

$$r^2(n) = U r^2 U^\dagger \cdot \langle \Psi_d(n) | r^2(n) | \Psi_d(n) \rangle$$

* Since $Q |\Psi_d(n)\rangle \approx 0$
 $P |\Psi_d(n)\rangle \approx |\Psi_d(n)\rangle$

the relevant part is $P r^2(n) P$

* We want to decompose

$$\begin{aligned} P r^2(n) P &= P U r^2 U^\dagger P \\ &= \underbrace{P U P r^2 P U^\dagger P}_{\text{"P to P"}} + \overbrace{P U P r^2 Q U^\dagger P}^{\text{"P to Q"}} + P U Q r^2 P U^\dagger P \\ &\quad + \underbrace{P U Q r^2 Q U^\dagger P}_{\text{"Q to Q"}} \end{aligned}$$

* Since we're interested in $\delta r^2(n)$, we should really look at

$$P (r^2(n) - r^2) P \equiv P \delta r^2(n) P$$

* So, we know the exact answer $\langle \Psi_d(n) | P \delta r^2(n) P | \Psi_d(n) \rangle$.
 In the table, we want to see what the contributions of the "P-to-P", "P-to-Q", "Q-to-Q" terms are.