

Tree Parzen Estimator(TPE)

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In [2]: import numpy as np
import matplotlib.pyplot as plt
from sklearn.neighbors import KernelDensity
import tqdm, random
import os
# print(os.listdir())
import sys
sys.path.append('../..')
from base.testproblem.testfunction import Rastrigin
from base.kde.toy_kde import NaiveKDE
```

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In [3]: # 使用scikit-learn包中的 KernelDensity 类实现
class FloatVarKDE():
    def __init__(self, low=0, high=1, bandwidth=0.1):
        self.bandwidth = bandwidth
        # self.kde = NaiveKDE(bandwidth=bandwidth)
        self.kde = KernelDensity(bandwidth=bandwidth)
        self.low = low
        self.high = high
        # self.kde.fit(high-low)

    def sample(self, num):
        cnt = 0
        samples = []
        while cnt < num:
            sample = self.kde.sample().item()
            if self.low <= sample <= self.high:
                cnt += 1
                samples.append(sample)
        return np.asarray(samples)

    def fit(self, points):
        self.kde.fit(points.reshape(-1, 1))

    def log_pdf(self, x):
        return self.kde.score_samples(x.reshape(-1, 1))

class FloatNaiveKDE(NaiveKDE):
    def __init__(self, low=0, high=1, bandwidth=0.1):
        NaiveKDE.__init__(self, bandwidth=bandwidth)
        self.low = low
        self.high = high
        self.bandwidth = bandwidth

    def fit(self, x):
        NaiveKDE.fit(self, x)

    def log_pdf(self, x):
        return np.log(NaiveKDE.evaluate(self, x))

    def sample(self, num):
        ct = 0
        samples = []
        while ct < num:
            u = np.random.uniform(0, 1)
            idx = int(u * len(self.data))
            sample = np.random.normal(self.data[0, idx].item(), self.bandwidth
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        if self.low <= sample <= self.high:
            ct += 1
            samples.append(sample)

    return samples
# u = np.random.random.uniform(0, 1, size=num)
# idx = (u * len(self.data)).as_type(np.int64)
# return np.random.normal(self.data[idx], self.bandwidth)

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$$EI_{y^*}(x) = \frac{\gamma y^* \ell(x) - \ell(x) \int_{-\infty}^{y^*} p(y) dy}{\gamma \ell(x) + (1 - \gamma) g(x)} \propto \left(\gamma + \frac{g(x)}{\ell(x)} (1 - \gamma) \right)^{-1}$$

1. warmup一笔sample(随机采样等)
2. 将这笔sample按 γ 比例分成两类, good 和 bad
3. 对这笔sample的每一个样本为中心建一个Gaussian分布(james rule),称为为基 (basis)
4. 每次随机从 good Gaussian分布中sample一个candidate, 直到满足一定的candidate数量
5. 分别计算这些candidates在 good 与 bad 的似然,取似然比值最大的一个candidate为本次 suggest结果($\arg\max$ EI function)
6. evaluate刚得到的suggestion, 更新sample集合, 回到第二步

In [4]:

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class ToyTPE():
    def __init__(self,
                 config,
                 cls=FloatVarKDE,
                 bandwidth=1,
                 min_sample=30,
                 gamma=0.1,
                 candidates_num=24):
        self.gamma = gamma
        self.min_sample = min_sample
        self.bandwidth = bandwidth
        self.candidates_num = candidates_num
        self.hp_num = len(config)
        self.hp_range = []
        self.hp_names = list(sorted(config.keys()))
        for name in self.hp_names:
            self.hp_range.append(config[name])
        self.lx = [cls(*lh, bandwidth=bandwidth) for lh in (self.hp_range)]
        self.gx = [cls(*lh, bandwidth=bandwidth) for lh in (self.hp_range)]
        # self.lx = [FloatNaiveKDE(*lh) for lh in (self.hp_range)]
        # self.gx = [FloatNaiveKDE(*lh) for lh in (self.hp_range)]
        self.history = []
        self.history_y = []

    def suggest(self, ):
        # 只suggest一个
        if len(self.history_y) <= self.min_sample or np.random.rand() < 0.1:
            return self._random_suggest()
        else:
            suggest_array = []
            for i in range(self.hp_num):
                candidates = self.lx[i].sample(self.candidates_num)
                lx = self.lx[i].log_pdf(candidates)
                gx = self.gx[i].log_pdf(candidates)
                max_idx = np.argmax(lx - gx)
                suggest_array.append(candidates[max_idx])
            return {k: suggest_array[i] for i, k in enumerate(self.hp_names)}

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def _random_suggest(self):
    suggest_array = []
    for i in range(self.hp_num):
        suggest_array.append((np.random.rand() *
                             (self.hp_range[i][1] - self.hp_range[i][0])
                             + self.hp_range[i][0]))
    return {k: suggest_array[i] for i, k in enumerate(self.hp_names)}

def _split_l_g(self):
    samples = np.asarray(self.history)
    good_num = int(self.gamma * len(samples))
    samples_sorted = samples[np.argsort(self.history_y)]
    good_points = samples_sorted[:good_num, :]
    bad_points = samples_sorted[good_num:, :]
    return good_points, bad_points

def observe(self, x, y):
    sample_array = []
    for k in self.hp_names:
        sample_array.append(x[k])
    self.history.append(sample_array)
    self.history_y.append(y)
    if len(self.history_y) < self.min_sample:
        return

    good_points, bad_points = self._split_l_g()
    for i in range(self.hp_num):
        self.lx[i].fit(good_points[:, i])
        self.gx[i].fit(bad_points[:, i])

