

Tutorial 1  
E. Khan (KIP RIKEN)  
- DL w. Bayesian Principles -

Tutorial 2  
Litkriver, Sutherland, Croton  
- Interpretable Comparison of  
Distributions and Models -

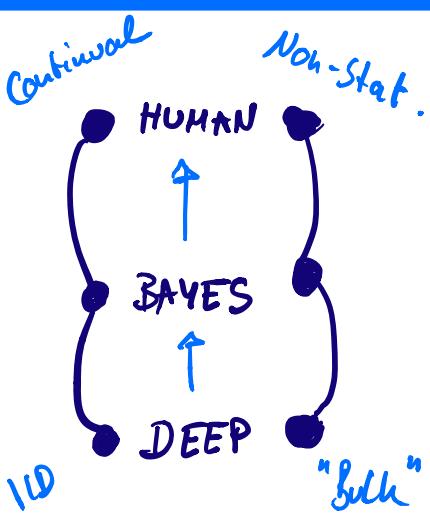
## NeurIPS 2019

- DAY 1 -

Tutorial 3  
K. Hoffmann (Microsoft)  
- RL: Past, Present, Future -

Keynote 1  
C. Kidwell (Berkeley)  
- How to Know -

# Entiyaz Khan (RIKEN) - DL with Bayesian Principles -



BAYESIAN PRINCIPLE  
 ↓  
 POSTERIOR APPROX.  
 ↓  
 \* SGD / Adam  
 \* Exact, Laplace, VI  
 ⇒ BRING TOGETHER!

	DL	BL
COMPLEX DATA/TIME	✓	✗
SCALABLE	✓	✗
UNCERT.	✗	✓
INCREM.	✗	✓

## DEEP LEARNING

- START: Emp. Risk Min/Max. Lth  
 $\min_{\Theta} \ell(D; \Theta)$ , PRE-COND.
- SGD:  $\Theta \leftarrow \Theta - \rho H^{-1} \nabla_{\Theta} \ell$   
 ↳ Point Estimate ⇒ Local

## BAYESIAN LEARNING

- Prior:  $\Theta \sim p(\Theta)$
- Score:  $p(D|\Theta)$  (via Lth)
- $p(\Theta|D) = \frac{p(\Theta) p(D|\Theta)}{\int p(D|\Theta) p(\Theta) d\Theta}$
- ↳ Weights ⇒ Global

### COMPLEXITIES OF POSTERIOR APPROX.

#### ① SGD ( $H=I$ )

⇒ Gaussian w.  
fixed Covariance



#### ② Newton

⇒ Multivariate Gaussian



#### ③ Ensemble

⇒ Gaussian Mixture



### I CHOOSE POSTERIOR APPROX.

$$q(\Theta) \propto \exp(-\frac{1}{2} \Theta^T T(\Theta)) \quad \text{w. } \mu = \mathbb{E}_q[\Theta]$$

Exp. Family      Natural Param.      Sufficient Stat.      Exp. Param.

$$\min_{\Theta} \mathbb{E}_{q(\Theta)} [\ell(\Theta)] - \text{KL}(q)$$

BAYES. L.  
RULE:

GENTROPY: PREVENT  
COLLAPSE

$$\lambda \leftarrow \lambda - \rho \nabla_{\lambda} [\mathbb{E}_q [\ell(\Theta)] - \text{KL}(q)]$$

### II LET GLOBALITY GO TWISTY

⇒ Khan et al. 18' - ICML

- RMS prop  $\Rightarrow$  can be derived using Multivariate Gaussian w. diag.  $\Sigma$

$$\text{BAYES} = \text{OPTIM: } \hat{\theta}(\Theta|D) = \arg \min_{\theta \in \mathcal{P}} \mathbb{E}_{q(\theta)} [\ell(\theta)] - H(q)$$

all approx.  $-\log \frac{p(D|\theta)}{p(\theta)}$  entropy

$\hookrightarrow$  View HMM, Kalman Filter, etc. from exact same perspective

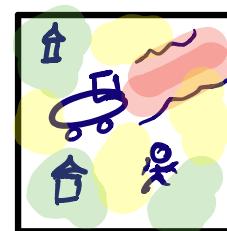
$\Rightarrow$  Gradient update gives correct approximation!  $\rightarrow$  PRINCIPLE  $\rightarrow$  VI ONLY!

