

Øgsl'sf -*- texinfo -*-

`gsl_sf ()` [Loadable Function]

Octave bindings to the GNU Scientific Library. All GSL functions can be called with by the GSL names within octave.

Øclausen -*- texinfo -*-

`y = clausen (x)` [Loadable Function]

`[y, err] = clausen (...)` [Loadable Function]

The Clausen function is defined by the following integral,

$$\text{Cl}_2(x) = - \int_0^x dt \log(2 \sin(t/2))$$

It is related to the dilogarithm by $\text{Cl}_2(\theta) = \text{Im Li}_2(\exp(i \theta))$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødawson -*- texinfo -*-

`y = dawson (x)` [Loadable Function]

`[y, err] = dawson (...)` [Loadable Function]

The Dawson integral is defined by $\exp(-x^2) \int_0^x dt \exp(t^2)$. A table of Dawson integral can be found in Abramowitz & Stegun, Table 7.5.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'1 -*- texinfo -*-

`y = debye_1 (x)` [Loadable Function]

`[y, err] = debye_1 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'2 -*- texinfo -*-

`y = debye_2 (x)` [Loadable Function]

`[y, err] = debye_2 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'3 *- texinfo -*-

`y = debye_3 (x)` [Loadable Function]
`[y, err] = debye_3 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'4 *- texinfo -*-

`y = debye_4 (x)` [Loadable Function]
`[y, err] = debye_4 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerf'gsl *- texinfo -*-

`y = erf_gsl (x)` [Loadable Function]
`[y, err] = erf_gsl (...)` [Loadable Function]

These routines compute the error function $\text{erf}(x) = (2/\sqrt{\pi}) \int_0^x dt \exp(-t^2)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerfc'gsl *- texinfo -*-

`y = erfc_gsl (x)` [Loadable Function]
`[y, err] = erfc_gsl (...)` [Loadable Function]

These routines compute the complementary error function $\text{erfc}(x) = 1 - \text{erf}(x) = (2/\sqrt{\pi}) \int_x^\infty \exp(-t^2) dt$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølog'erfc *- texinfo -*-

`y = log_erfc (x)` [Loadable Function]
`[y, err] = log_erfc (...)` [Loadable Function]

These routines compute the logarithm of the complementary error function $\log(\text{erfc}(x))$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerf_Z *- texinfo *-

`y = erf_Z (x)` [Loadable Function]

`[y, err] = erf_Z (...)` [Loadable Function]

These routines compute the Gaussian probability function $Z(x) = (1/(2\pi)) \exp(-x^2/2)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerf_Q *- texinfo *-

`y = erf_Q (x)` [Loadable Function]

`[y, err] = erf_Q (...)` [Loadable Function]

These routines compute the upper tail of the Gaussian probability function $Q(x) = (1/(2\pi)) \int x^{\infty} dt \exp(-t^2/2)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhazard *- texinfo *-

`y = hazard (x)` [Loadable Function]

`[y, err] = hazard (...)` [Loadable Function]

The hazard function for the normal distribution, also known as the inverse Mill's ratio, is defined as $h(x) = Z(x)/Q(x) = \sqrt{2/\pi} \exp(-x^2/2) / \operatorname{erfc}(x/\sqrt{2})$. It decreases rapidly as x approaches $-\infty$ and asymptotes to $h(x) \sim x$ as x approaches $+\infty$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpm1 *- texinfo *-

`y = expm1 (x)` [Loadable Function]

`[y, err] = expm1 (...)` [Loadable Function]

These routines compute the quantity $\exp(x)-1$ using an algorithm that is accurate for small x .

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexprel *- texinfo *-

`y = exprel (x)` [Loadable Function]

`[y, err] = exprel (...)` [Loadable Function]

These routines compute the quantity $(\exp(x)-1)/x$ using an algorithm that is accurate for small x . For small x the algorithm is based on the expansion $(\exp(x)-1)/x = 1 + x/2 + x^2/(2*3) + x^3/(2*3*4) + \text{dots}$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexprel'2 -*- texinfo -*-

`y = exprel_2 (x)` [Loadable Function]

`[y, err] = exprel_2 (...)` [Loadable Function]

