

F1/10

Autonomous Racing

Scan Matching

Madhur Behl

CS 4501/SYS 4582
Spring 2018
Rice Hall 120

Localization and Mapping

Where am I ?

Scene Understanding

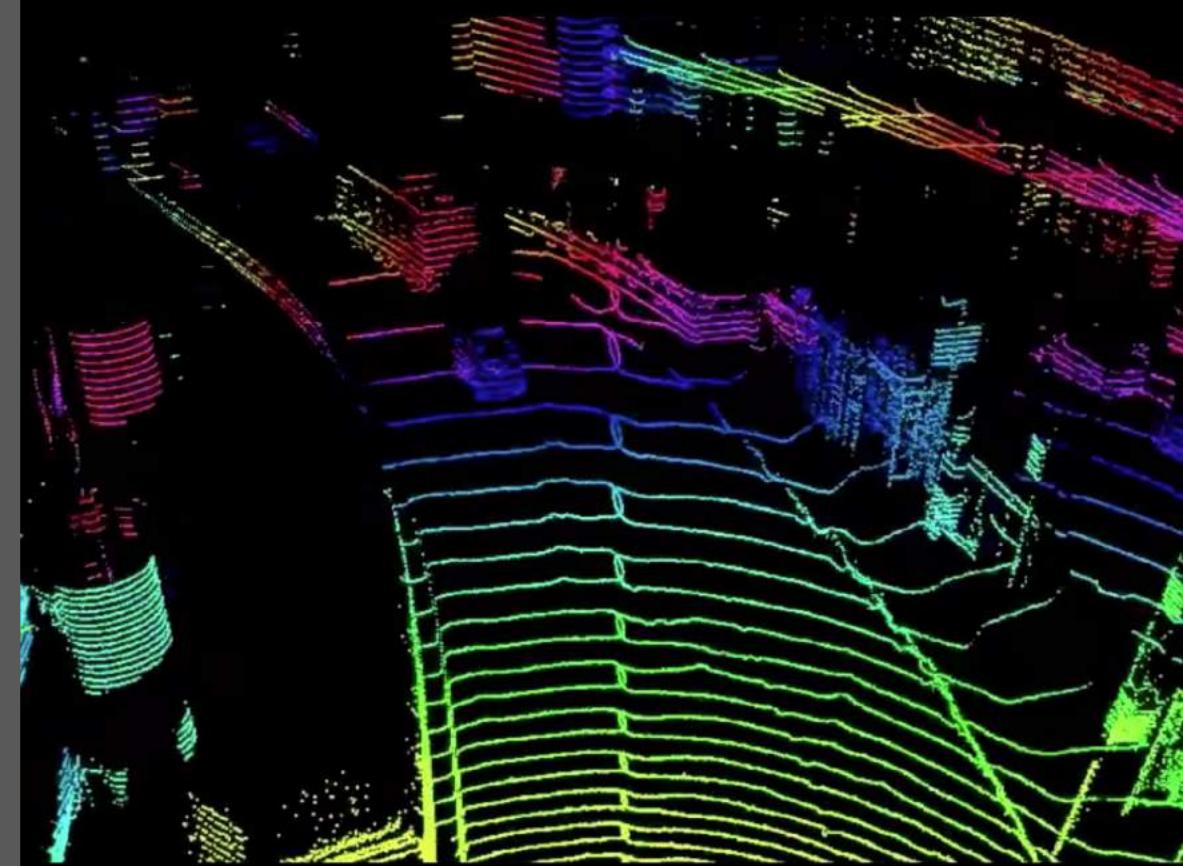
Where/who/what/why of everyone/everything else ?

Trajectory Planning and Control

Where should I go next ?
How do I steer and accelerate ?

Human Interaction

How do I convey my intent to the passenger and everyone else ?



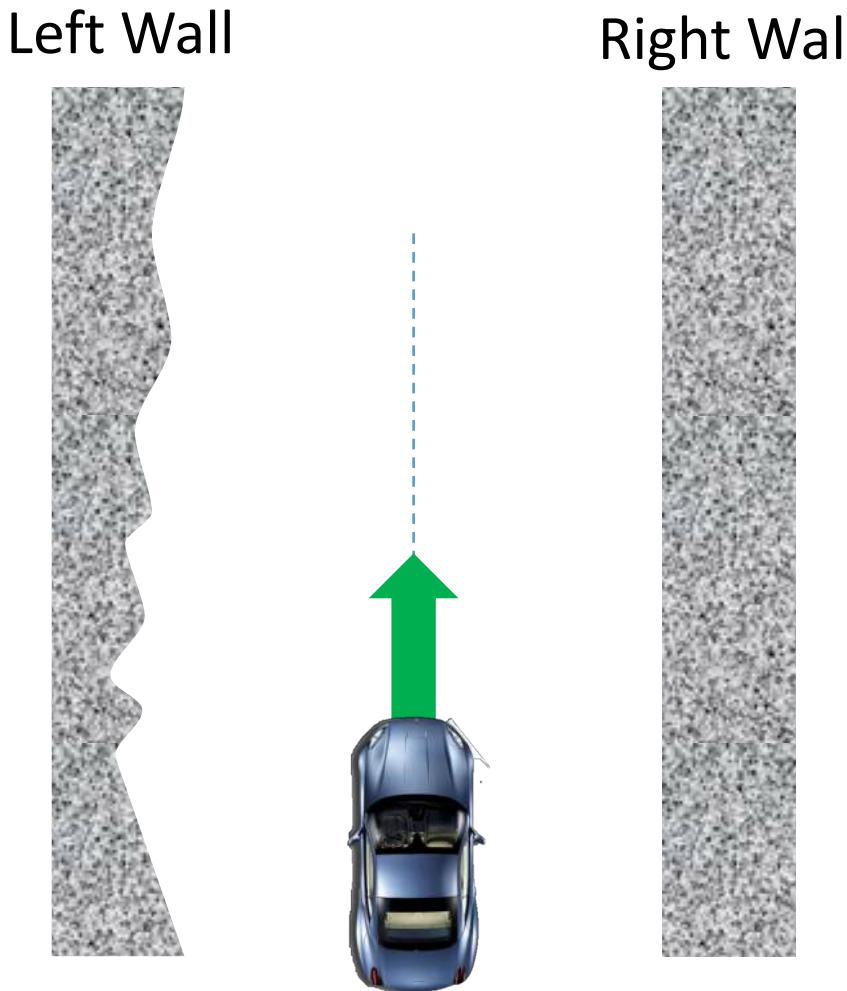
Scan Matching



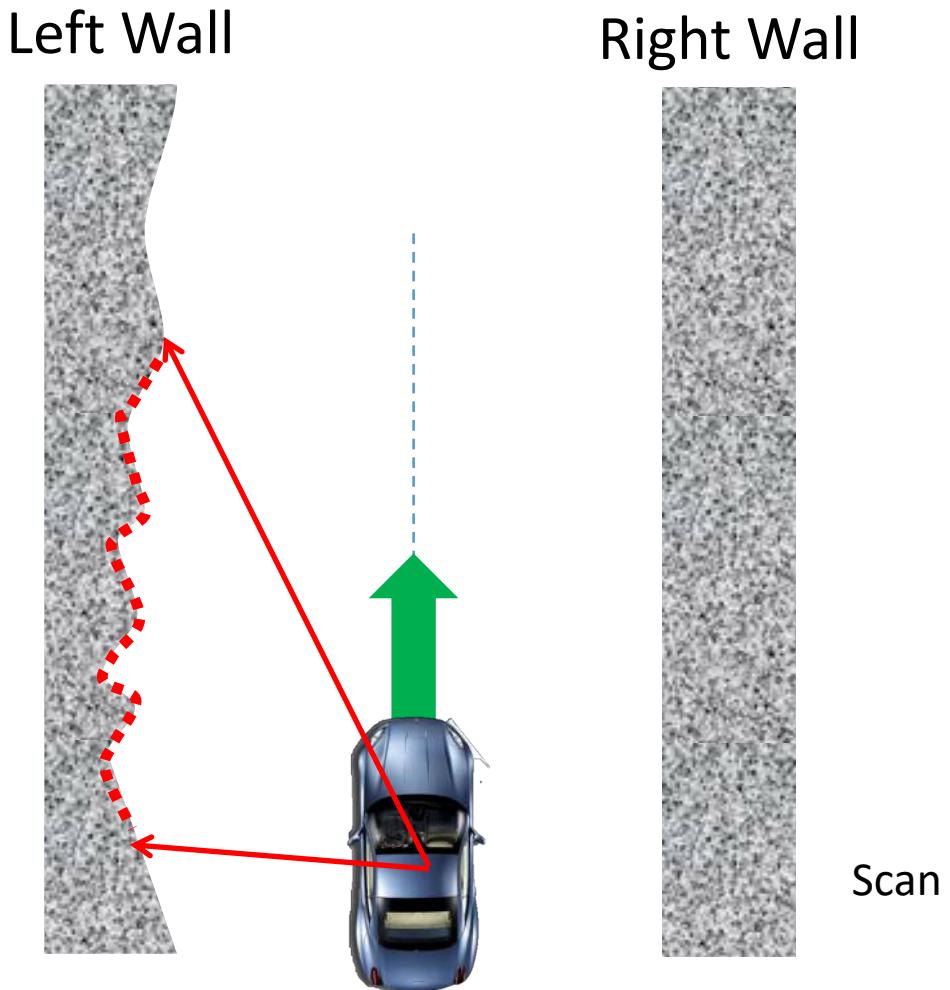
Odometry with LIDAR

- Odometry = Estimation of position (x, y, z) and attitude (θ, φ, ψ)
- In what follows, will use “position” as short for “position and attitude”