## I BUILDING BETTER DL MODELS: UNCERTAINTY ESTIMATION

### A SGD-based

- MC Dropout - Gal & Ghahramani '16'
- SWAG - Maddox et al. '19'
- Laplace - Ritter et al. '18'

$\Rightarrow$  PROBLEM: NOT FLEXIBLE!



### B VI Methods

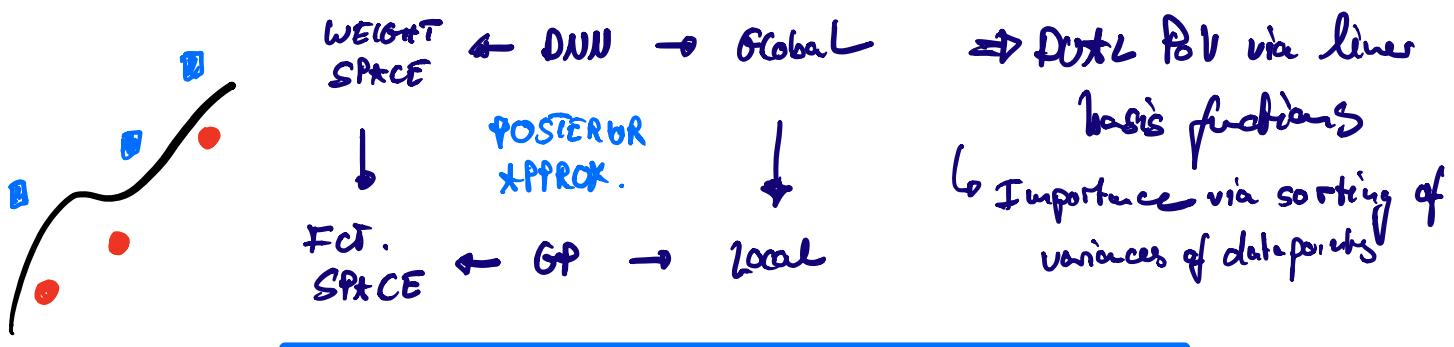
- Flexible  $q$  distr.
- Graves '11'

$\Rightarrow$  PROBLEM: HARD TO SCALE!

$\hookrightarrow$  VOGN: Osawa et al. '19' (NeurIPS)  $\Rightarrow$  Variational Online Gauss-Newton  
 \* Adam-like optimizer: Sampling around solution space to estimate uncertainty

$\hookrightarrow$  Challenge: Non-convexity  $\rightarrow$  local approx.  $\Rightarrow$  Only local uncertainty

## II BUILDING BETTER DL MODELS: PTTI IMPORTANCE



## III BUILDING BETTER DL MODELS: LIFEZONG LEARNING ( $\rightarrow$ active DL)

Continual learning

$\rightarrow$  Regularization-based (EWC, SI, VCL)

- Classification: Past classes not visited

$\hookrightarrow$  BROKEN PRINCIPLE: BETTER APPROX.  $\neq$  BETTER RESULTS  
 $\hookrightarrow$  VOGN can fix problem!

