# **Tyler Chen**

tyler.chen@nyu.edu https://chen.pw

#### **Academic Positions**

Assistant Professor / Courant Instructor

- Mathematics at Courant, Computer Science and Engineering at Tandon
- Sponsor: Christopher Musco

#### Education

Ph.D. in Applied Mathematics

- Thesis: Lanczos-based methods for matrix functions
- Advisors: Anne Greenbaum, Thomas Trogdon

M.Sc. in Applied Mathematics

B.S. Summa Cum Laude in Mathematics and Physics; Minor in Studio Art

#### Research Interests

I'm particularly interested in incorporating probabilistic techniques into classical algorithms to develop methods which are fast and reliable, both in theory and in practice. I hope that my work will help to bridge the gaps between numerical analysis, theoretical computer science, and applied computational sciences such as quantum physics with the ultimate goal of supporting the advancement of knowledge in the basic sciences.

#### Papers (in progress)

- [6] David Persson, Tyler Chen, and Christopher Musco. "Randomized block Krylov subspace methods for low rank approximation of matrix functions". 2024.
- [5] Tyler Chen, Feyza Duman Keles, Diana Halikias, Cameron Musco, Christopher Musco, and David Persson. "Near-optimal hierarchical matrix approximation from matrix-vector products". 2024. arXiv: 2407.04686 [cs.DS].
- [4] Noah Amsel, Tyler Chen, Feyza Duman Keles, Diana Halikias, Cameron Musco, and Christopher Musco. "Fixed-sparsity matrix approximation from matrix-vector products". 2024. arXiv: 2402. 09379 [cs.DS]. INTRO: https://research/chen.pw/intros/fixed\_sparsity\_matrix\_approximation.html
- [3] Tyler Chen, Anne Greenbaum, and Natalie Wellen. "Optimal Polynomial Approximation to Rational Matrix Functions Using the Arnoldi Algorithm". 2023. arXiv: 2306.17308 [math.NA].

- [2] Noah Amsel, Tyler Chen, Anne Greenbaum, Cameron Musco, and Christopher Musco. "Near-Optimality Guarantees for Approximating Rational Matrix Functions by the Lanczos Method". 2023. arXiv: 2303.03358 [math.NA].
- [1] Tyler Chen, Thomas Trogdon, and Shashanka Ubaru. "Randomized matrix-free quadrature for spectrum and spectral sum approximation". 2022. arXiv: 2204.01941 [math.NA].INTRO: https://research/chen.pw/intros/randomized\_quadrature.html