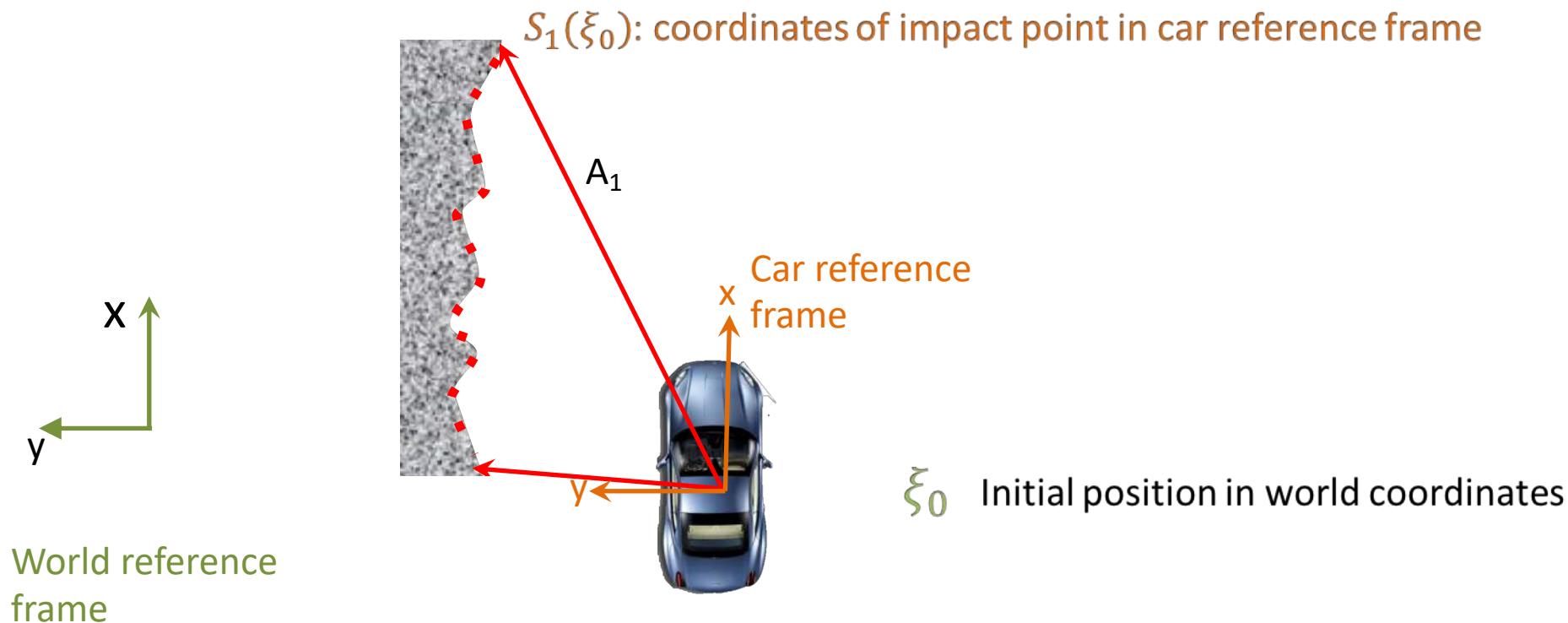
LIDAR for odometry: Scan matching



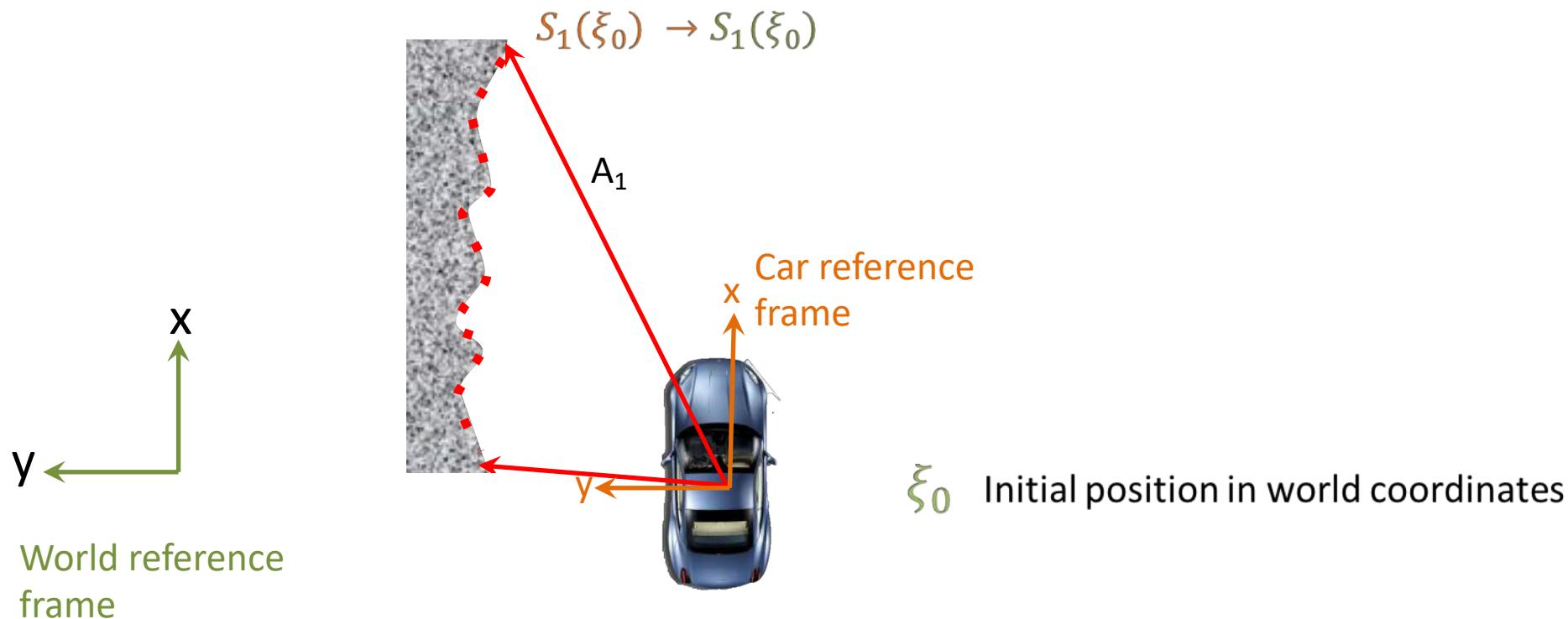
LIDAR for odometry: Scan matching

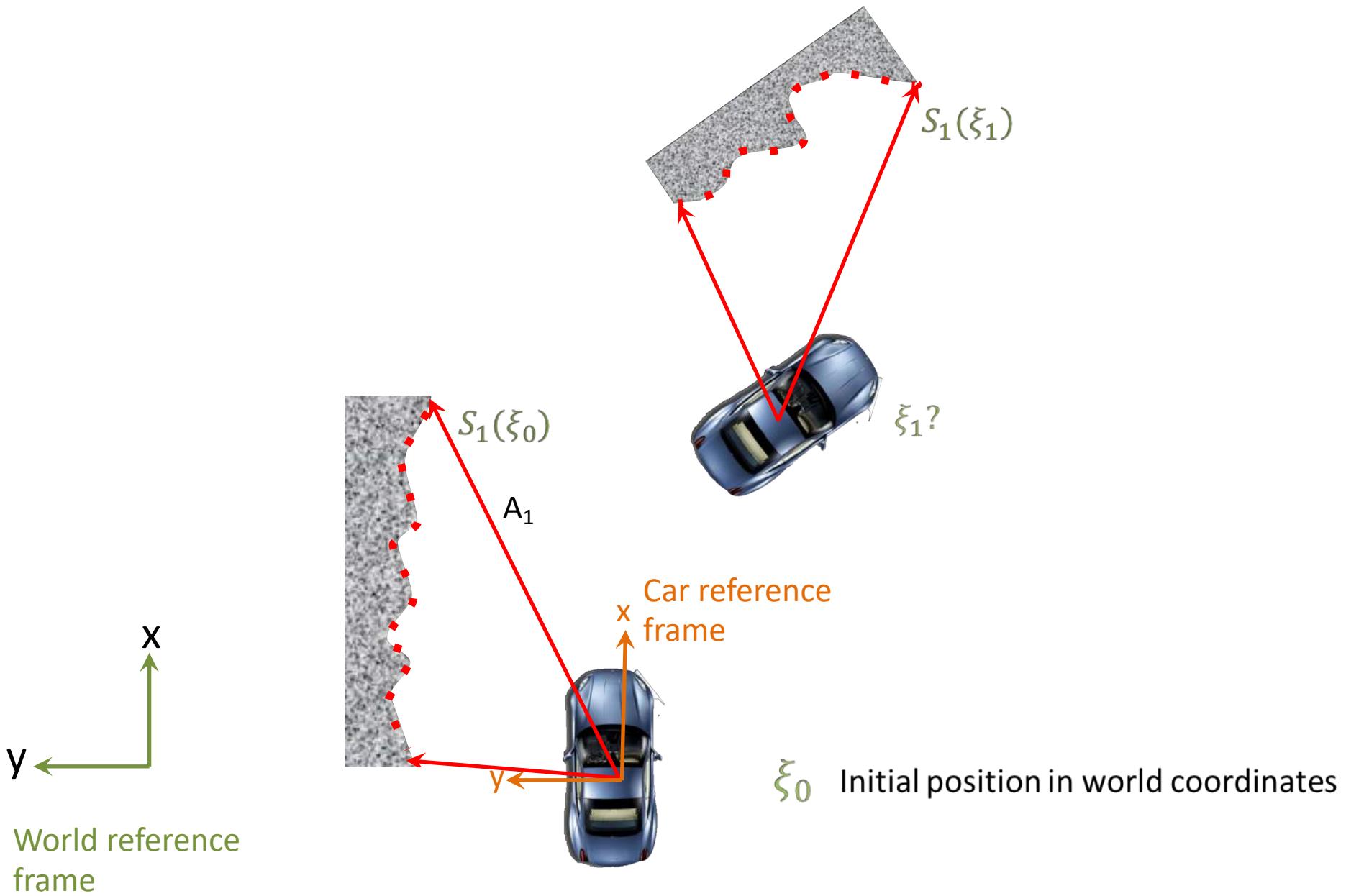


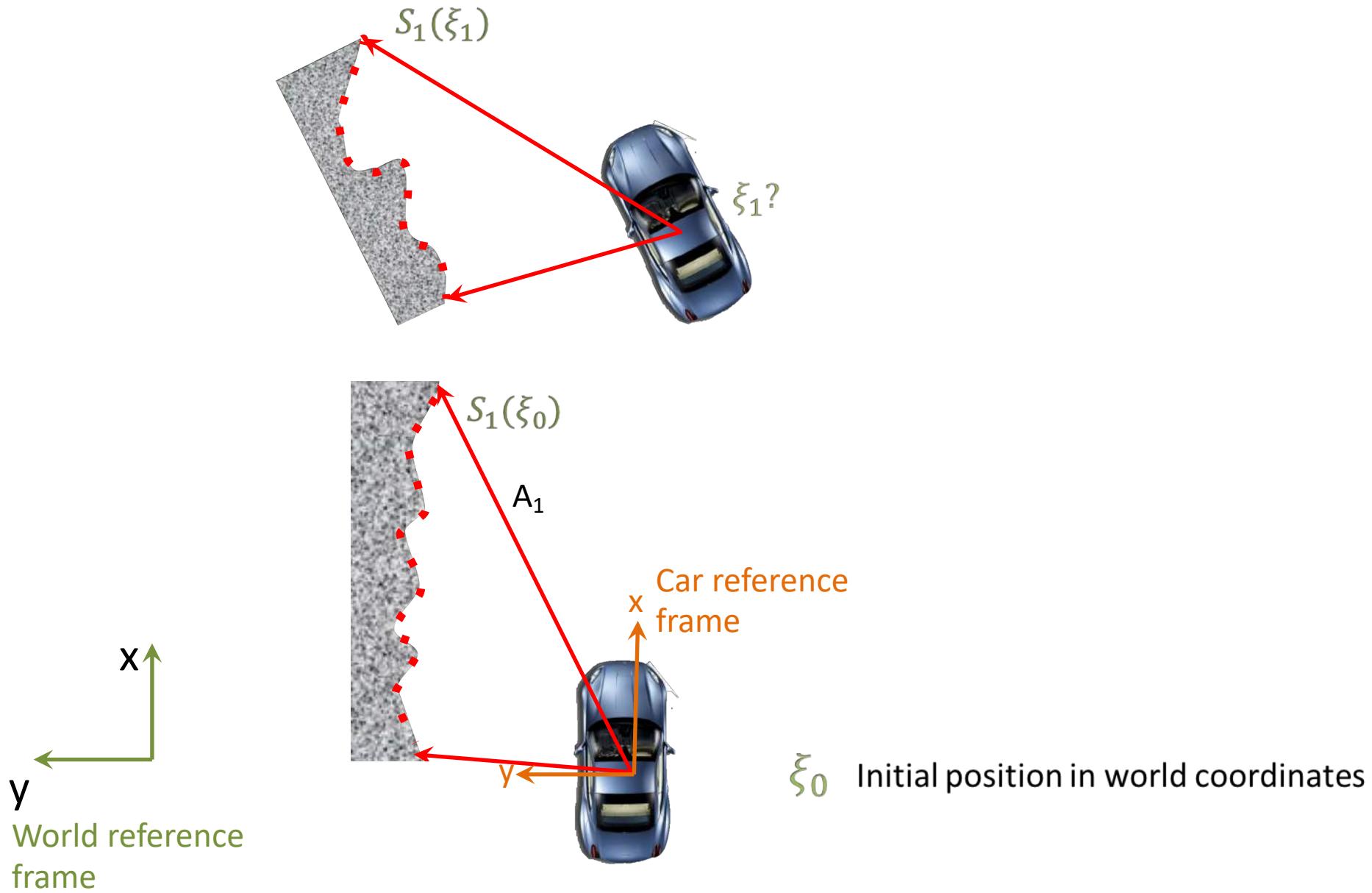
LIDAR for odometry: Scan 1

