

# RANK-NOSH: Efficient Predictor-Based Architecture Search via Non-Uniform Successive Halving

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- 代码：暂无

## 论文主要内容

### 摘要

Predictor-based方法在NAS上效果显著，但是这些方法受到高计算代价限制（训练predictor所需）。本文方法通过削减架构训练的计算budget来提升搜索效率。本文提出Non-uniform Successive Halving (NOSH)，这是一个层次调度算法来中断训练中表现差的架构来防止浪费budget。相比SOTA Predictor-based方法在不同搜索空间、数据集上减少budgets 到原来1/5.

### 贡献

1. 给了一种新的解决搜索效率的方法
2. 扩展Successive Halving

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## 研究内容

### Motivation

- NAS的高效搜索、supernet的weight sharing带来搜索空间限制与inductive biases
- Predictor-based NAS可以解决这些缺点
  - a. 训练、评估在pool中的所有架构
  - b. fit a surrogate performance predictor

- c. 用predictor来propose新的架构并加到pool中
  - 但是已有的Predictor-based方法在第一步仍然计算开销大（对此解决办法主要关注在开发一个需要更小的training pool的predictor，sample efficiency）
  - 这篇文章就主要关注于怎么通过缩小pool中架构个体的training length（就是减少candidate pool中的training epoch）
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## 方法

### 介绍

Successive Halving:

- 训练一个pool（随机生成的一些configuration），通过一定的schedule逐渐从pool中扔掉performance不好的。主要用在超参搜索技术上。
- 先前的Successive Halving方法是uniform的。即在任一时刻，pool中的candidates都是训练过相同epochs的（因为只是简单的把poor performance的从pool中丢掉）
- 在这篇文章中对Successive Halving进行扩展：新架构会迭代的加入pool，poor performance会保留（用来构造架构pairs）

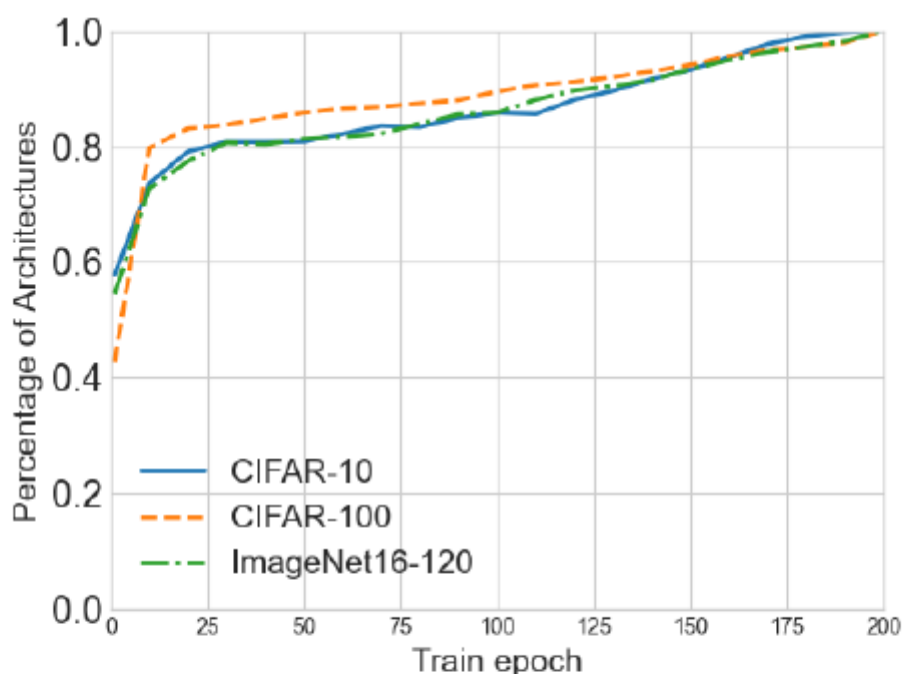


Figure 1: Percentage of architectures with bottom-50% validation accuracy at intermediate epochs that remain at bottom 50% when fully trained on NAS-Bench-201.

