t-1}^P + \kappa_{t|t}^2)$ is common to both the partial derivatives and scales the Jacobian \mathbf{H}_t . If agents believe this term to be small, they perceive a poor *signal-to-noise ratio* in the interest rate signal. Hence their beliefs π_t^{*P} and λ_t^P update more inertially. The expression implies that the degree to which agents stick to their prior beliefs about the Fed's policy preferences is increasing in λ_{t-1}^P . A clear implication being that the more weight the agents perceive policy to attach to real-side stabilization, the less volatile their beliefs about the inflation target would be. It is hence useful to define the *reciprocal* of this term as the *anchoring coefficient*, denoting it as

$$\zeta_t = \tau \cdot \kappa_{t|t} \cdot \left(\frac{\lambda_{t-1}^P}{\kappa_{t|t}^2} + 1 \right)$$

The direction of \mathbf{H}_t : The orientation of \mathbf{H}_t determines the direction in the $\pi^* - \lambda$ space that the observation i_{t+1} points towards, and hence, the direction that the agents' beliefs π_t^{*P}, λ_t^P would move in, upon observing i_{t+1} . The orientation of \mathbf{H}_t is determined by the ratio of the partials, given by the distortionary wedge χ_t . It can be shown that:

$$\chi_t := \frac{\rho \xi_{t|t}^p}{\lambda_{t-1}^P [(1 - \rho) + \kappa_{t|t}^2 / \lambda_{t-1}^P]} \quad (32)$$

Given a policy surprise, it determines how the surprise loads on to beliefs about λ_t and π_t^* . When χ_t is large, agents perceive the surprise to contain more information about λ_t than π_t^* . Clearly, when $\chi_t = 0$, the policy surprise would be perceived as being entirely uninformative about λ_t since there is no policy trade-off. In this case, only π_t^{*P} gets updated and $\lambda_t^P = \lambda_{t-1}^P$

5 Estimation

To characterize the path of beliefs and expectations, we must pin down the vector of parameters:

$$\Phi = [\tau, g_u, \sigma_{\xi,P}^2 / \sigma_{\xi,T}^2, \sigma_i^2, \sigma_{\pi^*}^2, \sigma_\lambda^2]$$

These parameters govern how private agents update beliefs conditional on observations. Given a vector of parameters Φ and a history of realizations \mathcal{H}^t , the path of private-sector beliefs regarding the state of the economy $\{\kappa_t, \xi_t^p, u_t^n, r_t^n\}$ as well as the central bank's policy preferences $\{\pi_t^*, \lambda_t\}$ are determined under the learning algorithm described earlier.

I set the parameter ρ governing the persistence of the persistent component of the supply shocks as perceived by the agents to 0.99, so that it is meaningfully distinct from the transitory i.i.d component so that it doesn't pose identification problems. It also captures a particularly low-frequency component of the supply shocks which would be the most relevant for forming expectations.

5.1 Data

The learning algorithm is implemented with monthly data on Headline CPI Inflation (CPI-AUCSL), Unemployment rate (UNRATE) and the Effective Fed Funds rate (FEDFUNDS) from 1958:01-2024:12 (available from FRED St Louis) as observations. For the zero-lower bound period, the Wu-Xia shadow interest rate is used as the measure of the nominal interest rate instead of the effective Fed funds rate. The initial beliefs are set to have large variance in order to allow them to adjust freely in response to data. I allow 48 periods (4 years) for the filter to converge to steady-state and the estimates from this period are discarded.

To discipline the estimates, I use survey data on long-run inflation expectations from the Survey of Professional Forecasters (SPF)—specifically, the cross-sectional mean of the 10-year-ahead CPI inflation forecasts—as a proxy for private agents' beliefs about the Federal Reserve's inflation target.¹⁹ The SPF series is available at a quarterly frequency over the period 1991–2024. The implicit assumption here is that professional forecasters' long-run inflation expectations are broadly representative of those held by firms and households. Given the low volatility of long-run inflation expectations during this period, this assumption is reasonable: discrepancies

¹⁹Short-run inflation forecasts depend upon a combination of π_t^{*P}, λ_t^P and $\xi_{t|t}^p$, which makes identification much more difficult. Long-run inflation expectations have the advantage that they isolate shifts in π_t^{*P} alone.

between types are unlikely to be large.²⁰

Although alternative measures covering a longer sample period exist such as the Michigan Survey of Consumers and Cleveland Fed's 10-year ahead inflation expectations series, they are not used in the baseline estimation. However, they are employed in an out-of-sample validation test (see [Appendix A](#)) to assess the robustness of the results. Not explicitly including long-run inflation expectations data for the Great Inflation period allows us to test if the structural dynamics captured by the model can provide a consistent explanation for the expectations-formation process during this period without explicitly being fit to the data.

5.2 Estimation results

The goal of estimation is to pin down the vector Φ that generates a path of long-run expectations closest to the observed survey measure under the agents' learning mechanism given their observations. A least-squares minimum-distance estimator is used, matching the path of model-implied private-sector beliefs regarding the inflation target π_t^{*P} with the observations from the SPF. The minimum-distance estimate Φ^* is the solution of the resulting minimization problem:

$$\Phi^* = \underset{\Phi}{\operatorname{argmin}} \sum_{t=1991:01}^{2024:12} ([\pi_t^{*P} | \mathcal{H}^t, \Phi] - \pi_t^{10y, SPF})^2$$

I discard values of Φ that generate explosive paths for beliefs. This problem arises because beliefs are a non-differentiable function of Φ : even small perturbations in the parameters can induce large changes in the updating process across all variables, setting off some beliefs on divergent paths.²¹

The point-estimate of Φ^* along with 95% credibility intervals generated using Sequential Monte Carlo (SMC) sampling are shown in [Table 1](#). The point-estimate implies that the variance of innovations in the policy preference parameters is very small compared with the idiosyncratic policy errors. The innovations to persistent cost-push shocks are also approximately 10^3 times

²⁰For a relatively short sample covering the recent surge, data from Survey of Firms' Inflation Expectations (SoFIE) from the Cleveland Fed is available, which explicitly includes firm managers' perceptions about the Fed's target. This series is in extremely close agreement with the SPF series used.

²¹This also makes the use of gradient-based optimization algorithms infeasible. I use the Nelder-Mead direct search method that does not require the computation of gradients or derivatives of the objective function.

smaller than i.i.d. innovations.

Table 1: Estimated parameters of the baseline model

Parameter	Description	Estimate (95% CI)
τ	Ratio of IES to Okun's law coefficient	0.647 (0.430, 1.184)
g_u	Gain for updating u_t^n	0.329 (0.209, 0.351)
σ_i^2	Variance of idiosyncratic monetary policy errors	0.488 (0.389, 1.334)
$\sigma_{\pi^*}^2$	Variance of innovations to (log)inflation target	$6.696 (5.186, 7.772) \times 10^{-4}$
σ_λ^2	Variance of innovations to (log)weight on unemployment-stabilization	$6.802 (3.611, 9.173) \times 10^{-5}$
$\frac{\sigma_{\varepsilon^t}^2}{\sigma_{\varepsilon^p}^2}$	Ratio of the variance of innovations to the transitory component of cost-push shocks to that of the persistent component	911.901 (196.125, 5176.436)

Note: Confidence intervals are constructed using Sequential Monte Carlo sampling. The likelihood function is not differentiable in the parameters Φ , so asymptotic standard errors cannot be used.

Appendix B compares the agents' ex-ante forecasts of inflation, unemployment rate and the nominal interest rate informed by their model with the actual realizations to assess the fit. The agents' perceived model is able to track the target variables closely and in this sense, delivers a satisfactory "fit" to their observations.

6 Evolution of the agents' beliefs

This section discusses time-paths of private-sector agents' beliefs regarding the structural variables describing the economy as implied by the point estimates given in Table 1. The section also provides context on how beliefs evolved and their bearing on the macroeconomic outcomes in the post-war period.

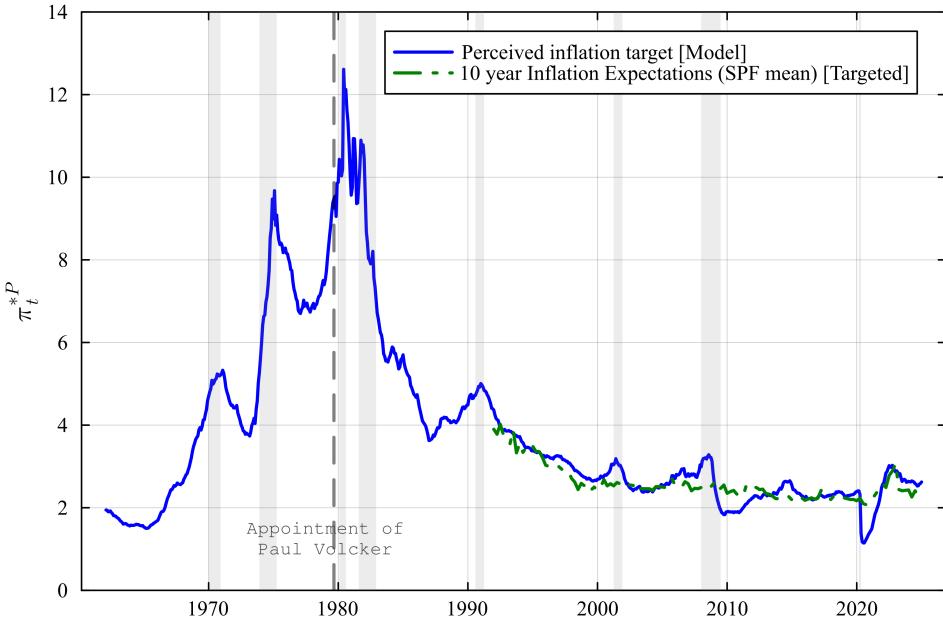


Figure 2: Perception of the Fed's inflation target

Note: Private agents' beliefs regarding the Fed's inflation target as implied by the model (π_t^{*P}) (solid) vs SPF 10-year inflation expectations (dashed) which serves as the empirical proxy. During the Great inflation, private-sector beliefs about the inflation target exhibit sharp upward revisions. This is not the case during the recent surge. The shaded regions indicate NBER recessions. The SPF 10-year ahead inflation expectations series begins in 1991:Q1 and is obtained from the Philadelphia Fed website.