These routines compute the quantity $2(\exp(x)-1-x)/x^2$ using an algorithm that is accurate for small x . For small x the algorithm is based on the expansion $2(\exp(x)-1-x)/x^2 = 1 + x/3 + x^2/(3*4) + x^3/(3*4*5) + \text{dots}$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint'E1 -*- texinfo -*-

`y = expint_E1 (x)` [Loadable Function]

`[y, err] = expint_E1 (...)` [Loadable Function]

These routines compute the exponential integral $E_1(x)$,
 $E_1(x) := \text{Re} \int_1^\infty dt \exp(-xt)/t$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint'E2 -*- texinfo -*-

`y = expint_E2 (x)` [Loadable Function]

`[y, err] = expint_E2 (...)` [Loadable Function]

These routines compute the second-order exponential integral $E_2(x)$,
 $E_2(x) := \text{Re} \int_1^\infty dt \exp(-xt)/t^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint'Ei -*- texinfo -*-

`y = expint_Ei (x)` [Loadable Function]

`[y, err] = expint_Ei (...)` [Loadable Function]

These routines compute the exponential integral $E_i(x)$,
 $E_i(x) := -\text{PV}(\int_{-x}^\infty dt \exp(-t)/t)$

where PV denotes the principal value of the integral.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØShi *-*- texinfo -*-*

y = Shi (*x*) [Loadable Function]

[*y*, *err*] = Shi (...) [Loadable Function]

These routines compute the integral $\text{Shi}(x) = \int_0^x dt \sinh(t)/t$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØChi *-*- texinfo -*-*

y = Chi (*x*) [Loadable Function]

[*y*, *err*] = Chi (...) [Loadable Function]

These routines compute the integral

$\text{Chi}(x) := \text{Re}[\gamma'E + \log(x) + \int_0^x dt (\cosh[t]-1)/t]$,

where $\gamma'E$ is the Euler constant.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint'3 *-*- texinfo -*-*

y = expint_3 (*x*) [Loadable Function]

[*y*, *err*] = expint_3 (...) [Loadable Function]

These routines compute the exponential integral $\text{Ei}'_3(x) = \int_0^x dt \exp(-t^3)$ for $x \geq 0$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØSi *-*- texinfo -*-*

y = Si (*x*) [Loadable Function]

[*y*, *err*] = Si (...) [Loadable Function]

These routines compute the Sine integral $\text{Si}(x) = \int_0^x dt \sin(t)/t$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØCi *-*- texinfo -*-*

`y = Ci (x)` [Loadable Function]
`[y, err] = Ci (...)` [Loadable Function]

These routines compute the Cosine integral $Ci(x) = -\int_x^\infty dt \cos(t)/t$ for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øatanint *- texinfo *-

`y = atanint (x)` [Loadable Function]
`[y, err] = atanint (...)` [Loadable Function]

These routines compute the Arctangent integral $AtanInt(x) = \int_0^x dt \arctan(t)/t$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi'dirac'mhalf *- texinfo *-

`y = fermi_dirac_mhalf (x)` [Loadable Function]
`[y, err] = fermi_dirac_mhalf (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral $F_{-1/2}(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi'dirac'half *- texinfo *-

`y = fermi_dirac_half (x)` [Loadable Function]
`[y, err] = fermi_dirac_half (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral $F_{1/2}(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi'dirac'3half *- texinfo *-

`y = fermi_dirac_3half (x)` [Loadable Function]
`[y, err] = fermi_dirac_3half (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral $F_{3/2}(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma'gsl *- texinfo *-

`y = gamma_gsl (x)` [Loadable Function]
`[y, err] = gamma_gsl (...)` [Loadable Function]

These routines compute the Gamma function $\Gamma(x)$, subject to x not being a negative integer. The function is computed using the real Lanczos method. The maximum value of x such that $\Gamma(x)$ is not considered an overflow is given by the macro `GSL_SF_GAMMA_XMAX` and is 171.0.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

`Ølngamma`gsl`-`-` texinfo`-`-`

`y = lngamma_gsl (x)` [Loadable Function]
`[y, err] = lngamma_gsl (...)` [Loadable Function]

These routines compute the logarithm of the Gamma function, $\log(\Gamma(x))$, subject to x not being negative integer. For $x < 0$ the real part of $\log(\Gamma(x))$ is returned, which is equivalent to $\log(|\Gamma(x)|)$. The function is computed using the real Lanczos method.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

