# **DrNAS: Dirichlet Neural Architecture Search**

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· 会议: ICLR2021

· 地址: https://arxiv.org/abs/2006.10355

· 代码: https://github.com/xiangning-chen/DrNAS

## 论文主要内容

### 摘要

本文将NAS建模成一个学习分布的问题,将op连续松弛的权重看作随机变量(服从Dirichlet分布)。这种方式能自然的引入探索、提高泛化能力。其次为了减轻微分NAS的内存开销,本文提出了一个简单的渐进学习策略能够直接在large-scale 任务上搜索。最后在不同数据集、搜索空间下验证DrNAS的有效性。

### 研究内容

### 方法

### 方法

· DARTs:

$$\min_{\theta} \mathcal{L}_{val}(w^*, \theta) \quad \text{s.t. } w^* = \underset{w}{\operatorname{arg\,min}} \mathcal{L}_{train}(w, \theta), \quad \sum_{o=1}^{|\mathcal{O}|} \theta_o^{(i,j)} = 1, \ \forall \ (i,j), \ i < j, \quad (1)$$

- · DARTs那套做法把 heta 看作一个可学习参数,直接对其优化。
  - (**点估计**) 导致在  $\theta$  在验证集上过拟合,引入巨大的泛化误差。
  - 。 直接优化 heta 导致搜索算法开始阶段快速收敛到次优路径,缺乏探索。
- · 由此将DARTs建模成学习一个distribution的问题:  $\theta$  是一个**随机变量**,从一个可学习的分布(分布参数  $\beta$ )中采样得到

$$\min_{\beta} E_{q(\theta|\beta)} \left[ \mathcal{L}_{val}(w^*, \theta) \right] + \lambda d(\beta, \hat{\beta}) \text{ s.t. } w^* = \underset{w}{\operatorname{arg \, min}} \ \mathcal{L}_{train}(w, \theta). \tag{2}$$

取  $q(\theta \mid \beta) \sim \mathrm{Dir}(\beta)$  。 设置Anchor  $\hat{\beta} = 1$  ,避免  $\beta$  太小(sparse sample、high variance、unstable)太大(dense sample、low variance、insufficient exploration)。

$$\frac{d\theta_i}{d\beta_j} = -\frac{\frac{\partial F_{Beta}}{\partial \beta_j}(\theta_j | \beta_j, \beta_{tot} - \beta_j)}{f_{Beta}(\theta_j | \beta_j, \beta_{tot} - \beta_j)} \times \left(\frac{\delta_{ij} - \theta_i}{1 - \theta_j}\right) \quad i, j = 1, ..., |\mathcal{O}|, \tag{3}$$

#### 获得最优架构

$$o^{(i,j)} = \arg\max_{o \in \mathcal{O}} E_{q(\theta_o^{(i,j)}|\beta^{(i,j)})} [\theta_o^{(i,j)}]. \tag{4}$$

这个期望就是Dirichlet分布均值:  $\frac{eta_o^{(i,j)}}{\sum_{o'}eta_{o'}^{(i,j)}}$ 

#### 正则性

· DARTs的泛化误差和验证集loss关于架构参数的hessian矩阵特征值高度相关

Hessian矩阵的<mark>特征值</mark>就是形容其在该点附近<mark>特征向量</mark>方向的凹凸性,特征值越大,凸性越强。你可以把函数想想成一个小山坡,陡的那面是特征值大的方向,平缓的是特征值小的方向。

· 优化目标公式(2)等价于公式(5):

$$\min_{\beta} E_{q(\theta|\beta)} \left[ \mathcal{L}_{val}(w^*, \theta) \right] \text{ s.t. } w^* = \arg\min_{w} \mathcal{L}_{train}(w, \theta) , \ d(\beta, \hat{\beta}) \le \delta, \tag{5}$$

**Proposition 1** Let  $d(\beta, \hat{\beta}) = \|\beta - \hat{\beta}\|_2 \le \delta$  and  $\hat{\beta} = 1$  in the bi-level formulation (5). Let  $\mu$  denote the mean under the Laplacian approximation of Dirichlet. If  $\nabla^2_{\mu} \tilde{\mathcal{L}}_{val}(w^*, \mu)$  is Positive Semi-definite, the upper-level objective can be approximated bounded by:

$$E_{q(\theta|\beta)}(\mathcal{L}_{val}(w,\theta)) \gtrsim \tilde{\mathcal{L}}_{val}(w^*,\mu) + \frac{1}{2}\left(\frac{1}{1+\delta}\left(1 - \frac{2}{|\mathcal{O}|}\right) + \frac{1}{|\mathcal{O}|}\frac{1}{1+\delta}\right)tr\left(\nabla_{\mu}^2 \tilde{\mathcal{L}}_{val}(w^*,\mu)\right) \quad (6)$$

with:

$$\tilde{\mathcal{L}}_{val}(w^*, \mu) = \mathcal{L}_{val}(w^*, Softmax(\mu)), \ \mu_o = \log \beta_o - \frac{1}{|\mathcal{O}|} \sum_{o'} \log \beta_{o'}, \ o = 1, \dots, |\mathcal{O}|.$$

