

For periodic functions  $x_1(t)$ ,  $x_2(t)$  with periods  $T_1$  and  $T_2$  respectively, the period of  $x_1(t) + x_2(t)$  is  $LCM(T_1, T_2)$

$$\begin{aligned} E &= \int_{t_1}^{t_2} |x(t)|^2 dt \\ &= \int_{t_1}^{t_2} (x_{Re}(t)^2 + x_{Im}(t)^2) dt. \end{aligned}$$

$$\begin{aligned} E &= \sum_{n=n_1}^{n_2} |x[n]|^2 \\ &= \sum_{n=n_1}^{n_2} (x_{Re}[n]^2 + x_{Im}[n]^2). \end{aligned}$$

$$P_{avg} = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} |x(t)|^2 dt.$$

$$P_{avg} = \frac{1}{n_2 - n_1 + 1} \sum_{n=n_1}^{n_2} |x[n]|^2.$$

$$P_{\infty} = \lim_{T \rightarrow \infty} \frac{1}{2T} \int_{-T}^T |x(t)|^2 dt$$

$$P_{\infty} = \lim_{N \rightarrow \infty} \frac{1}{2N + 1} \sum_{n=-N}^N |x[n]|^2$$

$$\begin{aligned} x(t) &= x_{even}(t) + x_{odd}(t) \\ &= \frac{x(t) + x(-t)}{2} + \frac{x(t) - x(-t)}{2} \end{aligned}$$

$$\begin{aligned} x[n] &= x_{even}[n] + x_{odd}[n] \\ &= \frac{x[n] + x[-n]}{2} + \frac{x[n] - x[-n]}{2} \end{aligned}$$

$$x_k(t) = e^{jk\omega_0 t}, k \in \mathbb{Z}$$

$$\omega_0 = \frac{2\pi}{T}, \text{ period } T$$

$$x_k[n] = e^{jk\omega_0 n}, k \in \mathbb{Z}$$

$$\omega_0 = \frac{2\pi}{N}, \text{ period } N$$

- A *memoryless* system depends only on input at time  $t$  (or  $n$  for DT systems).
- A *linear* system satisfies  $S\{ax_1(t) + bx_2(t)\} = aS\{x_1(t)\} + bS\{x_2(t)\}$ .
- A system is *time invariant* if a time shift ( $t_0$  or  $n_0$ ) in the input results in an identical shift in the output.
- A *linear time invariant*'s impulse response  $h$  is found by calculating  $S(\delta(t))$  (or  $S(\delta[n])$ ).  $y(t) = x(t) * h(t)$  (or  $y[n] = x[n] * h[n]$ ).
- A system is *invertible* if there exists an inverse  $S_2$  such that  $S_2(S_1(x(t))) = S_1(S_2(x(t))) = x(t)$ .
- A system is *causal* if its output at time  $t$  (index  $n$ ) depends only on present and past inputs.
- A system is *stable* if there exist constants  $B, M > 0$  such that  $|x(t)| < B \forall t \implies |y(t)| < M \forall t$ .

Name	Series	Sum
Geometric	$\sum_{i=0}^n a_0 r^i$	$a_0 \frac{1-r^{n+1}}{1-r}$
Arithmetic	$\sum_{i=0}^n (a + id)$	$\frac{n+1}{2} (2a + nd)$