说明使用少量epoch训练的结果具有一定的参考价值（训练10epoch，70%的架构满足：如果在开始落后，后面就再也追不上了）

## 算法流程

### NOSH

维护一个金字塔形式的architecture pool（金字塔排序：粗粒度、细粒度的综合，在少train epoch下）

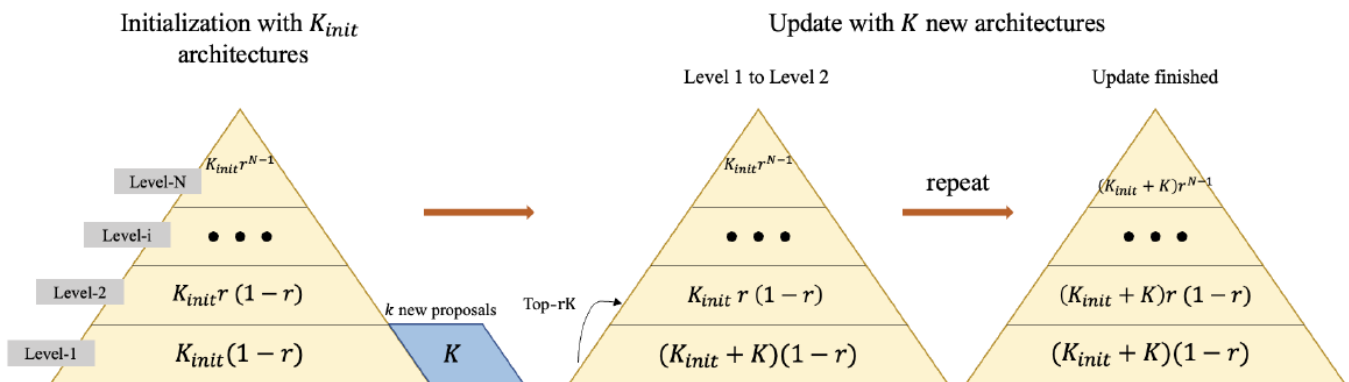


Figure 2: A N-level NOSH pyramid, including its initialization (left) and update (middle & right) processes. Equation inside each level represents the corresponding number of architectures. All architectures in level- $i$  will be trained to epoch  $e^{(i)}$ . **Left:** During initialization, we populate the pool pyramid. Then we train the predictor and propose  $K$  new architectures. **Middle:** We train the  $K$  new candidates for  $e^{(i)}$  epochs and move Top- $rK$  architectures from level-1 to level-2. **Right:** The pyramid after the update. Then we retrain the predictor and perform the next update, this process continues until a maximum pool size  $M$  is achieved.

- 性质：金字塔每一层的architecture的训练epoch一致
- 性质：金字塔level越高（越顶层），训练epoch越多，越充分。金字塔的最顶层是fully trained
- Level  $i$  的architecture被训练次数为  $e^i$  epoch。  $E = \left\{ e^{(i)} \right\}_{i=1}^N$ ，  $e^{(i)} < e^{(i+1)}$ ；move ratio  $r \in (0, 1)$
- 每次迭代会用当前金字塔candidates pool训练一个predictor，用来propose  $K$  个新architecture，再更新金字塔pool

#### 1. Initialization

- $K_{init}$  个architecture
- train这些architecture  $e^{(1)}$  个epochs，并排序
- top  $K_{init}r$  的会进一步训练到  $e^{(2)}$  个epochs且升到 Level-2；bottom  $K_{init}(1-r)$  的留在Level-1.
- 重复升level的过程，直到训练epochs达到  $e^{(N)}$ ，即达到金字塔顶层。
- 初始化结束后，Level-1会有  $K_{init}(1-r)$  candidates，Level-N会有  $K_{init}r^{(N-1)}$  candidates

2. Update (propose、加入pool)
  - a. 训练predictor (ranker-based predictor) , 然后propose  $K$  个new architecture (untrained)
  - b. 把这个  $K$  个架构训练  $e^{(1)}$  个epochs、加入Level-1。
  - c. 排序后, top  $rK$  训练至  $e^{(2)}$  个epochs、移到 Level-2。
  - d. 重复上步直到 Level达到  $N$
3. 增加Level-0

Table 1: Spearman ranking correlation between architectures ranked by training-free metrics and true validation accuracy on CIFAR-10 in NAS-Bench-201 space.