## Papers (published)

- [15] Tyler Chen, Robert Chen, Kevin Li, Skai Nzeuton, Yilu Pan, and Yixin Wang. "Faster randomized partial trace estimation". In: SIAM Journal on Scientific Computing (2023). To appear. arXiv: 2310. 12364 [math.NA].
- [14] Tyler Chen and Gérard Meurant. "Near-optimal convergence of the full orthogonalization method". In: Electronic Transactions on Numerical Analysis (2024). To appear. arXiv: 2403.07259 [math.NA].
- [13] Raghu Bollapragada, Tyler Chen, and Rachel Ward. "On the fast convergence of minibatch heavy ball momentum". In: *IMA Journal of Numerical Analysis* (2024). To appear. arXiv: 2206. 07553 [cs.LG].
- [12] Tyler Chen, Anne Greenbaum, and Thomas Trogdon. "GMRES, pseudospectra, and Crouzeix's conjecture for shifted and scaled Ginibre matrices". In: *Mathematics of Computation* (Mar. 2024). ISSN: 1088-6842. arXiv: 2303.02042 [math.NA].
- [11] Qichen Xu and Tyler Chen. "A posteriori error bounds for the block-Lanczos method for matrix function approximation". In: *Numerical Algorithms* (Apr. 2024). ISSN: 1572-9265. arXiv: 2211. 15643 [math.NA].
- [10] Tyler Chen and Thomas Trogdon. "Stability of the Lanczos algorithm on matrices with regular spectral distributions". In: *Linear Algebra and its Applications* 682 (Feb. 2024), pp. 191–237. ISSN: 0024-3795. arXiv: 2302.14842 [math.NA].
- [9] Tyler Chen. "A spectrum adaptive kernel polynomial method". In: The Journal of Chemical Physics 159.11 (Sept. 2023), p. 114101. arXiv: 2308.15683 [physics.comp-ph]. INTRO: https://research/chen.pw/intros/spectrum\_adaptive\_kpm.html
  - This approach is implemented in the spectral\_density package
- [8] Tyler Chen and Eric Hallman. "Krylov-Aware Stochastic Trace Estimation". In: SIAM Journal on Matrix Analysis and Applications 44.3 (Aug. 2023), pp. 1218–1244. arXiv: 2205.01736 [math.NA].
- [7] Tyler Chen, Anne Greenbaum, Cameron Musco, and Christopher Musco. "Low-Memory Krylov Subspace Methods for Optimal Rational Matrix Function Approximation". In: SIAM Journal on Matrix Analysis and Applications 44.2 (May 2023), pp. 670–692. arXiv: 2202.11251 [math.NA].
- [6] Tyler Chen and Yu-Chen Cheng. "Numerical computation of the equilibrium-reduced density matrix for strongly coupled open quantum systems". In: *The Journal of Chemical Physics* 157.6 (Aug. 2022), p. 064106. arXiv: 2204.08147 [quant-ph]. INTRO: https://research/chen.pw/intros/mean\_force.html

- [5] Tyler Chen, Anne Greenbaum, Cameron Musco, and Christopher Musco. "Error Bounds for Lanczos-Based Matrix Function Approximation". In: SIAM Journal on Matrix Analysis and Applications 43.2 (May 2022), pp. 787-811. arXiv: 2106.09806 [math.NA]. INTRO: https:// research/chen.pw/intros/lanczos\_function\_CIF.html
- [4] Tyler Chen, Thomas Trogdon, and Shashanka Ubaru. "Analysis of stochastic Lanczos quadrature for spectrum approximation". In: *Proceedings of the 38th International Conference on Machine Learning*. Vol. 139. Proceedings of Machine Learning Research. PMLR, July 2021, pp. 1728–1739. arXiv: 2105.06595 [cs.DS].
  - selected for long presentation (top 3%)
- [3] Anne Greenbaum, Hexuan Liu, and Tyler Chen. "On the Convergence Rate of Variants of the Conjugate Gradient Algorithm in Finite Precision Arithmetic". In: SIAM Journal on Scientific Computing (July 2021), S496–S515. arXiv: 1905.05874 [cs.NA].
- [2] Tyler Chen. "Non-asymptotic moment bounds for random variables rounded to non-uniformly spaced sets". In: Stat (June 2021), e395. arXiv: 2007.11041 [math.ST].
- [1] Tyler Chen and Erin C. Carson. "Predict-and-recompute conjugate gradient variants". In: SIAM Journal on Scientific Computing 42.5 (Jan. 2020), A3084–A3108. arXiv: 1905.01549 [cs.NA].
  - abridged version was Student Paper Competition winner at 16<sup>th</sup> Copper Mountain Conference on Iterative Methods

#### **Student Mentoring**

| State it i entering                   |                  |
|---------------------------------------|------------------|
| Active                                |                  |
| Robert Chen (NYU)                     | 2023 - present   |
| Caroline Huber (NYU)                  | 2024 - present   |
| Ethan Lin (NYU)                       | 2024 - present   |
| Devin Tang (NYU)                      | 2024 - present   |
| Hajar Zaid (Graduate Center CUNY)     | 2024 - present   |
|                                       |                  |
| Previous                              |                  |
| Kevin Li (NYU)                        | 2022 - 2024      |
| Yixin Wang (NYU)                      |                  |
| Yue Geng (NYU)                        | summer/fall 2023 |
| Ismael Jimenez (NYU)                  | summer 2023      |
| Skai Nzeuton (Stuyvesant High School) | 2022 - 2023      |
| Yilu Pan (NYU Shanghai)               | 2022 - 2023      |
| Qichen Xu (UW)                        | 2021 - 2023      |
| Linda Zhao (NYU)                      | summer/fall 2023 |
| Aeron Langford (UW)                   | autumn 2019      |
|                                       |                  |