6.1 The Fed's inflation target

Figure 2 illustrates the model-implied path of the agents' perceptions regarding the Fed's inflation target. The beliefs exhibit a significant degree of volatility prior to the mid-1980s, with sizable high-frequency movements.²² According to the model, the private agents perceive the Fed's inflation target to be close to 2% in the early 1960s. In the latter half of the decade, the perceived target begins to rise, sitting above 4% by 1970.²³

From the eyes of the private sector, the 70s would be a period of great volatility in the Fed's inflation target. Their beliefs are sharply revised upwards on two occasions, each coinciding with an NBER recession—one during the beginning of the decade and the other around the time of the OPEC Embargo and the oil crisis of 1974. From the lens of the model, the private agents saw that the Fed had an *incentive* to inflate the economy, over and beyond any supply

²²This is in contrast with papers such as Bhattachari, Lee and Park (2016) that rely on identifying the inflation target from low-frequency movements in inflation and identify smooth variation.

²³Hence I find that the anchor had begun to loosen in the late 1960s, before the appointment of Arthur Burns (in 1970), similar to Reis (2021). In December 1965 a policy-tightening provoked an unprecedented backlash against Fed Chair Martin, marking what many observers regard as the beginning of a prolonged era of accommodative monetary policy.

disturbances creating policy trade-offs. From their point of view, the Fed displayed a tendency to deliberately inflate during recessions, operating with a higher inflation target, followed by dis-inflationary pursuits soon after. The Volcker-era, beginning with the chairmanship of Paul Volcker in 1979 is often cited as watershed moment in the Fed's eventual "conquest" of inflation. In October 1979, the Fed announced "new operating procedures" aimed at reining in inflation. But these do not immediately effect a disinflation (as also noted by [Goodfriend and King \(2005\)](#)). A recession follows and the perceived target shoots up yet again. It is not until 1982 that we see the perverse dynamics reverse course. The following years see a sharp decline in the perceived inflation target which coincides with a deep recession. By the mid 1980s, agents perceive the Fed's inflation target to be below 5% after nearly a decade. Thus the U.S. economy enters the "Great Moderation". Beliefs regarding the Fed's target are on a steady downward trajectory in the two decades that follow, under the chairmanship of Alan Greenspan (1987-2006). Only during the Great Financial crisis and the recent COVID-pandemic do we see the agents' perceptions exhibiting some modest revisions (interestingly, breaking away from the SPF series).

The model implies a modest uptick in the agents' perceptions regarding the Fed's inflation target during the post-pandemic episode, also observed in the SPF data, showing that there was some endogenous feedback from monetary policy in the post-pandemic period to private agents' long-run inflation expectations. Yet, beliefs about the target only rise to about 3%. This is remarkable considering that CPI inflation itself reached a peak of 9.1% in June 2022. The same learning mechanism that caused agents to anticipate inflation to remain put at levels as high as 11% during the 80s, told them that inflation was on course to settling around 3% - the inflation crisis left their long-run beliefs more or less unchallenged.

While the model implies that the conduct of policy created the perception among private agents that the inflation target had risen substantially during the 1970s, the model does not take a stand on what would cause the policymakers to acquire a taste for such exorbitant levels of inflation. Narrative evidence offered by [Romer and Romer \(2002\)](#), [DeLong \(1996\)](#) provide some valuable clues: inflation was deliberately pursued under the false notion that unemployment could be driven lower by inflationary surprises. [Bianchi and Ilut \(2017\)](#) offer a view that inflation was fiscally-led during this period. This view would be consistent with policymakers pursuing higher inflation in order to accommodate the government's fiscal expansion, effectively helping to "inflate the debt away". This would suggest that the rise in the inflation target was politically motivated. The focus here is not on understanding why the policymakers operated in this way but rather, how policy behavior shaped private agents' expectations.

[Figure 3](#) plots the agents' short-run inflation expectations (one-year ahead, as implied by the model) along with their perceptions regarding the inflation target, or the level of inflation that they expected to prevail in the *long-run*.

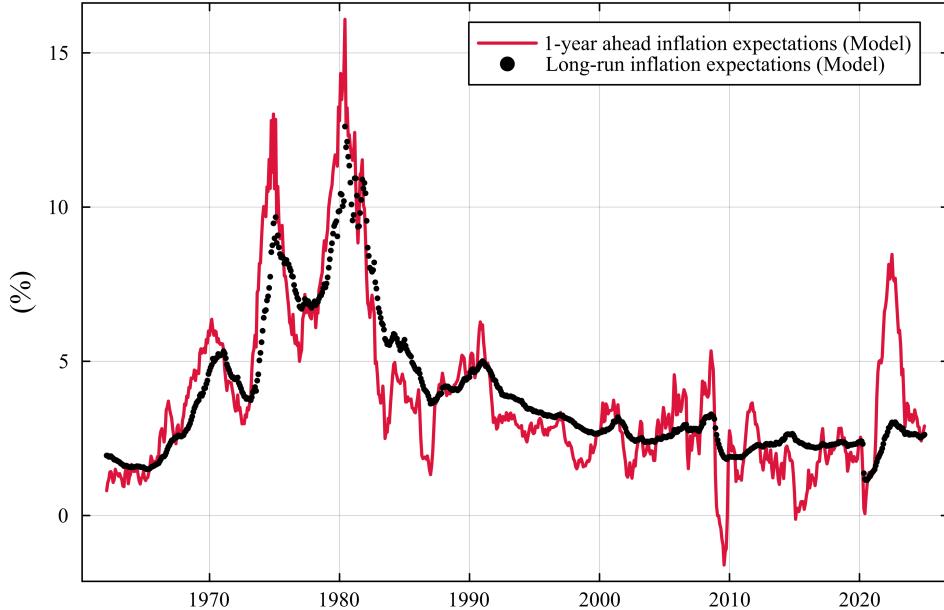


Figure 3: Weakening link between short-run and long-run inflation expectations

Note: The figure plots agents' 1-year ahead inflation expectations along with the long-run inflation expectations as implied by the model. This represents the model's reproduction of [Figure 1](#) and highlights the same pattern. Agents' perceptions regarding the persistence of inflation have changed considerably over the postwar sample period.

Owing to deflationary supply shocks corresponding to the oil glut in the mid-1980s, even as the agents expected inflation to be below 2.5% in the short-run, for the first time in nearly two decades, they still believed the Fed's inflation target to be near 4%. Hence, for a time, agents viewed the benign inflation as a temporary reprieve driven by the macroeconomic environment soon to be undone by policy. Over the recent period however, while short-run inflation expectations continued to be volatile, agents' beliefs about the target have held relatively stable, close to 2.5%. This shift has much to do with their perception regarding the Fed's emphasis on minimizing real-side volatility, as we will see in the next subsection.

6.2 The Fed's weight on unemployment gap stabilization

[Figure 4](#) plots the evolution of the private sector's estimates of λ_t : the relative weight the Fed puts on closing the unemployment-gap. The estimates suggest that, during the early 1960s, the

private sector attributed relatively little concern from the Fed towards closing the gap.

After a slow and steady rise following the Volcker disinflation, perceptions regarding λ were sharply revised upwards following the Global Financial Crisis and again in the aftermath of the COVID-19 pandemic: the emphasis of policy has shifted. As described in [subsection 4.5](#), this development has had important implications for the anchoring of long-run inflation expectations. A large λ implies that the Fed effectively “ties its hands”; unemployment gaps are perceived as costly and hence policy emphasizes keeping the gap closed - constraining policy-makers from responding to idiosyncratic shifts in their inflation target (owing to say, political pressure or short-term goals). A large λ_t also has the effect of making future unemployment gaps more predictable (since they are closer to zero) ultimately reducing real-side volatility.

