

Experimental design

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“To call in the statistician after the experiment is done may be no more than asking him to perform a postmortem examination: he may be able to say what the experiment died of.”

Sir Ronald Fisher, Indian Statistical Congress, Sankhya, around 1938



Stephen John Senn
@stephensenn



 Follow

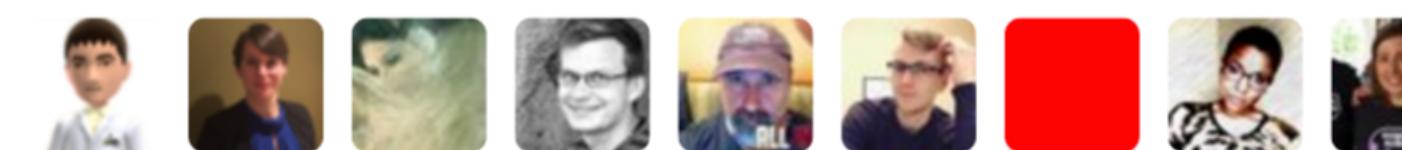
Statisticians are the bad fairies of research.
People forget to invite them until it's too late, at
which point they send everyone to sleep.

RETWEETS

92

LIKES

93



11:22 AM - 21 Feb 2016

Different types of experiments

Learning experiment questions	Confirming experiment questions
<ul style="list-style-type: none">• Does the drug have toxic side effects (at what dose, given for how long, in which tissue)?• Does stress affect rodent behaviour (what kind of stress, for how long, on what behavioural tasks)?• How does exercise affect cognitive functioning of older people (what type of exercise, how much, which aspect of cognition)?	<ul style="list-style-type: none">• Does 5 mg/kg of the drug given once a day for 5 days increase blood creatinine^a concentration?• Does fox urine odour (a stressor) affect the amount of food Wistar rats consume during the first 24 hours after exposure?• Does 30 min of aerobic activity (treadmill running) at 60% VO₂ max^b, 3 days a week for 6 weeks, in males between 55–70 years of age, improve performance on a mental rotation task?

^a Increased creatinine indicates kidney damage.

^b VO₂ max is the maximal oxygen uptake and is a measure of a person's aerobic fitness.

What is experimental design?

The organization of an experiment, to ensure that the **right type** of data, and **enough** of it, is available to answer the **questions of interest** as clearly and efficiently as possible.

What is **bad** experimental design?

Analysis batch I / Study center I / Processing protocol I ...

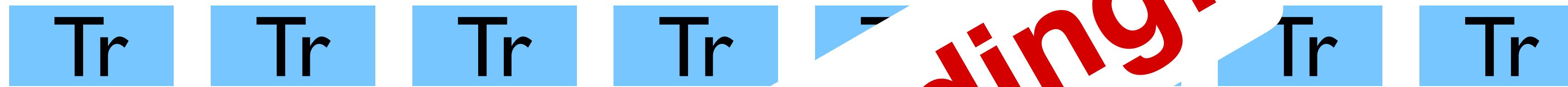
Tr Tr Tr Tr Tr Tr Tr Tr

Analysis batch II / Study center II / Processing protocol II ...

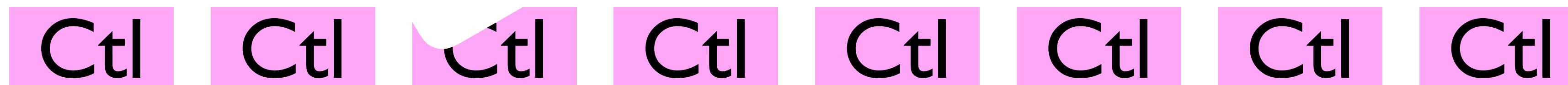
Ctl Ctl Ctl Ctl Ctl Ctl Ctl Ctl

What is **bad** experimental design?

Analysis batch I / Study center I / Processing protocol I ...



Analysis batch II / Study center II / Processing protocol II ...



Confounding!

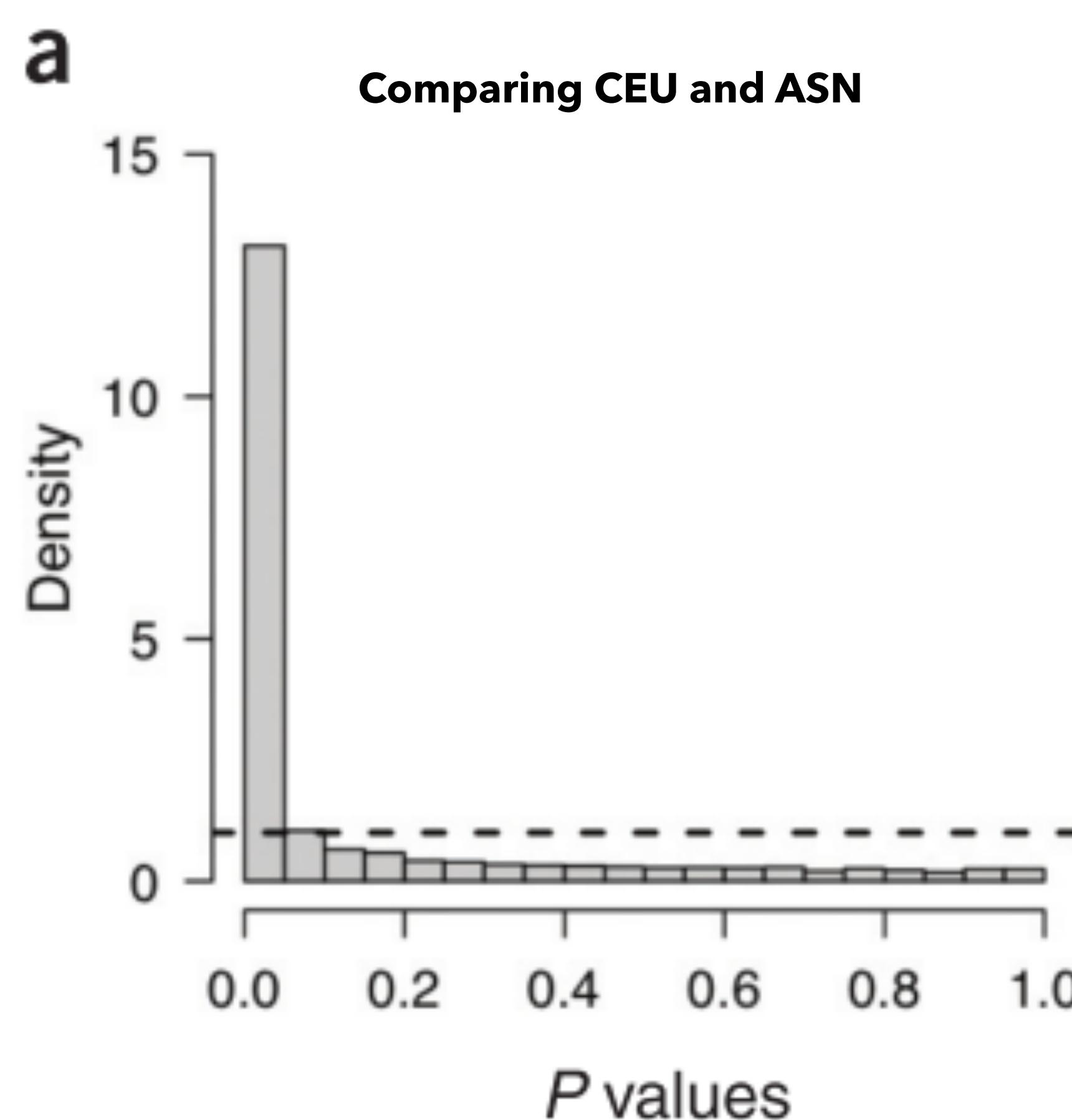
What can happen with bad experimental design?

- Example: gene expression study comparing 60 CEU and 82 ASN HapMap individuals
- 26% of the genes were found to be significantly differentially expressed (78% with less restrictive multiple testing correction)
- **But:** all CEU samples were processed (sometimes years) before all the ASN samples!