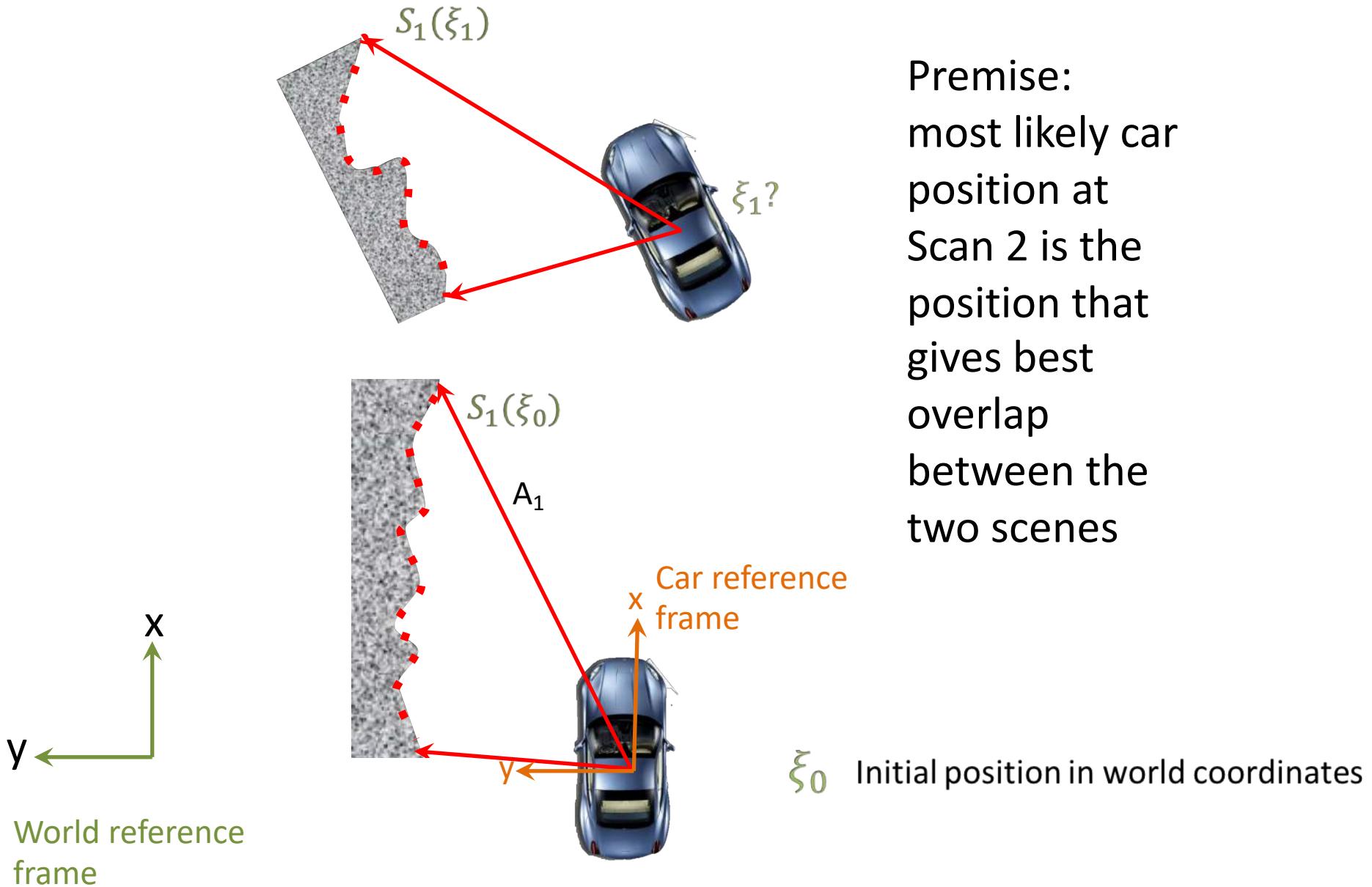


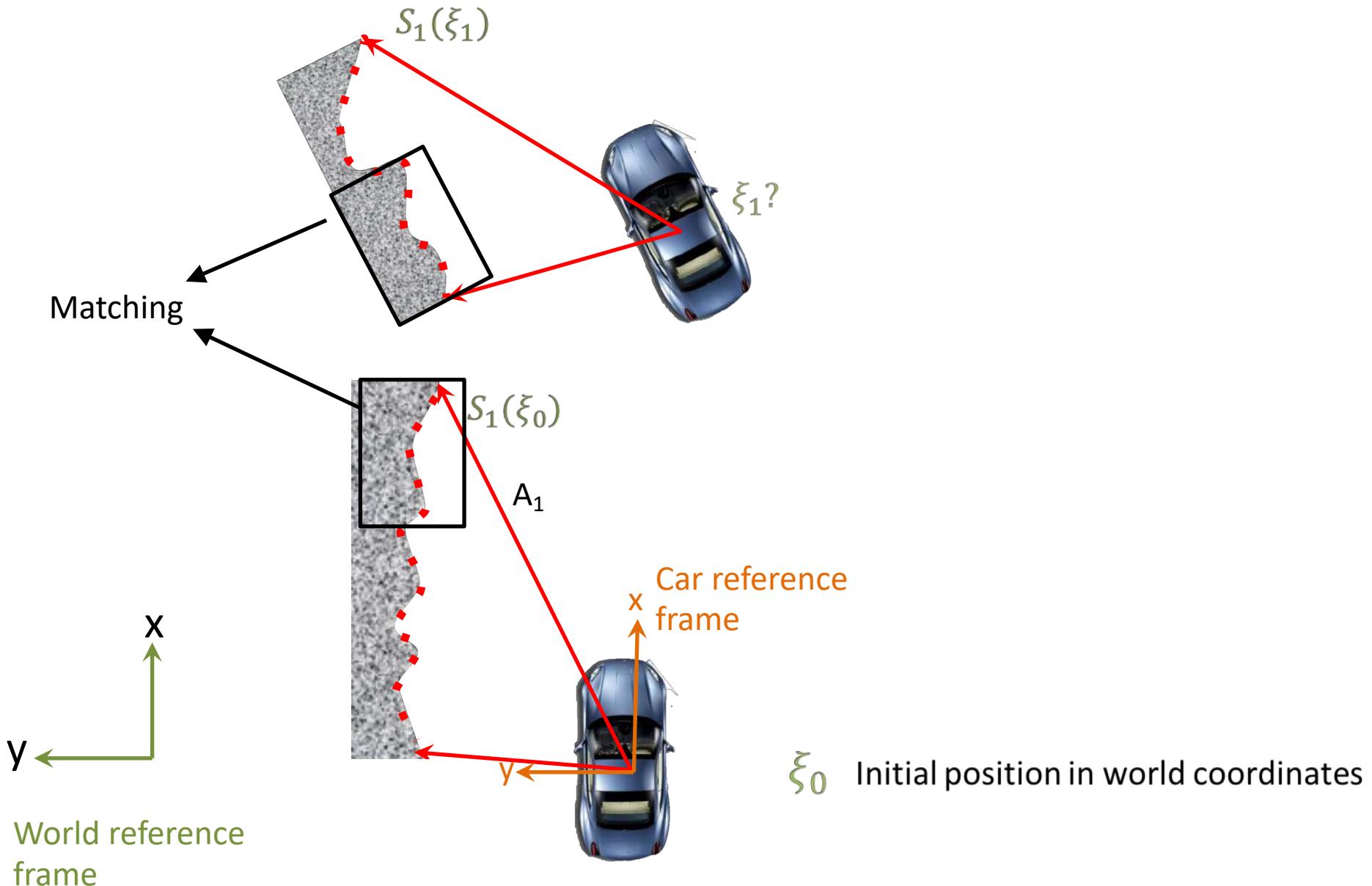
LIDAR for odometry: Scan 1

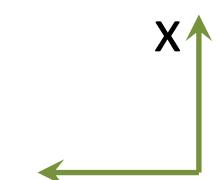


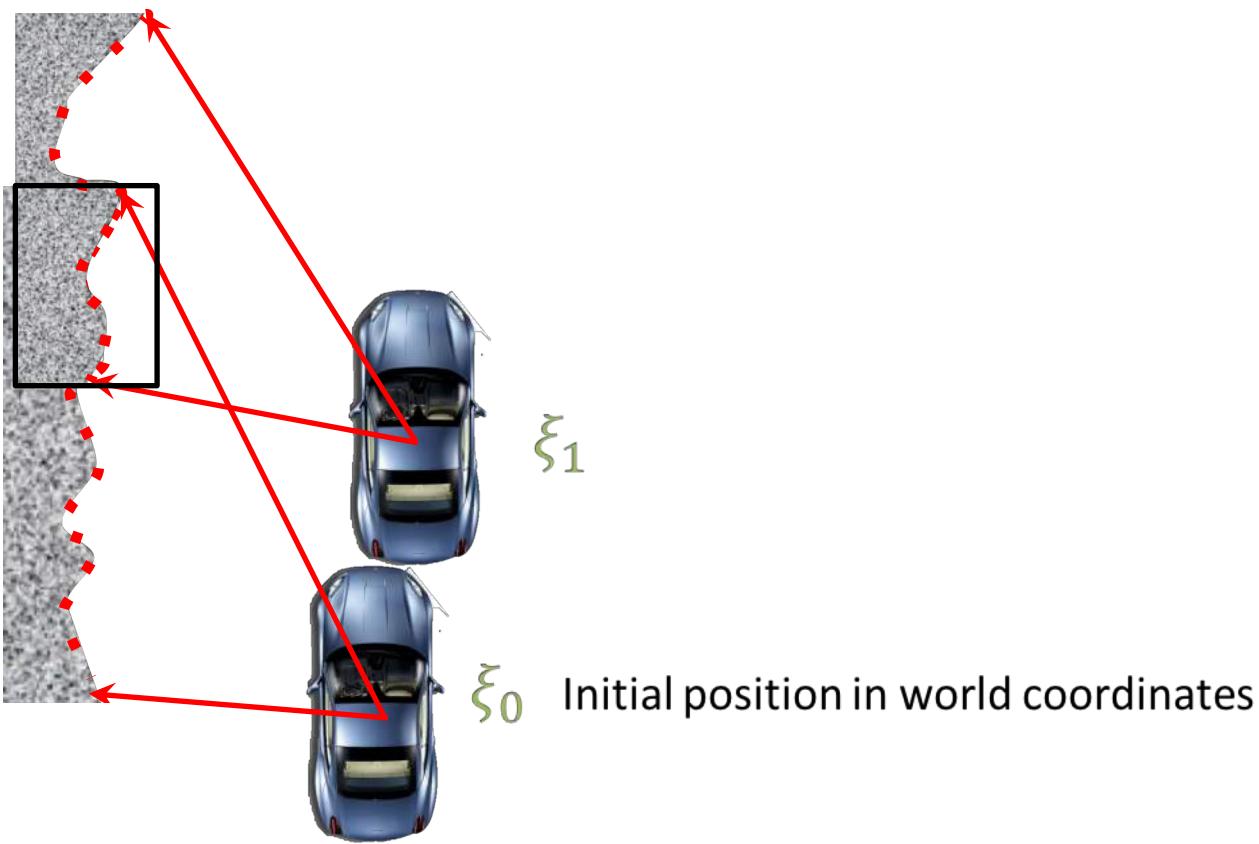




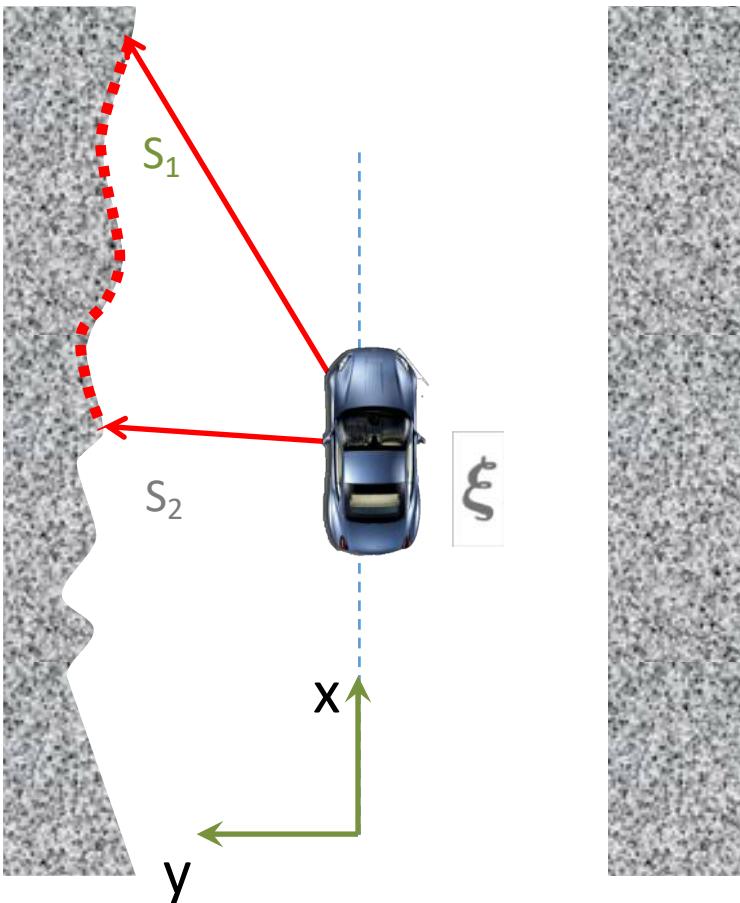




 World reference frame



Scan matching: optimization