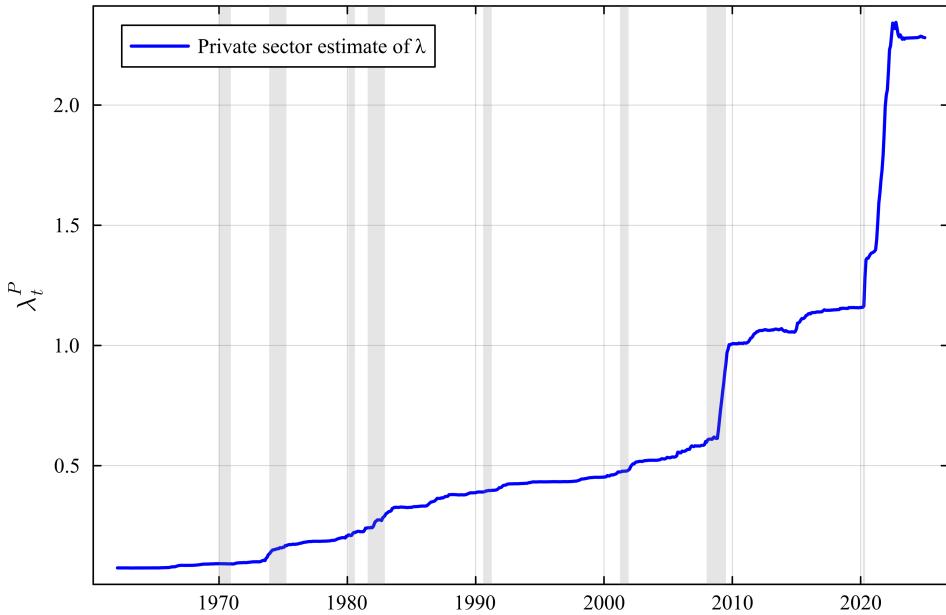


Figure 4: Perception of the Fed’s weight on unemployment-gap stabilization

Note: Evolution of the Private sector estimate of λ_t . The private sector perceives the Fed to put more emphasis on stabilizing the unemployment-gap. The shaded regions indicate NBER recessions

These findings are consistent with recent empirical literature using high-frequency identification utilizing changes in asset prices around Fed policy announcements to study how the private sector learns about the Fed’s “policy rule” (e.g., [Bauer and Swanson \(2023\)](#), [Bauer, Pflueger and Sunderam \(2024\)](#), [Pflueger \(2025\)](#)). These studies find that monetary policy in the recent period, following 2000, has been perceived to be increasingly responsive to output. A rise in λ_t , and the greater predictability of unemployment-gaps also complements earlier findings that output-gap volatility in the U.S. has declined significantly since the Volcker disinflation (see

Blanchard and Simon (2001); McConnell and Perez-Quiros (2000)), underscoring the role of systematic monetary policy in engineering this phenomenon.

6.3 The slope of the expectations-augmented Phillips Curve

The parameter κ , represents the sensitivity of aggregate inflation to contemporaneous unemployment gap. Hence, it serves as the connective tissue between the real and nominal side of the economy and is a key parameter that agents must learn. Figure 5 plots the evolution of the agents' beliefs regarding the slope of the expectational Phillips curve under their learning mechanism. Under the agents' prior, κ is time-invariant. However, their real-time estimates under learning exhibit significant time-variation over the sample period.

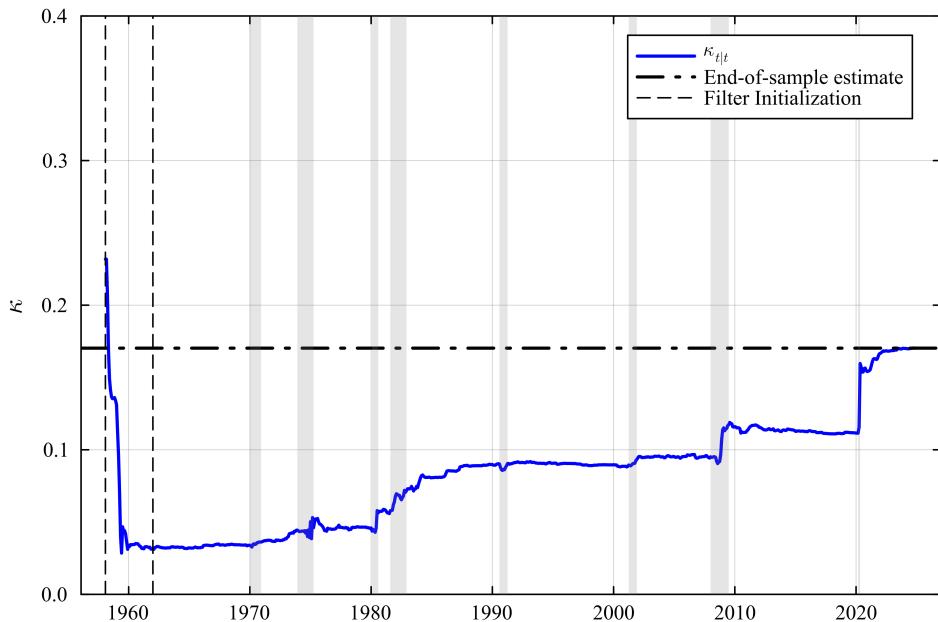


Figure 5: Slope of the expectations-augmented Phillips curve

Note: The figure plots the filtered estimates of the slope of the Phillips curve (*solid line*). From the private agents' perspective, the Phillips curve is steeper now than it was during the 70s and the 80s, meaning that inflation is *more* sensitive of real activity. Interestingly, though the agents learn under the assumption that the true slope of the structural Phillips curve is time-invariant, their beliefs are subject to constant revisions owing to the identification problems posed by the information structure of the economy. The shaded regions indicate NBER recessions

Since κ is not subject to innovations, the steady-state filter would be a decreasing-gain one. As new data is observed and beliefs are updated, each additional observation carries marginally less information and their beliefs should stabilize near a constant value. But it does not appear that any such convergence has attained within the sample period spanning about 60 years.

To understand why this is the case, let's revisit the observation equation through which agents update their beliefs regarding κ and ξ_t^p :

$$\pi_t - E_{t-1}^P \pi_{t+1} = -\kappa x_t + \xi_t^p + \xi_t^t$$

Note that current inflation, π_t delivers information about κ only through the independent variation in the unemployment gap x_t . It is not surprising then, that we see the bulk of the large updates in agents' estimates of κ around recessions (causing agents to perceive large demand shocks). During "normal" times, the unemployment gap is small because nominal rigidities play a smaller role, and it is evident that learning about κ would slow down. The signal informing the agents about κ is susceptible to getting drowned out owing to two reasons. (i) the unemployment gap x_t being of small magnitude most of the time ([Figure 14 in Appendix D](#) plots the evolution of the variable). The mean absolute value of the gap over the sample period is 0.27; implying that even if the "true" slope were twice as large as the agents' end-of-sample-estimate, it would create a discrepancy of about $\approx 0.05\%$ in aggregate inflation on an average. This would be hard to detect because of the presence of noise, bringing us to the second reason and (ii) under stabilization policy by the central bank, the unemployment gap would be correlated with persistent supply shocks, making inference particularly difficult. These challenges are outlined in [Mavroeidis et al. \(2014\)](#) who conclude that the Phillips curve is weakly identified using aggregate time-series. Indeed, learning about the Phillips curve relationship has been among the most enduring and difficult problems in macroeconomics. The agents in the model are not immune to the fundamental econometric challenges that learning poses. Models assuming full-information mask such issues entirely.

The agents perceive the slope to be relatively "flat" during the 1970s. This belief would be reinforced by the experience of high inflation in the face of rising unemployment experienced during this period. The perception of a flat Phillips curve is one of the primary reasons cited by [Primiceri \(2006\)](#) and [Sargent, Williams and Zha \(2006\)](#) for the policymakers' aversion to act decisively against inflation during this period. The agents revise their beliefs over time and see the slope become steeper. In the post-pandemic period, the large decline in inflation from its highs with little rise in unemployment leads the agents to update their beliefs about κ upwards. Overall, the results suggest that real-time identification of the Phillips curve is quite poor and agents' estimates would take an unreasonably long time to converge to a constant.

However, estimates during the entire sample period remain within an empirically plausible range (between 0.05-0.20), implying that the agents do not perceive the slope to be excessively flat at any point. Some recent papers argue in favor of using a nonlinear Phillips curve to

understand the behavior of inflation during the post-pandemic surge (see [Harding, Lindé and Trabandt \(2023\)](#) [Benigno and Eggertsson \(2024\)](#))²⁴. Though the model considered here does not nest such nonlinearities, the *perceived* slope becomes substantially steeper following the pandemic-induced recession, consistent with the findings. However, the model shows that this can happen even in an environment where the true slope is fixed, owing to imperfect information.

6.4 Anchoring Coefficient

The anchoring coefficient, ζ_t depends both on the perceived slope of the Phillips curve, $\kappa_{t|t}$ as well as ex-ante perception about the weight that the Fed puts on unemployment gap stabilization, λ_{t-1}^P . [Figure 6](#) plots the evolution of ζ_t over the postwar period. From the private agents'

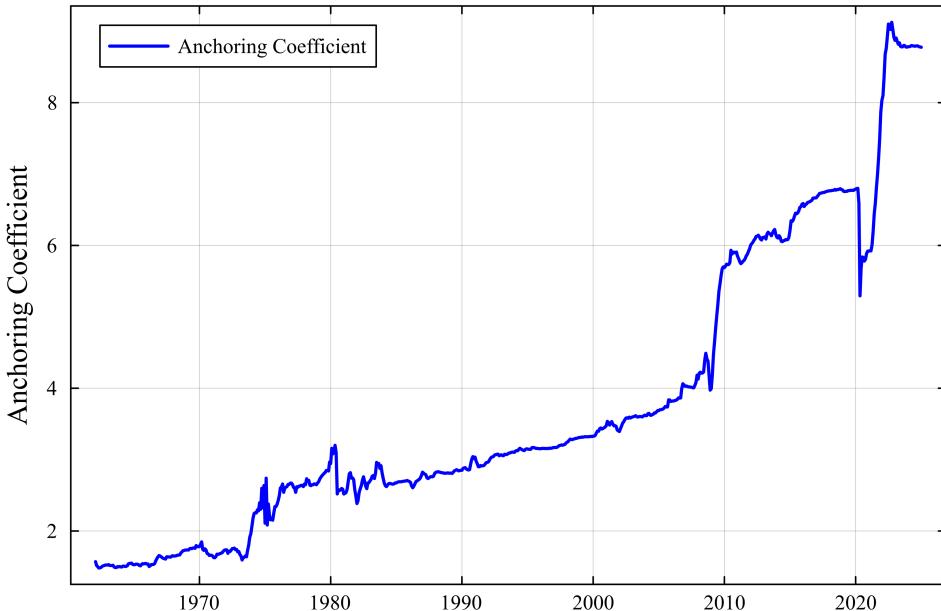


Figure 6: Evolution of the anchoring coefficient (ζ_t)