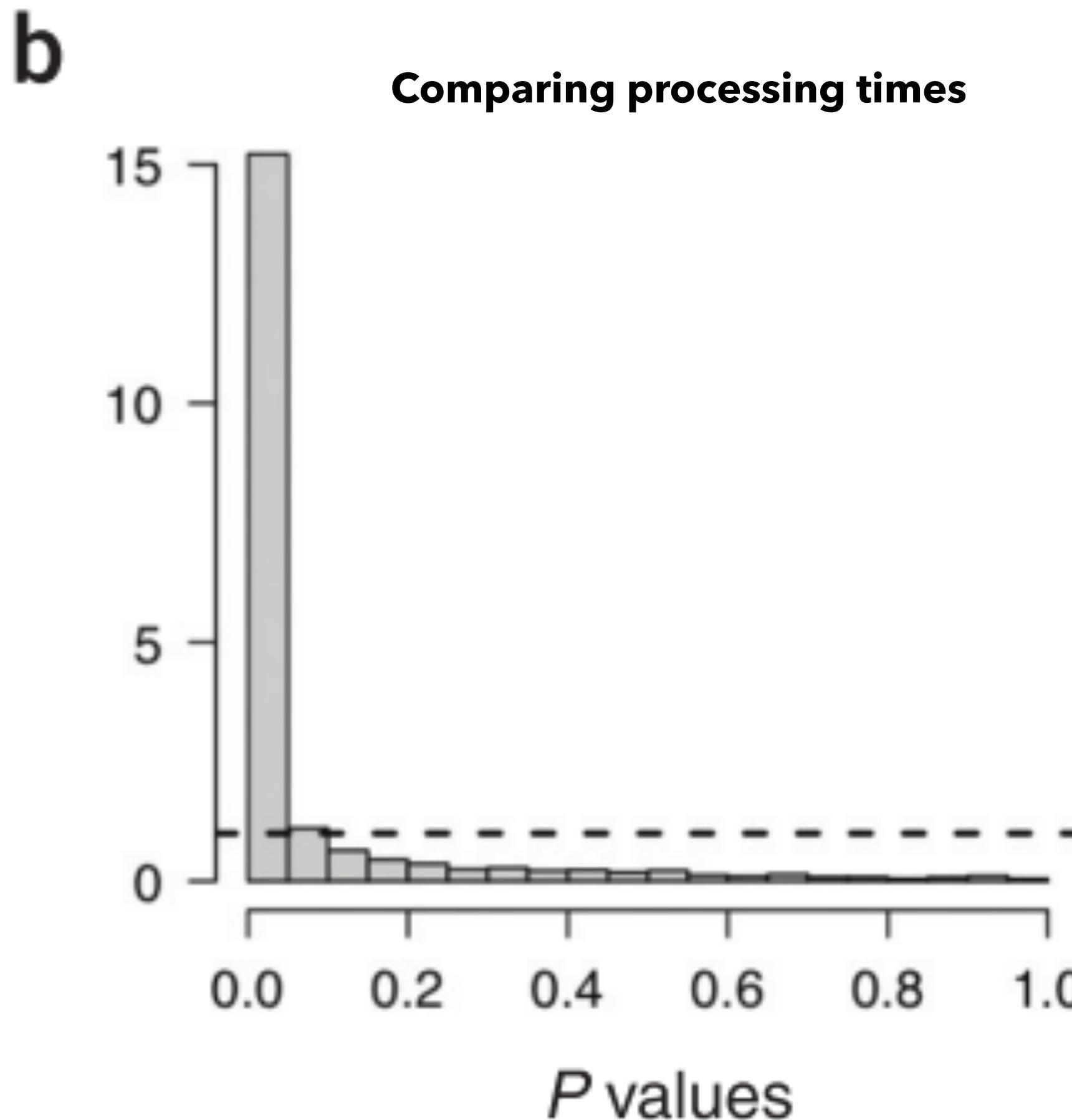
What can happen with bad experimental design?

- Example: gene expression study comparing 111 CEU and 82 ASN HapMap individuals
 - 26% of the genes were significantly differentially expressed (78% with less resampling after FDR multiple testing correction)
 - **But:** all CEU samples were processed (sometimes years) before all the ASN samples!
- Confounding!**

What can happen with bad experimental design?



78% differentially expressed



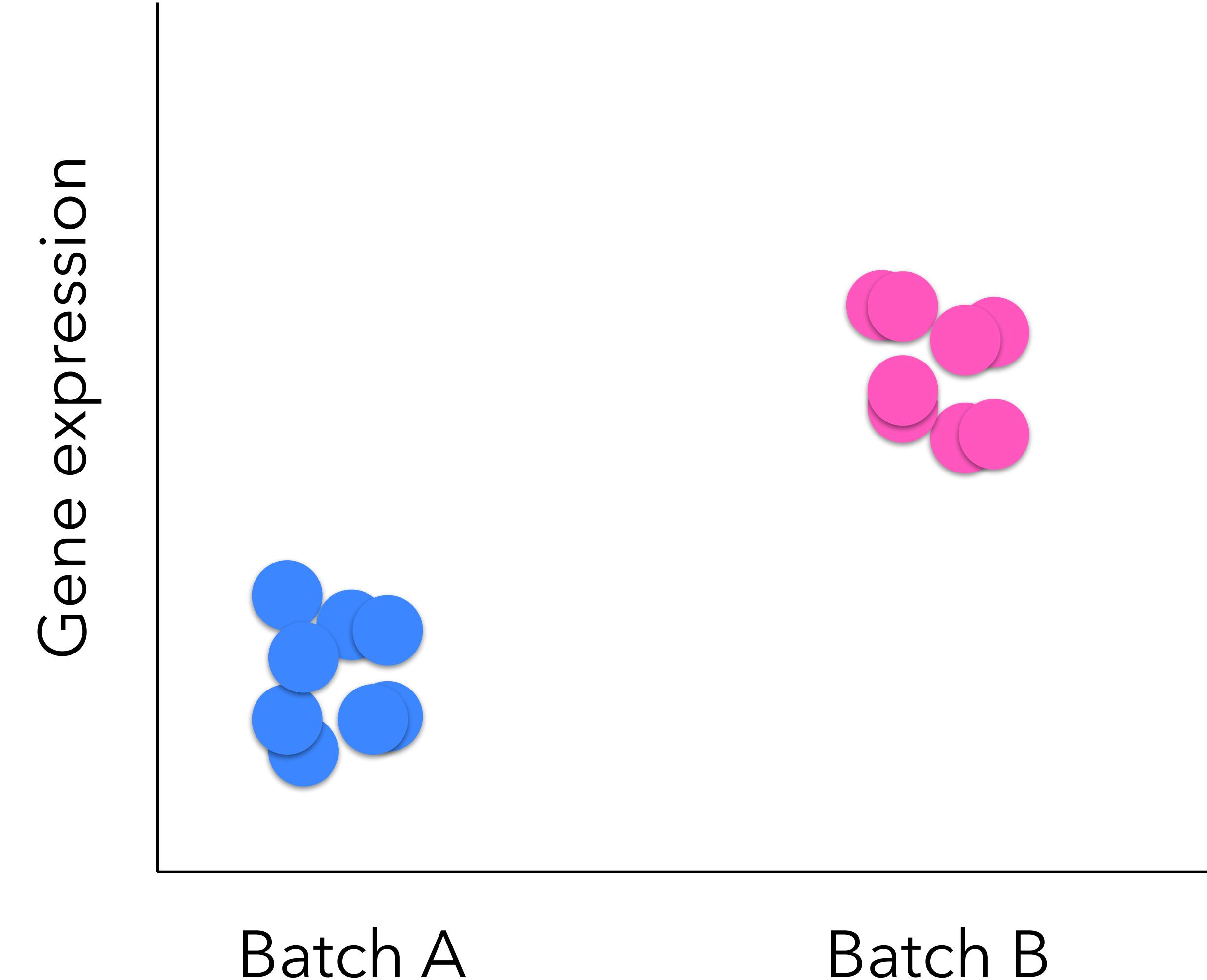
96% differentially expressed

What would be a better experimental design?

