



KTH Royal Institute of Technology

Omogen Heap

Simon Lindholm, Johan Sannemo, Mårten Wiman

2020-11-22

- 1 Contest
- 2 Data structures
- 3 Geometry
- 4 Graphs
- 5 Mathematics
- 6 Miscellaneous
- 7 Strings

Contest (1)

template.cpp10 lines

```
#include <bits/stdc++.h>
#define all(x) begin(x), end(x)
using namespace std;

using ll = long long;

int main() {
    cin.tie(0)->sync_with_stdio(0);
    cin.exceptions(cin.failbit);
}
```

Data structures (2)

BIT.h33f78c, 22 lines

```

Description: Query [l, r] sums, and point updates. kth() returns the small-
est index i s.t. query(0, i) >= k
Time:  $\mathcal{O}(\log n)$  for all ops.

template <typename T>
struct BIT {
    vector<T> s;
    int n;
    BIT(int n) : s(n + 1), n(n) {}
    void update(int i, T v) {
        for (i++; i <= n; i += i & -i) s[i] += v;
    }
    T query(int i) {
        T ans = 0;
        for (i++; i; i -= i & -i) ans += s[i];
        return ans;
    }
    T query(int l, int r) { return query(r) - query(l - 1); }
    int kth(T k) { // returns n if k > sum of tree
        if (k <= 0) return -1;
        int i = 0;
        for (int pw = 1 << __lg(n); pw; pw >>= 1)
            if (i + pw <= n && s[i + pw] < k) k -= s[i + pw];
        return i;
    }
};
```

KDBIT.h

Description: k -dimensional BIT. BIT<int, N, M> gives an $N \times M$ BIT.
Query: bit.query(x1, x2, y1, y2) Update: bit.update(x, y, delta)
Time: $\mathcal{O}(\log^k n)$ Status: Tested3b9692, 28 lines

```

template <class T, int... Ns>
struct BIT {
    T val = 0;
    void update(T v) { val += v; }
    T query() { return val; }
};

template <class T, int N, int... Ns>
struct BIT<T, N, Ns...> {
    BIT<T, Ns...> bit[N + 1];
    // map<int, BIT<T, Ns...>> bit;
    // if the memory use is too high
    template <class... Args>
    void update(int i, Args... args) {
        for (i++; i <= N; i += i & -i) bit[i].update(args...);
    }
    template <class... Args>
    T query(int i, Args... args) {
        T ans = 0;
        for (i++; i; i -= i & -i) ans += bit[i].query(args...);
        return ans;
    }
    template <class... Args,
              enable_if_t<(sizeof...(Args) ==
                          2 * sizeof...(Ns))>* = nullptr>
    T query(int l, int r, Args... args) {
        return query(r, args...) - query(l - 1, args...);
    }
};
```

DSU.hc22586, 14 lines

```

Description: Maintains union of disjoint sets
Time:  $\mathcal{O}(\alpha(N))$ 

struct DSU {
    vector<int> s;
    DSU(int n) : s(n, -1) {}
    int find(int i) { return s[i] < 0 ? i : s[i] = find(s[i]); }
    bool join(int a, int b) {
        a = find(a), b = find(b);
        if (a == b) return false;
        if (s[a] > s[b]) swap(a, b);
        s[a] += s[b], s[b] = a;
        return true;
    }
    int size(int i) { return -s[find(i)]; }
    bool same(int a, int b) { return find(a) == find(b); }
};
```

RMQ.h336eac, 15 lines

```

Description: Constant time subarray min/max queries for a fixed array
Time:  $\mathcal{O}(n \log n)$  initialization and  $\mathcal{O}(1)$  queries. Status: Tested

template <typename T, class Compare = less<T>>
struct RMQ {
    vector<vector<T>> t;
    Compare cmp;
    RMQ(vector<T>& a) : t(__lg(a.size()) + 1, a) {
        int n = a.size(), lg = __lg(n);
        for (int k = 1, len = 1; k <= lg; k++, len <= 1)
            for (int i = 0; i + 2 * len - 1 < n; i++)
                t[k][i] = min(t[k - 1][i], t[k - 1][i + len], cmp);
    }
    T query(int a, int b) {
        int k = __lg(b - a + 1), len = 1 << k;
        return min(t[k][a], t[k][b - len + 1], cmp);
    }
};
```