Note: The coefficient measuring the “anchoring” of long-run inflation expectations has risen drastically. Even as the perceived slope of the Phillips curve has risen, the rise in the perceived weight on unemployment gap stabilization λ_t^P has outpaced it and made the coefficient larger.

vantage point, the policy environment has changed drastically in the 40 years separating the Great Inflation and the post-pandemic surge. Through the lens of their model, interest rates are less responsive to idiosyncratic shifts in the inflation target than they were in the wake of

²⁴However, [Beaudry, Hou and Portier \(2025\)](#) find limited evidence in favor of nonlinear Phillips curve specifications once inflation expectations are explicitly taken into account.

the Great Inflation crisis. According to the model, long-run inflation expectations are more entrenched at this juncture than any other time in the post-war history of the United States. This development afforded the Fed enough room to “look-through” supply shocks and adopt a wait-and-see approach without triggering large revisions in the perceived inflation target. While this makes de-anchoring due to perceived mistakes unlikely, it also hampers the Fed’s ability to guide these beliefs back to target *if* they were to de-anchor. An implication of the model is that the steadfast disinflation we saw in the 80s, in large part due to the Fed strongly signaling a low inflation target, would be much less likely today.

6.5 “Bad luck” vs “bad policy” revisited

The following section contributes to the debate regarding whether the economic outcomes of the post-Volcker period were a result of luck (favorable economic environment, benign shocks) or systematic policy (shifts in the Fed’s implied policy objectives). I discuss how evolving perceptions regarding structural shocks and the Fed’s systematic monetary policy contributed to shaping macroeconomic outcomes in the post-war period in the U.S.

6.5.1 The role of policy in shaping agents’ expectations

In this section, I discuss the role of the Fed’s systematic monetary policy in signaling the policymakers’ preferences to the private agents. It is useful to consider the perceived real rate gap, defined as the difference between the ex-ante real interest rate and the perceived natural rate of interest, $r_{t|t}^n$. A positive real rate gap implies a contractionary policy stance and conversely, a negative real rate gap reflects an expansionary stance of policy.

[Figure 7](#) plots the evolution of the perceived real rate gap along with the agents’ real-time estimates of persistent supply shocks. As we can see, the late 1960s are characterized by moderate supply shocks. But the real rate gap tends to stay slightly negative throughout the latter half of the decade, signaling the policymakers’ attempts at monetary expansion during this period.²⁵ The mid-1970s see mounting supply pressures and the Fed effectively doubling down on its stimulative efforts, presumably in an effort to quell the recession coinciding with the OPEC embargo in 1974. With interest rates being seen as strongly indicative of the Fed policymakers’

²⁵Narrative evidence from this period suggests that Chairman Martin’s initial anti-inflation stance clashed with expansionary fiscal policy by the Congress. This ended up eroding the postwar monetary discipline of the Fed, with focus shifting from stabilizing inflation to accommodating the fiscal expansion.

inflation target, over-expansionary policy was interpreted as coming from a deliberate effort to achieve higher inflation. Long-run inflation expectations shot up.

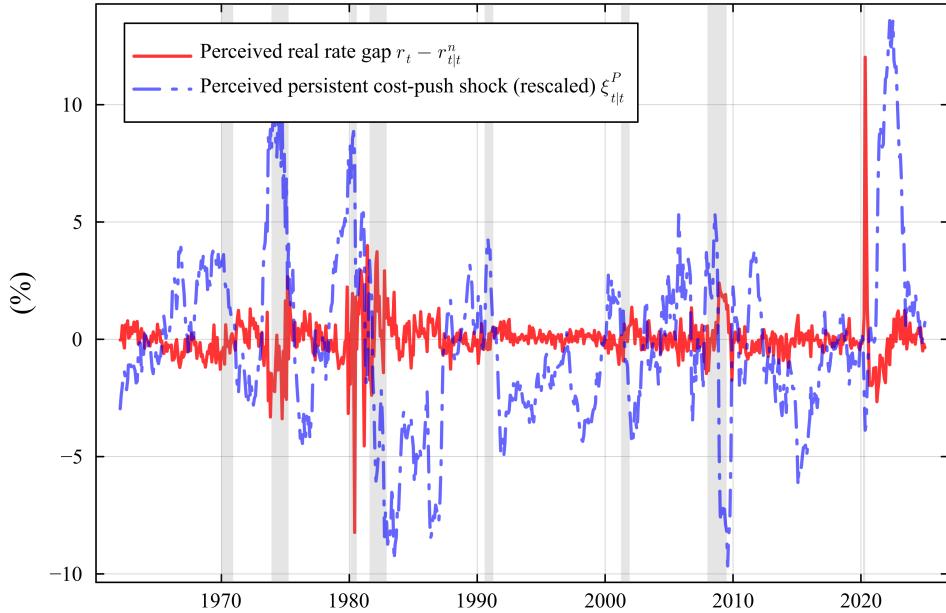


Figure 7: Policy response to inflationary shocks:

Note: The perceived real rate gap $r_t - r_{t|t}^n$ (*solid*) vs filtered estimates of persistent supply shocks $\xi_{t|t}^P$ (*dashed*). We can see that supply-side pressures in the 70s and 80s were met with accommodative policy by the Fed. Policy was perceived to be similarly accommodative at the beginning of the post-pandemic surge. The shaded regions indicate NBER recessions

“Forever inflation” takes hold with no resolve from policymakers to combat it. It is not until 1980, under the chairmanship of Paul Volcker that we see a sustained positive real rate gap leading to the eventual “conquest over inflation”. From the model’s perspective, two aspects of policy behavior in the post-Volcker period were important for the onset of the “Great Moderation”: (i) a positive real rate gap was maintained for a prolonged period signaling a lower inflation target and (ii) muted response of the real rate gap to supply shocks, signaling a steadily increasing weight on real-side stabilization represented by λ_t . These gradually led the agents to believe in a low, stable inflation target. Note that without (ii), the anchoring would be fragile and long-run beliefs would have been similarly volatile, shooting up at any hint that Fed policy was “too loose”.

Turning to the post-pandemic period, the agents see the mistakes of the 70s being repeated: persistent supply shocks re-emerge and the Fed is nowhere close to contain the imminent crisis. Yet, we see long-run inflation expectations remain largely stable. This time however, after a period of “looking through” supply shocks, the Fed quickly catches up and the agents see the real-rate gap close. From the model’s perspective, even as the agents perceived the policy-

makers to be making a similar kind of mistake at the beginning during the recent surge, their expectations responded differently: in large part due to a change in their perceptions regarding λ_t - agents were slower to revise their beliefs about the inflation target despite the “mistake”. Disciplined Fed policy has shaped agents’ beliefs in a way that prevented the sudden inflationary spiral of the 70s despite a delayed policy response. Good policy of the past continues to bear fruit. Since the Fed acted decisively when it did and managed to raise the real rates above the perceived natural rate, it managed to signal that the inflation target was intact.

6.5.2 Supply shocks: The structural drivers of policy trade-offs

As the only variable driving a trade-off between inflation and unemployment gap stabilization, persistent supply shocks cause all “involuntary” inflation, over and beyond the Fed’s targeted level. Agents’ beliefs about these shocks are an important determinant of their short-run inflation expectations and hence of inflation dynamics themselves.

[Figure 8](#) plots the time-series of the agents’ beliefs (real-time as well as smoothed) regarding persistent supply shocks in the Phillips curve. One fact that emerges is that the agents perceived large persistent supply shocks, both during the Great Inflation of the 70s and in the more recent inflation surge. Moreover, the shocks were of roughly similar magnitude across the two episodes if not larger during the recent episode. Hence, the going by the size of the shocks alone, one would find it hard to explain why the inflation crisis was much more benign this time.

The perceived supply shocks line up well with documented episodes of oil price surges. There is ample evidence in the literature that fluctuations in relative prices of energy goods are significant drivers of inflation (see [Afrouzi, Bhattacharai and Wu \(2024\)](#), [Gagliardone and Gertler \(2023\)](#) for recent work examining the link between crude oil prices and the post-pandemic inflation surge). Interestingly, the period of recovery from the Great Financial Crisis (GFC) also coincides with persistent cost-push shocks. This is consistent with the theory that oil price shocks in the aftermath of the crisis kept inflation expectations propped up, accounting for the “missing deflation” ([Coibion and Gorodnichenko \(2015\)](#)). According to the model, even as the agents’ long-run inflation expectations remain stable during this period, their short-run expectations are quite responsive to inflationary supply shocks during this period.

To aid interpretation of these “persistent supply shocks”, in [Figure 9](#) I plot the series against food and energy price inflation derived as the difference between Headline CPI and Core CPI.