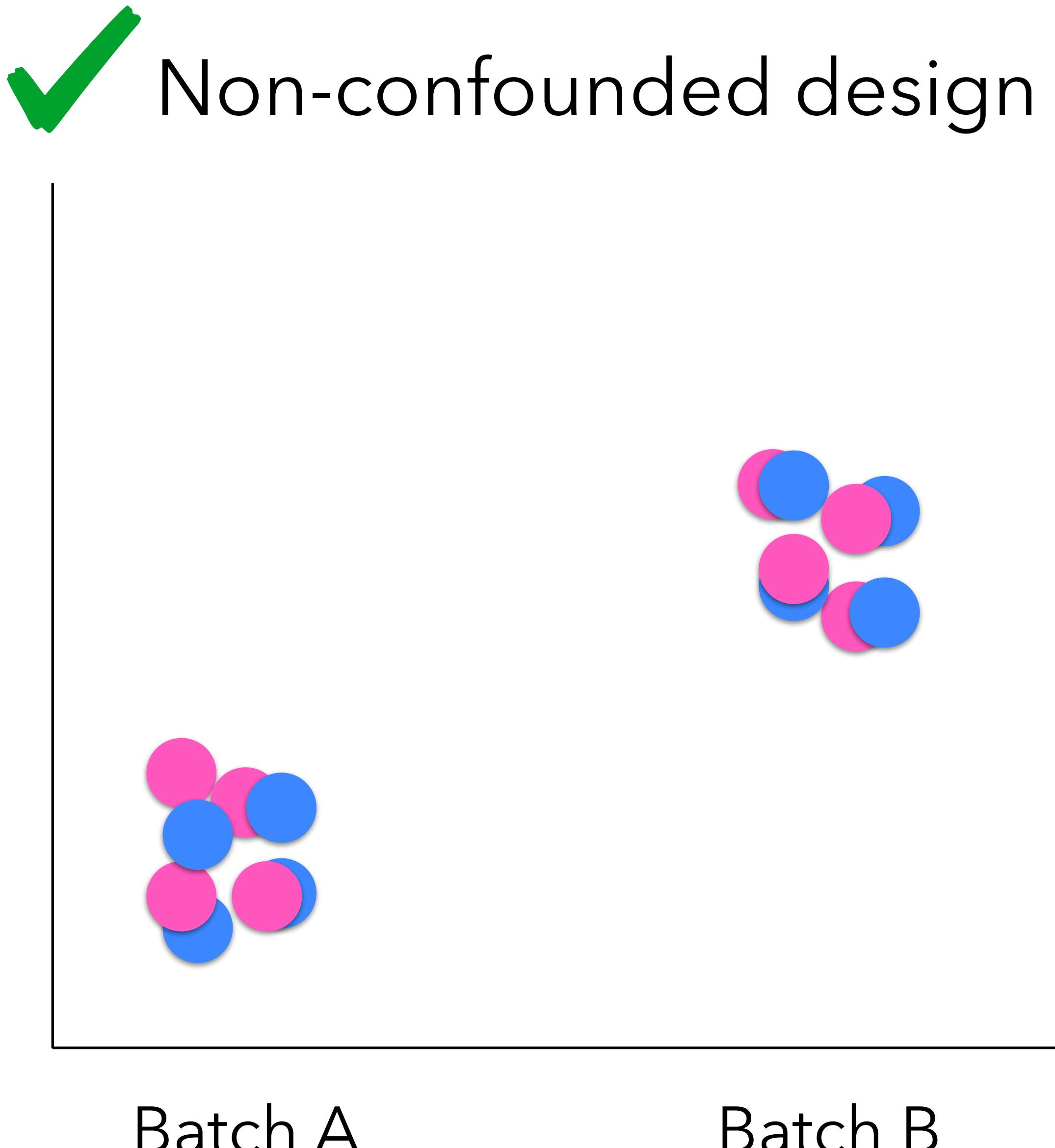
- Process all samples at the same time/in one batch (not always feasible)
- Minimize confounding as much as possible through
 - blocking
 - randomization
- Batch effects may still be present, but with an appropriate design we can account for them

