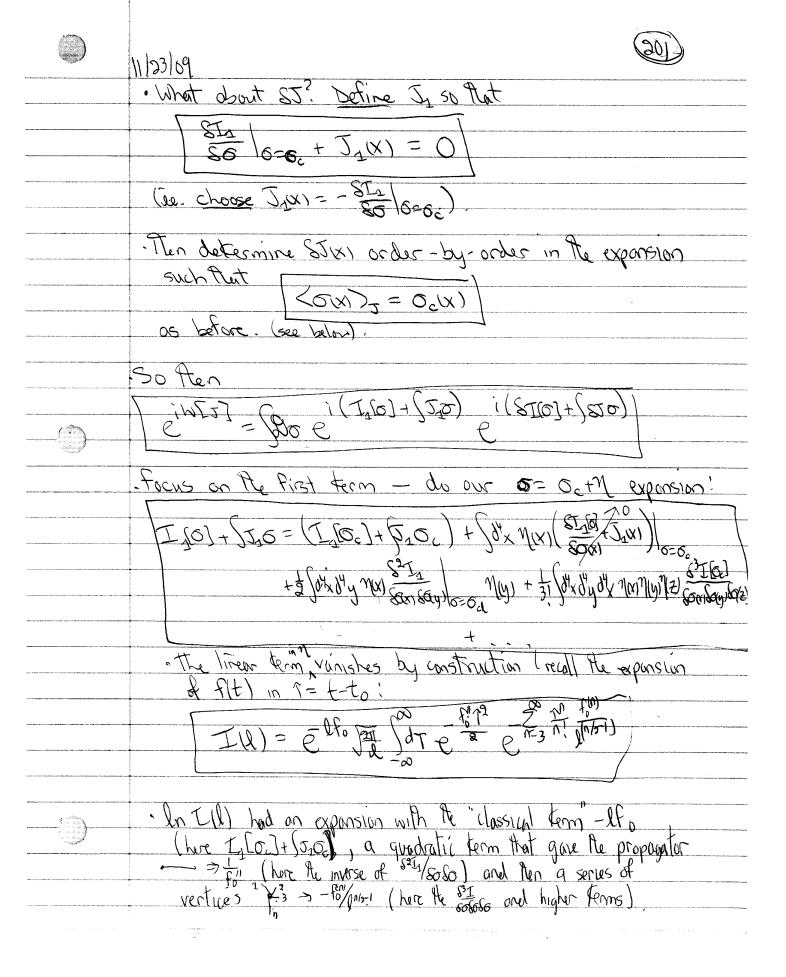
	162/10	(199)
	11/23/09 Morday 880.05 Glose	
	· alrestions on PS#3??	
	"Start effective action.	
	"Illustrate with saddle-point evalvation for lay V	
	· bose ends + honorrack greators	
	· regulators?	
3000		
	Recall where we're heading; small - Trying to reproduce Bose deluke gas (0570);	
	- hynny to reproduce store dilute gas (0670);	
	$\mathcal{E} = \frac{2\pi a_{5}}{m} g^{2} + \frac{2\pi a_{5}}{m} g^{2} \frac{128}{15\sqrt{\pi}} \sqrt{g}^{2} + \dots$	
	(Note == = 15 te energy per partide)	
		entrining generally to the second second
t i vi i vi vi vi i vi ji i madali vilga ji vi ji vi vi vi i vi ji vi vi vi vi ji vi vi vi vi ji vi vi vi vi j		
1990 Markitan Andrews (1990 Markitan Andrews)		TO THE RESIDENCE OF THE STATE O
and the second s		THE CHARGE PROPERTY OF THE CONTRACT OF THE CON
		TAKTOPAN (JAMAGAN TAKTONIN ALU TI , syringin syringin sabosyya