## **Teaching**

| Instr | uctor  |
|-------|--|
| Num   | erical Analysis (NYU MATH-UA 252) fall 2024  |
| Linea | ar Algebra I (NYU MATH-GA 2110)  |
| Num   | erical Analysis (NYU MATH-UA 252) fall 2023  |
| Num   | erical Analysis (NYU MATH-UA 252) spring 2023  |
| Math  | nematical Statistics (NYU MATH-UA 234)   |
| Appl  | ied Linear Algebra and Numerical Analysis (UW AMATH 352) spring 2021   |
| Inter | disciplinary Writing/Natural Science (UW ENGL 199) winter 2021   |
| Inter | disciplinary Writing/Natural Science (UW ENGL 199) autumn 2020   |
| TA o  | r Grader   |
| Prob  | ability and Statistics for Computational Finance, TA (UW CFRM 410) winter 2019   |
| Calcu | ılus with Analytic Geometry I, TA (UW MATH 124) autumn 2018  |
| Calcu | ılus with Analytic Geometry II, TA (UW MATH 12) winter 2018  |
| Calcu | ılus with Analytic Geometry II, TA (UW MATH 125) autumn 2017   |
| Elect | ronics, TA (Tufts PHY 41)  |
| Elect | ronics, TA (Tufts PHY 41)  |
| Discı | rete Mathematics, Grader (Tufts MATH 61)spring 2016  |
| Calcu | ılus III, Grader (Tufts MATH 42) fall 2015   |
| Diffe | rential Equations, Grader (Tufts MATH 51) spring 2015  |
| Calcı | ılus III, Grader (Tufts MATH 42) fall 2014   |
| Talk  | s and Posters  |
| [22]  | "Near-optimal hierarchical matrix approximation from matrix-vector products". Presentation at Precond 2024. Atlanta, GA, June 2024.  |
| [21]  | "Is the Lanczos-Method for Matrix Functions Nearly Optimal?" Presentation at SIAM Linear Algebra 2024. Paris, France, May 2024.  |
| [20]  | "Krylov Subspace Methods and Matrix Functions: new directions in design, analysis, and applications". Presentation at Georgia Tech. Atlanta, GA, Jan. 2024.                |
| [19]  | "Randomized Numerical Linear Algebra and Iterative Methods". Presentation at NYU Math Modeling workshop. New York, NY, Nov. 2023.  |
| [18]  | "An introduction to (Randomized) Numerical Linear Algebra". Presentation at NYU Math Society meeting. New York, NY, Nov. 2023.   |
| [17]  | "Peering into the black box: Krylov-aware stochastic trace estimation". Presentation at SIAM New York, New Jersey, and Pennsylvania Annual Meeting. Newark, NJ, Oct. 2023. |
| [16]  | "Lanczos-based typicality methods for Quantum Thermodynamics". Presentation at Univer-   |

sität Bielefeld. Virtual, Oct. 2023.

- [15] "Krylov subspace methods for matrix function trace approximation". Presentation at NYU Shanghai. Shanghai, China, Aug. 2023.
- [14] "Krylov-aware low-rank approximation". Presentation at International Congress on Industrial and Applied Mathematics. Tokyo, Japan, Aug. 2023.
- [13] "Randomized trace estimation". Presentation at Sampling Theory and Applications Conference. New Haven, CT, July 2023.
- [12] "Randomized matrix-free quadrature". Presentation at Foundations of Computational Mathematics. Paris, France, June 2023.
- [11] "Stochastic trace estimation and quantum typicality: a case study in interdisciplinary research".