Nonzero batch effect
Zero treatment effect

X Confounded design



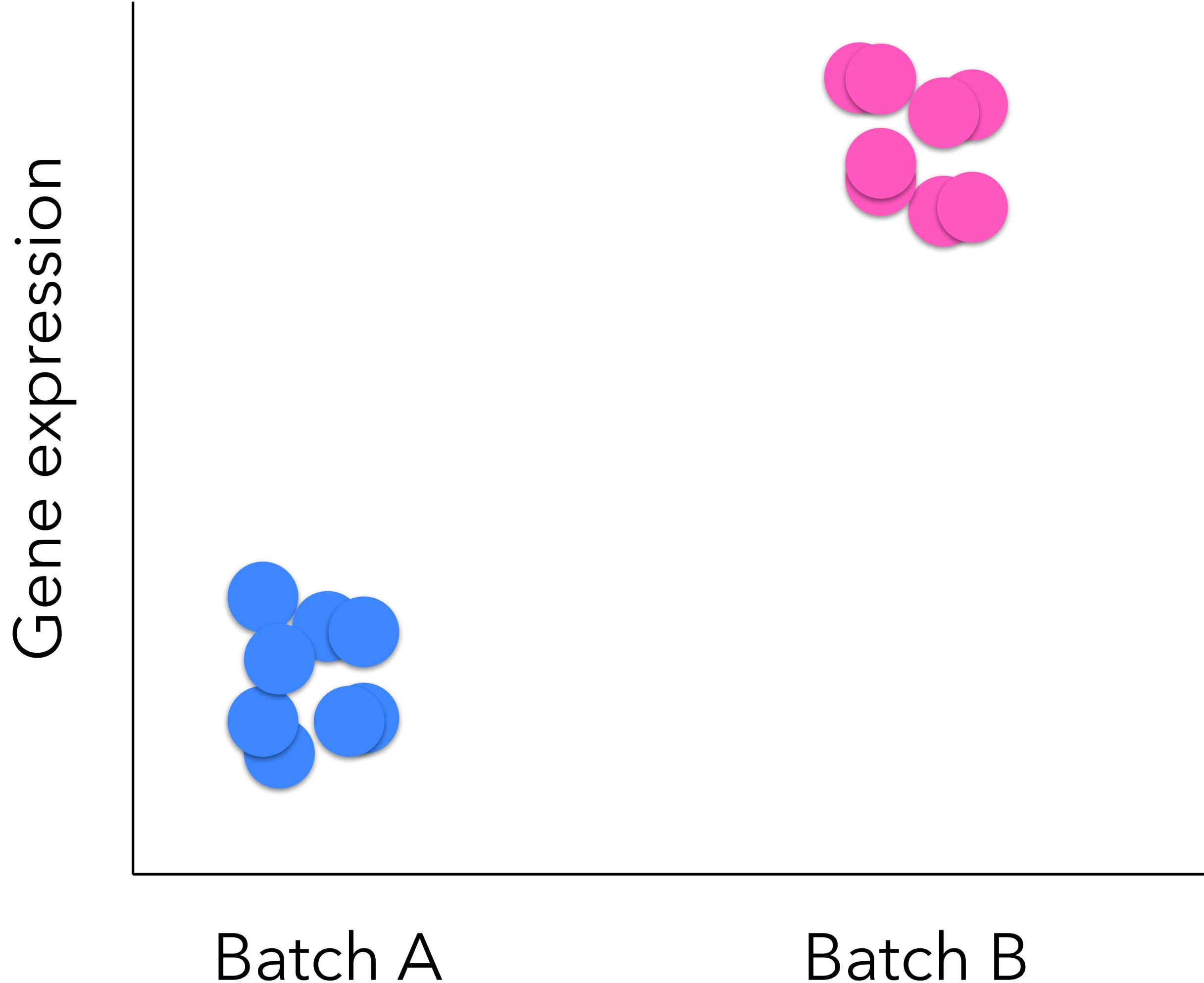
Treated
Untreated



Nonzero batch effect

Nonzero treatment effect

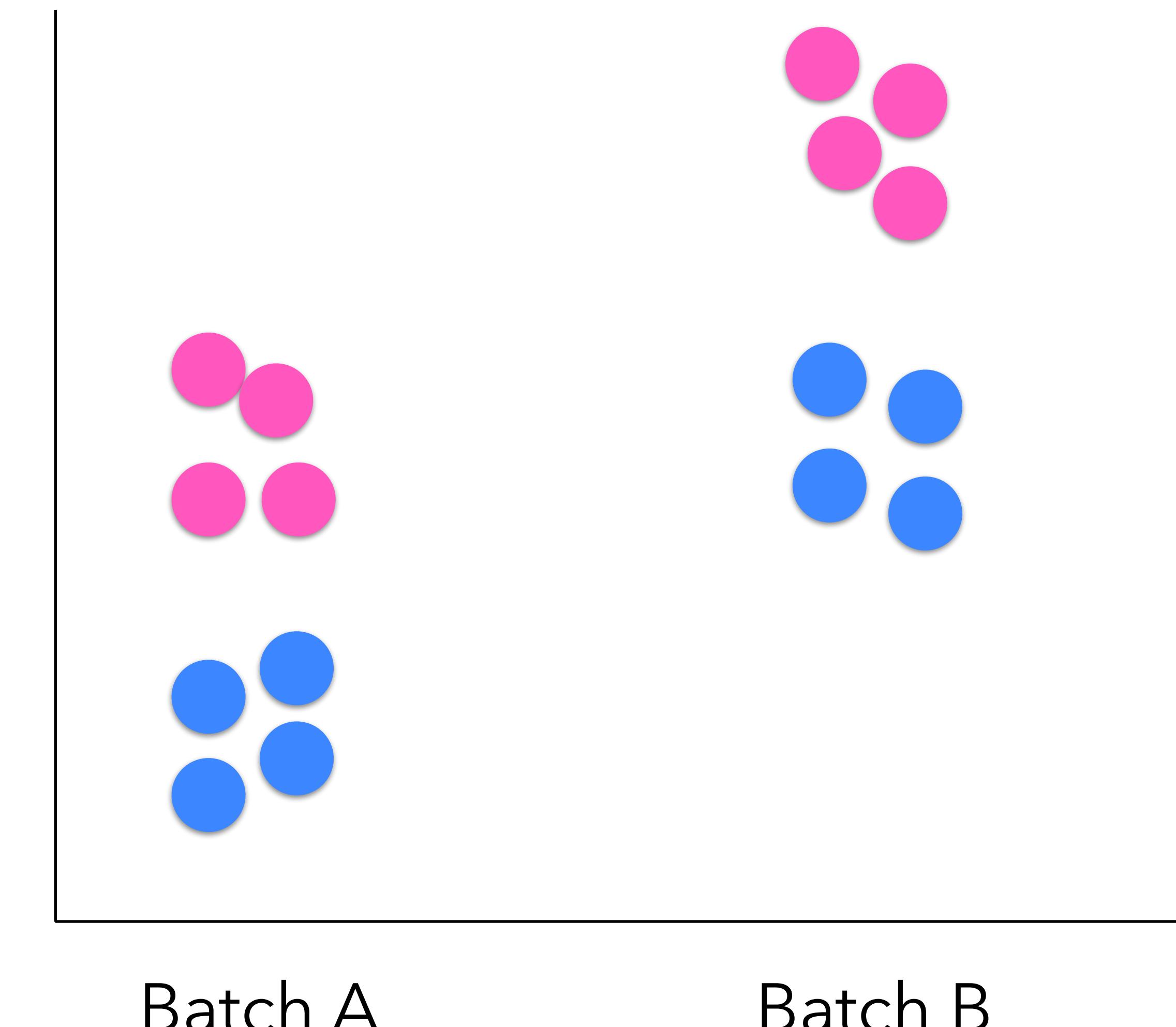
X Confounded design



Treated

Untreated

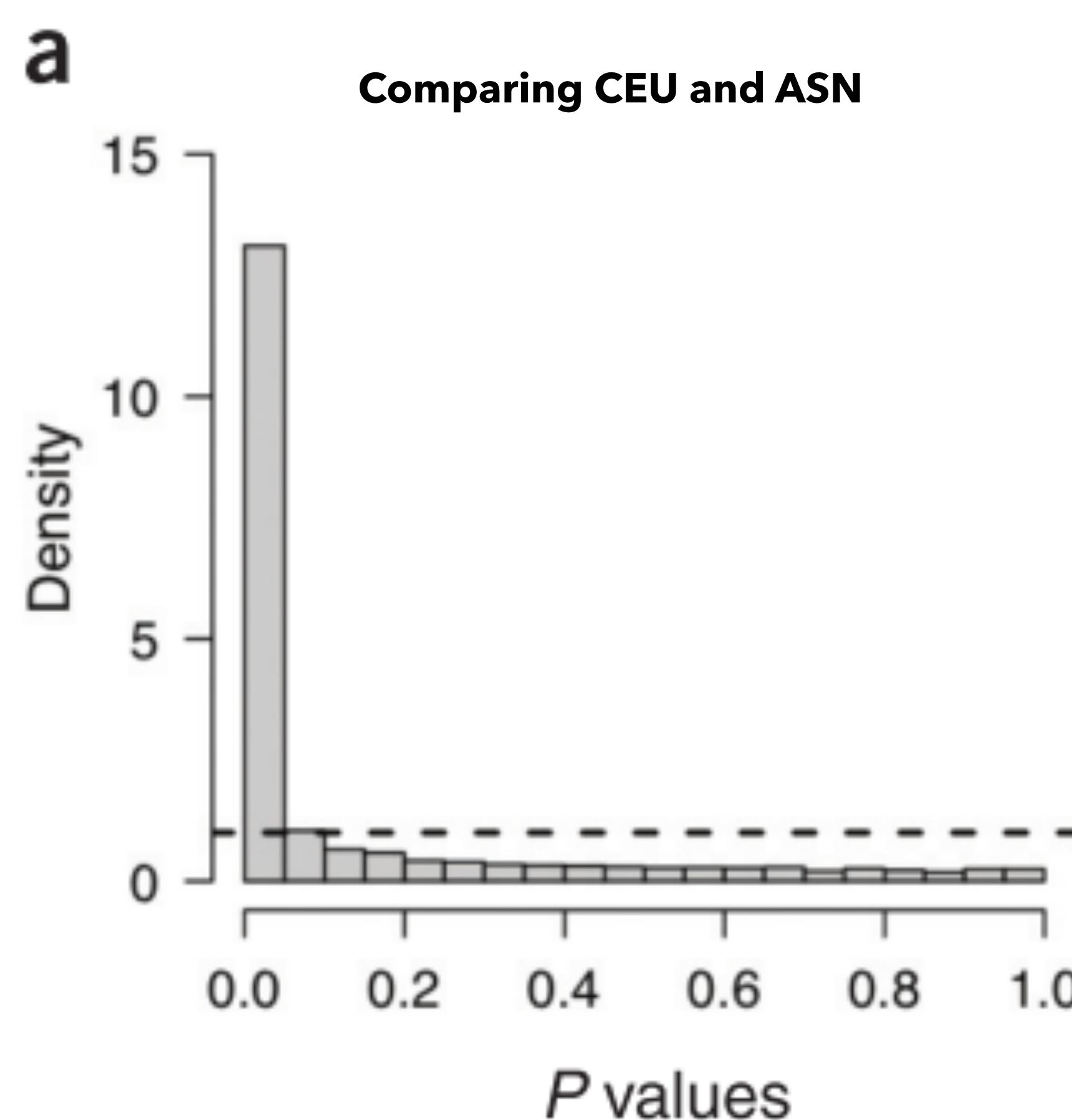
✓ Non-confounded design



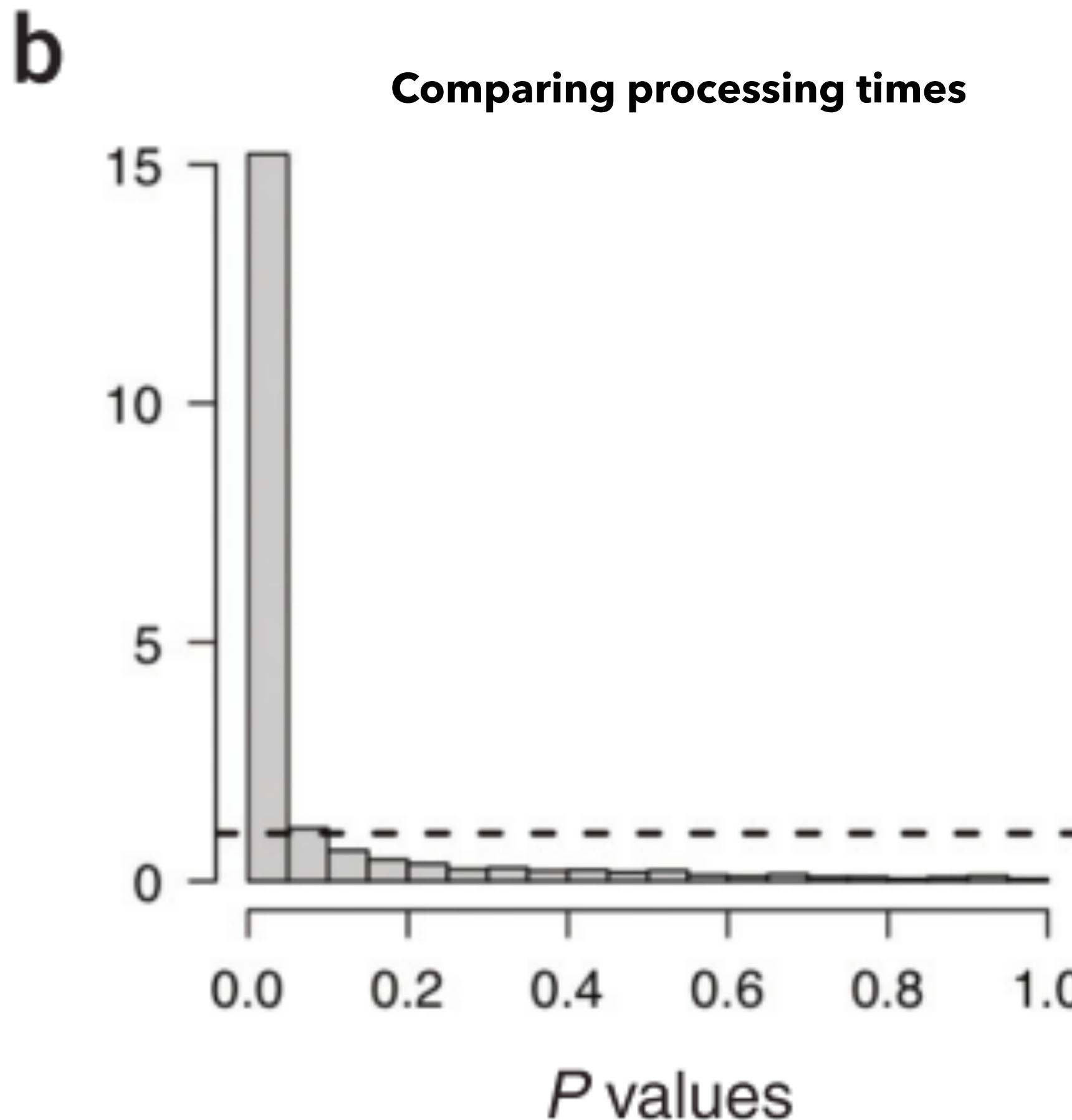
Dealing with batch effects

- In statistical modeling, batch effects can be included as **covariates** (additional predictors) in the model.
- For exploratory analysis, we often attempt to “eliminate” or “adjust for” such unwanted variation in advance, by subtracting the estimated effect from each variable (e.g. the expression of a gene).
- Even partial confounding between batch and signal of interest can lead to problems.