3b9692, 28 lines

```

};

Splay.h
Description: An implicit balanced BST. You only need to change update()
and prop().
If used for link-cut tree, code everything up to splay(). Time: amortized
 $\mathcal{O}(\log n)$  for all operations0d0cee, 92 lines

struct node {
    node *ch[2] = {0}, *p = 0;
    int cnt = 1, val;

    node(int val, node* l = 0, node* r = 0)
        : ch{l, r}, val(val) {}
};

int cnt(node* x) { return x ? x->cnt : 0; }
int dir(node* p, node* x) { return p && p->ch[0] != x; }
void setLink(node* p, node* x, int d) {
    if (p) p->ch[d] = x;
    if (x) x->p = p;
}

node* update(node* x) {
    if (!x) return 0;
    x->cnt = 1 + cnt(x->ch[0]) + cnt(x->ch[1]);
    setLink(x, x->ch[0], 0);
    setLink(x, x->ch[1], 1);
    return x;
}

void prop(node* x) {
    if (!x) return;
    // update(x); // needed if prop() can change subtree sizes
}

void rotate(node* x, int d) {
    if (!x || !x->ch[d]) return;
    node *y = x->ch[d], *z = x->p;
    setLink(x, y->ch[d ^ 1], d);
    setLink(y, x, d ^ 1);
    setLink(z, y, dir(z, x));
    update(x);
    update(y);
}

node* splay(node* x) {
    while (x && x->p) {
        node *y = x->p, *z = y->p;
        // prop(z), prop(y), prop(x); // needed for LCT
        int dy = dir(y, x), dz = dir(z, y);
        if (!z)
            rotate(y, dy);
        else if (dy == dz)
            rotate(z, dz), rotate(y, dy);
        else
            rotate(y, dy), rotate(z, dz);
    }
    return x;
}
```

```

// the returned node becomes the new root, update the root
// pointer!
node* nodeAt(node* x, int pos) {
    if (!x) return 0;
    while (prop(x), cnt(x->ch[0]) != pos)
        if (pos < cnt(x->ch[0]))
            x = x->ch[0];
    else
```

```
        pos -= cnt(x->ch[0]) + 1, x = x->ch[1];
        return splay(x);
    }

node* merge(node* l, node* r) {
    if (!l || !r) return l ?: r;
    l = nodeAt(l, cnt(l) - 1);
    setLink(l, r, 1);
    return update(l);
}

// first is everything < pos, second is >= pos
pair<node*, node*> split(node* t, int pos) {
    if (pos <= 0 || !t) return {0, t};
    if (pos > cnt(t)) return {t, 0};
    node *l = nodeAt(t, pos - 1), *r = l->ch[1];
    if (r) l->ch[1] = r->p = 0;
    return {update(l), update(r)};
}

// insert a new node between pos-1 and pos
node* insert(node* t, int pos, int val) {
    auto [l, r] = split(t, pos);
    return update(new node(val, l, r));
}

// apply lambda to all nodes in an inorder traversal
template <class F>
void each(node* x, F f) {
    if (x) prop(x), each(x->ch[0], f), f(x), each(x->ch[1], f);
}
```

Geometry (3)

Graphs (4)

SCCTarjan.h

Description: Finds strongly connected components of a directed graph. Visits/indexes SCCs in reverse topological order.
Usage: scc(graph) returns an array that has the ID of each node’s SCC. scc(graph, [&](vector<int>& v) { ... }) calls the lambda on each SCC, and returns the same array.
Time: $\mathcal{O}(|V| + |E|)$

