· A simple demonstration of ill-conditioning >> A = [1 2; 2 4.0001]using MATLAB. 2.0000 a 22 matrix A that is almost 1.0000 2.0000 4.0001 Tirevery dependent (3rd row & 2 * 1st row) >> b = [3; 6.0001]consider a vector b and the linear equation \(\mathbb{A} \) 3.0000 Ac = b6.0001 >> inv(A)*b Solve for <= £12 b and we get a reasonable result.</p> ans = 1 e check the eigenvalues. One is two (to the number of digits we printed). >> eig(A) ans = 0.0000 5.0001 e print more digits >> format long >> eig(A) e now in see a very small eigenvalue > ans = 0.000019999680004 5.000080000319996 e a shight change (perturbation) of A >> A_perturbed = [1.0001 2; 2 4.0001] A perturbed = 1.000100000000000 2.0000000000000000 2.0000000000000000 4.000100000000000 >> eig(A_perturbed) a still has a small eigenvalue, although changel. ans = 0.000100000000000 5.000100000000000 e but now c' = Atrobed & is radically >> inv(A_perturbed)*b ans = different bution ATL. The is a disaster 0.199996000079409 ta numerical colculations. 1.399992000160637

>> b_perturbed = [2.9999; 6.0001]

b_perturbed =

etry perturbing b

2.999900000000000

6.000100000000000

>> inv(A)*b_perturbed

ans =

-3.000100000019302

3.00000000014552

>> inv(A_perturbed)*b_perturbed

the other calculations of a go all over the place!

ans =

>>

-0.600007999841182

1.799984000321274

Clearly this is a problem we need to fix! [more later.,]