What can happen with bad experimental design?



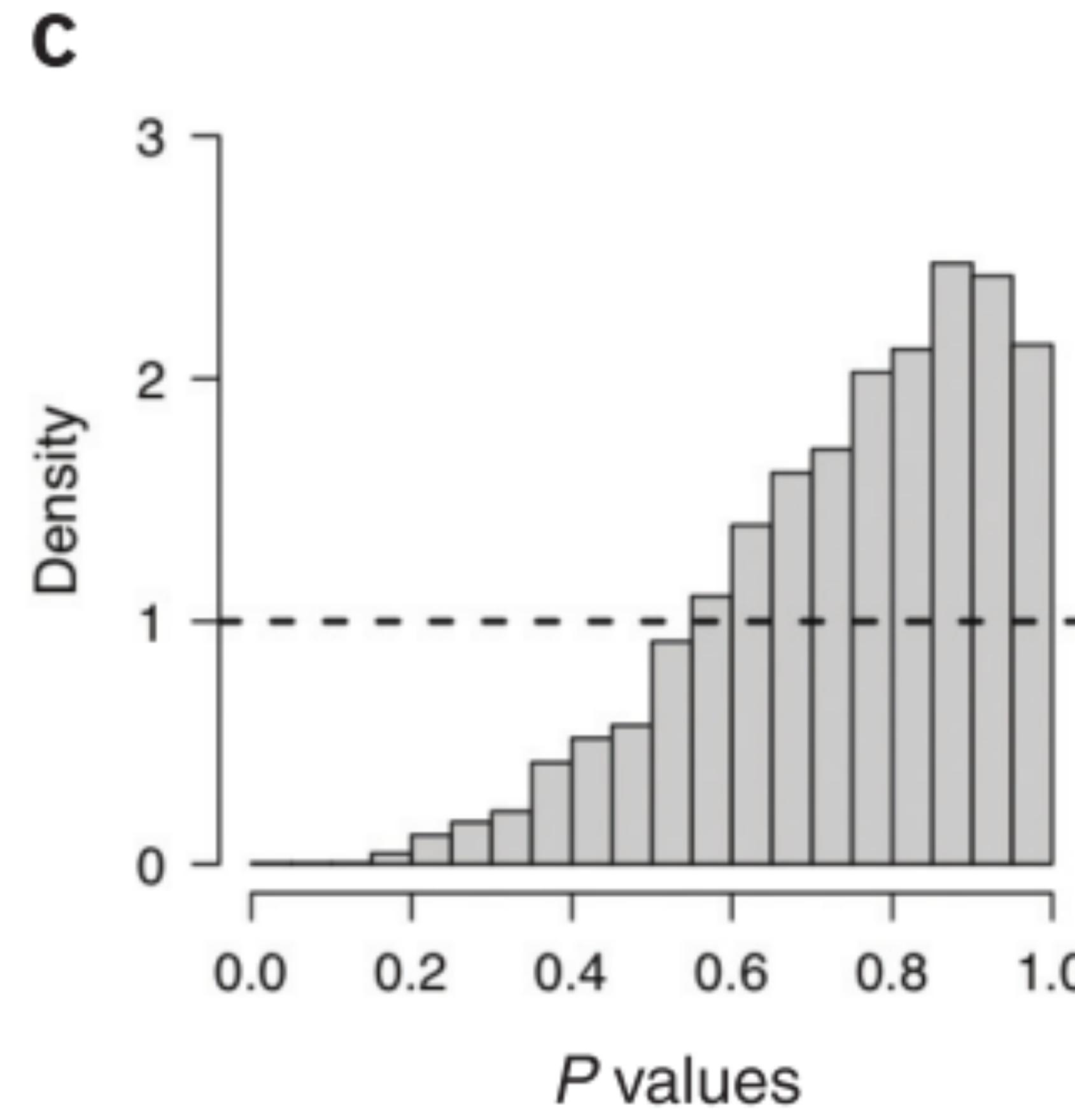
78% differentially expressed



96% differentially expressed

“Batch effect correction” won’t work here

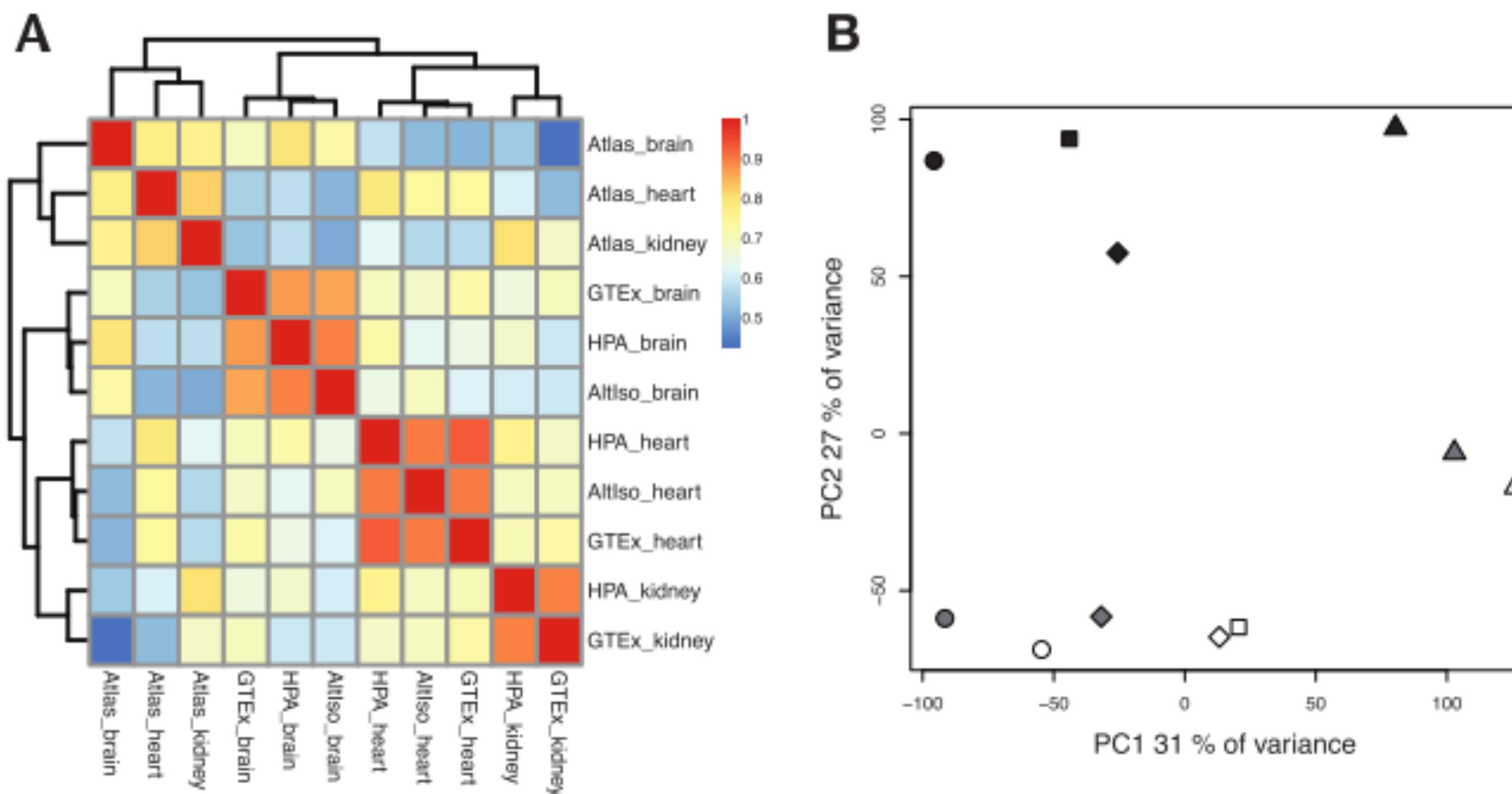
p-values from test comparing CEU and ASN, after controlling for the processing year