# Jitkrittum, Sutherland & Gretton

## - Interpretable Comparison of Distributions & Models -

Scenarios / Distr.	P	Q
I	Samples	Samples
II	Model	Samples
⇒ Example: GANs		

### OUTLINE

- Divergence measures
  - Integral probability metrics
  - Φ-divergence (f-divergence)
- Statistical hypothesis testing
  - Using integral probability metrics
  - Learned features for powerful tests
  - Rejection of testing and classification
- Linear-time features and model criticism
  - Interpretable, linear-time features for testing
  - Stein's method for model evaluation

### (I) DIVERGENCE METRICS

(A)  $D_{\phi}(P, Q)$

↓ Difference

↓ Integral Prob. Metrics

↓ Total variation

(B)  $\frac{P}{Q}$

↓ Ratio

↓ Φ-divergences

#### (A) I Max. Mean Discrepancies (MMD)

$$\sup_{\|f\| \leq 1} |E_P f(X) - E_Q f(Y)|$$

↳ RKHS: Smoothness / Fct. lies in features

↳ Different witness functions ⇒ Metrics

↳ MMD: Infinite many features ⇒ Kernel Trick

$$f^* \propto \mu_p - \mu_q$$

#### (B) II Wasserstein-1 Distance

$$\sup_{\|f\|_L \leq 1} |E_P f(X) - E_Q f(Y)|$$

→ Quality of teacher signal depends on choice of kernel!

⇒ COMPARISON: What to use? WTE over!

↳ IPM more stable in terms of hyperparameter robustness

⇒ RIGHT SMOOTHING OF RATIO IS REQUIRED

### (II) STATISTICAL HYPOTHESIS TESTING (Two Sample)

→ Example: CIFAR-10 vs. CIFAR-10.1 ⇒ Are P & Q equal?  
 problem: (P) (Q)

- Practice: Compute kernel matrix and sample average of  $\hat{MMD}^2$
- ↳  $P \neq Q$ : asymptotic normal
  - ↳  $P = Q$ :  $\chi^2$  distribution matrix  
→ depends on kernel
- Hypothesis Test Construction  
Choose  $C_\alpha \rightarrow$  false rejection rate

- ⇒ How to get  $C_\alpha$ ? → Permutation Testing ⇒ Mix Data Randomly!
- ⇒ How to choose kernel? → Exp. Quadratic ⇒ "Characteristic" for all  $\alpha$   
Only asymptotic ⇒ finite case:  $\alpha$  usually ↗  
↳ power  $\rightarrow 1$  as  $n \rightarrow \infty$
- ↳ Choose a meaningful representation?  $\Phi: X \rightarrow \mathbb{R}^d$   
 $\vec{\Phi}$ : Prediction from Classifier //  $\Phi$ : Hidden Layer Features (feature embedding)

- "Best Test": Data Adaptation of Kernel ⇒ Goal: Highest Power!

↳  $\max_k \frac{MMD^2(P, Q)}{\sigma_{MMD}(P, Q)}$  ⇒ Trade-Off Large MMD with confidence!  
↳ Differentiable! ⇒ AutoDiff Custom Loss Def.

learn kernel! → "Deep Kernel"

↳ Kernel as Classifier:  $k_f(x, y) = \frac{1}{4} \mathbf{1}(f(x) > 0) \mathbf{1}(f(y) > 0)$   
⇒  $MMD(P, Q) = 1 - \frac{1}{2}$

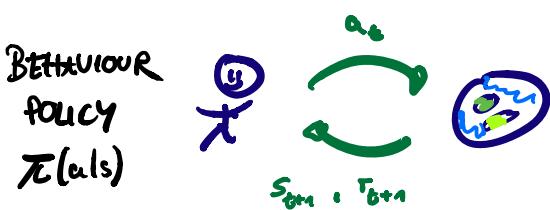
- Interpretability ⇒ learned kernel + Large Witness fat. Vectors

### III LINEAR-TIME FEATURES & MODEL CRITICISM

- Test location  $V: \sum_j v_j z_j^3$  optimisation for witness function
- ↳ Problem: tensile quadratic time
- ↳ Normalized Mean Euclidean (NME)
- ↳ Unnormalized Mean Euclidean (UME)
- Optimisation ⇒ where does GAN model do well? → witness function
- Explicit model  $P$  with Stein Discrepancy ⇒ 'Goodness-of-fit' Test
- density ↳  $\sup_{\|f\|_F \leq 1} [E_f[T_P f] - E_{P \mid T_P} f]$  Stein Operator:  
but no super! ↳ Kernel Stein Discrepancy (KSD)  
 $[T_P f]_I(x) = \frac{1}{p(x)} \frac{df}{dx} (f(x)p(x))$   
↳ derive Stein Witness Function