`Øgammastar`-`-` texinfo`-`-`

`y = gammastar (x)` [Loadable Function]
`[y, err] = gammastar (...)` [Loadable Function]

These routines compute the regulated Gamma Function $\Gamma^*(x)$ for $x > 0$. The regulated gamma function is given by,

$$\Gamma^*(x) = \Gamma(x) / (\sqrt{2\pi} x^{x-1/2} \exp(-x)) = (1 + (1/12x) + \dots)$$
 for x to infity

and is a useful suggestion of Temme.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

`Øgammainv`gsl`-`-` texinfo`-`-`

`y = gammainv_gsl (x)` [Loadable Function]
`[y, err] = gammainv_gsl (...)` [Loadable Function]

These routines compute the reciprocal of the gamma function, $1/\Gamma(x)$ using the real Lanczos method.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

`Ølambert`W0`-`-` texinfo`-`-`

```
y = lambert_W0 (x) [Loadable Function]
[y, err] = lambert_W0 (...) [Loadable Function]
```

These compute the principal branch of the Lambert W function, $W_0(x)$.

Lambert's W functions, $W(x)$, are defined to be solutions of the equation $W(x)\exp(W(x)) = x$. This function has multiple branches for $x < 0$; however, it has only two real-valued branches. We define $W_0(x)$ to be the principal branch, where $W > -1$ for $x < 0$, and $W_{-1}(x)$ to be the other real branch, where $W < -1$ for $x < 0$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølambert_Wm1 -*- texinfo -*-

```
y = lambert_Wm1 (x) [Loadable Function]
[y, err] = lambert_Wm1 (...) [Loadable Function]
```

These compute the secondary real-valued branch of the Lambert W function, $W_{-1}(x)$.

Lambert's W functions, $W(x)$, are defined to be solutions of the equation $W(x)\exp(W(x)) = x$. This function has multiple branches for $x < 0$; however, it has only two real-valued branches. We define $W_0(x)$ to be the principal branch, where $W > -1$ for $x < 0$, and $W_{-1}(x)$ to be the other real branch, where $W < -1$ for $x < 0$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølog_1plusx -*- texinfo -*-

```
y = log_1plusx (x) [Loadable Function]
[y, err] = log_1plusx (...) [Loadable Function]
```

These routines compute $\log(1 + x)$ for $x > -1$ using an algorithm that is accurate for small *x*.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølog_1plusx_mx -*- texinfo -*-

```
y = log_1plusx_mx (x) [Loadable Function]
[y, err] = log_1plusx_mx (...) [Loadable Function]
```

These routines compute $\log(1 + x) - x$ for $x > -1$ using an algorithm that is accurate for small *x*.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi -*- texinfo -*-

`y = psi (x)` [Loadable Function]

`[y, err] = psi (...)` [Loadable Function]

These routines compute the digamma function $\psi(x)$ for general x , $x \in \mathbb{R}$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi`1piy *- texinfo *-

`y = psi_1piy (x)` [Loadable Function]

`[y, err] = psi_1piy (...)` [Loadable Function]

These routines compute the real part of the digamma function on the line $1 + i y$, $\operatorname{Re}[\psi(1 + i y)]$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øsynchrotron`1 *- texinfo *-

`y = synchrotron_1 (x)` [Loadable Function]

`[y, err] = synchrotron_1 (...)` [Loadable Function]

These routines compute the first synchrotron function $x \int_0^x dt K_{5/3}(t)$ for $x \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øsynchrotron`2 *- texinfo *-

`y = synchrotron_2 (x)` [Loadable Function]

`[y, err] = synchrotron_2 (...)` [Loadable Function]

These routines compute the second synchrotron function $x K_{2/3}(x)$ for $x \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`2 *- texinfo *-

`y = transport_2 (x)` [Loadable Function]

`[y, err] = transport_2 (...)` [Loadable Function]

These routines compute the transport function $J(2, x)$.

The transport functions $J(n, x)$ are defined by the integral representations $J(n, x) := \int_0^\infty t^n dt e^{-t} / (e^t - 1)^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`3 *- texinfo *-

`y = transport_3 (x)` [Loadable Function]
`[y, err] = transport_3 (...)` [Loadable Function]

These routines compute the transport function $J(3,x)$.