0% differentially expressed

Accounting for batch effects in practice

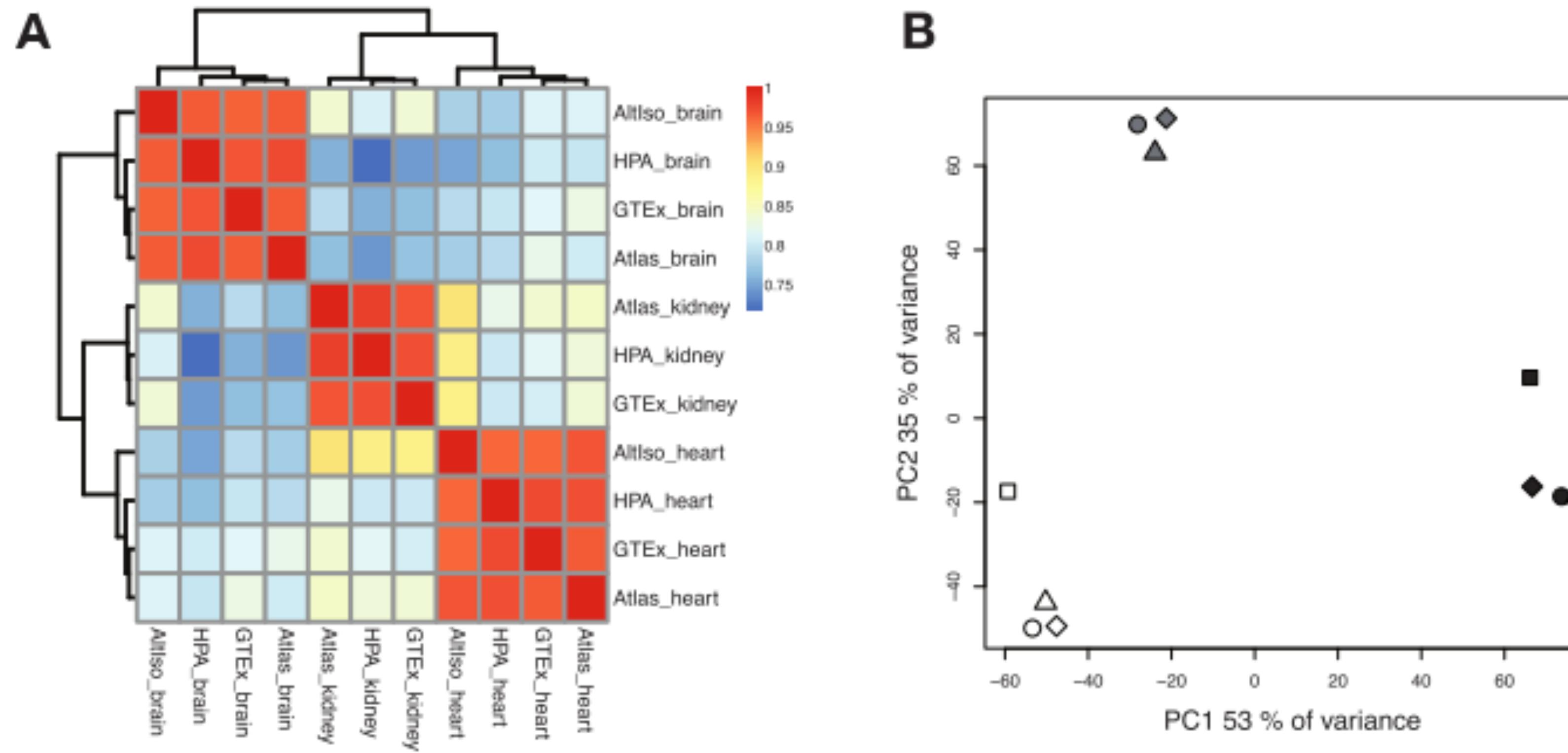
Public, processed RNA-seq data from 3 tissues, 4 studies show strong “study” (=batch) signal



color = tissue; symbol = study (batch)

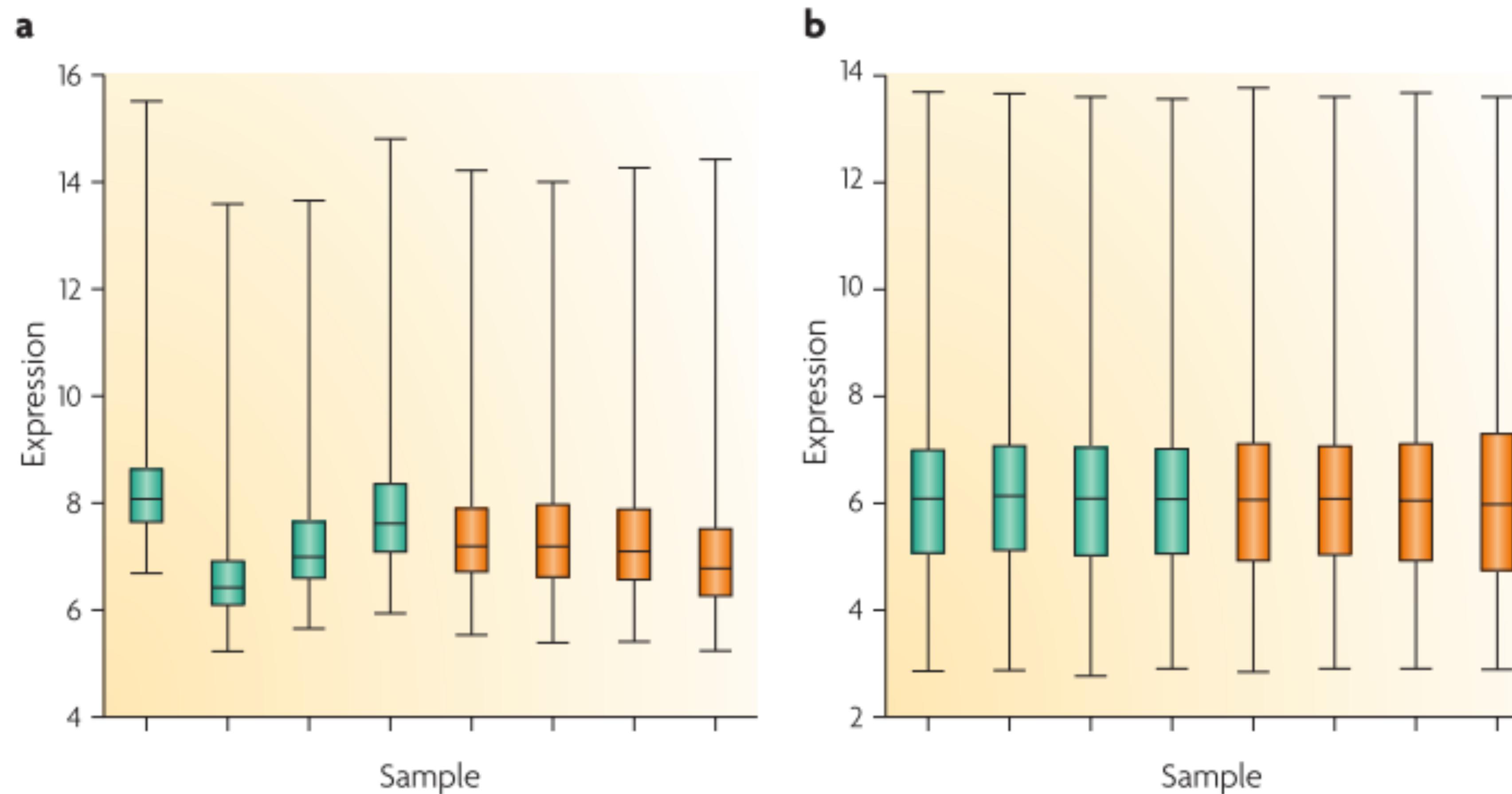
Accounting for batch effects in practice