100030	11123109
	OK lots back in sad san where the margane
	Ok, let's back up and see where the expression we wrote on pg. 1980 comes From.
	we wrote on pa. 1700 comes from.
	Returning to 25 1 after the 4th 4 integration: (from 200)
	Returning to 215] after the 4t, 4 integration: (from 276) [2[5] = e 1650 = 500 e 25/16 (x,y) + \$ (050 x (6 x))^2 + i/d x 5 x x (6 x)
	15(2) = (10/2) = (20/2) = (20/2) + (20/2) + (20/2) + (20/2)
	15137-6 - 100 E
	= \\ \(\frac{1}{\pi_0} + \frac{1}{20} \)
	= 8000
	Which defines [6].
	Will A I to the CTO L (H Tropo)
	which defines 16]. We'll use the schematic notation 500 to mem (d'x Jixxxx). Note that ITO] shows up in the path integral as the action for the of field.
	· Note that Ital shows up in the path integral
	as the action for the or full.
	WA A. rescaling C=(b) 5=25/
	NATA The rescaling Co-colv, 6=26', we see again There is an oxerall factor of v in the exponent
	let is an oxerall tuctor of V in the exponent
***************************************	=> sabble point evaluation.
	So we've come to expand around the stationary point.
	So he've going to expand around the stationary point. At lovest order, this is $\sigma(x) = \sigma_{ol}(x)$ but this can change
	11 (00031 01 000), (1/15 15 (011) - 021) BOX (1/15 (01) CHONGE
	as we go higher in the expansion, unless we make sure it
	notes. So we will by introducing a counterterm for J. 150 split into a pure that is stationary about or by construction and the rest, which we tradit in perturbation reary.
	DO split into a pure that is stationary about the by construction and the rest,
	· Me mittel may be wall in belongation, read.
	[I6] = 1,6] + SI[6]
	T(x) = T(x) + T(x)
	$J(x) = J_2(x) + SJ(x)$
4-74.	
	SIG contains the "usual" counterforms we have in aumotum
	Fold Rever which fix in the short-dictages behavior
	Francisco Total & Field &
According to the second	of the short take effective real lung, using amensional regularization
	SIG contains the "usual" counterforms we have in quantum field theory, which fix is the short-distance behavior. For our short-range effective field they, using dimensional regularization on a minimal substraction, we will not need to write it-explicitly Decopressional



11/23/09	and the second s
11/23/09 - So identify WIJ) reglecting the 505056 and higher terms at first	V AND AND CONTRACT CONTRACTOR CON
Earnes at first [inter] = [= [= NTchG(x,n)] == och = [] dx (och) + [dx Inno	[(x
(80=01) × (81 = 30x dy ma) [82[4 Tolor G-1] + Cost xy)	\n(y)
where used sansay (\$CoSO" = (0(z))2 = CoS" (x-y)	
N. 1	ong pen-1196 . 2. shak ar managan ana ana
$ Nw $ $ S^{-2}(x,y) _{S=S_c} = [S^{-2} + S^{-2} + V - C_0 S(x)] S^{-1}(x-y) = [S^{-2}(x,y)]_{S=S_c}$	$G_{H}(x,y)$
(suppressing spin here), which is call the "Hortree" properties Green's function in the	
prosence & the "background field" ocix).	Annual Company of the
prosence & the "background field" ocix). Social is just like an external potential, Whe can solve for GH(X, Y) by methods analogue	
* We can solve for GH(X, Y) by methods onalogue to the problem set problem,	<u>.</u>
The M integral is just a Gaussian integral, with a scar	V
The M integral is just a Gaussian integral, with a scar looking operator botween the M's, which we define as the inverse & propagator Do:	J
inverse & propagator Do!	One of the second second second 2 A
[106(x,y) = Cost(x-y) + 52(ytrln61) 0=0c	what is Aps
$= C_0 S^{4}(x-y) + i v C_0^{2} G_{H}(y,x) G_{H}(x,y)$	as a mility?
· Here we've used (in schematic notation). Note Do = +-	D+DD
$\frac{5 \text{ in ln G-1}}{66} = 6 \frac{66}{66} = -0.06 \text{ and } \frac{666-1}{66} = 0 = \frac{66}{66} = 0 = 6$	$\frac{S}{S} = -C_0GG$
(fill in indices for pottern)	