Prior Scores	Whole Space	Top 1% Architectures
grad_norm [1]	0.58	0.42
jacob_cov [25]	0.73	0.13
mag [35]	0.76	0.37

- 这些代理metric (training-free) 用于整个NAS空间, performance rank效果好, 但是对top configurations的rank不准确
- 基于这个观察结果, 把这个metric用来作为Level-0的rank。top configurations放到更高Level上去refine

区别于一般的successive halving:

- non-uniform: pool中的架构有着不同训练程度 (Level)
- 先前训练中断的架构有机会resume (如果performance能比新propose加入的好)

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**Algorithm 1:** NOSH: Non-Uniform Successive Halving

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**Input:** Candidate pool  $\mathcal{S}$ , schedule  $E = \{e^{(l)}\}_{l=1}^N$ ,  
move ratio  $r$ , Proposal size  $K$  (use  $K_{init}$   
during the initialization round)

**Result:** updated training pool  $\mathcal{S}$

**for** level  $l = 0 \sim (N - 1)$  **do**

**if**  $l == 0$  **then**

        Sort all architectures in level- $l$  according to  
        their prior scores;

**else**

        Sort all architectures in level- $l$  according to  
        their current validation accuracy;

**end**

    Train top  $rK$  architectures in level- $l$  to epoch  
     $e^{(l+1)}$  and upgrade them to level- $(l + 1)$ ;

$K \leftarrow rK$ ;

**end**

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Predictor (learning to rank)

Pairwise Ranking

label定义:

$$y(\alpha_1, \alpha_2) = \begin{cases} 1 \{e_{\alpha_1} < e_{\alpha_2}\} & e_{\alpha_1} \neq e_{\alpha_2} \\ 1 \{acc_{\alpha_1} < acc_{\alpha_2}\} & e_{\alpha_1} = e_{\alpha_2} \end{cases}$$

- 同一Level (同样的epoch训练) 的架构: 比acc (validation accuracy) 大小
- 不同Level的架构直接用Level大小比较

目标:

$$\min_{\mathcal{M}} E_{(\alpha_1, \alpha_2) \sim \mathcal{X}} [\ell(\mathcal{M}(\alpha_1, \alpha_2), y(\alpha_1, \alpha_2))]$$
$$\mathcal{X} = \{(\alpha_1, \alpha_2) \mid \alpha_1 \in \mathcal{S}, \alpha_2 \in \mathcal{S}, \alpha_1 \neq \alpha_2\}$$

- $\mathcal{M}$  表示rank model,  $\ell$  表示loss function (BCE),  $\mathcal{S}$  表示candidates pool

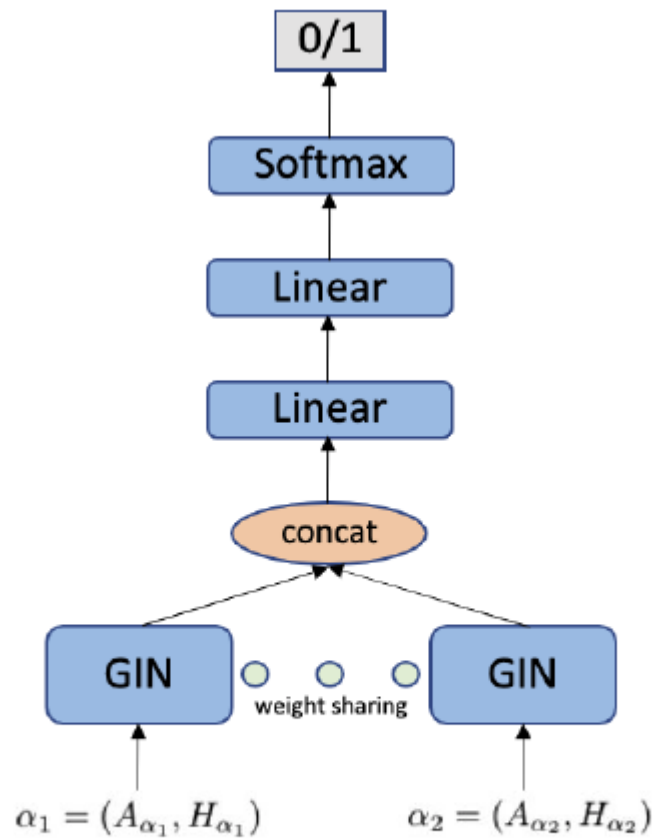


Figure 3: Ranker Network

### Propose (Search Algorithm)

- $K_{init}$  通过从搜索空间里随机采样出来
  - $K$  的选择，由于直接枚举整个search space是不可能的，就是用搜索空间随机选择出来一个子集的枚举rank。加入explicit exploration
    - global ranking选择top  $\frac{K}{2}$
    - 剩下的从top  $2K$  中随机选择（排除top  $\frac{K}{2}$  已选择的，保证不重复）
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**Algorithm 2: RANK-NOSH Main Search**