Accounting for the batch effect brings out the signal of interest



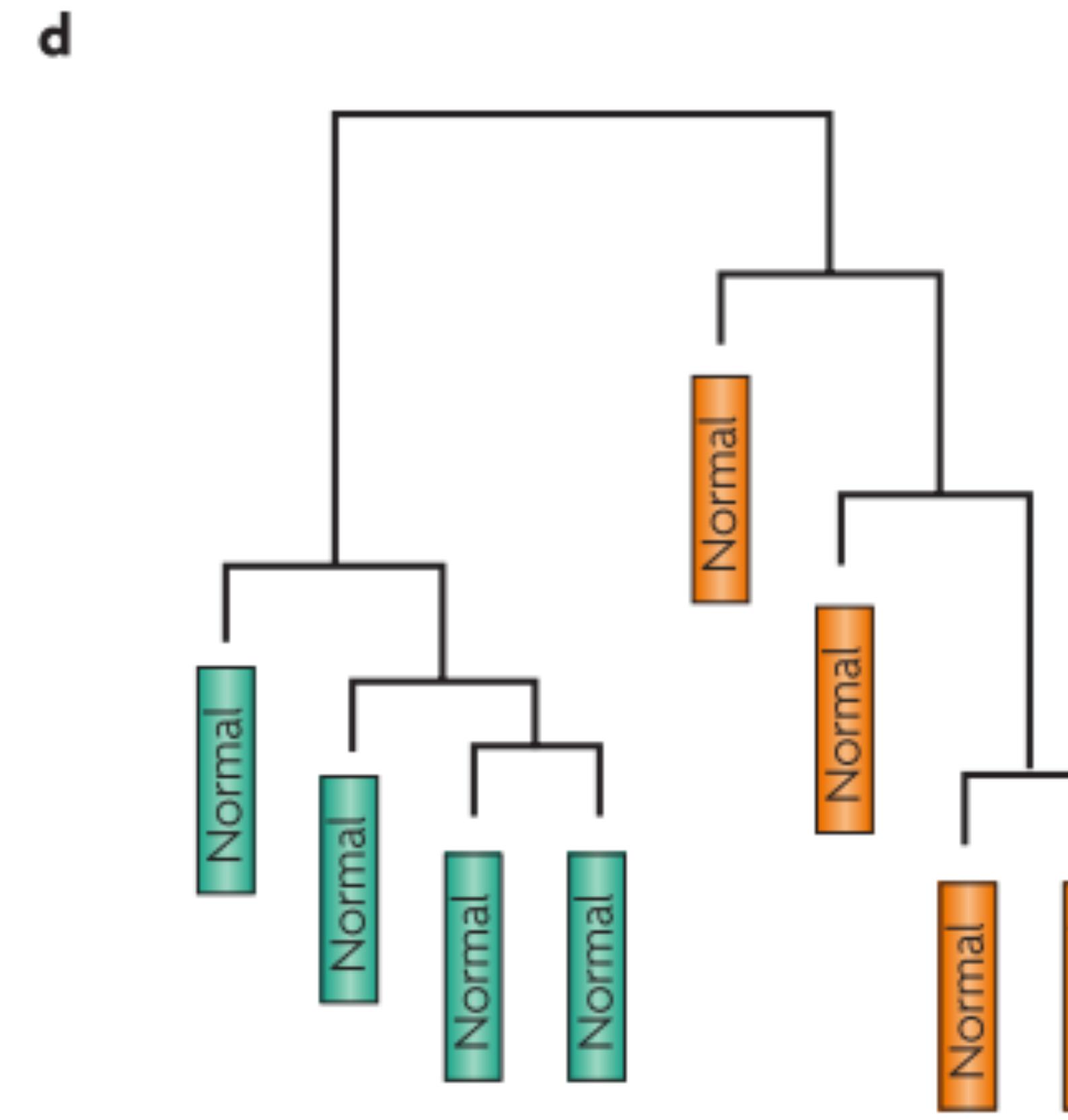
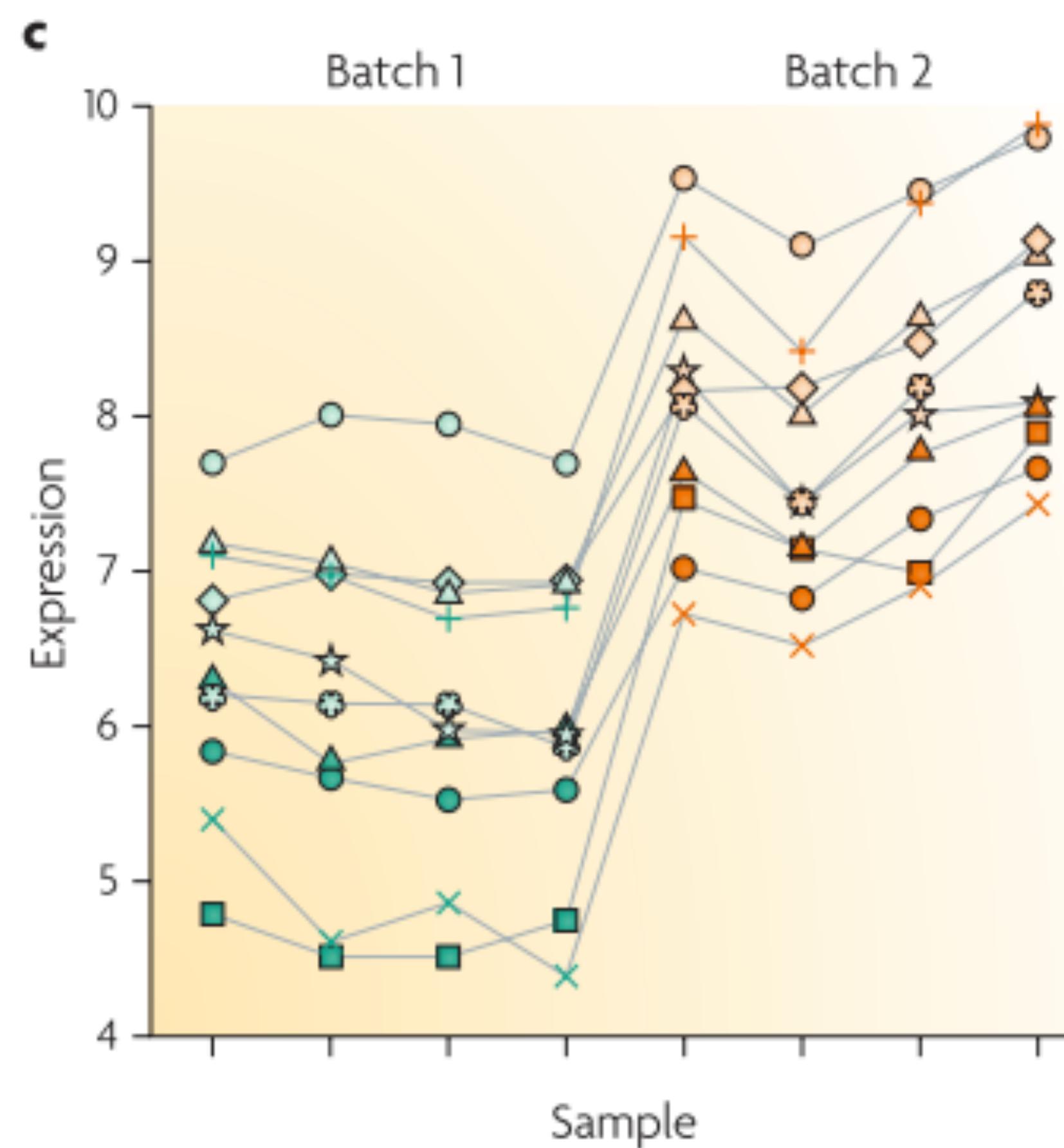
Batch effect adjustment vs normalization

Batch effect adjustment goes *beyond* the “global” between-sample normalization methods



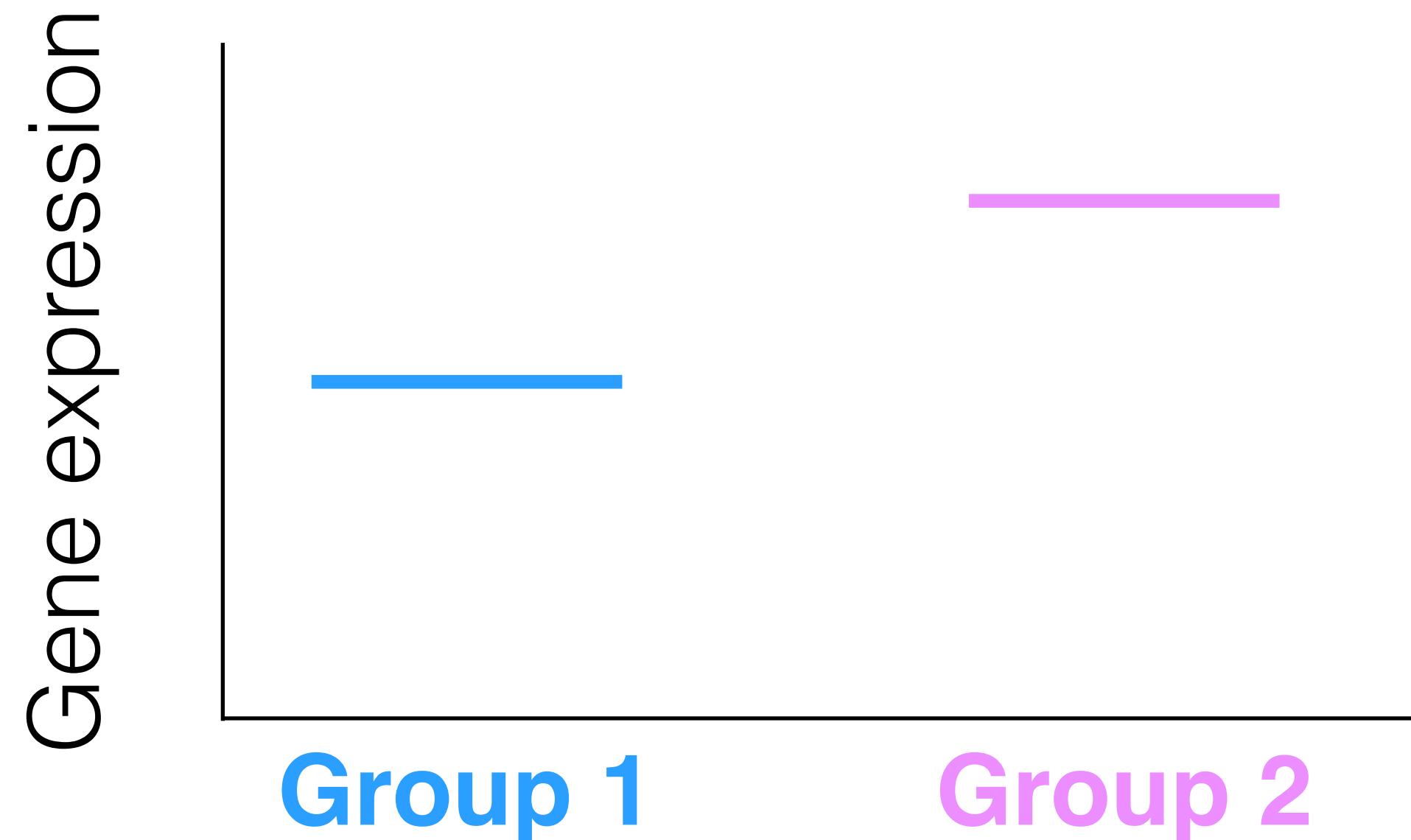
Batch effect adjustment vs normalization

