

propagated with velocity  $c$  when measured in the moving system. For a ray of light emitted at the time  $\tau = 0$  in the direction of the increasing  $\xi$

$$\xi = c\tau \text{ or } \xi = ac \left( t - \frac{v}{c^2 - v^2} x' \right).$$

But the ray moves relatively to the initial point of  $k$ , when measured in the stationary system, with the velocity  $c - v$ , so that

$$\frac{x'}{c - v} = t.$$

If we insert this value of  $t$  in the equation for  $\xi$ , we obtain

$$\xi = a \frac{c^2}{c^2 - v^2} x'.$$

In an analogous manner we find, by considering rays moving along the two other axes, that

$$\eta = c\tau = ac \left( t - \frac{v}{c^2 - v^2} x' \right)$$

when

$$\frac{y}{\sqrt{c^2 - v^2}} = t, \quad x' = 0.$$

Thus

$$\eta = a \frac{c}{\sqrt{c^2 - v^2}} y \text{ and } \zeta = a \frac{c}{\sqrt{c^2 - v^2}} z.$$

Substituting for  $x'$  its value, we obtain

$$\begin{aligned} \tau &= \phi(v) \beta (t - vx/c^2), \\ \xi &= \phi(v) \beta (t - vt), \\ \eta &= \phi(v) y, \\ \zeta &= \phi(v) z, \end{aligned}$$

where

$$\beta = \frac{1}{\sqrt{1 - v^2/c^2}},$$

and  $\phi$  is an as yet unknown function of  $v$ . If no assumption whatever be made as to the initial position of the moving system and as to the zero point of  $\tau$ , an additive constant is to be placed on the right side of each of these equations.