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**Input:** Max candidate pool size  $M$ , init pool size  $K_{init}$ , proposal size  $K$ , schedule  $E = \{e^{(l)}\}_{l=1}^N$ , move ratio  $r$

**Result:** Discovered best architecture  $\alpha^*$

Randomly select  $K_{init}$  architectures and add them to  $\mathcal{S}$ ;

Initialize Pyramid:  $\mathcal{S} = \text{NOSH}(\mathcal{S}, E, r, K_{init})$ ;

$M \leftarrow M + K_{init}$ ;

**while**  $|\mathcal{S}| < M$  **do**

    Generate pairwise labels according to Eq. (1);

    Fit the ranker model with labeled  $\mathcal{S}$ ;

    Use the ranker to propose top  $\min(K, M - |\mathcal{S}|)$  architectures and add them to  $\mathcal{S}$ ;

    Update Pyramid:  $\mathcal{S} = \text{NOSH}(\mathcal{S}, E, r, K)$ ;

**S**  $M \leftarrow M + K$ ;

**end**

$\alpha^* = \arg \max_{\alpha \in \mathcal{S}} \text{Valid\_Acc}_\alpha$

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## 实验结果

### 实验设置

- Ranker: 用arch2vec **pretrain** GIN encoder, 来提高架构的representation
- $r = \frac{1}{2}$ , Level-0用1/3 (no cost下能容纳更多架构)
- metric (prior score) 选用magnitude of weights
- 对每个搜索空间 (nasbench、DARTS) 利用标准full training epoch来确定 schedule E
- $K_{init}$  为16\*3,  $K$  为10\*3. (有2/3的架构在Level-0无训练代价)

## Results

### NAS-Bench-201

$E = (1, 2, 3, 12)$  for CIFAR-10,  $E = (10, 50, 100, 200)$  CIFAR-100 and ImageNet16-120 to match the maximum training epochs



Table 2: Comparison with state-of-the-art NAS methods on NAS-Bench-201.

Method	CIFAR-10			CIFAR-100			ImageNet16-120		
	validation	test	budget	validation	test	budget	validation	test	budget
DARTS [23]	39.77 $\pm$ 0.00	54.30 $\pm$ 0.00	-	38.57 $\pm$ 0.00	38.97 $\pm$ 0.00	-	18.87 $\pm$ 0.00	18.41 $\pm$ 0.00	-
SNAS [43]	90.10 $\pm$ 1.04	92.77 $\pm$ 0.83	-	69.69 $\pm$ 2.39	69.34 $\pm$ 1.98	-	42.84 $\pm$ 1.79	43.16 $\pm$ 2.64	-
GDAS [10]	90.01 $\pm$ 0.46	93.23 $\pm$ 0.23	-	71.14 $\pm$ 0.27	70.61 $\pm$ 0.26	-	41.70 $\pm$ 1.26	41.84 $\pm$ 0.90	-
PC-DARTS [44]	89.96 $\pm$ 0.15	93.41 $\pm$ 0.30	-	67.12 $\pm$ 0.39	67.48 $\pm$ 0.89	-	40.83 $\pm$ 0.08	41.31 $\pm$ 0.22	-
ENAS [29]	39.77 $\pm$ 0.00	54.30 $\pm$ 0.00	-	15.03 $\pm$ 0.00	15.61 $\pm$ 0.00	-	16.43 $\pm$ 0.00	16.32 $\pm$ 0.00	-
Prior Score: jacob_cov [25]	89.69 $\pm$ 0.73	92.96 $\pm$ 0.80	-	69.87 $\pm$ 1.22	70.03 $\pm$ 1.16	-	43.99 $\pm$ 2.05	44.43 $\pm$ 2.07	-
Prior Score: mag [35]	89.94 $\pm$ 0.34	93.35 $\pm$ 0.04	-	70.18 $\pm$ 0.66	70.47 $\pm$ 0.18	-	42.57 $\pm$ 2.14	43.17 $\pm$ 2.57	-
RE [30] *	91.04 $\pm$ 0.51	93.81 $\pm$ 0.46	1,200	72.18 $\pm$ 0.91	72.06 $\pm$ 0.97	20,000	45.78 $\pm$ 0.72	45.67 $\pm$ 0.83	20,000
RS [3] *	90.91 $\pm$ 0.41	93.69 $\pm$ 0.42	1,200	71.36 $\pm$ 0.84	71.32 $\pm$ 0.95	20,000	45.26 $\pm$ 0.67	45.24 $\pm$ 0.84	20,000
REINFORCE [41] *	90.32 $\pm$ 0.85	93.21 $\pm$ 0.76	1,200	70.95 $\pm$ 1.22	70.87 $\pm$ 1.23	20,000	44.66 $\pm$ 1.44	44.63 $\pm$ 1.52	20,000
arch2vec-BO [45] *	91.4 $\pm$ 0.35	94.24 $\pm$ 0.21	1,200	73.29 $\pm$ 0.41	73.41 $\pm$ 0.22	20,000	46.27 $\pm$ 0.39	46.32 $\pm$ 0.27	20,000
RANK-NOSH	<b>91.4 <math>\pm</math> 0.18</b>	<b>94.26 <math>\pm</math> 0.17</b>	<b>292</b>	<b>73.49 <math>\pm</math> 0.00</b>	<b>73.51 <math>\pm</math> 0.00</b>	<b>5,550</b>	<b>46.37 <math>\pm</math> 0.0</b>	<b>46.34 <math>\pm</math> 0.0</b>	<b>5,550</b>
oracle	91.61	94.37	-	73.49	73.51	-	46.77	47.31	-

\* Reproduced by directly searching on every dataset with a candidate pool size of 100 architectures following [45]. Note that the original arch2vec paper [45] measures the search budget in seconds, which translates to approximately 100 architectures on all three datasets.

## NAS-Bench-101

Table 4: Comparison with SOTA methods on NAS-Bench-101. We report the avg test accuracy for our method over 10 random seeds.

Methods	Search Budget (#epochs)	Test Accuracy (%)
Prior Score: jacob_conv [25]	-	89.11
Prior Score: mag [35]	-	92.66
Random Search [46]	108,000	93.54
REINFORCE [46]	108,000	93.58
Regularized Evolution [46]	108,000	93.72
NAO [24]	108,000	93.74
BANANAS [40]	54,000	94.08
arch2vec-BO [45]	43,200	94.05
RANK-NOSH	8,400	93.97

本文的方法和 SOTA 方法 performance 相当，但只有 19% 的 budget.

## DARTS Space

总共  $10^9$  可能的架构，从中随机采样 600k 架构，在这个子集上实验

## CIFAR-10

Search budgets: 990 epochs (1.65x DARTS)



Table 3: Comparison with state-of-the-art NAS methods on DARTS Space.

Architecture	Test Error(%)		Param (M)	Search Budget (#epochs)	Search Method
	Best	Avg			
RSWS [20]	2.71	$2.85 \pm 0.08$	4.3	-	Weight Sharing
DARTS [23]	$2.76 \pm 0.09^*$	-	3.6	-	Weight Sharing
SNAS [43]	-	$2.85 \pm 0.02$	2.8	-	Weight Sharing
BayesNAS [49]	$2.81 \pm 0.04^*$	-	3.4	-	Weight Sharing
ProxylessNAS [4]	<b>2.08<sup>†</sup></b>	-	4.0	-	Weight Sharing
ENAS [29]	$2.89^{\dagger}$	-	4.6	-	Weight Sharing
P-DARTS [8]	2.50	-	3.4	-	Weight Sharing
PC-DARTS [44]	$2.57 \pm 0.07^*$	-	3.6	-	Weight Sharing
SDARTS-ADV [6]	-	$2.61 \pm 0.02$	3.3	-	Weight Sharing
Random Search [23]	$3.29 \pm 0.15^*$	-	3.2	2,400	Random
GATES [27]	$2.58^{\dagger}$	-	4.1	64,000	Predictor
BRP-NAS (high) [12]	-	$2.59 \pm 0.11$	-	36,000	Predictor
BRP-NAS (med) [12]	-	$2.66 \pm 0.09$	-	18,000	Predictor
BANANAS [40]	2.57	2.64	3.6	5,000	Predictor
arch2vec-BO [45]	<b>2.48</b>	$2.56 \pm 0.05$	3.6	5,000	Predictor
RANK-NOSH	2.50	<b><math>2.53 \pm 0.02</math></b>	3.5	<b>990</b>	Predictor

<sup>†</sup> Obtained on different search spaces than DARTS.

\* Error bars are computed by retraining the best discovered architecture multiple times.

## ImageNet

用搜出来的架构放在ImageNet上评估（用transfer learning setting）

Table 5: Transfer learning results on ImageNet

Architecture	Test Error(%)	Params (M)
NASNet-A [51] *	26.0	5.3
AmoebaNet-A [31] *	25.5	5.1
PNAS [22] *	25.8	5.1
SNAS [43] *	27.3	4.3
DARTS [23] *	26.7	4.7
SDARTS-ADV [6]	25.2	4.8
arch2vec-BO [45] *	25.5	5.2
RANK-NOSH	25.2	5.3

\* Results obtained from the arch2vec paper [45].

## 消融实验

实验使用NAS-Bench-201

## Train-free Prior scores

验证是否直接用score就能完成NAS任务。

- 直接从搜索空间中采样1000个架构，并用prior score最高来选取best架构
- 结果明显poor performance（比random search差）
- 原因是这些 scores 不能够区分top architecture

## Comparison with Early Stopping

验证是否直接使用简单的 Early Stopping 就行（任何一个架构都不会被完全训练）

Table 6: Validation accuracy (%) of the final architectures obtained by RANK-NOSH v.s. arch2vec-BO with early stopping on NAS-Bench-201.

Dataset	Search Budget	arch2vec-BO	RANK-NOSH
CIFAR-10	5,550	91.00 $\pm$ 0.61	91.60 $\pm$ 0.02
	2,969	90.35 $\pm$ 0.62	91.56 $\pm$ 0.07
CIFAR-100	5,550	73.23 $\pm$ 0.61	73.49 $\pm$ 0.00
	2,969	71.88 $\pm$ 1.19	73.44 $\pm$ 0.09
ImageNet16-120	5,550	46.08 $\pm$ 0.75	46.37 $\pm$ 0.00
	2,969	45.10 $\pm$ 1.07	46.43 $\pm$ 0.21

结论：

- Early stop的budget越小，结果越差，variance也越大
- 简单使用early-stopping并没有达到文章的性能
- RANK-NOSH方法具有更小的 variance

## NOSH Schedules

定义资源分配的超参有两个  $E$  和  $r$

Table 7: Validation Accuracy of final architectures from RANK-NOSH on CIFAR-10 under various schedules and move ratios. Our method is relatively stable across various  $E$  and  $r$ .

$E$	Search Budget	Valid Accuracy (%)
(10,50,200)	6,750	$91.60 \pm 0.03$
(10,50,100,200)	5,550	$91.60 \pm 0.02$
(5,25,50,200)	4,075	$91.59 \pm 0.03$
(5,10,25,200)	3,400	$91.57 \pm 0.06$

(a) Under different  $E$

$r$	Search Budget	Valid Accuracy (%)
0.7	9,750	$91.58 \pm 0.06$
0.6	7,400	$91.59 \pm 0.06$
0.5	5,550	$91.60 \pm 0.02$
0.4	4,100	$91.58 \pm 0.08$
0.3	2,950	$91.40 \pm 0.16$

(b) Under different  $r$

- 固定  $r = \frac{1}{2}$  , 改变  $E$ 
  - 结论: stable (无视 Levels数量与 epoch 间隔)
- 固定  $E$  为(10, 50, 100, 200) , 改变  $r$ 
  - 结论: robust
- 建议: 选择  $r = \frac{1}{2}$  ,  $E$  根据不同搜索budgets来确定

Moreover, the proposed framework could be extended to other applications. For instance, RANK-NOSH can be applied to **hyperparameter optimization** by **concatenating the hyperparameters with the architecture embeddings**