

In this case, the Σ symbol lets us know that this is a sum. The $i = 1$ serves two functions. It tells us that the index variable is i , and that i has a starting value of 1. The 10 is the final value, and the $(i + 2)$ to the right of the Σ is the formula. The i in the formula, takes each integer value from the starting value (1) to the final value (10). Therefore we have:

$$\sum_{i=1}^{10} (i + 2) = 3 + 4 + 5 + 6 + 7 + 8 + 9 + 10 + 11 + 12 = 75.$$



This notation has a lot of flexibility. For example, the sum's formula can be a constant value:

$$\sum_{i=1}^{10} 5 = 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 50.$$

Or we could have the index as an exponent:

$$\sum_{i=1}^{10} (2^i) = 2^1 + 2^2 + 2^3 + 2^4 + 2^5 + 2^6 + 2^7 + 2^8 + 2^9 + 2^{10}$$

Now all the examples so far have a numerical value that can be calculated. However, summation notation can also be used to express functions of variables such as:

$$\sum_{i=1}^{10} (x^i) = x^1 + x^2 + x^3 + x^4 + x^5 + x^6 + x^7 + x^8 + x^9 + x^{10}$$

Note that any variables in the formula that do not match the index are left as variables (such as x in the previous example). While we do not know what the sum value is other than in terms of x , we can much more concisely state the sum in sigma notation.

Another typical use for the index in the formula is to denote an index in a coefficient. Consider the polynomial:

$$ax^2 + bx + c.$$

Instead of using a different letter, we can use a subscript to denote a different value but use the same letter:

$$a_2x^2 + a_1x + a_0.$$