358d18, 37 lines

```
namespace SCCTarjan {
    vector<int> val, comp, z, cont;
    int Time, ncomps;
    template <class G, class F>
    int dfs(int j, G& g, F& f) {
        int low = val[j] = ++Time, x;
        z.push_back(j);
        for (auto e : g[j])
            if (comp[e] < 0) low = min(low, val[e] ?: dfs(e, g, f));
        if (low == val[j]) {
            do {
                x = z.back();
                z.pop_back();
                comp[x] = ncomps;
                cont.push_back(x);
            } while (x != j);
            f(cont);
            cont.clear();
            ncomps++;
        }
        return val[j] = low;
    }
    template <class G, class F>
```

```
vector<int> scc(G& g, F f) {
    int n = g.size();
    val.assign(n, 0);
    comp.assign(n, -1);
    Time = ncomps = 0;
    for (int i = 0; i < n; i++)
        if (comp[i] < 0) dfs(i, g, f);
    return comp;
}
template <class G> // convenience function w/o lambda
vector<int> scc(G& g) {
    return scc(g, [](auto& v) {});
}
} // namespace SCCTarjan
```

SCCKosaraju.h

Description: Finds strongly connected components of a directed graph. Visits/indexes SCCs in topological order.
Usage: scc(graph) returns an array that has the ID of each node’s SCC.
Time: $\mathcal{O}(|V| + |E|)$

9b78e7, 29 lines

```
namespace SCCKosaraju {
    vector<vector<int>> adj, radj;
    vector<int> todo, comp;
    vector<bool> vis;
    void dfs1(int x) {
        vis[x] = 1;
        for (int y : adj[x])
            if (!vis[y]) dfs1(y);
        todo.push_back(x);
    }
    void dfs2(int x, int i) {
        comp[x] = i;
        for (int y : radj[x])
            if (comp[y] == -1) dfs2(y, i);
    }
    vector<int> scc(vector<vector<int>>& _adj) {
        adj = _adj;
        int time = 0, n = adj.size();
        comp.resize(n, -1), radj.resize(n), vis.resize(n);
        for (int x = 0; x < n; x++)
            for (int y : adj[x]) radj[y].push_back(x);
        for (int x = 0; x < n; x++)
            if (!vis[x]) dfs1(x);
        reverse(todo.begin(), todo.end());
        for (int x : todo)
            if (comp[x] == -1) dfs2(x, time++);
        return comp;
    }
}; // namespace SCCKosaraju
```

Dinic.h

Description: Max flow algorithm. Can find a valid circulation given vertex and/or edge demands. Time: $\mathcal{O}(VE \log U)$