# Katja Hofmann (HSR) - Reinforcement Learning: Past, Present & Future Perspectives

**RL = SEQUENTIAL DECISION MAKING UNDER UNCERTAINTY**



**ORIGINS - MARKOV DECISION PROCESS**  
→ Bellman (1953, 1954)

$T(s_t, a_t)$        $\Rightarrow$  Many decision choices  
DYNAMICS       $\hookrightarrow$  State/action representation  
 $R(r_t, s_t, a_t)$        $\Rightarrow$  Extensions: POMDPs / SMDPs  
REWARDS

## OPTIMALITY

Finite Horizon	Infinite Horizon	Average Reward
$\mathbb{E}\left[\sum_{t=0}^n r_t\right]$	$\mathbb{E}\left[\sum_{t=0}^{\infty} r_t\right]$	$\lim_n \mathbb{E}\left(\frac{1}{n} \sum_{t=0}^n r_t\right)$

## PERFORMANCE

Assympt. Convergence	PAC	Regret
$\pi_{\theta_n} \rightarrow \pi^*$	$\Pr_{\pi^*} U_{\text{err}} > F(\cdot)$	$\max_j \sum_t r_{tj} - r_{tj}^*$

**DYNAMIC PROGRAMMING** → Break problem into components      → BOOTSTRAPPED BACKUP!  
→ Based on Markov assumption       $\hookrightarrow$  VALUE FCT. ESTIMATES

$$\Rightarrow V^*(s_t) = R(s, \pi(s_t)) + \gamma \sum_{s_{t+1}} T(s_{t+1}, s_t, \pi(s_t)) V^*(s_{t+1})$$

Δ: TD Error

↳ TEMPORAL DIFFERENCE:  $V(s_t) \leftarrow V(s_t) + \kappa [r_t + \gamma V(s_{t+1}) - V(s_t)]$

↳ Q-LEARNING:  $Q(s_t, a_t) \leftarrow Q(s_t, a_t) + \alpha [r_t + \gamma \max_a Q(s_{t+1}, a) - Q(s_t, a)]$

↳ FUNCTION APPROX.:  $Q(s_t, a_t, \Theta_k)$   $\Rightarrow$  Instable: DEADLY TRAP

Off-Policy      bootstrapping      fct. approx.

⇒ BREAKTHROUGH: DQN's (H)

- ① Experience Replay Buffer
- ② Separate Target Networks
- ③ Clip TD error to [-1, 1] range

$$\min_{\Theta} J_{\text{MSBE}} = \mathbb{E}[Q(s, a; \Theta) - y_k]$$

$$y_k = r + \gamma \max_a Q(s', a'; \Theta')$$

Double Q  
AveragE  
EXTENSIONS → DUELING  
HER

OPTIMISTIC INIT  
UCB  
POSTERIOR SAMPLING!  
EXPLORATION  
! E-Greedy  
Softmax

- ① Posterior Sampling for DQN  $\Rightarrow$  bootstrapped DQN (Osband et al., 16')
    - ↳ Uncertainty estimate via ensemble  $\Rightarrow$  Several Output Heads
    - ↳ Osband et al., 18'  $\Rightarrow$  Systematic exploration via randomized prior jet.
    - ↳ Janez et al., 19'  $\Rightarrow$  Successor Uncertainties based on Successor Features
- 