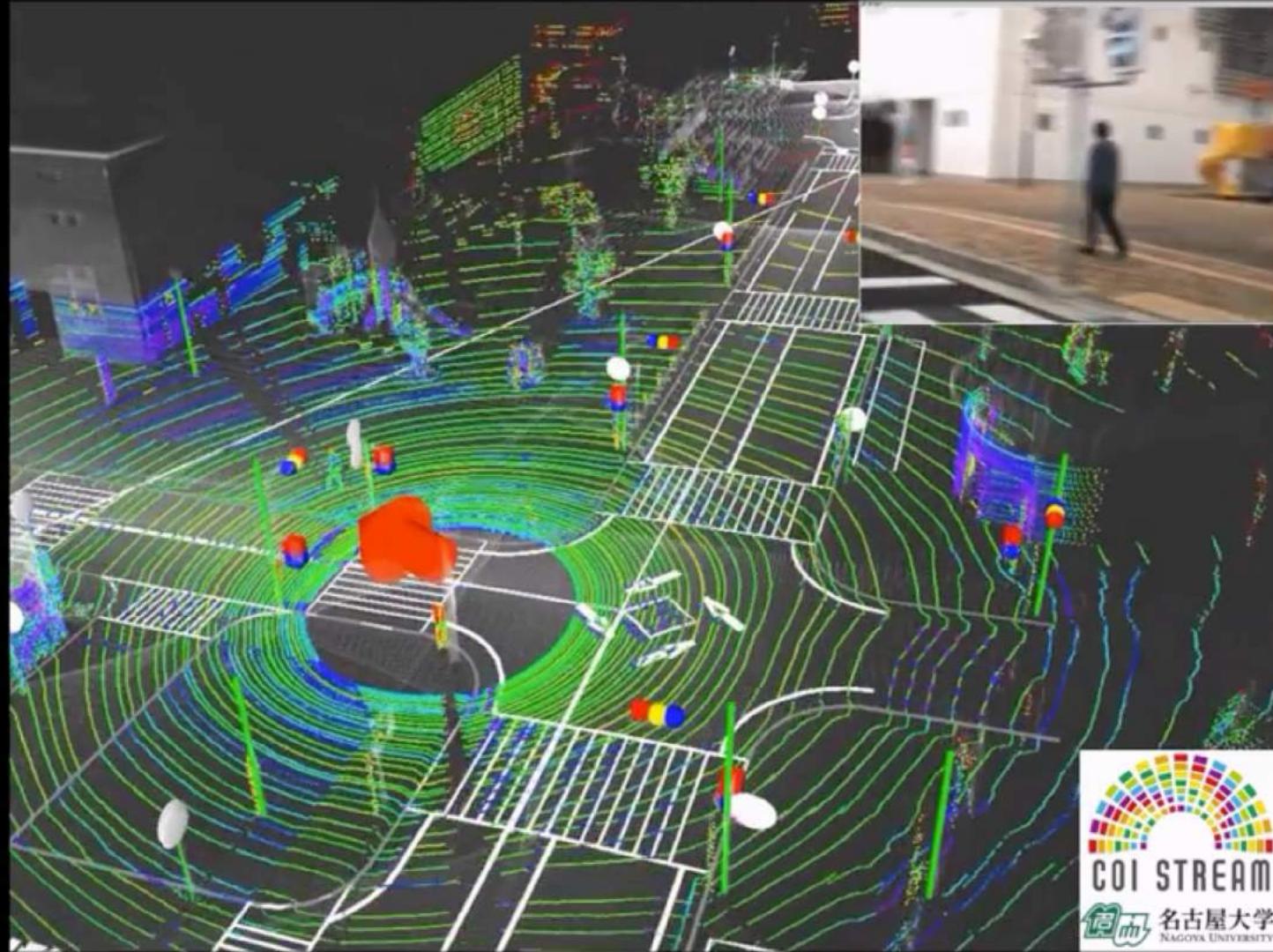
Impact coordinates of i^{th} step in world frame

Total of n steps ($n = 1084$)

$$\xi^* = \underset{\xi}{\operatorname{argmin}} \sum_{i=1}^n [1 - M(\mathbf{S}_i(\xi))]^2$$

Measure of match





Iterative Closest Point (ICP)