·公式(6)的hessian矩阵迹就是特征值之和,被验证集loss的期望bound

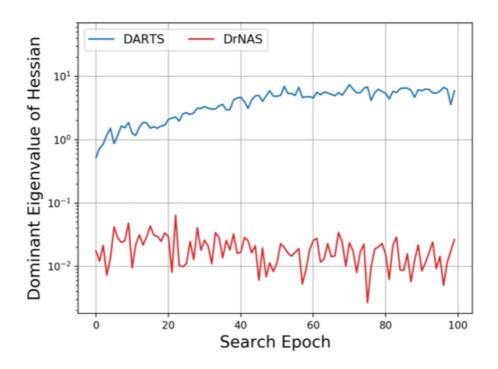


Figure 4: Trajectory of the Hessian norm on NAS-Bench-201 when searching with CIFAR-10 (best viewed in color).

### 渐进式架构学习

- · GPU memory会随着DARTs的候选op增加而线性增长。
  - 。常会使用一些proxy task(用更小的数据集、更少的网络层、channel数)
  - PC-DARTs提出partial channel,训练中随机使用1/k channel,剩余channel shotcut。这样会损失信息、带来随机性,直接结合分布学习加大不稳定

CIFAR-10								
K	Test Accuracy	GPU Memory						
	(%)	(MB)						
1	$94.36 \pm 0.00$	2437						
2	$93.49 \pm 0.28$	1583						
4	$92.85 \pm 0.35$	1159						
8	$91.06 \pm 0.00$	949						
Ours	$94.36 \pm 0.00$	949						
CIFAR-100								
	CIFAR-10	JU						
$\nu$	Test Accuracy	GPU Memory						
K								
K 1	Test Accuracy	<b>GPU Memory</b>						
	Test Accuracy (%)	GPU Memory (MB)						
1	<b>Test Accuracy</b> (%) 73.51 ± 0.00	GPU Memory (MB) 2439						
1 2	<b>Test Accuracy</b> (%) 73.51 ± 0.00 68.48 ± 0.41	GPU Memory (MB) 2439 1583						

- · 提出逐渐增加使用channel的比例,同时逐渐剪枝op(根据分布)
- · 每次在一定搜索步后,增加partial channel比例,超网会逐渐变宽。调整卷积权重:

$$g(j) = \begin{cases} j & j \le n \\ \text{random sample from } \{1, 2, \dots, n\} & j > n \end{cases}$$
 (7)

$$\mathbf{U}_{o,i,h,w}^{(l)} = \mathbf{W}_{g(o),g(i),h,w}^{(l)}, \tag{8}$$

·加宽超网后,根据dirichlet分布参数 eta ,剪掉不重要的op,保持GPU memory不变

## 实验结果

### Darts space

#### CIFAR-10

· CIFAR-10搜索中堆20cell, initial channel=36

Table 2: Comparison with state-of-the-art image classifiers on CIFAR-10.

Architecture	Test Error (%)	Params (M)	Search Cost (GPU days)	Search Method
DenseNet-BC (Huang et al., 2017)*	3.46	25.6	-	manual
NASNet-A (Zoph et al., 2018)	2.65	3.3	2000	RL
AmoebaNet-A (Real et al., 2019)	$3.34 \pm 0.06$	3.2	3150	evolution
AmoebaNet-B (Real et al., 2019)	$2.55 \pm 0.05$	2.8	3150	evolution
PNAS (Liu et al., 2018)*	$3.41 \pm 0.09$	3.2	225	SMBO
ENAS (Pham et al., 2018)	2.89	4.6	0.5	RL
DARTS (1st) (Liu et al., 2019)	$3.00 \pm 0.14$	3.3	0.4	gradient
DARTS (2nd) (Liu et al., 2019)	$2.76 \pm 0.09$	3.3	1.0	gradient
SNAS (moderate) (Xie et al., 2019)	$2.85 \pm 0.02$	2.8	1.5	gradient
GDAS (Dong & Yang, 2019)	2.93	3.4	0.3	gradient
BayesNAS (Zhou et al., 2019)	$2.81 \pm 0.04$	3.4	0.2	gradient
ProxylessNAS (Cai et al., 2019) <sup>†</sup>	2.08	5.7	4.0	gradient
PARSEC (Casale et al., 2019)	$2.81 \pm 0.03$	3.7	1	gradient
P-DARTS (Chen et al., 2019)	2.50	3.4	0.3	gradient
PC-DARTS (Xu et al., 2020)	$2.57 \pm 0.07$	3.6	0.1	gradient
SDARTS-ADV (Chen & Hsieh, 2020)	$2.61 \pm 0.02$	3.3	1.3	gradient
GAEA + PC-DARTS (Li et al., 2020)	$2.50 \pm 0.06$	3.7	0.1	gradient
DrNAS (without progressive learning)	$2.54 \pm 0.03$	4.0	$0.4^{\ddagger}$	gradient
DrNAS	$2.46 \pm 0.03$	4.1	$0.6^{\ddagger}$	gradient

<sup>\*</sup> Obtained without cutout augmentation.

### **Imagenet**

· 堆叠14cells, inital channel=48

<sup>†</sup> Obtained on a different space with PyramidNet (Han et al., 2017) as the backbone. ‡ Recorded on a single GTX 1080Ti GPU.

Table 3: Comparison with state-of-the-art image classifiers on ImageNet in the mobile setting

Architecture		Test Error(%)		Search Cost	Search
		top-5	(M)	(GPU days)	Method
Inception-v1 (Szegedy et al., 2015)	30.1	10.1	6.6	-	manual
MobileNet (Howard et al., 2017)	29.4	10.5	4.2	-	manual
ShuffleNet $2 \times (v1)$ (Zhang et al., 2018)	26.4	10.2	$\sim 5$	-	manual
ShuffleNet $2 \times (v2)$ (Ma et al., 2018)	25.1	-	$\sim 5$	-	manual
NASNet-A (Zoph et al., 2018)	26.0	8.4	5.3	2000	RL
AmoebaNet-C (Real et al., 2019)	24.3	7.6	6.4	3150	evolution
PNAS (Liu et al., 2018)	25.8	8.1	5.1	225	SMBO
MnasNet-92 (Tan et al., 2019)	25.2	8.0	4.4	-	RL
DARTS (2nd) (Liu et al., 2019)	26.7	8.7	4.7	1.0	gradient
SNAS (mild) (Xie et al., 2019)	27.3	9.2	4.3	1.5	gradient
GDAS (Dong & Yang, 2019)	26.0	8.5	5.3	0.3	gradient
BayesNAS (Zhou et al., 2019)	26.5	8.9	3.9	0.2	gradient
DSNAS (Hu et al., 2020)†	25.7	8.1	-	-	gradient
ProxylessNAS (GPU) (Cai et al., 2019) <sup>†</sup>	24.9	7.5	7.1	8.3	gradient
PARSEC (Casale et al., 2019)	26.0	8.4	5.6	1	gradient
P-DARTS (CIFAR-10) (Chen et al., 2019)	24.4	7.4	4.9	0.3	gradient
P-DARTS (CIFAR-100) (Chen et al., 2019)	24.7	7.5	5.1	0.3	gradient
PC-DARTS (CIFAR-10) (Xu et al., 2020)	25.1	7.8	5.3	0.1	gradient
PC-DARTS (ImageNet) (Xu et al., 2020)	24.2	7.3	5.3	3.8	gradient
GAEA + PC-DARTS (Li et al., 2020)†	24.0	7.3	5.6	3.8	gradient
DrNAS (without progressive learning) <sup>†</sup>	24.2	7.3	5.2	3.9	gradient
DrNAS <sup>†</sup>	23.7	7.1	5.7	4.6	gradient

 $<sup>^{\</sup>dagger}$  The architecture is searched on ImageNet, otherwise it is searched on CIFAR-10 or CIFAR-100.

### NAS-bench-201

· 4个不同随机种子实验

Table 4: Comparison with state-of-the-art NAS methods on NAS-Bench-201.