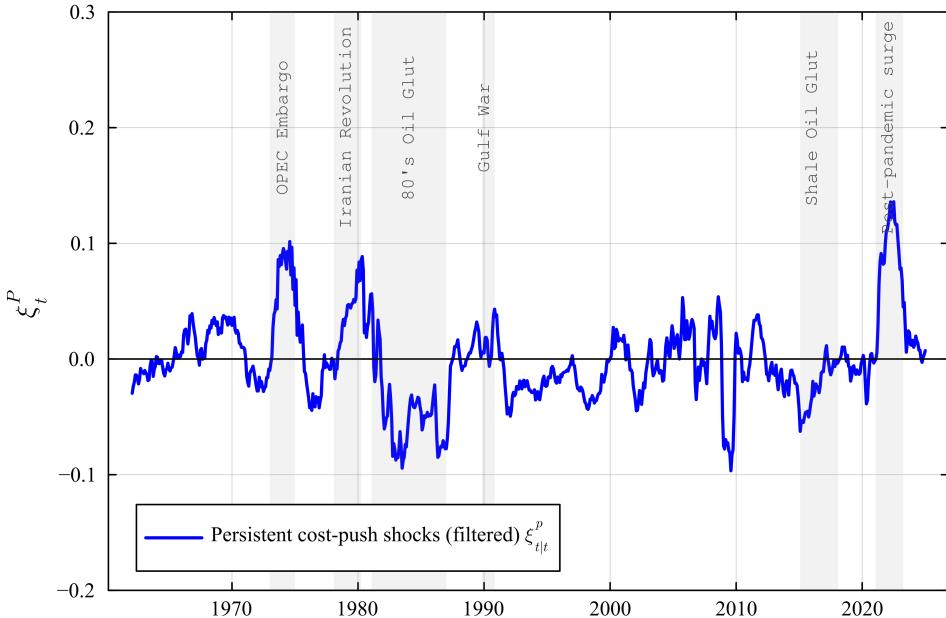


Figure 8: Structural drivers of inflation

Note: Private agents' estimates of the persistent component of the cost-push process ξ_t^p : Filtered (*solid*) vs smoothed (*dashed*). The magnitude of persistent cost-push shocks perceived by the agents during the post-COVID period were similar to those during the Great Inflation period. The shaded regions indicate known episodes of significant supply pressures.

The series are de-meaned and re-scaled for comparison. The two series display significant co-movement. Since Core CPI is not a series that the model has “seen” (only Headline CPI data is used during estimation), it is remarkable that such a link emerges.

The post-pandemic episode was characterized by structural shifts over and above oil price surges, such as sectoral shocks shifting consumption between goods and services (see [Guerrieri et al. \(2021\)](#)) structural changes in the labor market ([Blanchard and Bernanke \(2023\)](#), [Ball et al. \(2022\)](#)), increasing attention to inflation ([Pfauti \(2023\)](#)) to name a few. However, shocks to relative food and energy prices appear to explain a large part of the variation in these persistent supply shocks perceived by the agents. This is intuitive considering how *salient* these prices are (as also argued by [Coibion and Gorodnichenko \(2015\)](#)). It makes sense that firms and households’ perceptions about inflation in the short run would respond to these prices given their pervasive impact on the rest of the economy (as argued in [Afrouzi et al. \(2024\)](#) using a model of input-output linkages). Hence, the model adds support to the literature emphasizing the importance of relative price disturbances in driving aggregate inflation dynamics.

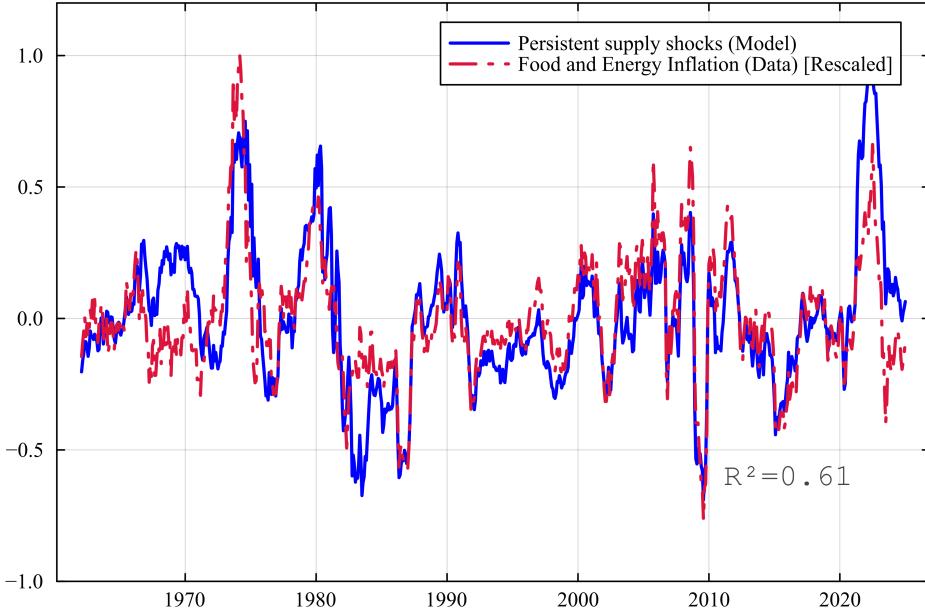


Figure 9: Relative prices and perceptions about inflation

Note: Persistent supply shocks as perceived by the agents vs inflation in food and energy prices (Untargeted). Measure of Food and Energy inflation is constructed as the difference between headline and core CPI inflation

7 Conclusions

The rational expectations revolution—spearheaded by the work of Lucas and Sargent—marked a profound shift in macroeconomic thought. New Keynesian macroeconomics incorporated this transformation by explicitly modeling how aggregate outcomes emerge from the optimizing behavior of individual agents. The model developed in this paper presents a natural extension of the standard New Keynesian framework to an environment characterized by imperfect knowledge where neither the true structure of the economy nor the objectives of the central bank policymakers are known to the agents. Their expectations reflect their changing beliefs as they continue to *learn*. In doing so, it describes postwar U.S. macroeconomic dynamics from the perspective of agents reasoning from New-Keynesian principles about observed macroeconomic outcomes in real-time.

A central implication of the model is that, because expectations are pivotal in shaping macroeconomic outcomes, the function of monetary policy extends beyond mechanical stabilization. Policy actions not only influence current economic conditions but also actively shape agents' expectations—a point emphasized by Kydland and Prescott (1977). The learning mechanism

embedded in the model illustrates how the anchoring of expectations emerges endogenously from the systematic conduct of monetary policy. The evolution of postwar U.S. macroeconomic dynamics is thus closely linked to how Federal Reserve policymakers have signaled the policy objectives underlying their decisions. The model provides a structural interpretation of how monetary policy contributes to the anchoring of expectations, highlighting its dual role as both a stabilizing instrument and a signal relaying information and affecting expectations.

A demonstrated emphasis by the Fed on minimizing policy-driven fluctuations in unemployment has contributed to the anchoring of long-run inflation expectations, *cushioning* people's long-run beliefs against policy misbehavior; while simultaneously amplifying the inflationary impact of persistent supply shocks. From the lens of the model, these perceptions afforded the Fed the ability to "look-through" supply shocks without de-anchoring long-run expectations. Beliefs shaped by the disciplined conduct of monetary policy over the forty years following the Volcker disinflation have contributed greatly to the "soft-landing" that we saw recently. While recent work (e.g., [Coibion and Gorodnichenko \(2025\)](#)) has warned of inflationary risks resulting from de-anchoring of expectations from inflationary pressures in the short-run, the model presented here paints a less grim picture while recognizing the risks that an indecisive policy response to supply shocks could pose in the future.

This work also highlights the explanatory power of the textbook New-Keynesian model when augmented with imperfect information and learning. The model reconciles the empirically observed persistence in macroeconomic aggregates, delivering an excellent fit to macroeconomic data without resorting to backward-looking mechanisms such as indexation to past prices, habit formation in consumption or interest rate smoothing. Finally, the model highlights the *state-dependent* nature of agents' learning: the rate at which information arrives is neither uniform over time nor identical across structural parameters. One key parameter for which this distinction is particularly relevant is the slope of the expectations-augmented Phillips curve, which remains poorly identified under learning. This finding suggests that the full-information assumption commonly imposed in macroeconomic models may be far less innocuous than often presumed.

