

- b. Possibly skip some items.
  - c. Don't get more than 2 of any particular item.
- 2. After a late night of math studying, you and your friends decide to go to your favorite tax-free fast food Mexican restaurant, *Burrito Chime*. You decide to order off of the dollar menu, which has 6 items. Your group has \$17 to spend (and will spend all of it).
  - a. How many different orders are possible? (The *order* in which the order is placed does not matter - just which and how many of each item that is ordered.)
  - b. How many different orders are possible if you want to get at least one of each item?
  - c. How many different orders are possible if you don't get more than 4 of any one item?
- 3. After another gym class you are tasked with putting the 14 identical dodgeballs away into 5 bins. This time, no bin can hold more than 6 balls. How many ways can you clean up?
- 4. Consider the equation  $x_1 + x_2 + x_3 + x_4 = 19$ . How many solutions are there with  $1 \leq x_i \leq 6$  for all  $i \in \{1, 2, 3, 4\}$ ?
- 5. Suppose you planned on giving 7 gold stars to some of the 12 star students in your class. Each student can receive at most one star. How many ways can you do this?
  - a. Use Pascal's triangle to find the numeric answer.
  - a. Use the Principle of Inclusion and Exclusion.
- 6. How many permutations of  $\{1, 2, 3, 4\}$  leave exactly 1 element fixed?
- 7. 12 ladies of a certain age drop off their red hats at the hat check of a museum. As they are leaving, the hat check attendant gives the hats back randomly. In how many ways can exactly 8 of the ladies receive their own hat (and the other 4 not)?
- 8. The Grinch sneaks into a room with 8 Christmas presents to 8 different people. He proceeds to switch the name-labels on the presents. How many ways could he do this if:
  - a. No present is allowed to end up with its original label? Explain what each term in your answer represents.
  - b. Exactly 4 presents keep their original labels? Explain.
  - c. Exactly 7 presents keep their original labels? Explain.