Method	CIFAR-10		CIFA	R-100	ImageNet-16-120		
Method	validation	test	validation	test	validation	test	
ResNet (He et al., 2016)	90.83	93.97	70.42	70.86	44.53	43.63	
Random (baseline)	$90.93 \pm 0.36$	$93.70 \pm 0.36$	$70.60 \pm 1.37$	$70.65 \pm 1.38$	$42.92 \pm 2.00$	$42.96 \pm 2.15$	
RSPS (Li & Talwalkar, 2019)	$84.16 \pm 1.69$	$87.66 \pm 1.69$	$45.78 \pm 6.33$	$46.60 \pm 6.57$	$31.09 \pm 5.65$	$30.78 \pm 6.12$	
Reinforce (Zoph et al., 2018)	$91.09 \pm 0.37$	$93.85 \pm 0.37$	$70.05 \pm 1.67$	$70.17 \pm 1.61$	$43.04 \pm 2.18$	$43.16 \pm 2.28$	
ENAS (Pham et al., 2018)	$39.77 \pm 0.00$	$54.30 \pm 0.00$	$10.23 \pm 0.12$	$10.62 \pm 0.27$	$16.43 \pm 0.00$	$16.32 \pm 0.00$	
DARTS (1st) (Liu et al., 2019)	$39.77 \pm 0.00$	$54.30 \pm 0.00$	$38.57 \pm 0.00$	$38.97 \pm 0.00$	$18.87 \pm 0.00$	$18.41 \pm 0.00$	
DARTS (2nd) (Liu et al., 2019)	$39.77 \pm 0.00$	$54.30 \pm 0.00$	$38.57 \pm 0.00$	$38.97 \pm 0.00$	$18.87 \pm 0.00$	$18.41 \pm 0.00$	
GDAS (Dong & Yang, 2019)	$90.01 \pm 0.46$	$93.23 \pm 0.23$	$24.05 \pm 8.12$	$24.20 \pm 8.08$	$40.66 \pm 0.00$	$41.02 \pm 0.00$	
SNAS (Xie et al., 2019)	$90.10 \pm 1.04$	$92.77 \pm 0.83$	$69.69 \pm 2.39$	$69.34 \pm 1.98$	$42.84 \pm 1.79$	$43.16 \pm 2.64$	
DSNAS (Hu et al., 2020)	$89.66 \pm 0.29$	$93.08 \pm 0.13$	$30.87 \pm 16.40$	$31.01 \pm 16.38$	$40.61 \pm 0.09$	$41.07 \pm 0.09$	
PC-DARTS (Xu et al., 2020)	$89.96 \pm 0.15$	$93.41 \pm 0.30$	$67.12 \pm 0.39$	$67.48 \pm 0.89$	$40.83 \pm 0.08$	$41.31 \pm 0.22$	
DrNAS	$91.55 \pm 0.00$	$94.36 \pm 0.00$	$73.49 \pm 0.00$	$73.51 \pm 0.00$	$46.37 \pm 0.00$	$46.34 \pm 0.00$	
optimal	91.61	94.37	73.49	73.51	46.77	47.31	

# **Exploration and exploitation**

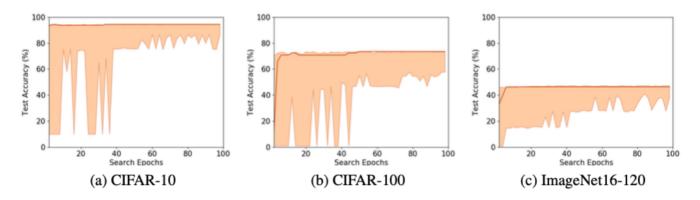


Figure 1: Accuracy range (min-max) of the 100 sampled architectures. Note that the solid line is our derived architecture according to the Dirichlet mean as described in Section 2.2.

- · 在搜索过程中每个epoch依照分布采样100个 heta 。再对这100个 heta 分别argmax获得子网
- · 早期采样的架构准确率分布很散,代表探索。
- · 晚期采样的架构准确率范围变窄,代表开发

## 消融实验

Table 5: Test accuracy of the searched architecture with different  $\lambda$ s on NAS-Bench-201 (CIFAR-10).  $\lambda = 1e^{-3}$  is what we used for all of our experiments.

$\lambda$	0	$5e^{-4}$	$1e^{-3}$	$5e^{-3}$	$1e^{-2}$	$1e^{-1}$	1
Accuracy	93.78	94.01	94.36	94.36	94.36	93.76	93.76

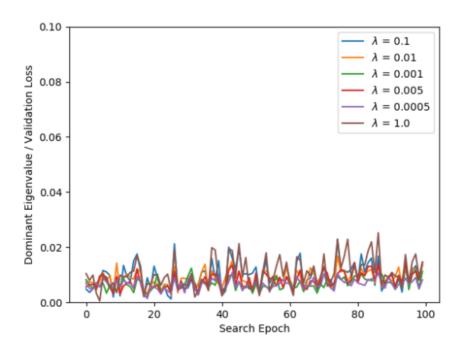


Figure 5: Trajectory of the Hessian norm under various  $\lambda$ s on NAS-Bench-201 when searching with CIFAR-10 (best viewed in color).