Algorithm



- Given: two corresponding point sets:

$$X = \{x_1, \dots, x_n\}$$

$$P = \{p_1, \dots, p_n\}$$

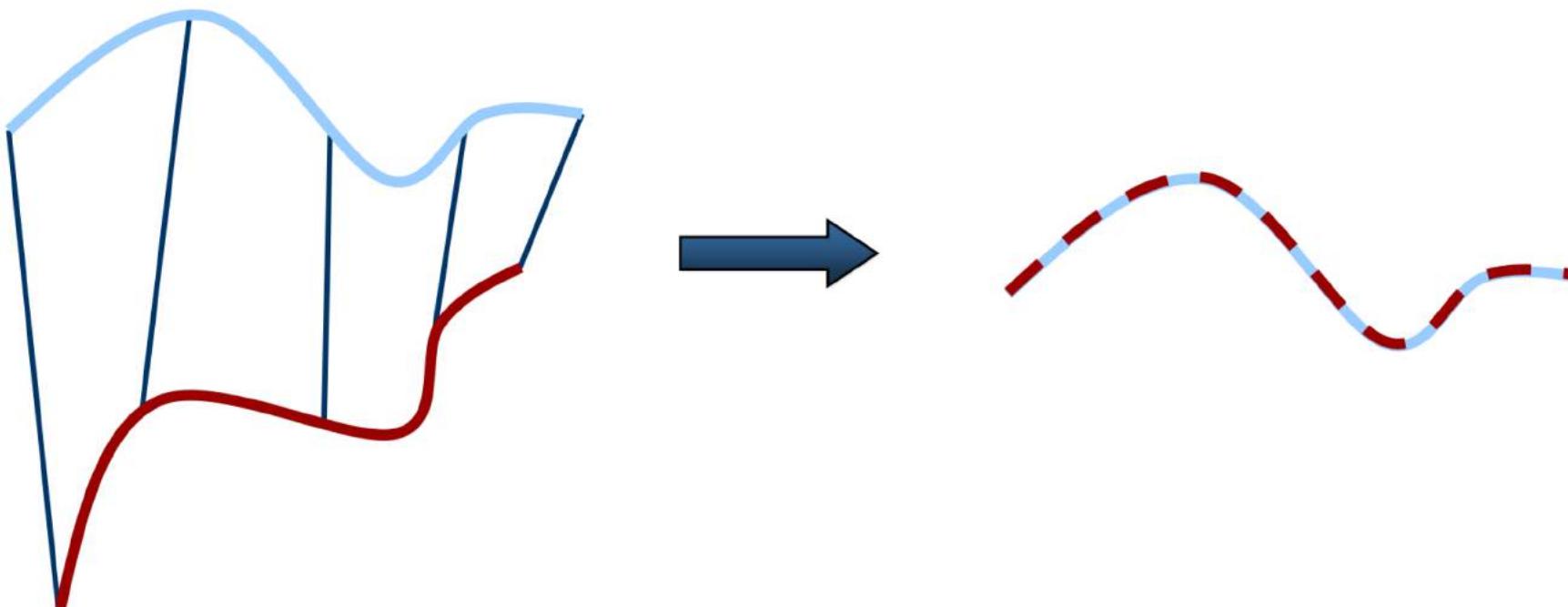
- Wanted: translation t and rotation R that minimizes the sum of the squared error:

$$E(R, t) = \frac{1}{N_p} \sum_{i=1}^{N_p} \|x_i - Rp_i - t\|^2$$

Where x_i and p_i are corresponding points.

Key Idea

- If the correct correspondences are known, the correct relative rotation/translation can be calculated in closed form.



Center of Mass

$$\mu_x = \frac{1}{N_x} \sum_{i=1}^{N_x} x_i \quad \text{and} \quad \mu_p = \frac{1}{N_p} \sum_{i=1}^{N_p} p_i$$

are the centers of mass of the two point sets.

Idea:

- Subtract the corresponding center of mass from every point in the two point sets before calculating the transformation.
- The resulting point sets are:

$$X' = \{x_i - \mu_x\} = \{x'_i\}$$

and

$$P' = \{p_i - \mu_p\} = \{p'_i\}$$

SVD

Let $W = \sum_{i=1}^{N_p} x'_i p_i'^T$

denote the singular value decomposition (SVD) of W by:

$$W = U \begin{bmatrix} \sigma_1 & 0 & 0 \\ 0 & \sigma_2 & 0 \\ 0 & 0 & \sigma_3 \end{bmatrix} V^T$$

where $U, V \in \mathbb{R}^{3 \times 3}$ are unitary, and
 $\sigma_1 \geq \sigma_2 \geq \sigma_3$ are the singular values of W.

SVD

Theorem (without proof):

If $\text{rank}(W) = 3$, the optimal solution of $E(R,t)$ is unique and is given by:

$$R = UV^T$$

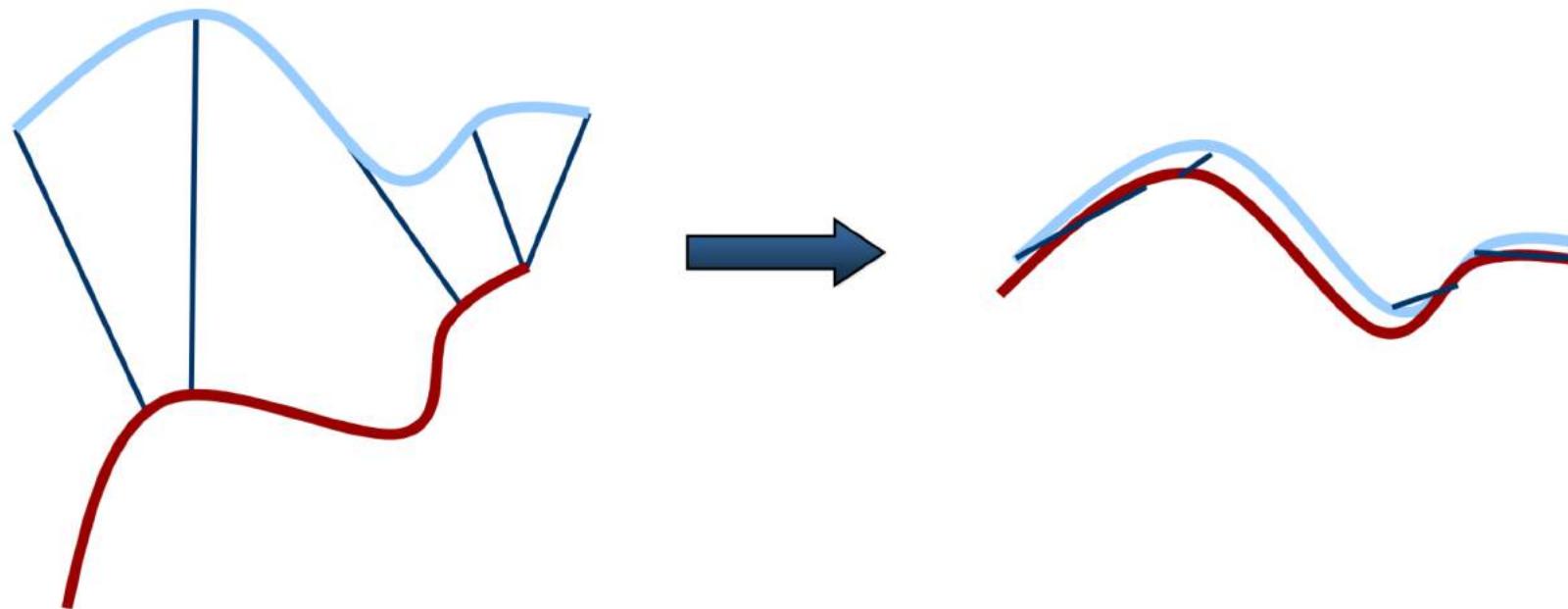
$$t = \mu_x - R\mu_p$$

The minimal value of error function at (R,t) is:

$$E(R, t) = \sum_{i=1}^{N_p} (||x'_i||^2 + ||y'_i||^2) - 2(\sigma_1 + \sigma_2 + \sigma_3)$$

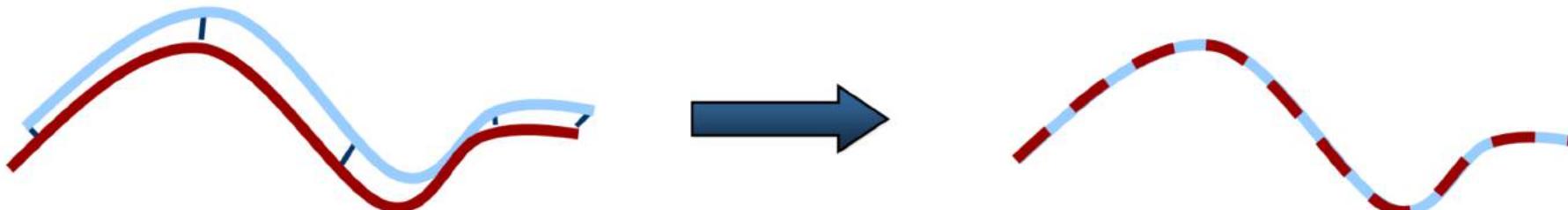
ICP with Unknown Data Association

- If correct correspondences are not known, it is generally impossible to determine the optimal relative rotation/translation in one step



ICP-Algorithm

- Idea: iterate to find alignment
- Iterated Closest Points (ICP)
[Besl & McKay 92]
- Converges if starting positions are
“close enough”



ICP-Variants

- Variants on the following stages of ICP have been proposed:
 1. Point subsets (from one or both point sets)
 2. Weighting the correspondences
 3. Data association
 4. Rejecting certain (outlier) point pairs

Performance of Variants

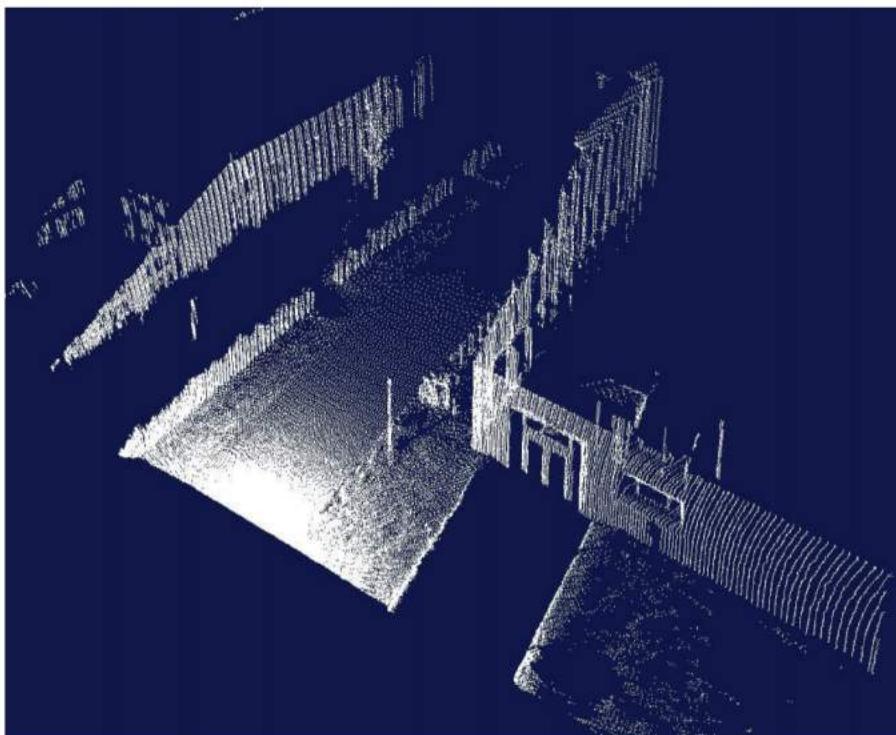
- Various aspects of performance:
 - Speed
 - Stability (local minima)
 - Tolerance wrt. noise and/or outliers
 - Basin of convergence
(maximum initial misalignment)
- Here: properties of these variants