```

In [5]:

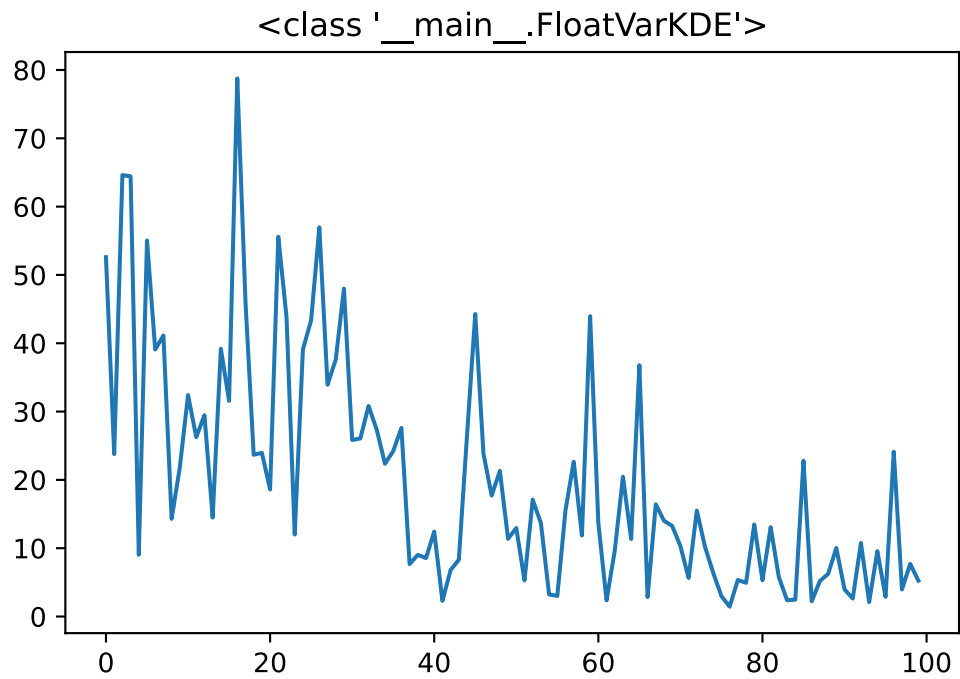
```

def tpe_test(cls):
    np.random.seed(42)
    random.seed(42)

    func = Rastrigin(dim=2)
    opt = ToyTPE(config=func._load_api_config(), cls=cls)
    for iter in tqdm.tqdm(range(100)):
        x = opt.suggest()
        y = func(x)
        opt.observe(x, y)
    plt.figure()
    plt.plot(opt.history_y)
    plt.title(str(cls))
    plt.show()
    print(min(opt.history_y))
    tpe_test(FloatVarKDE)
    tpe_test(FloatNaiveKDE)

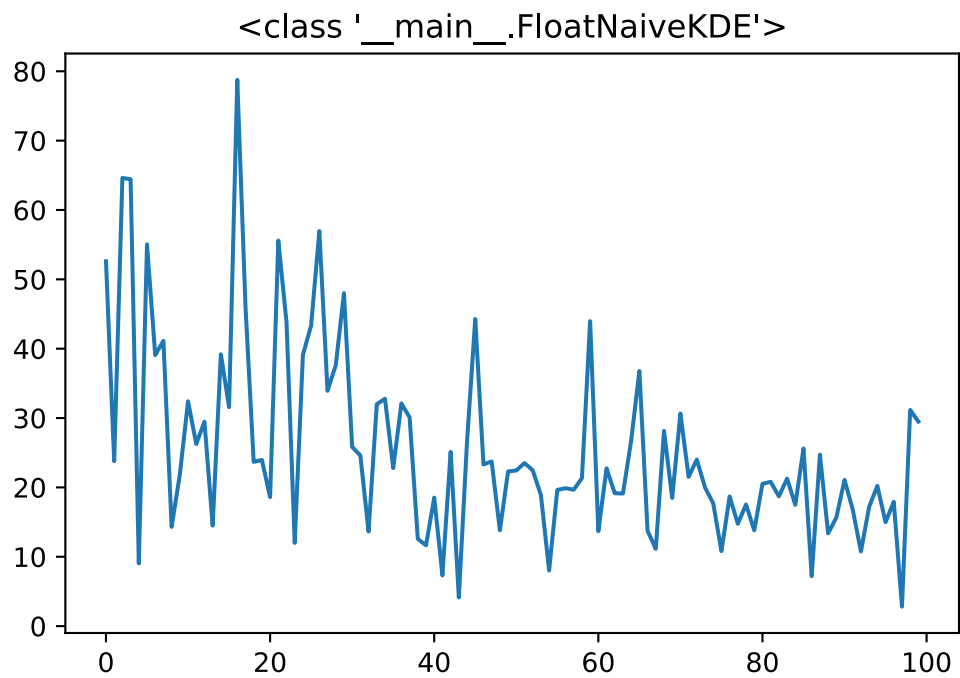
```