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8 Appendix

A Long-run inflation expectations

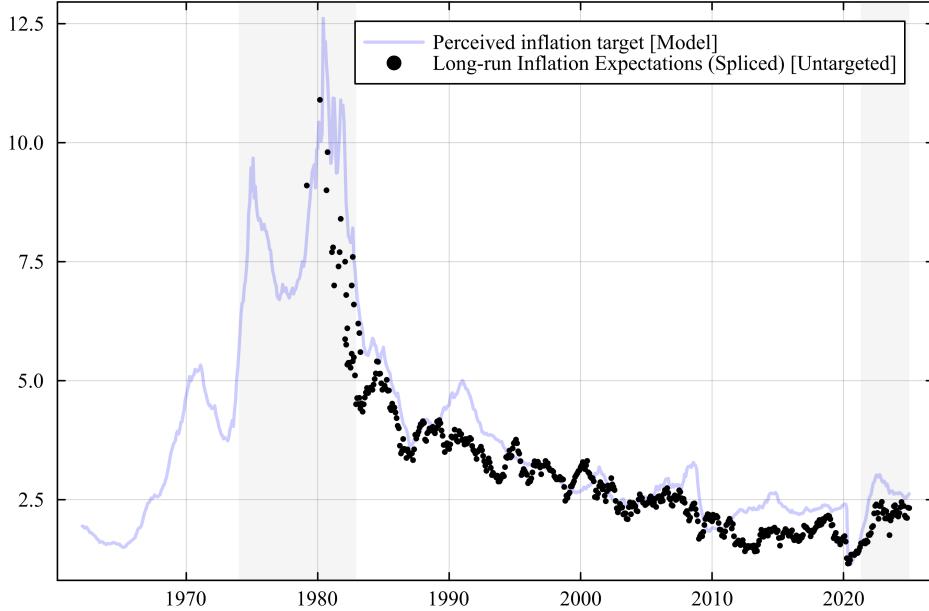
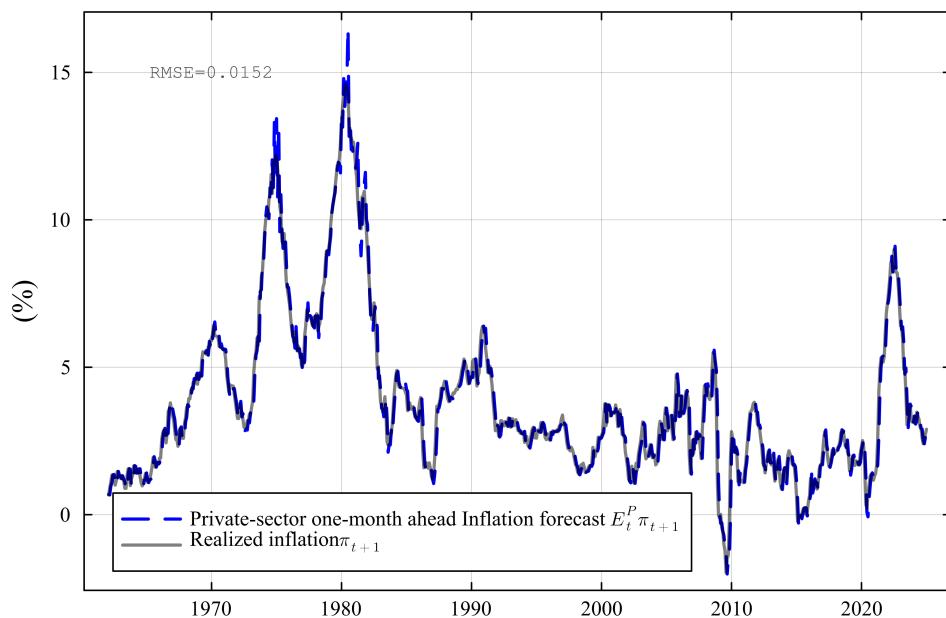


Figure 10: Comparing with untargeted measures of long-run inflation expectations

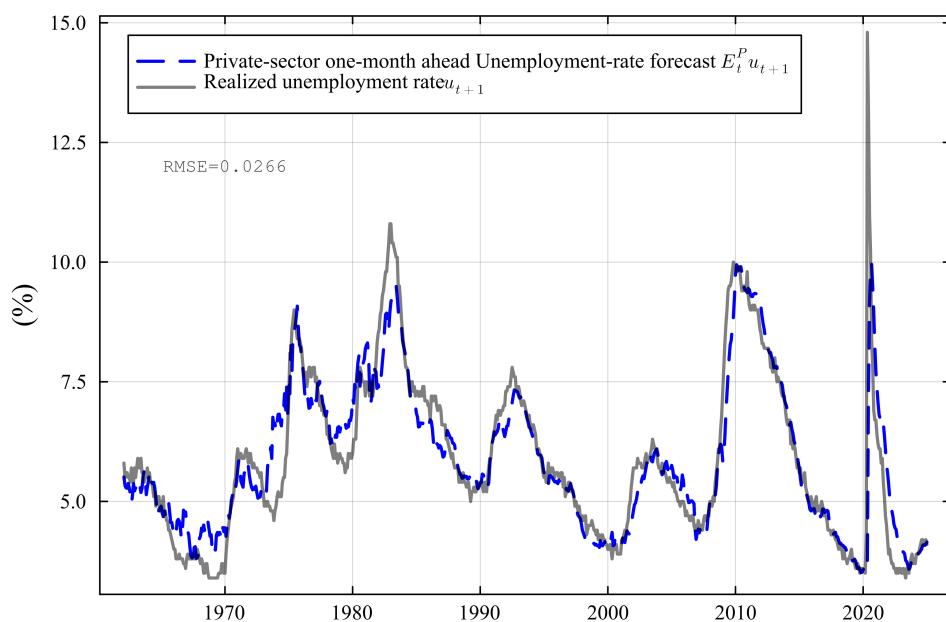
Note: Long-run Inflation Expectations series is constructed by splicing together 5-year ahead inflation expectations from Michigan Survey before 1982 and 10-year ahead inflation expectations from the Cleveland Fed afterwards (due to a shorter sample). The series is not used for estimation and is hence untargeted.

B Forecast performance of agents' model

If the learning algorithm arising from the agents' assumed model of economic dynamics implies forecasts that are persistently off-target, it wouldn't make sense to assume that the agents would continue using it. Rational agents would abandon the model. Hence, it is useful to check how well the agents' ex-ante forecasts agree with the realizations of the inflation, unemployment rate and interest rates or in other words if the agents' assumed model remains plausible given what they observe. [Figure 12](#) plots the agents' ex-ante expectation of the policy rate (prior to announcement) and the realized effective Fed funds rate. Similarly, in [Figure 11](#) I plot the agents' one-period ahead forecasts of inflation and unemployment rate against their corresponding realized values.



(a) Agents' one-month ahead forecast of inflation vs realized value



(b) Agents' one-month ahead forecast of unemployment rate vs realized value

Figure 11: Forecast performance of agents' model

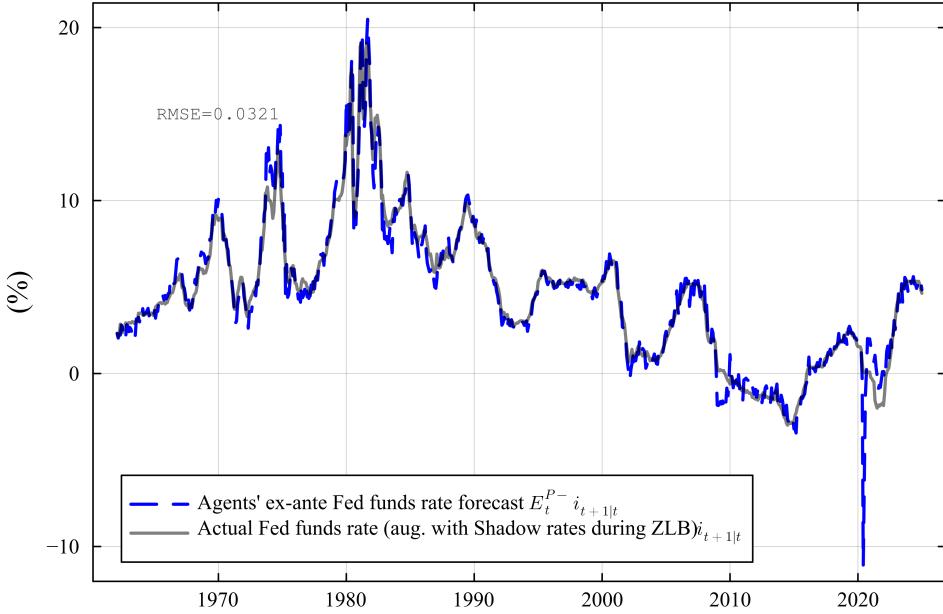


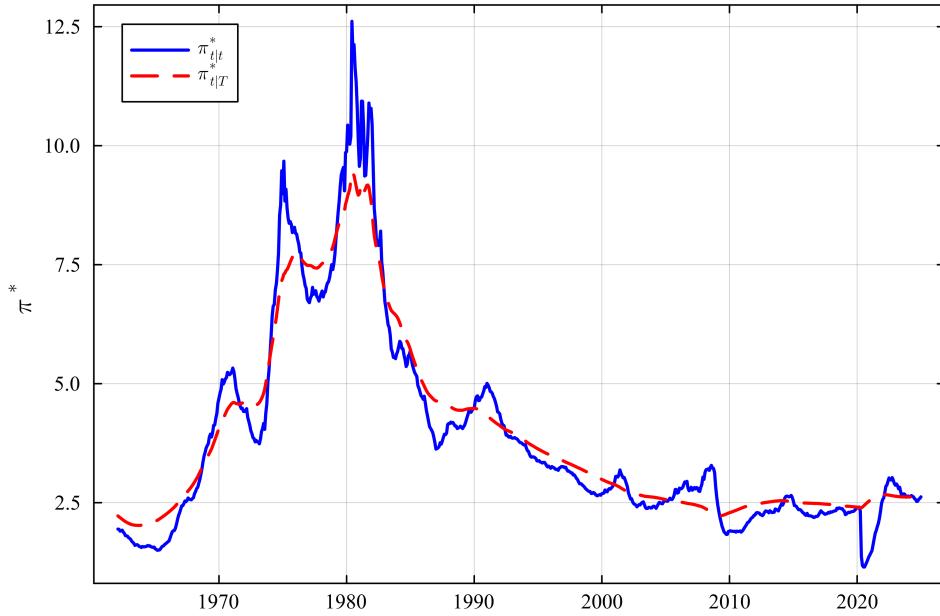
Figure 12: How well do private agents track policy behavior?

Note: The figure compares the private agents' expected nominal interest rates based on their ex-ante beliefs with the actual Fed funds rate (augmented with the shadow rate).

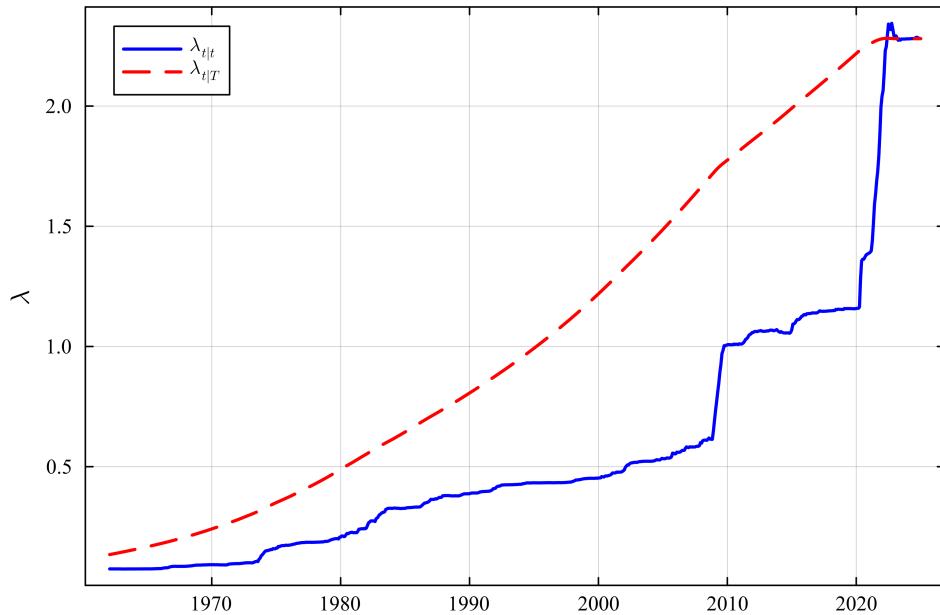
The learning model generates forecasts errors of small magnitude (in the RMSE sense). Thus, their model of the economy “works” - they wouldn’t find a compelling reason to abandon learning. It is also worth noting that their expectations display a similar degree of persistence as the corresponding macroeconomic variables themselves. They are able to “match” the persistent behavior within a fully forward-looking model. Hence, forces such as price-indexation and habit-formation in consumption do not seem to be necessary to generate persistence in the macroeconomic aggregates once agents’ real-time learning is taken into account, as also demonstrated by [Milani \(2007\)](#) and [Erceg and Levin \(2003\)](#).

C What were the Fed’s “true” policy preferences?

While the parameters representing the “true” policy preferences of the Fed over the post-war period remain latent (it evolves as an exogenous structural variable as far as the model is concerned), it is possible to arrive at a best-guess using the model by obtaining the smoothed (backward-looking) estimates of the time- t policy preferences ([Figure 13](#)). These estimates represent the evolution of Fed’s policy preferences in the post-war period from the perspective of a private agent in the model looking back at the end of the sample period (Dec 2024).



(a) π_t^* : Filtered (*solid*) vs Smoothed (*dashed*) estimates



(b) λ_t : Filtered (*solid*) vs Smoothed (*dashed*) estimates

Figure 13: The Fed's “true” policy preferences

Note: The figure plots the smoothed estimates of π_t^* and λ_t along with the filtered estimates. The smoothed estimates represent the agents' best-estimates of the parameters representing the Fed's policy preferences conditional on the entire sample period.

The estimates suggest that the Fed's true inflation target was upwards of 8 percent during the peak of the 80s-era inflation. Notably, the estimates of the time-varying inflation target are also

in line with [Ireland \(2007\)](#) who uses a specification that is very different from the one used here.

Taken at face value, the smoothed estimates of λ suggest that Fed was hardly concerned with keeping the unemployment-gap closed during the 70s-80s. Over time however, the Fed has steadily emphasized closing the gap as part of its monetary policy strategy: which brings us to present-day. The estimated weight on unemployment-stabilization is almost twice as large as that on inflation-stabilization. The backward-looking estimates of λ_t display periods of departure from the real-time ones. This is because meaningful information regarding λ only arrives during periods where agents perceive large cost-push shocks driving policy tradeoffs (since λ is only relevant to policy when such a trade-off exists). Thus from the private agents' perspective, though λ has been evolving continuously, information regarding λ only arrives in clumps during episodes involving large persistent cost-push shocks driving policy trade-offs. Not much learning regarding λ takes place during "normal" times.

D Unemployment gap

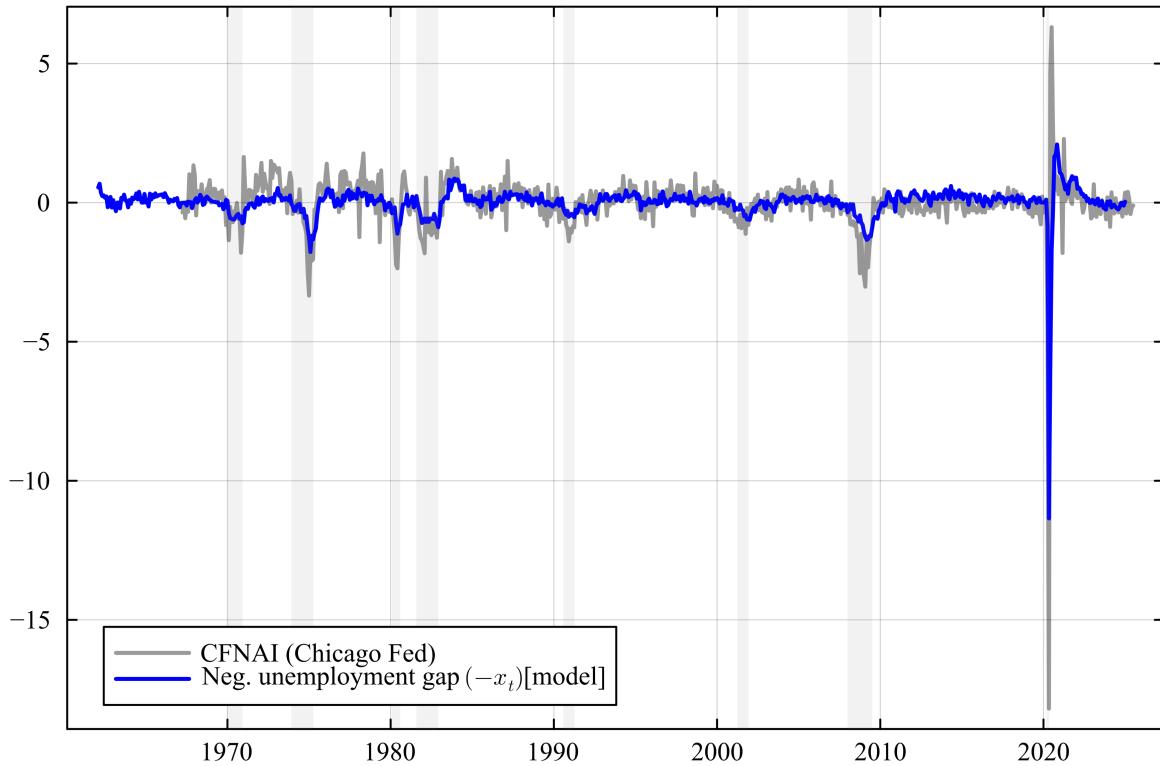


Figure 14: Estimated unemployment-gap

Note: The figure plots the agents' real-time estimates of the (negative of) unemployment gap with the CFNAI (Chicago Fed National Activity Index), a composite measure of real activity based on 81 series. The shaded regions indicate NBER recessions. CFNAI is obtained from the Chicago Fed website.

E Perceived natural rate of interest $r_{t|t}^n$

Figure 15 plots the evolution of the natural rate of interest as inferred by agents in real-time. This is a useful measure and serves as a barometer to gauge the stance of policy.

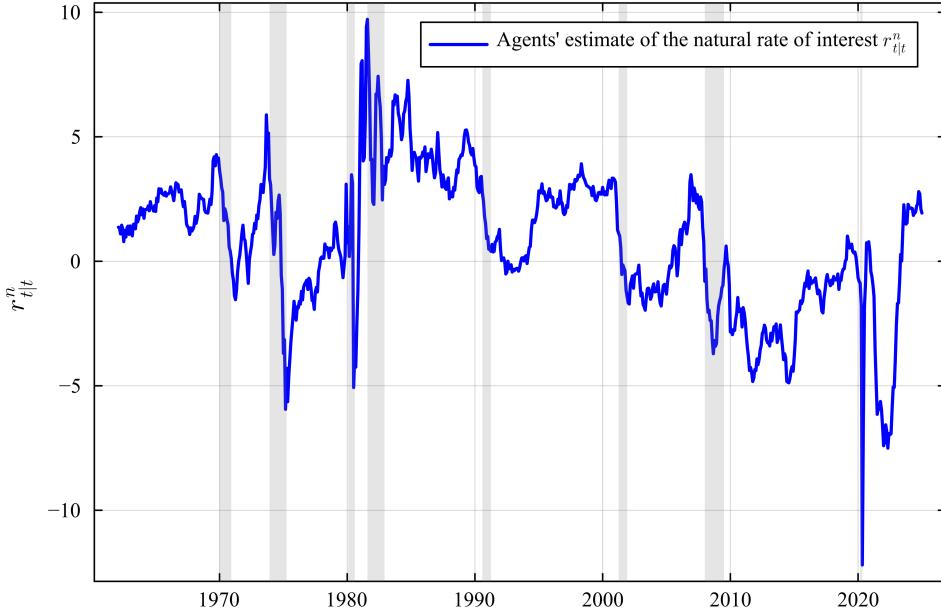


Figure 15: Estimates of the natural rate of interest

Note: Shaded regions indicate NBER recessions

The estimates are broadly in line with the secular decline reported in the literature. They typically fall with NBER recessions, which is rather intuitive based on the IS-curve.

