# Distribution XML reference for Warteschlangensimulator

ALEXANDER HERZOG (alexander.herzog@tu-clausthal.de)

This reference refers to version 5.8.0 of Warteschlangensimulator. Download address: https://a-herzog.github.io/Warteschlangensimulator/.

When storing distribution settings to xml files the following xml tags will be used:

English version:

<ModelElementDistribution>distribution name (parameters)</modelElementDistribution>

German version:

<ModellElementVerteilung>distribution name (parameters)/ModellElementVerteilung>

The English or German version will be used when storing xml data in Warteschlangensimulator. When reading xml files Warteschlangensimulator will always understand both versions.

In the following sections the possible values for "distribution name" and the corresponding "parameters" will be listed. Distribution parameters "mean" and "sd" correspond directly to the stochastic characteristics mean and standard deviation.

## **Empirical data**

```
Empirical data (point1;point2;point3;...)
Empirische Daten (point1;point2;point3;...)
```

The data points are interpreted as pdf values at equidistant points on the predefined range of the distribution.

# One point distribution

```
One point distribution (point)
Ein-Punkt-Verteilung (point)
```

Conversion between distribution parameters and stochastic characteristics

$$mean = point$$
$$sd = 0$$

#### Uniform distribution

Uniform distribution (lower;upper)
Gleichverteilung (lower;upper)

$$mean = (lower + upper)/2$$

$$sd = (upper - lower)/\sqrt{12}$$

$$lower = mean - sd \cdot \sqrt{12}/2$$

$$upper = mean + sd \cdot \sqrt{12}/2$$

## **Exponential distribution**

Exponential verteilung (mean)
Exponential distribution (mean)

Conversion between distribution parameters and stochastic characteristics

$$sd = mean$$

#### Normal distribution

Normal distribution (mean;sd) Normalverteilung (mean;sd)

## Lognormal distribution

Lognormal distribution (mean;sd) Lognormalverteilung (mean;sd)

# **Erlang distribution**

Erlang distribution (shape;scale)
Erlang-Verteilung (shape;scale)

Conversion between distribution parameters and stochastic characteristics

$$mean = shape \cdot scale$$
  
 $sd = \sqrt{shape} \cdot scale$   
 $scale = sd^2/mean$   
 $shape = mean^2/sd^2$ 

## **Gamma distribution**

Gamma distribution (shape;scale)
Gamma-Verteilung (shape;scale)

$$mean = shape \cdot scale$$
  
 $sd = \sqrt{shape} \cdot scale$   
 $scale = sd^2/mean$   
 $shape = mean^2/sd^2$ 

#### Beta distribution

Beta distribution (alpha; beta; lower; upper)
Beta-Verteilung (alpha; beta; lower; upper)

Conversion between distribution parameters and stochastic characteristics

$$mean = alpha/(alpha + beta) \cdot (upper - lower) + lower$$
  
 $sd = (upper - lower)^2 \cdot alpha \cdot beta/(alpha + beta)^2/(1 + alpha + beta)$ 

## **Cauchy distribution**

Cauchy-Verteilung (median; scale)
Cauchy distribution (median; scale)

#### Weibull distribution

Weibull distribution (scaleInvers; shape)
Weibull-Verteilung (scaleInvers; shape)

Conversion between distribution parameters and stochastic characteristics

$$mean = scale \cdot \Gamma(1 + (1/shape))$$
 
$$sd = scale \cdot \sqrt{\Gamma(1 + 2/shape) - (\Gamma(1 + 1/shape))^2}$$

#### Chi distribution

Chi distribution (degreesOfFreedom)
Chi-Verteilung (degreesOfFreedom)

Conversion between distribution parameters and stochastic characteristics

$$\begin{split} mean &= \sqrt{2} \cdot \Gamma((degreesOfFreedom+1)/2)/\Gamma(degreesOfFreedom/2) \\ sd &= \left[ (2 \cdot \Gamma(degreesOfFreedom/2) * \Gamma(1 + degreesOfFreedom/2) - (\Gamma((degreesOfFreedom+1)/2))^2)/\Gamma(degreesOfFreedom/2) \right]^{\frac{1}{2}} \end{split}$$

## Chi<sup>2</sup> distribution

Chi^2 distribution (degreesOfFreedom) Chi^2-Verteilung (degreesOfFreedom) Conversion between distribution parameters and stochastic characteristics

$$mean = degreesOfFreedom$$
 
$$sd = \sqrt{2 \cdot degreesOfFreedom}$$

#### F distribution

F distribution (NumeratorDegreesOfFreedom; DenominatorDegreesOfFreedom) F-Verteilung (NumeratorDegreesOfFreedom; DenominatorDegreesOfFreedom)

Conversion between distribution parameters and stochastic characteristics (let m := Numerator Degrees Of Freedom and n := Denominator Degrees Of Freedom)

$$\begin{split} mean &= \frac{n}{n-2} \\ sd &= \sqrt{2 \cdot n^2 \cdot \frac{m+n-2}{m \cdot (n-2) \cdot (n-2) \cdot (n-4)}} \\ m &= round \left( 2 \cdot (2 \cdot \widetilde{m})^2 \cdot \frac{2 \cdot \widetilde{m} - 2}{sd^2 \cdot (2 \cdot \widetilde{m} - 2)^2 \cdot (2 \cdot \widetilde{m} - 4) - 2 \cdot (2 \cdot \widetilde{m})^2} \right) \text{ with } \widetilde{m} := mean/(mean-1) \\ n &= round (2 \cdot mean/(mean-1)) \end{split}$$

#### Johnson SU distribution

Johnson SU distribution (gamma;xi;delta;lambda) Johnson-SU-Verteilung (gamma;xi;delta;lambda)

Conversion between distribution parameters and stochastic characteristics

$$mean = xi - lambda \cdot \exp(1/(2 \cdot delta^2)) \cdot \sinh(gamma/delta)$$
 
$$sd = \sqrt{lambda^2/2 \cdot (\exp(1/delta^2) - 1) \cdot (\exp(1/delta^2) * \cosh(2 * gamma/delta) + 1)}$$

# Triangular distribution

Triangular distribution (lowerBound;mostLikelyX;upperBound)
Dreiecksverteilung (lowerBound;mostLikelyX;upperBound)

$$\begin{split} mean &= (lowerBound + mostLikelyX + upperBound)/3 \\ sd &= \left[ (lowerBound^2 + upperBound^2 + mostLikelyX^2 - lowerBound \cdot upperBound - lowerBound \cdot mostLikelyX - upperBound \cdot mostLikelyX)/18 \right]^{\frac{1}{2}} \\ lowerBound &= mean - sd \cdot \sqrt{6} \\ mostLikelyX &= mean \\ upperBound &= mean + sd \cdot \sqrt{6} \end{split}$$

# Trapezoid distribution

Trapezoid distribution (a;b;c;d)
Trapezverteilung (a;b;c;d)

Conversion between distribution parameters and stochastic characteristics

$$\begin{array}{lll} h & = & \frac{2}{c+d-a-b} \\ \\ mean & = & h \cdot 16 \left( \frac{d^3-c^3}{d-c} - \frac{b^3-a^3}{b-a} \right) \\ \\ sd = \sqrt{h \cdot 112 \left( \frac{d^4-c^4}{d-c} - \frac{b^4-a^4}{b-a} \right) - mean^2} \end{array}$$

#### Pert distribution

Pert distribution (lowerBound;mostLikelyX;upperBound)
Pert-Verteilung (lowerBound;mostLikelyX;upperBound)

Conversion between distribution parameters and stochastic characteristics

$$\begin{split} mean &= (lowerBound + 4 \cdot mostLikelyX + upperBound)/6 \\ sd &= \left[ ((lowerBound + 4 \cdot mostLikelyX + upperBound)/6 - lowerBound) \cdot \\ & (upperBound - (lowerBound + 4 \cdot mostLikelyX + upperBound)/6)/7 \right]^{\frac{1}{2}} \\ lowerBound &= mean - sd \cdot \sqrt{7} \\ mostLikelyX &= mean \\ upperBound &= mean + sd \cdot \sqrt{7} \end{split}$$

# Laplace distribution

Laplace distribution (mean;b)
Laplace-Verteilung (mean;b)

Conversion between distribution parameters and stochastic characteristics

$$sd = b \cdot \sqrt{2}$$

#### Pareto distribution

Pareto distribution (xmin;alpha) Pareto-Verteilung (xmin;alpha)

$$mean = alpha \cdot xmin/(alpha - 1)$$
  
 $sd = xmin^2 \cdot alpha/(alpha - 1)^2/(alpha - 2)$   
 $alpha = mean/(mean - xmin)$ 

## Logistic distribution

Logistic distribution (mean;s)
Logistische Verteilung (mean;s)

Conversion between distribution parameters and stochastic characteristics

$$sd = s \cdot \pi / \sqrt{3}$$

## Inverse gaussian distribution

Inverse gaussian distribution (lambda;mu)
Inverse Gauß-Verteilung (lambda;mu)

Conversion between distribution parameters and stochastic characteristics

$$mean = mu$$
  
 $sd = mu \cdot \sqrt{mu/lambda}$   
 $lambda = mean^3/sd^2$ 

## Rayleigh distribution

Rayleigh distribution (mean)
Rayleigh-Verteilung (mean)

Conversion between distribution parameters and stochastic characteristics

$$sd = \sqrt{(4-\pi)/2} \cdot \sqrt{2/\pi} \cdot mean$$

# Log-logistic distribution

Log-logistic distribution (alpha; beta) Log-Logistische Verteilung (alpha; beta)

Conversion between distribution parameters and stochastic characteristics

$$mean = alpha \cdot \pi/beta/\sin(\pi/beta)$$
$$sd = alpha \cdot \sqrt{2 \cdot \pi/beta/\sin(2 \cdot \pi/beta) - \pi^2/beta^2}/\sin(\pi/beta)$$

#### Power distribution

Power distribution (a;b;c) Potenzverteilung (a;b;c)

$$mean = a + (b-a) \cdot c/(c+1)$$
$$sd = (b-a)/(c+1) \cdot \sqrt{c/(c+2)}$$

#### **Gumbel distribution**

Gumbel distribution (mean;sd)
Gumbel-Verteilung (mean;sd)

## **Fatigue life distribution**

Fatigue life distribution (mu;beta;gamma) Fatigue-Life-Verteilung (mu;beta;gamma)

Conversion between distribution parameters and stochastic characteristics

$$mean = mu + beta \cdot (1 + gamma \cdot gamma/2)$$
  
 $sd = beta \cdot gamma \cdot \sqrt{1 + 5 \cdot gamma^2/4}$ 

#### Frechet distribution

Frechet distribution (delta; beta; alpha)
Frechet-Verteilung (delta; beta; alpha)

Conversion between distribution parameters and stochastic characteristics

$$mean = delta + beta \cdot gamma(1 - 1/alpha)$$
  
 $sd = beta \cdot \sqrt{gamma(1 - 2/alpha) - gamma(1 - 1/alpha)^2}$ 

# Hyperbolic secant distribution

Hyperbolic secant distribution (mean;sd)
Hyperbolische Sekanten-Verteilung (mean;sd)

#### Left sawtooth distribution

Left sawtooth distribution (a;b)

Linke Sägezahnverteilung (a;b) Conversion between distribution parameters and stochastic characteristics

$$mean = (2 \cdot a + b)/2$$
$$sd = (b - a)^2/18$$

# Right sawtooth distribution

Right sawtooth distribution (a;b)

Rechte Sägezahnverteilung (a;b) Conversion between distribution parameters and stochastic characteristics

$$mean = (a + 2 \cdot b)/2$$
$$sd = (b - a)^2/18$$

## Levy distribution

Levy distribution (mu;c) Levy-Verteilung (mu;c)

#### Maxwell Boltzmann distribution

Maxwell Boltzmann distribution (a) Maxwell-Boltzmann-Verteilung (a)

$$mean = 2 \cdot a\sqrt{\frac{2}{\pi}}$$
 
$$sd = \sqrt{\frac{a^2(3\pi - 8)}{\pi}}$$
 
$$modus = a\sqrt{2}$$
 
$$a = \frac{mean}{2} \cdot \sqrt{\frac{\pi}{2}}$$

## Student t-distribution

Student t-distribution (mu;nu)

Studentsche t-Verteilung (mu; nu) Conversion between distribution parameters and stochastic characteristics

$$mean = \mu$$

$$sd = \sqrt{\frac{\nu}{\nu - 2}} \text{ for } \nu > 2$$

## Half normal distribution

Halbe Normalverteilung (s;mu)
Half normal distribution (s;mu)

$$\theta = \frac{1}{\mu}$$

$$mean = \frac{1}{\theta} + s$$

$$sd = \frac{\pi - 2}{2\theta^2}$$

# **U-quadratic distribution**

U-quadratische Verteilung (a;b) U-quadratic distribution (a;b)

Conversion between distribution parameters and stochastic characteristics

$$mean = \frac{a+b}{2}$$

$$sd = \frac{3}{20} \cdot (b-a)^2$$

$$a = mean - \frac{\sqrt{sd^2 \cdot \frac{20}{3}}}{2}$$

$$b = mean + \frac{\sqrt{sd^2 \cdot \frac{20}{3}}}{2}$$

# Reciprocal distribution

Reziproke Verteilung (a;b)
Reciprocal distribution (a;b)

Conversion between distribution parameters and stochastic characteristics

$$\begin{split} mean &= \frac{b-a}{\log\left(\frac{b}{a}\right)} \\ sd &= \sqrt{\frac{b^2-a^2}{\log\left(\frac{b}{a}\right)} - \left(\frac{b-a}{\log\left(\frac{b}{a}\right)}\right)^2} \end{split}$$

# Kumaraswamy distribution

Kumaraswamy-Verteilung (a;b;c;d)
Kumaraswamy distribution (a;b;c;d)

$$\begin{split} mean_{\text{unscaled}} &= \frac{b\Gamma\left(1 + \frac{1}{a}\right)\Gamma(b)}{\Gamma\left(1 + \frac{1}{a} + b\right)} \\ sd_{\text{unscaled}} &= \sqrt{\frac{b\Gamma\left(1 + \frac{2}{a}\right)\Gamma(b)}{\Gamma\left(1 + \frac{2}{a} + b\right)} - mean_{\text{unscaled}}^2} \\ mean &= mean_{\text{unscaled}} \cdot (d - c) + c \\ sd &= sd_{\text{unscaled}} \cdot (d - c) + c \end{split}$$

## **Irwin-Hall distribution**

Irwin-Hall-Verteilung (n)
Irwin-Hall distribution (n)

Conversion between distribution parameters and stochastic characteristics

$$mean = \frac{n}{2}$$
 
$$sd = \sqrt{\frac{n}{12}}$$

#### Sine distribution

Sinus-Verteilung (a;b) sine distribution (a;b)

Conversion between distribution parameters and stochastic characteristics

$$mean = \frac{a+b}{2}$$

$$sd = \sqrt{\frac{1}{4} - \frac{2}{\pi^2}} \cdot (b-a)^2$$

#### **Arcsine distribution**

Arcus Sinus-Verteilung (a;b) arcsine distribution (a;b)

Conversion between distribution parameters and stochastic characteristics

$$mean = \frac{a+b}{2}$$
 
$$sd = \frac{1}{8} \cdot (b-a)^2$$

# Wigner half-circle distribution

Wigner Halbkreis-Verteilung (m;R)
Wigner half-circle distribution (m;R)

Conversion between distribution parameters and stochastic characteristics

$$mean = m$$
$$sd = \frac{R}{2}$$

# Log-Cauchy distribution

Log-Cauchy-Verteilung (mu;sigma)
Log-Cauchy distribution (mu;sigma)

Conversion between distribution parameters and stochastic characteristics

$$median = \exp(mu)$$

#### Geometric distribution

Geometric distribution (p) Geometrische Verteilung (p) Conversion between distribution parameters and stochastic characteristics

$$mean = \frac{1-p}{p}$$
 
$$sd = \sqrt{\frac{1-p}{p^2}}$$
 
$$p = \frac{1}{1+mean}$$

## Hypergeometric distribution

Hypergeometric distribution (N;K;n) Hypergeometrische Verteilung (N;K;n) Conversion between distribution parameters and stochastic characteristics

$$mean = \frac{n \cdot K}{N}$$
 
$$sd = \sqrt{\frac{n \cdot K}{N} \cdot \left(1 - \frac{K}{N}\right) \cdot \frac{N - n}{N - 1}}$$

## **Binomial distribution**

Binomial distribution (n;p) Binomialverteilung (n;p) Conversion between distribution parameters and stochastic characteristics

$$mean = n \cdot p$$

$$sd = \sqrt{n \cdot p \cdot (1 - p)}$$

$$n = \frac{mean}{p}$$

$$p = 1 - \frac{sd^2}{mean}$$

## Poisson distribution

Poisson distribution (lambda) Poisson-Verteilung (lambda)

$$mean = \lambda$$
$$sd = \lambda$$

## **Negative binomial distribution**

Negative binomial distribution (n;r) Negative Binomialverteilung (n;r)

$$mean = r(1-p)/p$$
 
$$sd = \sqrt{\frac{r(1-p)}{p^2}}$$
 
$$p = \frac{mean}{sd^2}$$
 
$$r = \frac{mean \cdot p}{1-p}$$

# **Negative Hypergeometric distribution**

Negative hypergeometric distribution (N;K;n) Negative hypergeometrische Verteilung (N;K;n) Conversion between distribution parameters and stochastic characteristics

$$mean = n \cdot \frac{N+1}{R+1}$$
 
$$sd = \sqrt{n \cdot \frac{(R+1-n)(N-R)(N+1)}{(R+1)^2(R+2)}}$$

## Zeta distribution

Zeta distribution (s) Zeta-Verteilung (s)

$$mean = \frac{\zeta(s-1)}{\zeta(s)}$$
 
$$sd = \sqrt{\frac{\zeta(s)\zeta(s-2) - \zeta(s-1)^2}{\zeta(s)^2}}$$

## Discrete uniform distribution

Discrete uniform distribution (a;b) Diskrete Gleichverteilung (n;r)

$$\begin{array}{lll} mean & = & \frac{a+b}{2} \\ sd & = & \frac{(b-a+1)^2-1}{12} \\ b = \frac{\sqrt{(12\cdot sd^2+1)}}{2} + mean - \frac{1}{2} \\ a & = 2\cdot mean - b \end{array}$$

# Logarithmic distribution

Logarithmic distribution (p) Logarithmische Verteilung (p) Conversion between distribution parameters and stochastic characteristics

$$mean = -\frac{p}{(1-p)\log(1-p)}$$

## **Borel distribution**

$$mean = \frac{1}{1 - \mu}$$
$$variance = \frac{\mu}{(1 - \mu)^3}$$