100%|██████████| 100/100 [00:00<00:00, 339.47it/s]



1.4343788301755627

100%|██████████| 100/100 [00:00<00:00, 2727.74it/s]



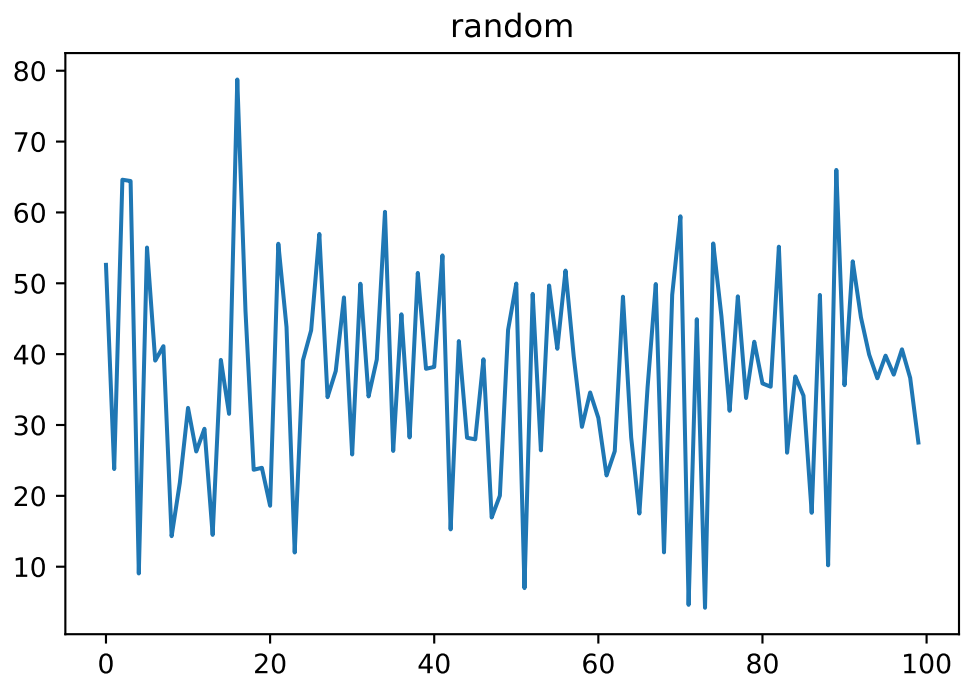
2.805671960962986

In [6]:

```
def random_test():
    np.random.seed(42)
    random.seed(42)

    func = Rastrigin(dim=2)
    opt = ToyTPE(config=func._load_api_config())
    for iter in tqdm.tqdm(range(100)):
        x = opt._random_suggest()
        y = func(x)
        opt.observe(x, y)
    plt.figure()
    plt.plot(opt.history_y)
    plt.title(str('random'))
    plt.show()
    print(min(opt.history_y))
random_test()
```

100%|██████████| 100/100 [00:00<00:00, 1663.55it/s]



4.201927272996498

In []:

In []: