Distribution XML reference for Warteschlangensimulator

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This reference refers to version 4.7.1 of Warteschlangensimulator. Download address: https://github.com/A-Herzog/Warteschlangensimulator/.

When storing distribution settings to xml files the following xml tags will be used:

English version:

<ModelElementDistribution>distribution name (parameters)</modelElementDistribution>

German version:

<ModellElementVerteilung>distribution name (parameters)/ModellElementVerteilung>

The English or German version will be used when storing xml data in Warteschlangensimulator. When reading xml files Warteschlangensimulator will always understand both versions.

In the following sections the possible values for "distribution name" and the corresponding "parameters" will be listed. Distribution parameters "mean" and "sd" correspond directly to the stochastic characteristics mean and standard deviation.

Empirical data

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Empirical data (point1;point2;point3;...)
Empirische Daten (point1;point2;point3;...)
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The data points are interpreted as pdf values at equidistant points on the predefined range of the distribution.

One point distribution

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One point distribution (point)
Ein-Punkt-Verteilung (point)
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Conversion between distribution parameters and stochastic characteristics

$$mean = point$$
$$sd = 0$$

Uniform distribution

Uniform distribution (lower;upper)
Gleichverteilung (lower;upper)

$$mean = (lower + upper)/2$$

$$sd = (upper - lower)/\sqrt{12}$$

$$lower = mean - sd \cdot \sqrt{12}/2$$

$$upper = mean + sd \cdot \sqrt{12}/2$$

Exponential distribution

Exponential verteilung (mean)
Exponential distribution (mean)

Conversion between distribution parameters and stochastic characteristics

$$sd = mean$$

Normal distribution

Normal distribution (mean;sd) Normalverteilung (mean;sd)

Lognormal distribution

Lognormal distribution (mean;sd)
Lognormalverteilung (mean;sd)

Erlang distribution

Erlang distribution (shape;scale)
Erlang-Verteilung (shape;scale)

Conversion between distribution parameters and stochastic characteristics

$$mean = shape \cdot scale$$

 $sd = \sqrt{shape} \cdot scale$
 $scale = sd^2/mean$
 $shape = mean^2/sd^2$

Gamma distribution

Gamma distribution (shape;scale)
Gamma-Verteilung (shape;scale)

$$mean = shape \cdot scale$$

 $sd = \sqrt{shape} \cdot scale$
 $scale = sd^2/mean$
 $shape = mean^2/sd^2$

Beta distribution

Beta distribution (alpha; beta; lower; upper)
Beta-Verteilung (alpha; beta; lower; upper)

Conversion between distribution parameters and stochastic characteristics

$$mean = alpha/(alpha + beta) \cdot (upper - lower) + lower$$

 $sd = (upper - lower)^2 \cdot alpha \cdot beta/(alpha + beta)^2/(1 + alpha + beta)$

Cauchy distribution

Cauchy-Verteilung (median; scale)
Cauchy distribution (median; scale)

Weibull distribution

Weibull distribution (scaleInvers; shape)
Weibull-Verteilung (scaleInvers; shape)

Conversion between distribution parameters and stochastic characteristics

$$mean = scale \cdot \Gamma(1 + (1/shape))$$

$$sd = scale \cdot \sqrt{\Gamma(1 + 2/shape) - (\Gamma(1 + 1/shape))^2}$$

Chi distribution

Chi distribution (degreesOfFreedom)
Chi-Verteilung (degreesOfFreedom)

Conversion between distribution parameters and stochastic characteristics

$$\begin{split} mean &= \sqrt{2} \cdot \Gamma((degreesOfFreedom+1)/2)/\Gamma(degreesOfFreedom/2) \\ sd &= \left[(2 \cdot \Gamma(degreesOfFreedom/2) * \Gamma(1 + degreesOfFreedom/2) - (\Gamma((degreesOfFreedom+1)/2))^2)/\Gamma(degreesOfFreedom/2) \right]^{\frac{1}{2}} \end{split}$$

Chi² distribution

Chi^2 distribution (degreesOfFreedom) Chi^2-Verteilung (degreesOfFreedom) Conversion between distribution parameters and stochastic characteristics

$$mean = degreesOfFreedom$$

$$sd = \sqrt{2 \cdot degreesOfFreedom}$$

F distribution

F distribution (NumeratorDegreesOfFreedom; DenominatorDegreesOfFreedom)
F-Verteilung (NumeratorDegreesOfFreedom; DenominatorDegreesOfFreedom)

Conversion between distribution parameters and stochastic characteristics (let m := Numerator Degrees Of Freedom and n := Denominator Degrees Of Freedom)

$$\begin{split} mean &= \frac{n}{n-2} \\ sd &= \sqrt{2 \cdot n^2 \cdot \frac{m+n-2}{m \cdot (n-2) \cdot (n-2) \cdot (n-4)}} \\ m &= round \left(2 \cdot (2 \cdot \widetilde{m})^2 \cdot \frac{2 \cdot \widetilde{m} - 2}{sd^2 \cdot (2 \cdot \widetilde{m} - 2)^2 \cdot (2 \cdot \widetilde{m} - 4) - 2 \cdot (2 \cdot \widetilde{m})^2} \right) \text{ with } \widetilde{m} := mean/(mean-1) \\ n &= round (2 \cdot mean/(mean-1)) \end{split}$$