9ad873, 84 lines

```
struct Dinic {
    // disable scaling when max flow/capacity is small, or
    // sometimes on random data
    const static bool SCALING = true;
    struct Edge {
        int v, dual;
        ll cap, res;
        constexpr ll flow() { return max(cap - res, 0ll); }
    };
    int n, s, t;
    vector<int> lvl, q, blk;
    vector<vector<Edge>> adj;
    vector<pair<int, int>> edges;
```

```
Dinic(int n) : n(n + 2), s(n++), t(n++), q(n), adj(n) {}
int add(int u, int v, ll cap, ll flow = 0) {
    adj[u].push_back({v, int(adj[v].size()), cap, cap - flow});
    adj[v].push_back({u, int(adj[u].size()) - 1, 0, 0});
    edges.emplace_back(u, adj[u].size() - 1);
    return edges.size() - 1; // this Edge’s ID
}
ll dfs(int u, ll in) {
    if (u == t || !in) return in;
    ll flow = 0;
    for (auto& e : adj[u]) {
        if (e.res && !blk[e.v] && lvl[e.v] == lvl[u] - 1)
            if (ll out = dfs(e.v, min(in, e.res))) {
                flow += out, in -= out, e.res -= out;
                adj[e.v][e.dual].res += out;
                if (!in) return flow;
            }
    }
    blk[u] = 1;
    return flow;
}
ll flow() {
    ll flow = 0;
    q[0] = t;
    for (int B = SCALING * 30; B >= 0; B--) do {
        lvl = blk = vector<int>(n);
        int qi = 0, qe = lvl[t] = 1;
        while (qi < qe && !lvl[s]) {
            int u = q[qi++];
            for (auto& e : adj[u])
                if (!lvl[e.v] && adj[e.v][e.dual].res >> B)
                    q[qi++] = e.v, lvl[e.v] = lvl[u] + 1;
        }
        if (lvl[s]) flow += dfs(s, LLONG_MAX);
    } while (lvl[s]);
    return flow;
}
Edge& get(int id) { // get Edge object from its ID
    return adj[edges[id].first][edges[id].second];
}
void clear() {
    for (auto& it : adj)
        for (auto& e : it) e.res = e.cap;
}
bool leftOfMinCut(int u) { return lvl[u] == 0; }
// d is a list of vertex demands, d[u] = flow in - flow out
// negative if u is a source, positive if u is a sink
bool circulation(vector<ll> d = {}) {
    d.resize(n);
    vector<int> circEdges;
    Dinic g(n);
    for (int u = 0; u < n; u++)
        for (auto& e : adj[u]) {
            d[u] += e.flow(), d[e.v] -= e.flow();
            if (e.res) circEdges.push_back(g.add(u, e.v, e.res));
        }
    int tylerEdge = g.add(t, s, LLONG_MAX, 0);
    ll flow = 0;
    for (int u = 0; u < n; u++)
        if (d[u] < 0)
            g.add(g.s, u, -d[u]);
        else if (d[u] > 0)
            g.add(u, g.t, d[u]), flow += d[u];
    if (flow != g.flow()) return false;
    int i = 0; // reconstruct the flow into this graph
    for (int u = 0; u < n; u++)
        for (auto& e : adj[u])
            if (e.res) e.res -= g.get(circEdges[i++]).flow();
    return true;
```

```
    }
};
```

Mathematics (5)

Fraction.h
Description: Struct for representing fractions/rationals. All ops are $O(\log N)$ due to GCD in constructor. Uses cross multiplication

<pre>template <typename T> struct Q { T a, b; Q(T p, T q = 1) { T g = gcd(p, q); a = p / g; b = q / g; if (b < 0) a = -a, b = -b; } T gcd(T x, T y) const { return __gcd(x, y); } Q operator+(const Q& o) const { return {a * o.b + o.a * b, b * o.b}; } Q operator-(const Q& o) const { return *this + Q(-o.a, o.b); } Q operator*(const Q& o) const { return {a * o.a, b * o.b}; } Q operator/(const Q& o) const { return *this * Q(o.b, o.a); } Q recip() const { return {b, a}; } int signum() const { return (a > 0) - (a < 0); } bool operator<(const Q& o) const { return a * o.b < o.a * b; } friend ostream& operator<<(ostream& cout, const Q& o) { return cout << o.a << "/" << o.b; } };</pre>	a1de34, 27 lines
---	------------------

FractionOverflow.h
Description: Safer struct for representing fractions/rationals. Comparison is 100% overflow safe; other ops are safer but can still overflow. All ops are $O(\log N)$.

<pre>template <typename T> struct QO { T a, b; QO(T p, T q = 1) { T g = gcd(p, q); a = p / g; b = q / g; if (b < 0) a = -a, b = -b; } T gcd(T x, T y) const { return __gcd(x, y); } QO operator+(const QO& o) const { T g = gcd(b, o.b), bb = b / g, obb = o.b / g; return {a * obb + o.a * bb, o.b * obb}; } QO operator-(const QO& o) const { return *this + QO(-o.a, o.b); } QO operator*(const QO& o) const { T g1 = gcd(a, o.b), g2 = gcd(o.a, b); return {(a / g1) * (o.a / g2), (b / g2) * (o.b / g1)}; } QO operator/(const QO& o) const { return *this * QO(o.b, o.a); } QO recip() const { return {b, a}; } int signum() const { return (a > 0) - (a < 0); }</pre>	a42e99, 43 lines
---	------------------