REINFORCE:  
Policy Gradient algo  
 $\nabla \Theta$

$$\begin{aligned} * R_i &= \sum_{n=i}^t \gamma^{t-n} r_n && \Rightarrow MC \text{ Returns} \\ * \hat{x}_i &= R_i - b && \Rightarrow \text{Baseline Correction} \\ * \Theta &= \Theta + \alpha \nabla_\Theta \log \pi_\Theta(a|s_i) \hat{x}_i && \Rightarrow PG \text{ Update} \end{aligned}$$

$\Rightarrow$  Actor-Critic Methods: learn value fn. to provide sample-efficient signals



LEARNING SPEED vs. STABILITY	
CPI	SURROGATE + MONOTONIC IMPROVEMENT
TRPO	APPROX. CPI w. TRUST REGION
PPO	KL PENALTY + CLIPPING
StC	MAX ENTROPY RL

## SAMPLE EFFICIENT RL

- GENERALIZATION: Need for RL-specific regularizers
  - \* Igl 19': Selective noise injection  $\oplus$  info bottleneck
- STRUCTURE: Meta-Learning  $\Rightarrow$  augmented MDP
  - \* Relationship via low-dim. embedding
  - \* MAML: Inner + Outer Loop  $\Rightarrow$  learn init  $\Theta$
  - \* CAVIT: Separate context  $\Rightarrow$  Rapid adaptation

## MODEL-BASED:

- \* PILCO - Deisenroth, Petersen 11'
- \* World Models - Ha, Schmidhuber 18'
- \* Bayesian NNs - Chua et al. 18'
- \* Meta-L. - Saezundson et al. 18', 19'

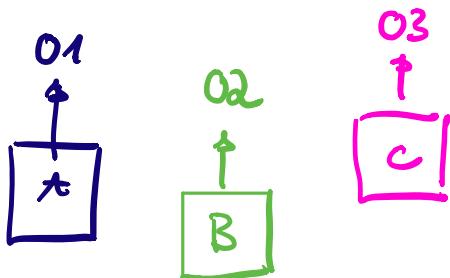
## CHALLENGES:

- \* MTRLO  $\neq$  2 player mini-games
- \* Mine RL  $\Rightarrow$  human priors

# Celeste Kidd (UC Berkeley) - How to Know

DEVELOPMENTAL PERSPECTIVE → BELIEF FORMATION ⇒  $\oplus$  Behavior Model

## 1 HUMANS CONTINUOUSLY FORM BELIEFS (Prob. Expectations)



→ Dirichlet - Multinomial  $\Rightarrow$  Surprise  
regressors  $\Rightarrow$  look away probs  
↳ Goldilocks effect:  $\uparrow/\downarrow$  Surprise  $\Rightarrow$  look aways  
↳ Predictable  $\longleftrightarrow$  Surprising

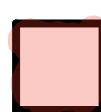
$\Rightarrow$  FIND / HIGHLIGHT DATA "AT THE EDGE"  $\rightarrow$  Attention  $\Rightarrow$  Learning Progress

## 2 CERTAINTY DIMINISHES INTEREST

$\Rightarrow$  INTEREST DETERMINED BY WHAT YOU THINK YOU KNOW  $\Rightarrow$  NOT REALITY

## 3 CERTAINTY IS DRIVEN BY FEEDBACK

→ Open Mind: "Doxyness"  $\Rightarrow$  META-COGNITION



↳ "Early stages of "making up your mind" is crucial to formation"

## 4 LESS FEEDBACK MAY ENCOURAGE OVERCONFIDENCE

Nixxon → Concepts of politicians across populations



$\Rightarrow$  t-SNE plot from Chinese Restaurant Process

$\rightarrow$  Increased deviant concept awareness

## 5 HUMANS FORM BELIEFS QUICKLY

$\rightarrow$  Importance of sequence of observation presentation

MAJOR

$\rightarrow$  NO NEUTRAL PLATFORMS

ETHICAL

$\rightarrow$  CHILDREN ARE SUSCEPTIBLE

CHALLENGES

$\rightarrow$  GENDER DISCRIMINATION