Selecting Source Points

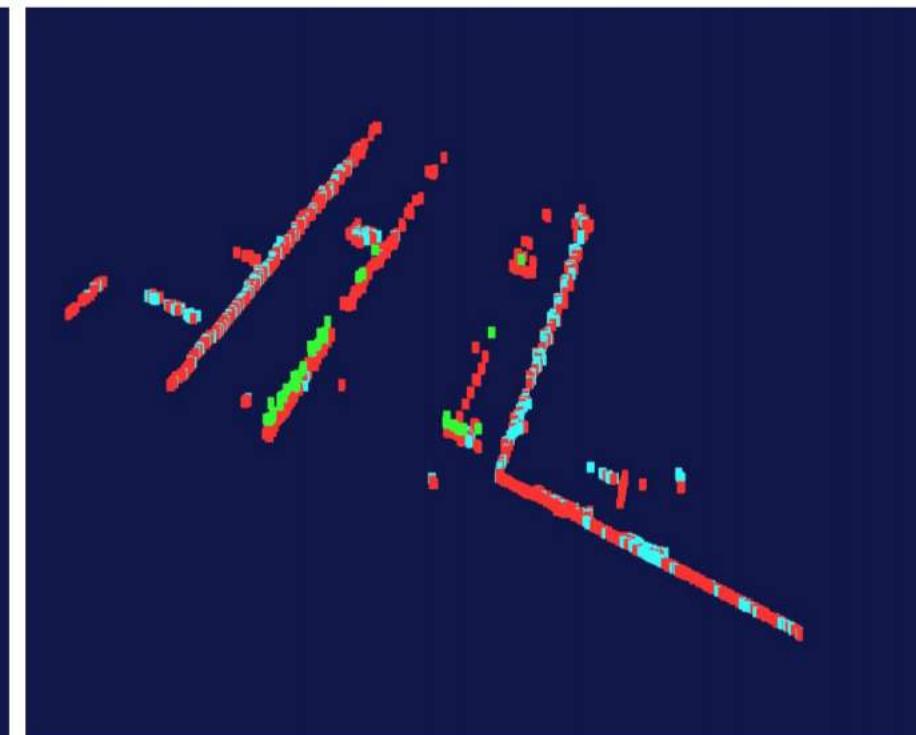
- Use all points
- Uniform sub-sampling
- Random sampling
- Feature based Sampling
- Normal-space sampling
 - Ensure that samples have normals distributed as uniformly as possible

Feature-Based Sampling

- try to find “important” points
- decrease the number of correspondences
- higher efficiency and higher accuracy
- requires preprocessing



3D Scan (~200.000 Points)



Extracted Features (~5.000 Points)

ICP Variants

1. Point subsets (from one or both point sets)
2. Weighting the correspondences
3. **Data association**
4. Rejecting certain (outlier) point pairs

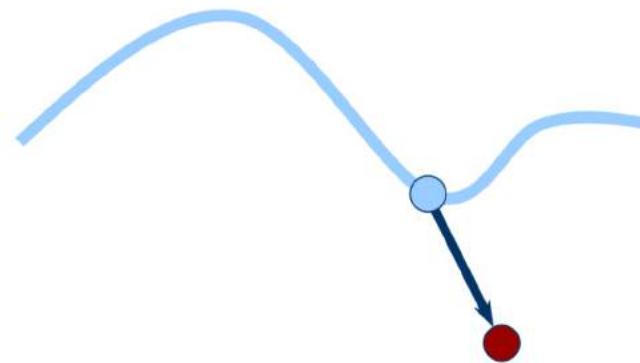


Data Association

- has greatest effect on convergence and speed
- Closest point
- Normal shooting
- Closest compatible point
- Projection
- Using kd-trees or oc-trees

Closest-Point Matching

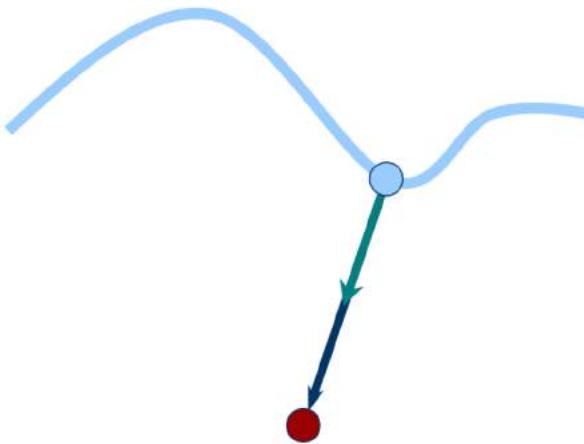
- Find closest point in other the point set



Closest-point matching generally stable,
but slow and requires preprocessing

Normal Shooting

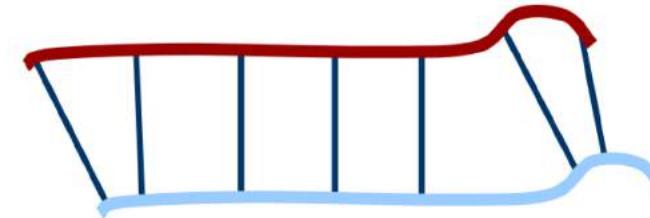
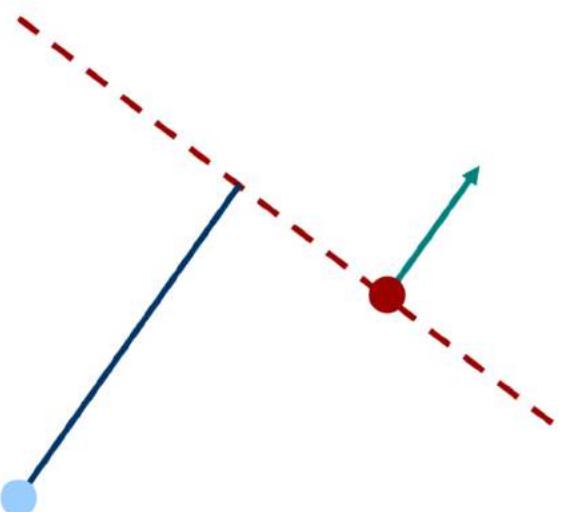
- Project along normal, intersect other point set



Slightly better than closest point for smooth structures, worse for noisy or complex structures

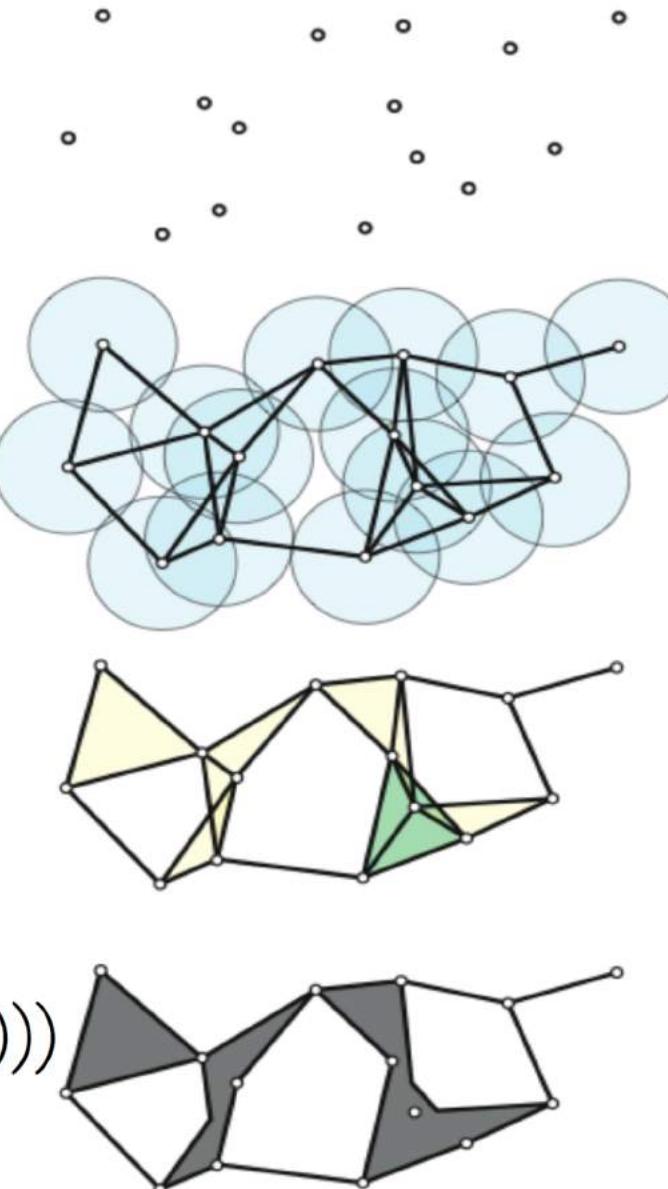
Point-to-Plane Error Metric

- Using point-to-plane distance instead of point-to-point lets flat regions slide along each other [Chen & Medioni 91]



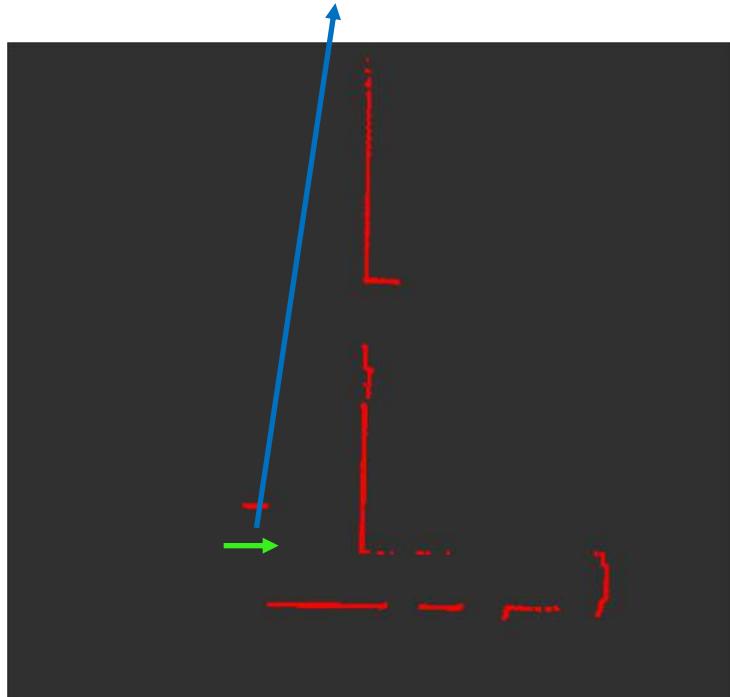
Data Types

- Point sets
- Line segment sets (polylines)
- Implicit curves : $f(x,y,z) = 0$
- Parametric curves : $(x(u),y(u),z(u))$
- Triangle sets (meshes)
- Implicit surfaces : $s(x,y,z) = 0$
- Parametric surfaces $(x(u,v),y(u,v),z(u,v))$