The transport functions $J(n,x)$ are defined by the integral representations $J(n,x) := \int_0^x dt t^n e^t / (e^t - 1)^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`4`- texinfo`-`-

`y = transport_4 (x)` [Loadable Function]
`[y, err] = transport_4 (...)` [Loadable Function]

These routines compute the transport function $J(4,x)$.

The transport functions $J(n,x)$ are defined by the integral representations $J(n,x) := \int_0^x dt t^n e^t / (e^t - 1)^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`5`- texinfo`-`-

`y = transport_5 (x)` [Loadable Function]
`[y, err] = transport_5 (...)` [Loadable Function]

These routines compute the transport function $J(5,x)$.

The transport functions $J(n,x)$ are defined by the integral representations $J(n,x) := \int_0^x dt t^n e^t / (e^t - 1)^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øsinc`gsl`- texinfo`-`-

`y = sinc_gsl (x)` [Loadable Function]
`[y, err] = sinc_gsl (...)` [Loadable Function]

These routines compute $\text{sinc}(x) = \sin(\pi x) / (\pi x)$ for any value of `x`.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølnsinh`- texinfo`-`-

`y = lnsinh (x)` [Loadable Function]
`[y, err] = lnsinh (...)` [Loadable Function]

These routines compute $\log(\sinh(x))$ for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølncosh *-*- texinfo -*-*

`y = lncosh (x)` [Loadable Function]
`[y, err] = lncosh (...)` [Loadable Function]

These routines compute $\log(\cosh(x))$ for any x .

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øzeta *-*- texinfo -*-*

`y = zeta (x)` [Loadable Function]
`[y, err] = zeta (...)` [Loadable Function]

These routines compute the Riemann zeta function $\zeta(s)$ for arbitrary s , $s \geq 1$.

The Riemann zeta function is defined by the infinite sum $\zeta(s) = \sum_{k=1}^{\infty} k^{-s}$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øeta *-*- texinfo -*-*

`y = eta (x)` [Loadable Function]
`[y, err] = eta (...)` [Loadable Function]

These routines compute the eta function $\eta(s)$ for arbitrary s .

The eta function is defined by $\eta(s) = (1-2^{1-s}) \zeta(s)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Jn *-*- texinfo -*-*

`y = bessel_Jn (n, x)` [Loadable Function]
`[y, err] = bessel_Jn (...)` [Loadable Function]

These routines compute the regular cylindrical Bessel function of order n , $J_n(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Yn *-*- texinfo -*-*

`y = bessel_Yn (n, x)` [Loadable Function]
`[y, err] = bessel_Yn (...)` [Loadable Function]

These routines compute the irregular cylindrical Bessel function of order n , $Y_n(x)$, for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_In -*- texinfo -*-

`y = bessell_In (n, x)` [Loadable Function]
`[y, err] = bessell_In (...)` [Loadable Function]

These routines compute the regular modified cylindrical Bessel function of order n , $I_n(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_In_scaled -*- texinfo -*-

`y = bessell_In_scaled (n, x)` [Loadable Function]
`[y, err] = bessell_In_scaled (...)` [Loadable Function]

These routines compute the scaled regular modified cylindrical Bessel function of order n , $\exp(-|x|) I_n(x)$

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Kn -*- texinfo -*-

`y = bessell_Kn (n, x)` [Loadable Function]
`[y, err] = bessell_Kn (...)` [Loadable Function]

These routines compute the irregular modified cylindrical Bessel function of order n , $K_n(x)$, for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Kn_scaled -*- texinfo -*-

`y = bessell_Kn_scaled (n, x)` [Loadable Function]
`[y, err] = bessell_Kn_scaled (...)` [Loadable Function]

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_jl -*- texinfo -*-

`y = bessell_jl (n, x)` [Loadable Function]
`[y, err] = bessell_jl (...)` [Loadable Function]

These routines compute the regular spherical Bessel function of order l , $j_l(x)$, for $l \geq 0$ and $x \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`yl`-* texinfo`-*

`y = bessel_yl (n, x)` [Loadable Function]
`[y, err] = bessel_yl (...)` [Loadable Function]
These routines compute the irregular spherical Bessel function of order l , $y_l(x)$, for $l \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`il`scaled`-* texinfo`-*

`y = bessel_il_scaled (n, x)` [Loadable Function]
`[y, err] = bessel_il_scaled (...)` [Loadable Function]
These routines compute the scaled regular modified spherical Bessel function of order l , $\exp(-|x|) i_l(x)$