Johnson SU distribution

Johnson SU distribution (gamma;xi;delta;lambda) Johnson-SU-Verteilung (gamma;xi;delta;lambda)

Conversion between distribution parameters and stochastic characteristics

$$mean = xi - lambda \cdot \exp(1/(2 \cdot delta^2)) \cdot \sinh(gamma/delta)$$

$$sd = \sqrt{lambda^2/2 \cdot (\exp(1/delta^2) - 1) \cdot (\exp(1/delta^2) * \cosh(2 * gamma/delta) + 1)}$$

Triangular distribution

Triangular distribution (lowerBound;mostLikelyX;upperBound)
Dreiecksverteilung (lowerBound;mostLikelyX;upperBound)

$$\begin{split} mean &= (lowerBound + mostLikelyX + upperBound)/3 \\ sd &= \left[(lowerBound^2 + upperBound^2 + mostLikelyX^2 - lowerBound \cdot upperBound - lowerBound \cdot mostLikelyX - upperBound \cdot mostLikelyX)/18 \right]^{\frac{1}{2}} \\ lowerBound &= mean - sd \cdot \sqrt{6} \\ mostLikelyX &= mean \\ upperBound &= mean + sd \cdot \sqrt{6} \end{split}$$

Pert distribution

Pert distribution (lowerBound;mostLikelyX;upperBound)
Pert-Verteilung (lowerBound;mostLikelyX;upperBound)

Conversion between distribution parameters and stochastic characteristics

$$\begin{split} mean &= (lowerBound + 4 \cdot mostLikelyX + upperBound)/6 \\ sd &= \left[((lowerBound + 4 \cdot mostLikelyX + upperBound)/6 - lowerBound) \cdot \\ & (upperBound - (lowerBound + 4 \cdot mostLikelyX + upperBound)/6)/7 \right]^{\frac{1}{2}} \\ lowerBound &= mean - sd \cdot \sqrt{7} \\ mostLikelyX &= mean \\ upperBound &= mean + sd \cdot \sqrt{7} \end{split}$$

Laplace distribution

Laplace distribution (mean;b)
Laplace-Verteilung (mean;b)

Conversion between distribution parameters and stochastic characteristics

$$sd = b \cdot \sqrt{2}$$

Pareto distribution

Pareto distribution (xmin;alpha) Pareto-Verteilung (xmin;alpha)

Conversion between distribution parameters and stochastic characteristics

$$mean = alpha \cdot xmin/(alpha - 1)$$

 $sd = xmin^2 \cdot alpha/(alpha - 1)^2/(alpha - 2)$
 $alpha = mean/(mean - xmin)$

Logistic distribution

Logistic distribution (mean;s)
Logistische Verteilung (mean;s)

Conversion between distribution parameters and stochastic characteristics

$$sd = s \cdot \pi / \sqrt{3}$$

Inverse gaussian distribution

Inverse gaussian distribution (lambda;mu)
Inverse Gauß-Verteilung (lambda;mu)

Conversion between distribution parameters and stochastic characteristics

$$mean = mu$$

 $sd = mu \cdot \sqrt{mu/lambda}$
 $lambda = mean^3/sd^2$

Rayleigh distribution

Rayleigh distribution (mean)
Rayleigh-Verteilung (mean)

Conversion between distribution parameters and stochastic characteristics

$$sd = \sqrt{(4-\pi)/2} \cdot \sqrt{2/\pi} \cdot mean$$

Log-logistic distribution

Log-logistic distribution (alpha; beta) Log-Logistische Verteilung (alpha; beta)

Conversion between distribution parameters and stochastic characteristics

$$mean = alpha \cdot \pi/beta/\sin(\pi/beta)$$

$$sd = alpha \cdot \sqrt{2 \cdot \pi/beta/\sin(2 \cdot \pi/beta) - \pi^2/beta^2}/\sin(\pi/beta)$$

Power distribution

Power distribution (a;b;c) Potenzverteilung (a;b;c)

Conversion between distribution parameters and stochastic characteristics

$$mean = a + (b-a) \cdot c/(c+1)$$

$$sd = (b-a)/(c+1) \cdot \sqrt{c/(c+2)}$$

Gumbel distribution

Gumbel distribution (mean;sd)
Gumbel-Verteilung (mean;sd)

Fatigue life distribution

Fatigue life distribution (mu;beta;gamma) Fatigue-Life-Verteilung (mu;beta;gamma)

$$mean = mu + beta \cdot (1 + gamma \cdot gamma/2)$$

 $sd = beta \cdot gamma \cdot \sqrt{1 + 5 \cdot gamma^2/4}$

Frechet distribution

Frechet distribution (delta; beta; alpha)
Frechet-Verteilung (delta; beta; alpha)

Conversion between distribution parameters and stochastic characteristics

$$mean = delta + beta \cdot gamma(1 - 1/alpha)$$

$$sd = beta \cdot \sqrt{gamma(1 - 2/alpha) - gamma(1 - 1/alpha)^2}$$

Hyperbolic secant distribution

Hyperbolic secant distribution (mean;sd)
Hyperbolische Sekanten-Verteilung (mean;sd)