<pre>static bool lessThan(T a, T b, T x, T y) { if (a / b != x / y) return a / b < x / y; if (x % y == 0) return false; if (a % b == 0) return true; return lessThan(y, x % y, b, a % b); } bool operator<(const QO& o) const { if (this->signum() != o.signum() a == 0) return a < o.a; if (a < 0) return lessThan(abs(o.a), o.b, abs(a), b); else return lessThan(a, b, o.a, o.b); } friend ostream& operator<<(ostream& cout, const QO& o) { return cout << o.a << "/" << o.b; } };</pre>	
--	--

PrimeSieve.h
Description: Prime sieve for generating all primes up to a certain limit. isprime[i] is true iff i is a prime.
Time: lim=100'000'000 \approx 0.8 s. Runs 30% faster if only odd indices are stored.

<pre>const int MAX_PR = 5'000'000; bitset<MAX_PR> isprime; vector<int> primeSieve(int lim) { isprime.set(); isprime[0] = isprime[1] = 0; for (int i = 4; i < lim; i += 2) isprime[i] = 0; for (int i = 3; i * i < lim; i += 2) if (isprime[i]) for (int j = i * i; j < lim; j += i * 2) isprime[j] = 0; vector<int> pr; for (int i = 2; i < lim; i++) if (isprime[i]) pr.push_back(i); return pr; }</pre>	dc4f55, 14 lines
---	------------------

PrimeSieveFast.h
Description: Prime sieve for generating all primes smaller than LIM.
Time: LIM=1e9 \approx 1.5s

<pre>const int LIM = 1e8; bitset<LIM> isPrime; vector<int> primeSieve() { const int S = round(sqrt(LIM)), R = LIM / 2; vector<int> pr = {2}, sieve(S + 1); pr.reserve(int(LIM / log(LIM) * 1.1)); vector<pair<int, int>> cp; for (int i = 3; i <= S; i += 2) if (!sieve[i]) { cp.push_back({i, i * i / 2}); for (int j = i * i; j <= S; j += 2 * i) sieve[j] = 1; } for (int L = 1; L <= R; L += S) { array<bool, S> block{}; for (auto& [p, idx] : cp) for (int i = idx; i < S + L; idx = (i += p)) block[i - L] = 1; for (int i = 0; i < min(S, R - L); i++) if (!block[i]) pr.push_back((L + i) * 2 + 1); } for (int i : pr) isPrime[i] = 1; return pr; }</pre>	a1933d, 23 lines
---	------------------

Miscellaneous (6)

NDimensionalVector.h	3c0f61, 12 lines
<pre>template<int D, typename T> struct Vec : public vector<Vec<D - 1, T>> { static_assert(D >= 1, "Vector dimension must be greater than zero!"); template <typename... Args> Vec(int n = 0, Args... args) : vector<Vec<D - 1, T>>(n, Vec<D - 1, T>(args...)) {} }; template <typename T> struct Vec<1, T> : public vector<T> { Vec(int n = 0, const T& val = T()) : vector<T>(n, val) {} };</pre>	

Submasks.h	35424b, 3 lines
<pre>for (int mask = 0; mask < (1 << n); mask++) for (int sub = mask; sub; sub = (sub - 1) & mask) // do thing</pre>	

Strings (7)

ZValues.h	151ee3, 10 lines
<pre>vector<int> zValues(string& s) { int n = (int)s.length(); vector<int> z(n); for (int i = 1, l = 0, r = 0; i < n; ++i) { if (i <= r) z[i] = min(r - i + 1, z[i - l]); while (i + z[i] < n && s[z[i]] == s[i + z[i]]) ++z[i]; if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1; } return z; }</pre>	