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`kl`scaled`-* texinfo`-*

`y = bessel_kl_scaled (n, x)` [Loadable Function]
`[y, err] = bessel_kl_scaled (...)` [Loadable Function]
These routines compute the scaled irregular modified spherical Bessel function of order l , $\exp(x) k_l(x)$, for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexprel`n`-* texinfo`-*

`y = exprel_n (n, x)` [Loadable Function]
`[y, err] = exprel_n (...)` [Loadable Function]
These routines compute the N -relative exponential, which is the n -th generalization of the functions `gsl_sf_exprel` and `gsl_sf_exprel2`. The N -relative exponential is given by,

$$\text{exprel}_N(x) = N! / x^N (\exp(x) - \sum_{k=0}^{N-1} x^k / k!) = 1 + x / (N+1) + x^2 / ((N+1)(N+2)) + \dots = {}_1F_1(1, 1+N, x)$$

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi`dirac`int`-* texinfo`-*

`y = fermi_dirac_int (n, x)` [Loadable Function]

`[y, err] = fermi_dirac_int (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral with an integer index of j ,
 $F^j(x) = (1/\Gamma(j+1)) \int_0^\infty dt (t^j / (\exp(t-x)+1))$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtaylorcoeff -*- texinfo -*-

`y = taylorcoeff (n, x)` [Loadable Function]

`[y, err] = taylorcoeff (...)` [Loadable Function]

These routines compute the Taylor coefficient $x^n / n!$ for $x \geq 0$, $n \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre_Pl -*- texinfo -*-

`y = legendre_Pl (n, x)` [Loadable Function]

`[y, err] = legendre_Pl (...)` [Loadable Function]

These functions evaluate the Legendre polynomial $P_l(x)$ for a specific value of l , x subject to $l \geq 0$, $|x| \leq 1$

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre_Ql -*- texinfo -*-

`y = legendre_Ql (n, x)` [Loadable Function]

`[y, err] = legendre_Ql (...)` [Loadable Function]

These routines compute the Legendre function $Q_l(x)$ for $x > -1$, $x \neq 1$ and $l \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi_n -*- texinfo -*-

`y = psi_n (n, x)` [Loadable Function]

`[y, err] = psi_n (...)` [Loadable Function]

These routines compute the polygamma function $\psi^{(m)}(x)$ for $m \geq 0$, $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Jnu -*- texinfo -*-

`z = bessel_Jnu (x, y)` [Loadable Function]
`[z, err] = bessel_Jnu (...)` [Loadable Function]

These routines compute the regular cylindrical Bessel function of fractional order ν , $J_\nu(x)$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Ynu *- texinfo *-

`z = bessel_Ynu (x, y)` [Loadable Function]
`[z, err] = bessel_Ynu (...)` [Loadable Function]

These routines compute the irregular cylindrical Bessel function of fractional order ν , $Y_\nu(x)$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Inu *- texinfo *-

`z = bessel_Inu (x, y)` [Loadable Function]
`[z, err] = bessel_Inu (...)` [Loadable Function]

These routines compute the regular modified Bessel function of fractional order ν , $I_\nu(x)$ for $x>0$, $u>0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Inu_scaled *- texinfo *-

`z = bessel_Inu_scaled (x, y)` [Loadable Function]
`[z, err] = bessel_Inu_scaled (...)` [Loadable Function]

These routines compute the scaled regular modified Bessel function of fractional order ν , $\exp(-|x|)I_\nu(x)$ for $x>0$, $u>0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Knu *- texinfo *-

`z = bessel_Knu (x, y)` [Loadable Function]
`[z, err] = bessel_Knu (...)` [Loadable Function]

These routines compute the irregular modified Bessel function of fractional order ν , $K_\nu(x)$ for $x>0$, $u>0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`lnKnu`-* texinfo`-*`

`z = bessel_lnKnu (x, y)` [Loadable Function]

`[z, err] = bessel_lnKnu (...)` [Loadable Function]

These routines compute the logarithm of the irregular modified Bessel function of fractional order ν , $\ln(K_\nu(x))$ for $x > 0$, $\nu > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Knu`scaled`-* texinfo`-*`

`z = bessel_Knu_scaled (x, y)` [Loadable Function]

`[z, err] = bessel_Knu_scaled (...)` [Loadable Function]