	11/23/09
	. If we put back the higher order of terms and
	treated tem in perturbation Reary Con taking derivatives
	with respect to a source)
	> diagrams with these votices and lines (populations)
	given by Do (x,y).
	So now ne can find [Toc] = WIJ- [d'x Jx1Qxx)] to quadratic order because we can just take the ho of 201
	to graduatic order because we can just take the host EDI
	to find WCJ]_
	=> W(2) = 1/2 ln (CHKN) + CO(NX (O.K)) + (DaK) OCK)
	3/ N/2] = 1 LYUTOH ((A)) + 3/0 × (0° K)) + DA(X)O^(X)
	5 - Corcoins + 5 Tr ln (56 K,v))
	1/1/4 (DW)
)	path integral
endonadar var var bekenningen var Saart (op var	· Now me still have SI(O) and SJ that we left
	behind We expand these around to as well:
	(SILOC)+/SIOC) + (SILOC+M)-SILOC)+/SIM)
arikuu dala 1900 km kalenda pelandak kalenda kelikat 1900 km	just while to counterform
enterconomica del transcrio con conservo	WLJ) about rections
	A L C L
	-Now we can do the Leapendre transformation, since where WIJ = + S (5+87)Oc = 7 dependence in TTOc) gives away, as expected.
namen namen en e	me have WIJ = -+) (0, +87) Oc
anna filosopal filosopa y marcheny photo de company	
	1. (to-tomo STO) / STO m? - (TO) do A - m / 2/
The state of the s	the county forms offer an offering affect to their what yes,
) ———	has choose of leader by code-) so that (M) - 0
	· To reactice this simple more we ignore any todade
	· The counterterms STOC) and STLOCTMJ-STLOCD do Plair usual job. · The term JSTM takes cure of ensuring $\langle \sigma \rangle = G_c$ because we choose ST (order by order) so that $\langle m \rangle = 0$. · In practice, this simply means we ignore any "tadpole" diagrams (1).
THE STATE OF	· · · · · · · · · · · · · · · · · · ·



	11/23/09
	We could continue and look at the higher order diagrams
	in the exponsion systematically,
	In the exponsion systematically, - For now now we'll stop at:
	[Toc] = 12 Tr Ln[G#(x,y)] + Sold x (0,x)) + STr ln [06(x,y)]
	· Let's turn to our unform dilute system. · Uniform > Ock) = Oc, a constant.
	- Later will need to test whether the assumption
- Andrew Control	Later will need to test whether the assumption that the ground state is uniform is valid. (true for Co70 repulsive, not true for Co60 attractive!)
	(true for Co70 regularie, not true for Co60 attractive!)
, 2 x 3 x 3 x 3 x 5 x 5 x 5 x 5 x 5 x 5 x 5	. We can evaluate Tr In[Gi'] most easily by diagonalizing Gi > Tr is simple.
	Space-Drop M and put in boundary conditions
	space. Drop M and put in boundary conditions
	=> Tr ln GH = VT (27)3 (200 ln (80-8))
	(VT is the space time volume), timeson (181-Kg) -latere [ep = 2m + CoCc] and convergence factor eight
and the state of t	· As it stands, this expression is divergent, so there
	must be countertern subtractions he've left out.
	·It's easiest to proceed by noticing that the same discrepance is present when Co = 0, when we know the answer is -VT Emmtouts = -VT \(\frac{3}{2} \) \(\frac{1}{2} \) \(\frac{1}{2} \)
	some discrepence is present when Co = 0, when we
	Know the answer is -VT Enormtoners = -VI 5 2mg
	=> calculate the difference between TrlnGn'/co and TrlnGn'/c=0.
	· τι τι το=0 ·

11/23/19 (dx of f(x) = f(1)-f(0) XCo and use! Ditch GH = Sax VI (30 Spo who po = 3- > CoGc+ in sinlipi-ke)) 1) 0 p (16(1/4-1/2)) = -iVT C05cQ So we get the lending order (LO) effective action as (Oc) = VT (-3/2) p - COCP + 5COC2 We require it to be stationen! Plugging back in to 41965 where we've used Co= · Note that this includes Hartne but not Fock (x vs. 2-1 consistent with the lage & timit,