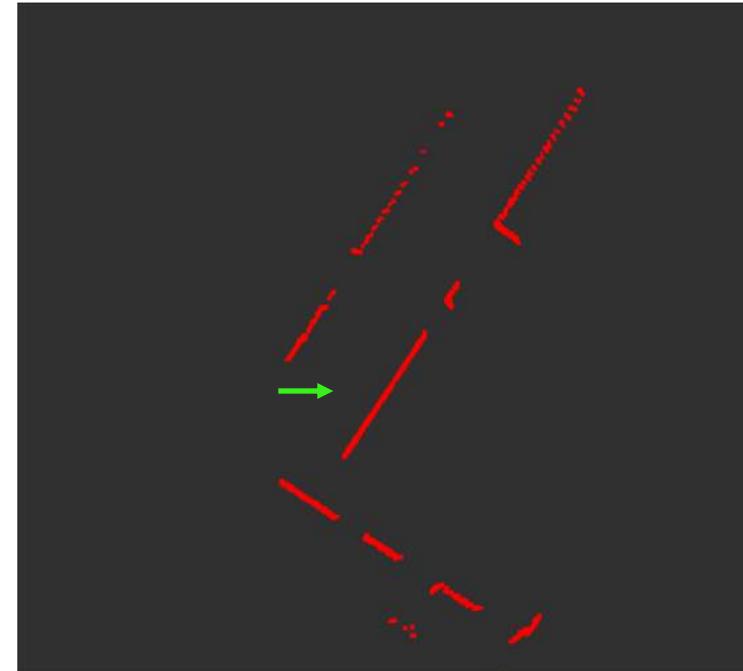


Scan Matching

Pose of the Car at $t = t_1$



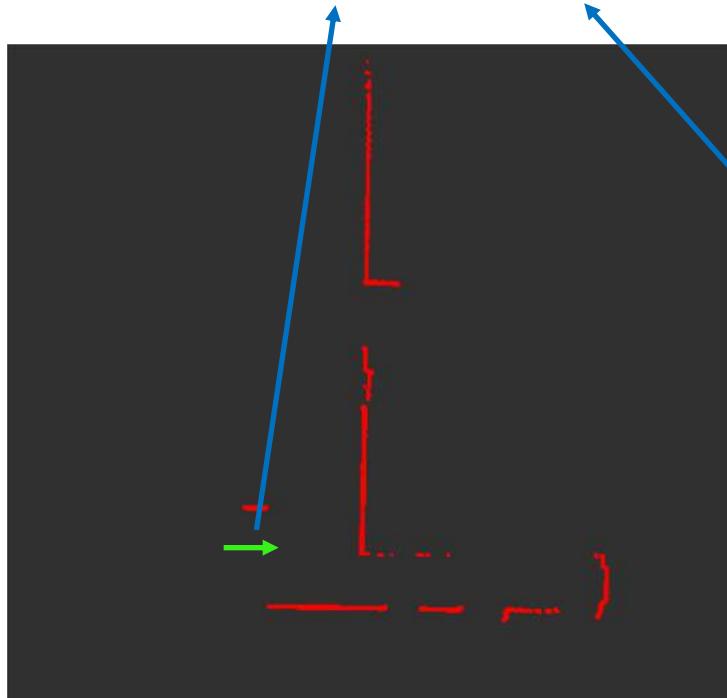
Laser Scans w.r.t car at Time $t = t_1$



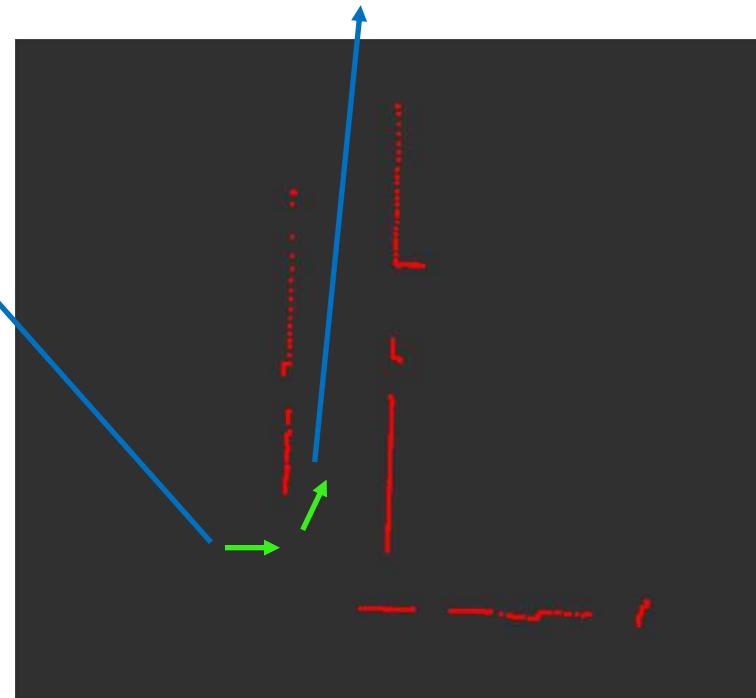
Laser Scans w.r.t car at Time $t = t_2$

Scan Matching

Pose of the Car at $t = t_1$



Pose of the Car at $t=t2$

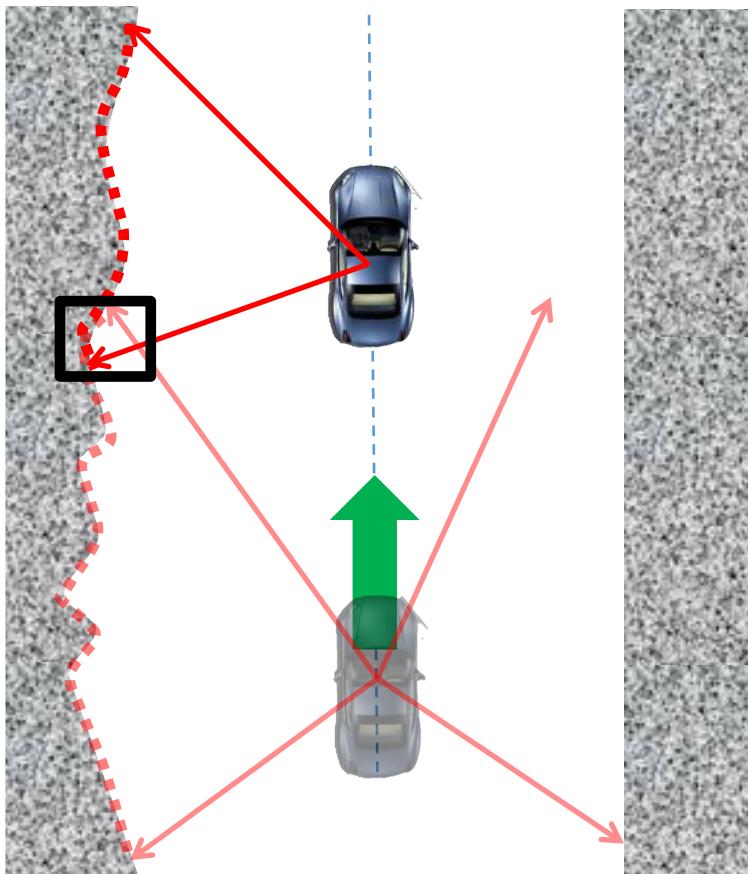


Laser Scans w.r.t car at Time $t = t_1$

Laser Scans w.r.t car at Time $t = t_2$

Scan matching: requirements

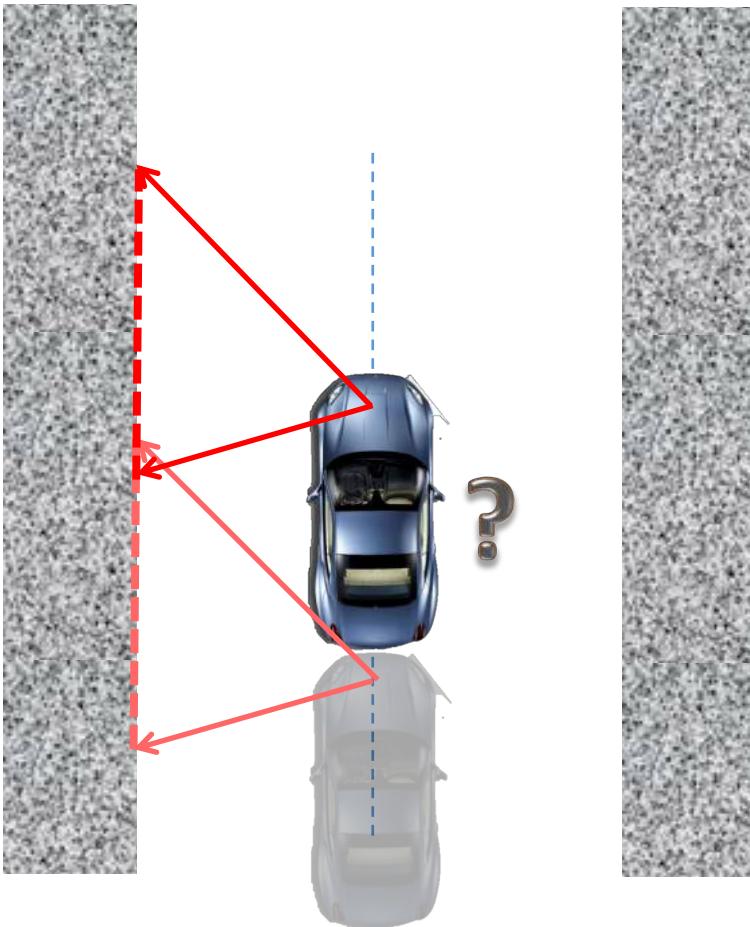
Left Wall



Right Wall

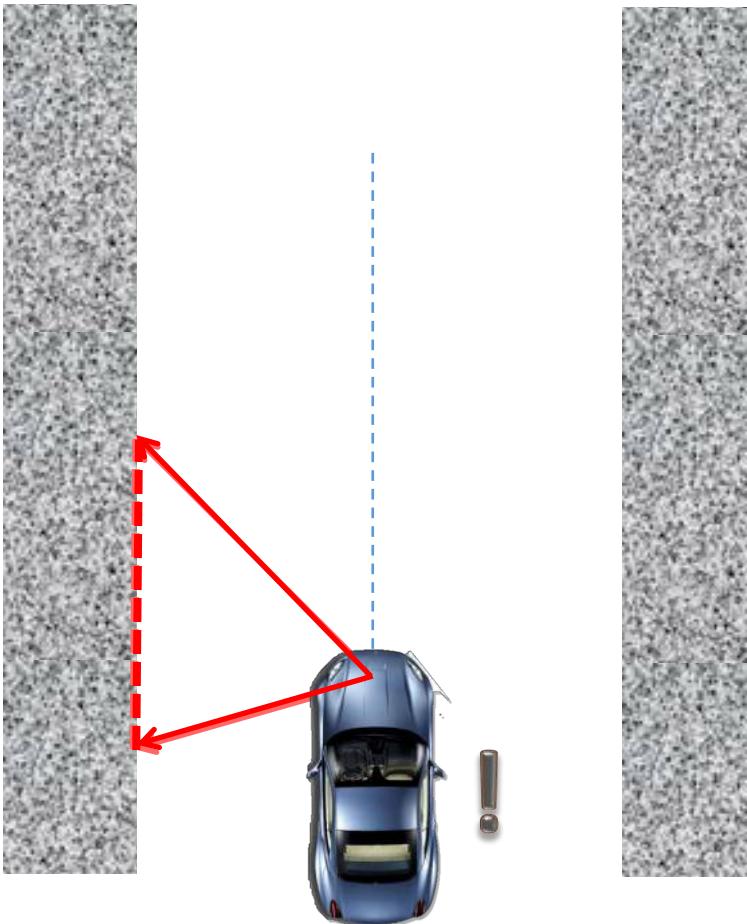
- Sufficiently fast scan rate
- A slow scan rate can lead to few matches between scans.
- Not really a risk for today's LIDARs