These routines compute the scaled irregular modified Bessel function of fractional order ν , $\exp(+|x|) K_\nu(x)$ for $x > 0$, $\nu > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexp`mult`-* texinfo`-*`

`z = exp_mult (x, y)` [Loadable Function]

`[z, err] = exp_mult (...)` [Loadable Function]

These routines exponentiate `x` and multiply by the factor `y` to return the product $y \exp(x)$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi`dirac`inc`0`-* texinfo`-*`

`z = fermi_dirac_inc_0 (x, y)` [Loadable Function]

`[z, err] = fermi_dirac_inc_0 (...)` [Loadable Function]

These routines compute the incomplete Fermi-Dirac integral with an index of zero, $F_0(x, b) = \ln(1 + e^{b-x}) - (b-x)$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpoch`-* texinfo`-*`

`z = poch (x, y)` [Loadable Function]

`[z, err] = poch (...)` [Loadable Function]

These routines compute the Pochhammer symbol

$(a)_x := \Gamma(a+x)/\Gamma(a)$,

subject to a and $a+x$ not being negative integers. The Pochhammer symbol is also known as the Apell symbol.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølnpoch *-*- texinfo -*-*

z = `lnpoch` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `lnpoch` (...) [Loadable Function]

These routines compute the logarithm of the Pochhammer symbol, $\log((a)_x) = \log(\Gamma(a+x)/\Gamma(a))$ for $a > 0$, $a+x > 0$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpochrel *-*- texinfo -*-*

z = `pochrel` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `pochrel` (...) [Loadable Function]

These routines compute the relative Pochhammer symbol $((a)_x - 1)/x$ where $(a)_x := \Gamma(a+x)/\Gamma(a)$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma`inc`Q *-*- texinfo -*-*

z = `gamma_inc_Q` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `gamma_inc_Q` (...) [Loadable Function]

These routines compute the normalized incomplete Gamma Function $Q(a,x) = 1/\Gamma(a) \int_0^x t^{a-1} \exp(-t) dt$ for $a > 0$, $x \geq 0$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma`inc`P *-*- texinfo -*-*

z = `gamma_inc_P` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `gamma_inc_P` (...) [Loadable Function]

These routines compute the complementary normalized incomplete Gamma Function $P(a,x) = 1/\Gamma(a) \int_0^x t^{a-1} \exp(-t) dt$ for $a > 0$, $x \geq 0$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma`inc *-*- texinfo -*-*

`z = gamma_inc (x, y)` [Loadable Function]
`[z, err] = gamma_inc (...)` [Loadable Function]

These functions compute the incomplete Gamma Function the normalization factor included in the previously defined functions: $\Gamma(a, x) = \int_0^x t^{a-1} \exp(-t) dt$ for a real and $x \geq 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbeta'gsl -*- texinfo -*-

`z = beta_gsl (x, y)` [Loadable Function]
`[z, err] = beta_gsl (...)` [Loadable Function]

These routines compute the Beta Function, $B(a, b) = \Gamma(a)\Gamma(b)/\Gamma(a+b)$ for $a > 0$, $b > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølnbeta -*- texinfo -*-

`z = lnbeta (x, y)` [Loadable Function]
`[z, err] = lnbeta (...)` [Loadable Function]

These routines compute the logarithm of the Beta Function, $\log(B(a, b))$ for $a > 0$, $b > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhyperg_0F1 -*- texinfo -*-

`z = hyperg_0F1 (x, y)` [Loadable Function]
`[z, err] = hyperg_0F1 (...)` [Loadable Function]

These routines compute the hypergeometric function ${}_0F_1(c, x)$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP_half -*- texinfo -*-

`z = conicalP_half (x, y)` [Loadable Function]
`[z, err] = conicalP_half (...)` [Loadable Function]

These routines compute the irregular Spherical Conical Function $P^{-1/2}_{-1/2 + i\lambda}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP_mhalf -*- texinfo -*-

`z = conicalP_mhalf (x, y)` [Loadable Function]
`[z, err] = conicalP_mhalf (...)` [Loadable Function]

These routines compute the regular Spherical Conical Function $P^{-1/2}\{-1/2 + i\lambda\}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP_0 -*- texinfo -*-

`z = conicalP_0 (x, y)` [Loadable Function]
`[z, err] = conicalP_0 (...)` [Loadable Function]