  Presentation at Perspectives on Matrix Computations: Theoretical Computer Science Meets
  Numerical Analysis. Banff, AB, Mar. 2023.
- [10] "Randomized matrix-free qudrature". Presentation at Courant Numerical Analysis and Scientific Computing Seminar. New York, NYU, Sept. 2022.
- [9] "GMRES, pseudospectra, and Crouzeix's conjecture for shifted and scaled Ginbre matrices". Presentation at Conference on Random Matrix Theory and Numerical Linear Algebra. Seattle, WA, June 2022.
- [8] "Simple Algorithms for Spectral Sum and Spectrum Approximation". Poster at Workshop on Algorithms for Large Data (Online). Virtual, Aug. 2021.
- [7] "Analysis of stochastic Lanczos quadrature for spectrum approximation". Oral at International Conference on Machine Learning. Virtual, July 2021.
- [6] "Concentration in the Lanczos Algorithm". Presentation at SIAM Linear Algebra 21. Virtual, May 2021.
- [5] "Analysis of stochastic Lanczos quadrature for spectrum approximation". Presentation at at Baidu Research. Seattle, WA, Mar. 2021.
- [4] "Analyzing the Effects of Local Roundoff Error on Predict-and-Recompute Conjugate Gradient Variants". Poster at Householder Symposium (Cancelled). Selva di Fasano, Italy, June 2020.
- [3] "Predict-and-recompute conjugate gradient variants". Presentation at Copper Mountain Student Paper Award Session (Cancelled). Copper Mountain, CO, Mar. 2020.
- [2] "Predict-and-recompute conjugate gradient variants". Presentation at SIAM Parallel Processing. Seattle, WA, Feb. 2020.
- [1] "Symmetric Preconditioner Refinement Using Low Rank Approximations". Presentation at Baidu Research. Seattle, WA, Feb. 2019.

### Service and Outreach

| Proud to Be First Faculty Connect |
|-----------------------------------|
| NYU SIAM podcast                  |

| NYU SIAM Grad School Info Session oct. 2022  |
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| Panelist for Q/A session for students interested in grad school  |
| Minisymposium Organizer may 2021   |
| Randommatricesandnumericallinearalgebra(atSIAMLinearAlgebra21, co-organizedwithThomas                                    |
| Trogdon) [program]   |
| Graduate Student Representative  |
| Represent interests of graduate students to the department   |
| Minisymposium Organizer feb. 2020  |
| High performance Krylov subspace methods: Theory, Implementation, and Application (at SIAM                               |
| Parallel Processing 20) [program]  |
| Diversity Committee Departmental Climate Orientation   |
| Panelist for event focused on building an inclusive department culture   |
| -  |
| Numerical Analysis Research Club   |
| Organize and plan weekly meetings for NARC   |
| SIAM UW Mental Health Conversation and Resources oct. 2018   |
| Organize and facilitate a discussion about mental health in grad school  |
| Software   |
| Research code (https://github.com/tchen-research)  |
| Repositories with code to generate figures and experiments from my papers.   |
| Spectral Density (https://pypi.org/project/spectral-density/)  |
| Develop spectral_density package to efficiently produce spectrum adaptive KPM approximations.                            |
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| PETSc (https://www.mcs.anl.gov/petsc/) Contribute PIPEPRCG. This method can be used by with the flag -ksp_type pipeprcg. |
|  |
| <pre>mpmath (https://github.com/mpmath)</pre>  |
| Update matrix multiplication driver to significantly improve performance for sparse matrices.                            |
| Awards & Honors  |
| Boeing Research Award (UW Department of Applied Mathematics)   |
| Student Paper Competition Winner (Copper Mountain Conference on Iterative Methods)                                       |
| Graduate Research Fellowship (NSF)   |
| Top Scholars Fellowship (UW)   |
|  |
| The Audrey Butvay Gruss Science Award (Tufts)  |
| The Audrey Butvay Gruss Science Award (Tufts) 2017 Phi Beta Kappa (Tufts) 2017   |
|  |