Scan matching : requirements



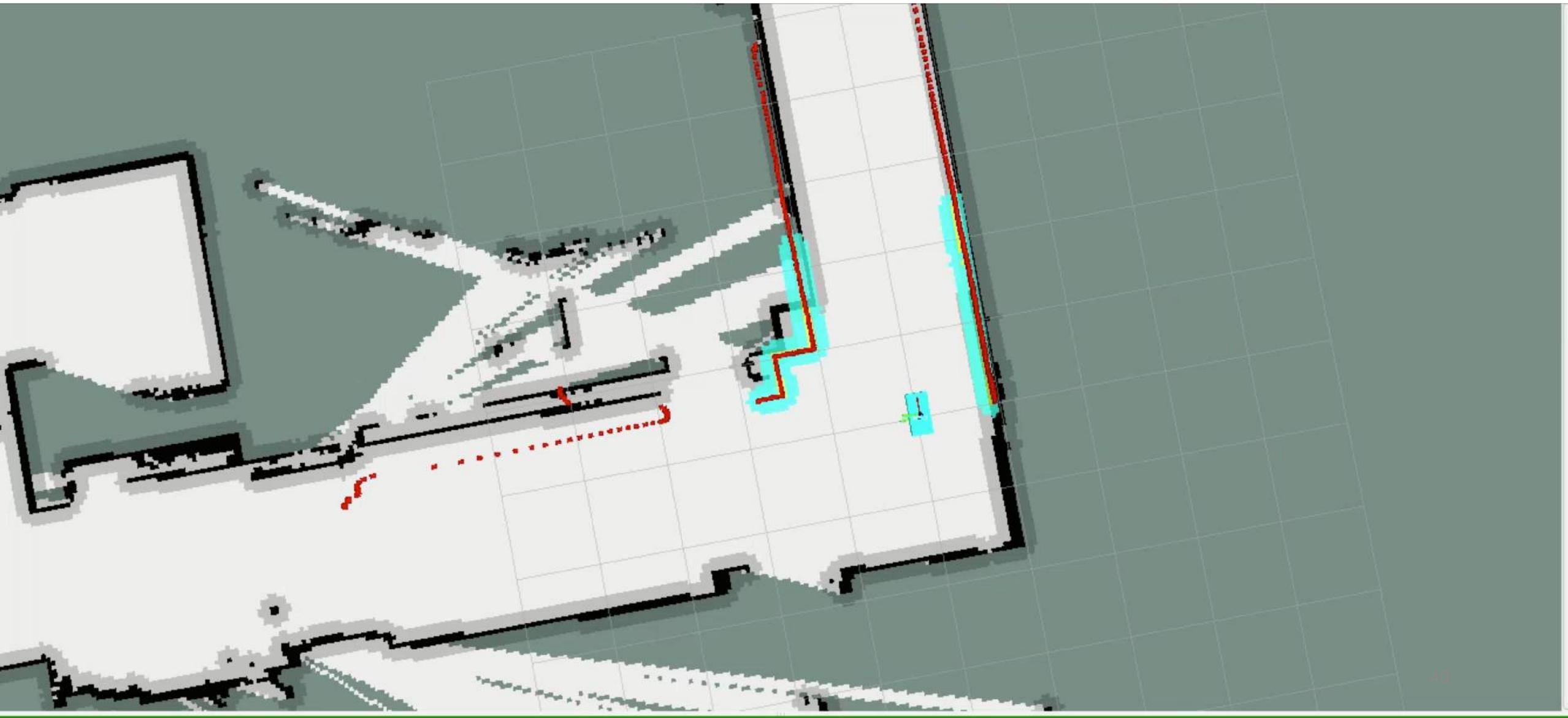
- Non-smooth, or heterogeneous, surfaces.
- Smooth surfaces all look the same to the matching algorithm.

Scan matching : requirements



- Non-smooth, or heterogeneous, surfaces.
- Best match between scans is if car did not move.

Failed scan matching



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Package Summary

✓ Released ✗ No API documentation

A ROS node to provide access to SCIP 2.0-compliant Hokuyo laser range finders (including 04LX).

- Maintainer status: maintained
- Maintainer: Chad Rockey <chadrockey AT gmail DOT com>
- Author: Brian P. Gerkey, Jeremy Leibs, Blaise Gassend
- License: LGPL

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Package Summary

[✓ Released](#)[✓ Continuous integration](#)[✓ Documented](#)

urg_node

- Maintainer status: maintained
- Maintainer: Tony Baltovski <tony.baltovski AT gmail DOT com>
- Author: Chad Rockey <chadrockey AT gmail DOT com>, Mike O'Driscoll <modriscoll AT clearpath DOT ai>
- License: BSD

Package Links

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Package Summary

 Released  Continuous integration  Documented

An incremental laser scan matcher, using Andrea Censi's Canonical Scan Matcher (CSM) implementation. See [the web site](#) for more about CSM. NOTE the CSM library is licensed under the GNU Lesser General Public License v3, whereas the rest of the code is released under the BSD license.

- Maintainer status: maintained
- Maintainer: Ivan Drvjanovski <cenvroboticslab@gmail.com>, Carlos <ciaramillo@ccn.univ.edu>, Isaac

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Package Summary

✓ Released ✓ Continuous integration ✓ Documented

Laser scan processing tools.

- Maintainer status: maintained
- Maintainer: Ivan Dryanovski <ccnyroboticslab AT gmail DOT com>, Carlos
ciaramillo AT cs.cuny DOT edu, Isaac LY Saito <iisaysaito AT opensource-robotics.tokyo DOT in>

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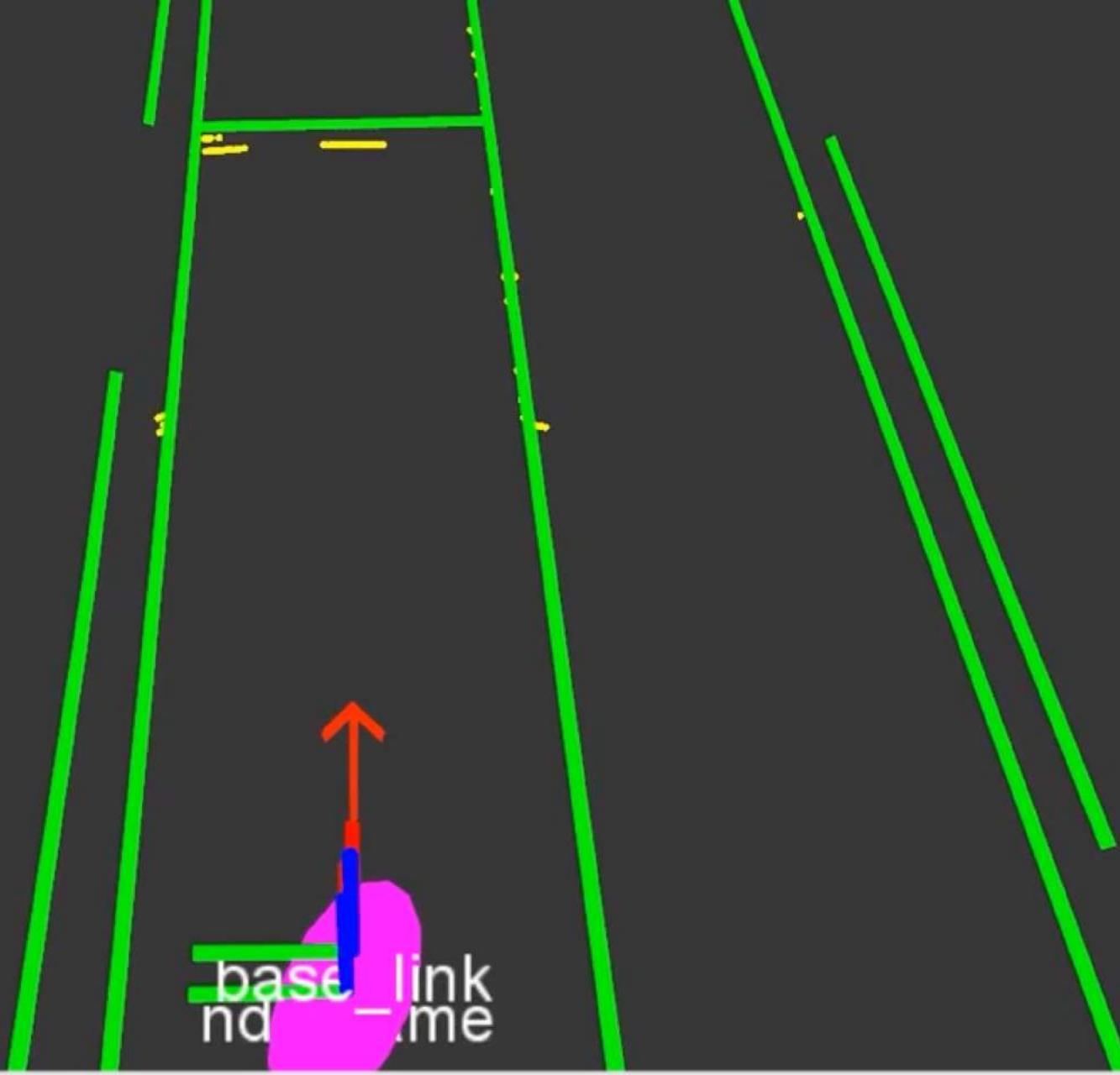
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NDT result is used as likelihood function in particle filtering algorithm.

Road marker matching is also used to improve localization accuracy.

Live Demo: /laserscan & Scan Matching