These routines compute the conical function $P^0\{-1/2 + i\lambda\}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP_1 -*- texinfo -*-

`z = conicalP_1 (x, y)` [Loadable Function]
`[z, err] = conicalP_1 (...)` [Loadable Function]

These routines compute the conical function $P^1\{-1/2 + i\lambda\}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhzeta -*- texinfo -*-

`z = hzeta (x, y)` [Loadable Function]
`[z, err] = hzeta (...)` [Loadable Function]

These routines compute the Hurwitz zeta function $\zeta(s, q)$ for $s > 1$, $q > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy_Ai -*- texinfo -*-

`y = airy_Ai (x, mode)` [Loadable Function]
`[y, err] = airy_Ai (...)` [Loadable Function]

These routines compute the Airy function $Ai(x)$ with an accuracy specified by `mode`.

The second argument `mode` must be an integer corresponding to

0 = `GSL_PREC_DOUBLE`

Double-precision, a relative accuracy of approximately 2×10^{-16} .

1 = `GSL_PREC_SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Bi *- texinfo *-

y = airy_Bi (*x*, *mode*) [Loadable Function]

[*y*, *err*] = airy_Bi (...) [Loadable Function]

These routines compute the Airy function Bi(*x*) with an accuracy specified by *mode*.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Ai'scaled *- texinfo *-

y = airy_Ai_scaled (*x*, *mode*) [Loadable Function]

[*y*, *err*] = airy_Ai_scaled (...) [Loadable Function]

These routines compute a scaled version of the Airy function S'A(*x*) Ai(*x*). For *x*>0 the scaling factor S'A(*x*) is $\exp(+ (2/3) x^{(3/2)})$, and is 1 for *x*<0.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Bi'scaled *- texinfo *-

```
y = airy_Bi_scaled (x, mode) [Loadable Function]
[y, err] = airy_Bi_scaled (...) [Loadable Function]
```

These routines compute a scaled version of the Airy function $S'B(x)$ $Bi(x)$. For $x > 0$ the scaling factor $S'B(x)$ is $\exp(-(2/3) x^{(3/2)})$, and is 1 for $x < 0$.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Ai'deriv *- texinfo *-

```
y = airy_Ai_deriv (x, mode) [Loadable Function]
[y, err] = airy_Ai_deriv (...) [Loadable Function]
```

These routines compute the Airy function derivative $Ai'(x)$ with an accuracy specified by *mode*.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Bi'deriv *- texinfo *-

```
y = airy_Bi_deriv (x, mode) [Loadable Function]
[y, err] = airy_Bi_deriv (...) [Loadable Function]
```

These routines compute the Airy function derivative $Bi'(x)$ with an accuracy specified by *mode*.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Ai'deriv'scaled *- texinfo *-

y = airy_Ai_deriv_scaled (*x*, *mode*) [Loadable Function]

[*y*, *err*] = airy_Ai_deriv_scaled (...) [Loadable Function]

These routines compute the derivative of the scaled Airy function S'A(x) Ai(x).

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Bi'deriv'scaled *- texinfo *-

y = airy_Bi_deriv_scaled (*x*, *mode*) [Loadable Function]

[*y*, *err*] = airy_Bi_deriv_scaled (...) [Loadable Function]

These routines compute the derivative of the scaled Airy function S'B(x) Bi(x).

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øellint'Kcomp *- texinfo *-

y = ellint_Kcomp (*x*, *mode*) [Loadable Function]

`[y, err] = ellint_Kcomp (...)` [Loadable Function]
 These routines compute the complete elliptic integral $K(k)$

$$K(k) = \int_0^{\pi/2} \frac{dt}{\sqrt{(1 - k^2 \sin^2(t))}}$$

The notation used here is based on Carlson, *Numerische Mathematik* 33 (1979) and differs slightly from that used by Abramowitz & Stegun, where the functions are given in terms of the parameter $m = k^2$.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øellint'Ecomp -*- texinfo -*-

`y = ellint_Ecomp(x, mode)` [Loadable Function]
`[y, err] = ellint_Ecomp (...)` [Loadable Function]

These routines compute the complete elliptic integral $E(k)$ to the accuracy specified by the mode variable *mode*.