11/23/09
-OK, now for TALO, where we use a similar evaluation of yetrla [Do(x,y)].
"We'll use in the wantorm system $G_{H}(x_{1},x_{2})=\left(\frac{d^{4}p}{2\pi},G_{H}(p),e^{-ip\cdot(x_{1}-x_{2})}\right)$
with the Guld we've almost a used'
$QH(b) = \frac{b^o - \epsilon b_1 i \epsilon}{2(b - k^c)} + \frac{b^o - \epsilon b_1 i \epsilon}{2(k^c - b)}$
$= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \text{ to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} \operatorname{to bisis where } D_{O}^{-1} \text{ is diagran} \Rightarrow q$ $= \int_{NLOC} \left[-\frac{i}{2} \operatorname{Tr} \ln \left[D_{O}^{-1} \right] \right] = \operatorname{cp} to$
(To(9) = -1) (3/10 Go(p+q) Go(p) = -ix) (3/10 GH(p+q) GH(p)
where the god equality is valid for a uniform system, - a Diagramatically, we're summing up
which are exactly the diagrams (after the first few) that he want for the Bose limit!



	11/23/09
	We can evaluate the In with the same trick as before?
	Co > > Co and take demonties
M 15 tables and the part of th	. There will be apparent divergences when 1=0 and
	exember, but they're all taken care of with dimensional regularisation for which
	dimensional regularization for which
	(dok 10
	SOR = 0
	and while we're at it (from feskint Schroder QFT text)
	(3m) \$\langle \langle
	2 (411) K/5+V3 MILLO (2) (1/2)
	[N20[0] = = VT (2/9 (d) d) (ln (-i)Cot i (Co TT o (q)))
	1) N2010cl = 2 VI)(211)4) 2) Tx(ln(-12ct (x(0)))
	= 5 VT Sal and 1 (-iCo+2i2Co16)
	20 1(211)4 -1XCo+1XCoNdq)
	(_ () () () () () () () () ()
	$= -\frac{1}{2}\sqrt{1}\int_{0}^{1}\frac{d\lambda}{\lambda}\left(\frac{d^{4}q}{\lambda}\right)\frac{\lambda C_{0}\pi_{0}(q)}{1-\lambda C_{0}\pi_{0}(q)}$
and the couple of the color standard area, replace with a supplied the color standard area.	where we've dropped a gotte term by DR.
r verificies e subtraction de la company e qu'en qu'en en propriété de la company de la company de la company e	or es the is displace of Jan 12 Him by DR.
	This he can evalvate using (exercise for reader to derive!)
	(6(p+q-kg) 6(p-q-kg))
	This he can evalvate using (exercise for reader to derive) To (qo,q) = y (de q) (kx-p) (6(p+q)-kp) (9+ kp-wp+q+ip q-ip) To (qo,q) = y (de q) (kx-p) (9+ kp-wp+q+ip) (9- wp+kp-q-ip)
	TO THE CHARTEST TE
	· This is ually and has to be done numerically
	(Tour Pat Big To can be evaluated)
Sign I	This is ugly and has to be done numerically, (The fat sig To can be evaluated,) Here we = 2m
	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \



11/23/19 - But if he apply the Bose limit y >0, \$50, point fixed at this stage, it's casy! (10 (90,9) Kero P) (30 (Ke-P) (1-4+18 - 9,+4) E = 2 wg 5 (90-wg+iE) (90+wg-iE) using 19/17 kg,p in the integrals So Dun $\frac{\lambda C_0 T_0}{1 - \lambda C_0 T_0} = \frac{\lambda C_0}{(T_0)^1 - \lambda C_0} = \frac{3 w_q g \lambda C_0}{q_0^2 - w_q^2 - 2 w_q g \lambda C_0 + 1 \epsilon}$ = 2 mg/ (0 90-Eg +18 definiz le Boapliubor quasiporticle eregies $\epsilon_{\vec{q}} = \sqrt{\omega_4^2 + 2\omega_4 \beta \zeta_0 \lambda}$ go integral picks up a simple pole and my get applying he DR formula, we get (for 0=3) $\mathcal{E}_{1}^{30x} = \frac{\mathcal{E}}{15\pi^{2}} (4m_{p})^{3/2} C_{0}^{5/2} = \frac{2\pi\alpha_{sp}^{2}}{m} \frac{128}{15\sqrt{\pi}} \sqrt{\rho a_{s}^{2}}$ as desired,