F Has the “true” slope of the Phillips curve changed over time?

In the baseline model, we proceeded with the assumption of a time-invariant Phillips curve in order to keep the model parsimonious and avoid over-reliance on time-variation Phillips curve to explain the observations. However, one can statistically test if there has been a change in the true relationship between unemployment-gap and inflation during the pandemic (motivated by literature arguing that structural shifts in the Phillips curve during the pandemic period were an important factor driving the inflation surge).

In order to do this, we can construct an expectation-adjusted measure of inflation π_t^{adj} as:

$$\pi_t^{adj} = \pi_t - E_{t-1}^P \pi_{t+1}$$

This expectations-adjusted measure of inflation is regressed against the unemployment-gap variable x_t . The OLS result would not recover the true underlying κ since we would expect x_t to be correlated with the supply shock ξ_t . It will only be able to recover the reduced-form relationship between inflation and unemployment gap, not the structural one.

[Table 2](#) shows that once expectations are taken into account, the relationship between inflation and the unemployment-gap is statistically significant - implying a 1% increase in the unemployment-gap associated with a roughly 10 bp decrease in inflation. It is worth noting that the estimate is quite close to the agents' beliefs about κ at the end of the sample shown in [Figure 5](#) (≈ -0.11). However, as the second column shows, the dummy representing the change in slope post 2020 is not found to be statistically significant at the 5% level. The regression does not give convincing evidence of a change in the reduced-form relationship during the recent surge.

Table 2: Expectations-augmented Phillips curve: Examining change in slope

	Model 1 Baseline	Model 2 Change in slope post-2020
\hat{x}_t	-0.106** (0.037)	-0.193** (0.063)
$\hat{x}_t \times \mathbf{1}_{\{t>2020\}}$	—	0.119 (0.067)
Observations	756	756
R^2 (uncentered)	0.023	0.028
F-stat	8.322	10.42
p-value	0.004	3.44e-05

Notes: Dependent variable is π_t^{adj} . Model 2 augments Model 1 with the interaction $x_t \times \mathbf{1}_{\{t>2020\}}$, where $\mathbf{1}_{\{t>2020\}}$ equals one for dates from 2020 onward. HAC (Newey-West) robust standard errors (Bartlett kernel, maxlags = 6). R^2 is computed without centering because the model has no constant. Significance: * indicates that the coefficient is significant at the 5% level.

Another way to shed light on whether time-variation in the Phillips curve slope is an important feature of economic dynamics necessary to explain the data is to directly test for time-variation in the κ_t against the null of a constant- κ_t in the relationship:

$$\pi_t^{\text{adj}} = -\kappa_t x_t + \xi_t$$

If the data supports time-variation in κ_t , then relaxing the restriction of a constant κ should result in a significantly better fit, as measured by log-likelihood. A likelihood-ratio (LR) test is conducted, testing the alternate hypothesis of time-variation in κ against the null of a constant

κ . The LR test is not statistically significant with $p \approx 1.00$. This suggests that the model finds no evidence in favor of time-variation slope of the Phillips curve once expectations are accounted for. The results of the test are reported in [Table 3](#). Re-estimating the model with a time-varying slope κ (allowing for innovations with a reasonably small variance 10^{-3} over time) produces nearly identical paths of beliefs as the baseline. Overall, the results suggest that changes in the slope of the structural Phillips curve are not a necessary feature to explain post-war U.S. economic dynamics.

Table 3: Results of the Likelihood Ratio Test

Model	Log-Likelihood	Parameters	χ^2	df	p-value
Restricted (Constant κ)	-402.460	3			
Full (Time-Varying κ)	-402.460	4	3.1×10^{-7}	1	1.000

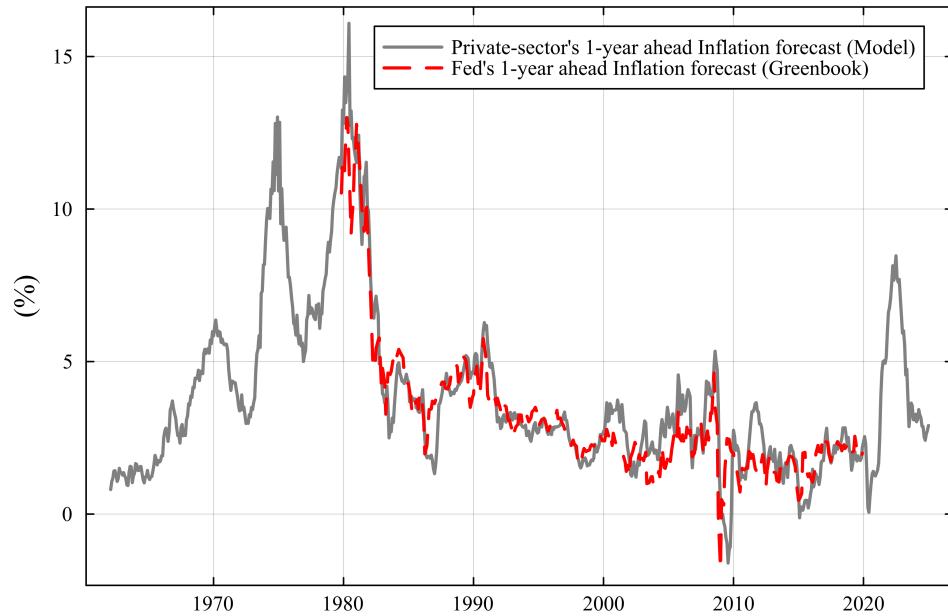
Note: The restricted model assumes a constant κ coefficient, while the full model allows it to vary over time. The constant parameter case is nested within the full time-varying parameter model. The Likelihood Ratio Test (LRT) statistic (χ^2) is calculated as $2 \times (\log L_{\text{Full}} - \log L_{\text{Restricted}})$, with degrees of freedom (df) equal to the difference in the number of parameters between the two models.

Overall, these results favor the time-invariant view of the Phillips curve adopted by the private agents in the model. Since the modeling framework in this paper explicitly accounts for endogenous formation of expectations, κ should not be interpreted as a purely a statistical relationship between inflation and unemployment described by [Phillips \(1958\)](#).

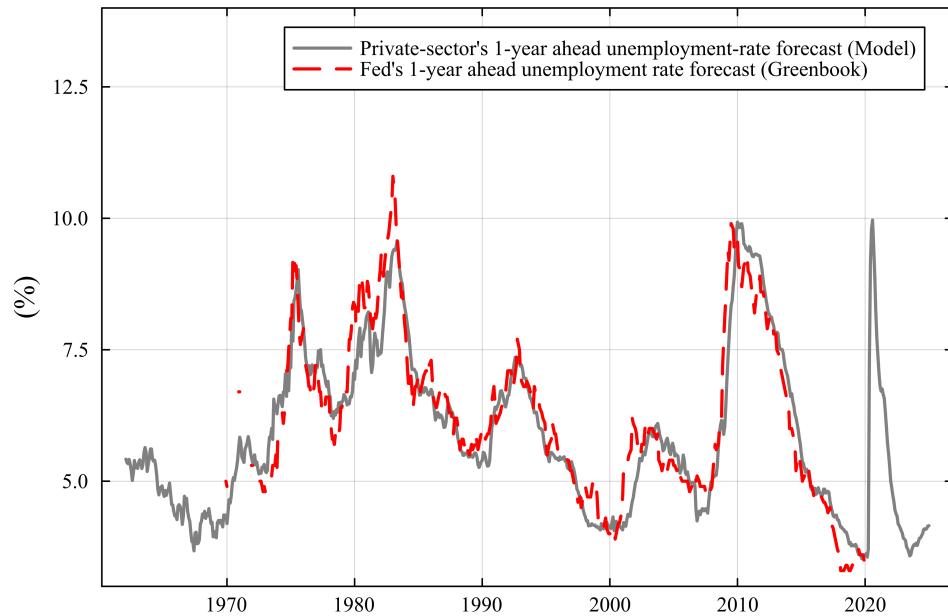
G Is the degree of information asymmetry small or large?

The analysis in this paper assumes very little information asymmetry between the Fed and the private-sector: (i) their beliefs about the structural parameters and shocks in the economy are shaped by the same data and the same economic model (ii) the filtering problem assumes that private-agents are able to track the true policy preferences efficiently, meaning that their tracked estimates never stray far away from the “true” underlying parameters describing the Fed policymakers’ stabilization preferences. One way to test whether these assumptions hold well during the sample period is to compare the agents’ forecasts as implied by the model with those from the Greenbook: the Fed’s internal forecasts prepared by the staff before each FOMC meeting. If the Fed policymakers do hold significantly different beliefs compared to the private agents, then it would be reflected as a discrepancy in their forecasts. From [Figure 16](#), we observe that Fed’s internal forecasts as seen in the Greenbook seem to be in line with those of the private agents in the model. This suggests that any information advantage that the Fed

possessed was of small order, at least to the extent that it influenced their outlook.



(a) **Inflation forecasts:** Comparing the Fed's 1-year ahead Headline CPI inflation forecast from Greenbook with 1-year ahead private-agents' forecasts from the baseline model



(b) **Unemployment rate forecasts:** Comparing the Fed's 1-year ahead unemployment rate forecast from Greenbook with 1-year ahead private agents' forecasts from the baseline model

Figure 16: **Macroeconomic outlook: Fed (Greenbook) vs Private Agents (Model)**