$$E(k) = \int_0^{\pi/2} \sqrt{(1 - k^2 \sin^2(t))} dt$$

The notation used here is based on Carlson, *Numerische Mathematik* 33 (1979) and differs slightly from that used by Abramowitz & Stegun, where the functions are given in terms of the parameter $m = k^2$.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy`zero`Ai -*- texinfo -*-

```
y = airy_zero_Ai (n) [Loadable Function]
[y, err] = airy_zero_Ai (...) [Loadable Function]
```

These routines compute the location of the s-th zero of the Airy function Ai(x).

err contains an estimate of the absolute error in the value y.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy`zero`Bi -*- texinfo -*-

```
y = airy_zero_Bi (n) [Loadable Function]
[y, err] = airy_zero_Bi (...) [Loadable Function]
```

These routines compute the location of the s-th zero of the Airy function Bi(x).

err contains an estimate of the absolute error in the value y.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy`zero`Ai`deriv -*- texinfo -*-

```
y = airy_zero_Ai_deriv (n) [Loadable Function]
[y, err] = airy_zero_Ai_deriv (...) [Loadable Function]
```

These routines compute the location of the s-th zero of the Airy function derivative Ai(x).

err contains an estimate of the absolute error in the value y.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy`zero`Bi`deriv -*- texinfo -*-

```
y = airy_zero_Bi_deriv (n) [Loadable Function]
[y, err] = airy_zero_Bi_deriv (...) [Loadable Function]
```

These routines compute the location of the s-th zero of the Airy function derivative Bi(x).

err contains an estimate of the absolute error in the value y.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`zero`J0 -*- texinfo -*-

```
y = bessel_zero_J0 (n) [Loadable Function]
[y, err] = bessel_zero_J0 (...) [Loadable Function]
```

These routines compute the location of the s-th positive zero of the Bessel function J₀(x).

err contains an estimate of the absolute error in the value y.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`zero`J1 -*- texinfo -*-

`y = bessel_zero_J1 (n)` [Loadable Function]
`[y, err] = bessel_zero_J1 (...)` [Loadable Function]

These routines compute the location of the s -th positive zero of the Bessel function $J_1(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi`1`int -*- texinfo -*-

`y = psi_1_int (n)` [Loadable Function]
`[y, err] = psi_1_int (...)` [Loadable Function]

These routines compute the Trigamma function $\psi_1(n)$ for positive integer n .

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øzeta`int -*- texinfo -*-

`y = zeta_int (n)` [Loadable Function]
`[y, err] = zeta_int (...)` [Loadable Function]

These routines compute the Riemann zeta function $\zeta(n)$ for integer n , $n \geq 1$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øeta`int -*- texinfo -*-

`y = eta_int (n)` [Loadable Function]
`[y, err] = eta_int (...)` [Loadable Function]

These routines compute the eta function $\eta(n)$ for integer n .

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre`Plm -*- texinfo -*-

`y = legendre_Plm (n, m, x)` [Loadable Function]
`[y, err] = legendre_Plm (...)` [Loadable Function]

These routines compute the associated Legendre polynomial $P_l^m(x)$ for $m \geq 0$, $l \geq m$, $|x| \leq 1$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre`sphPlm -*- texinfo -*-

`y = legendre_sphPlm (n, m, x)` [Loadable Function]

`[y, err] = legendre_sphPlm (...)` [Loadable Function]

These routines compute the normalized associated Legendre polynomial $\sqrt{\frac{2l+1}{4\pi}} \sqrt{\frac{(l-m)!}{(l+m)!}} P_l^m(x)$ suitable for use in spherical harmonics. The parameters must satisfy $m \geq 0$, $l \geq m$, $|x| \leq 1$. These routines avoid the overflows that occur for the standard normalization of $P_l^m(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhyperg`U *- texinfo *-

`out = hyperg_U (x0, x1, x2)` [Loadable Function]

`[out, err] = hyperg_U (...)` [Loadable Function]

Secondary Confluent Hypergeometric U function A&E 13.1.3 All input are double as is the output.

`err` contains an estimate of the absolute error in the value `out.a`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhyperg`1F1 *- texinfo *-

`out = hyperg_1F1 (x0, x1, x2)` [Loadable Function]

`[out, err] = hyperg_1F1 (...)` [Loadable Function]

Primary Confluent Hypergeometric U function A&E 13.1.3 All inputs are double as is the output.

`err` contains an estimate of the absolute error in the value `out.a`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.