Batch effect adjustment goes beyond the “global” between-sample normalization methods



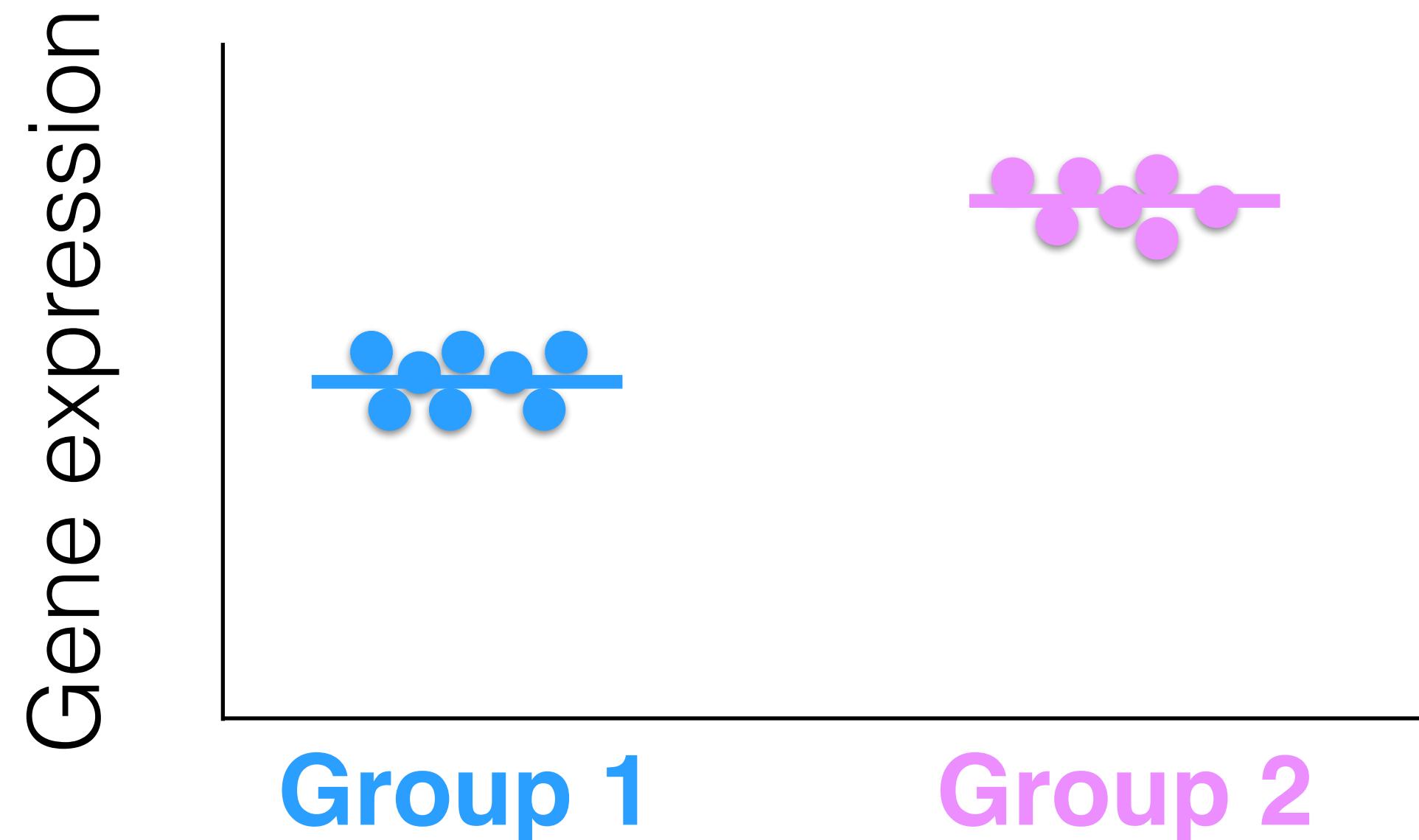
Other design issues: replication

- Replicates are **necessary** to estimate within-condition variability.
- Variability estimates are, in turn, **vital** for statistical testing.



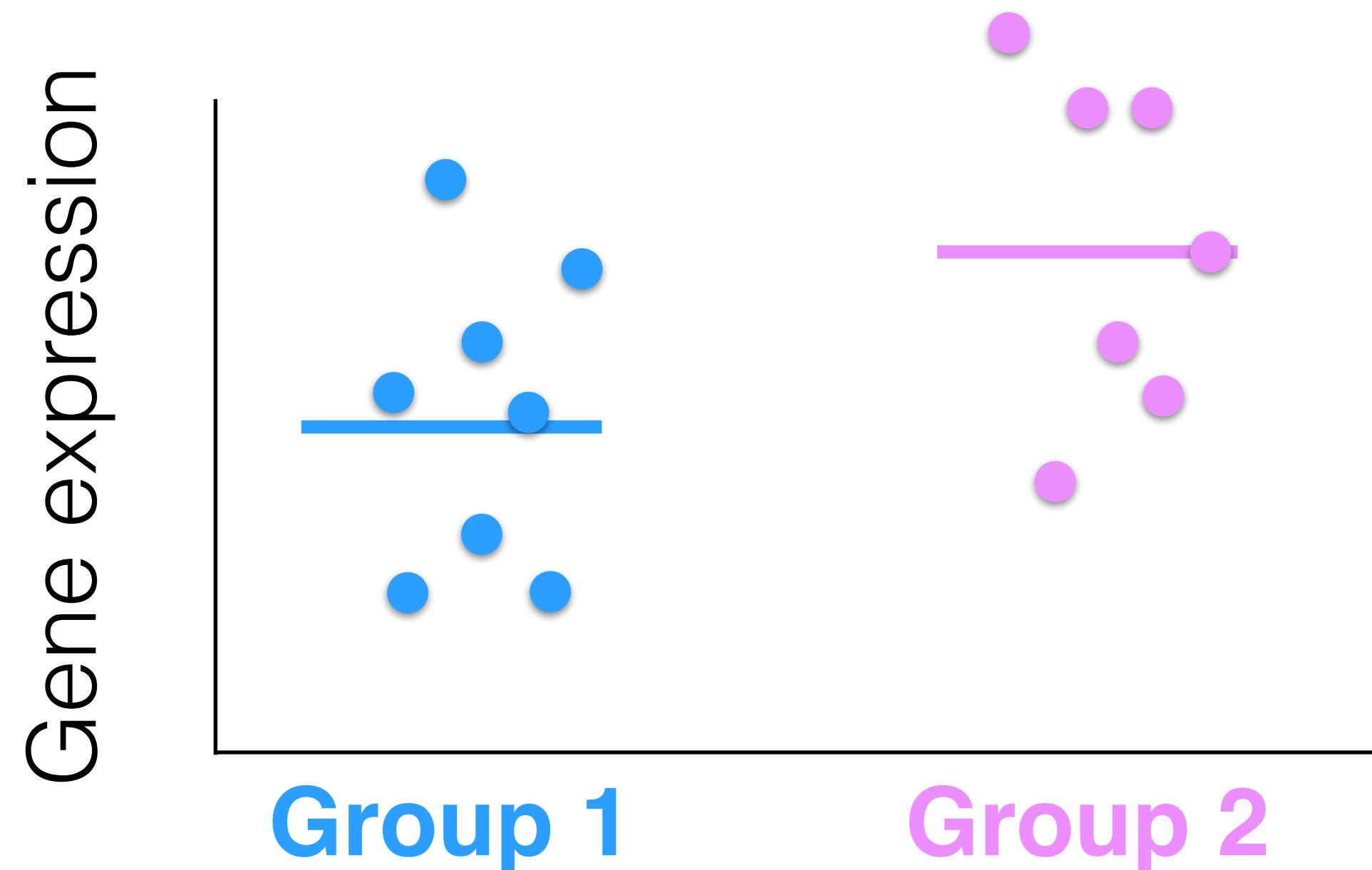
Other design issues: replication

- Replicates are **necessary** to estimate within-condition variability.
- Variability estimates are, in turn, **vital** for statistical testing.



Other design issues: replication

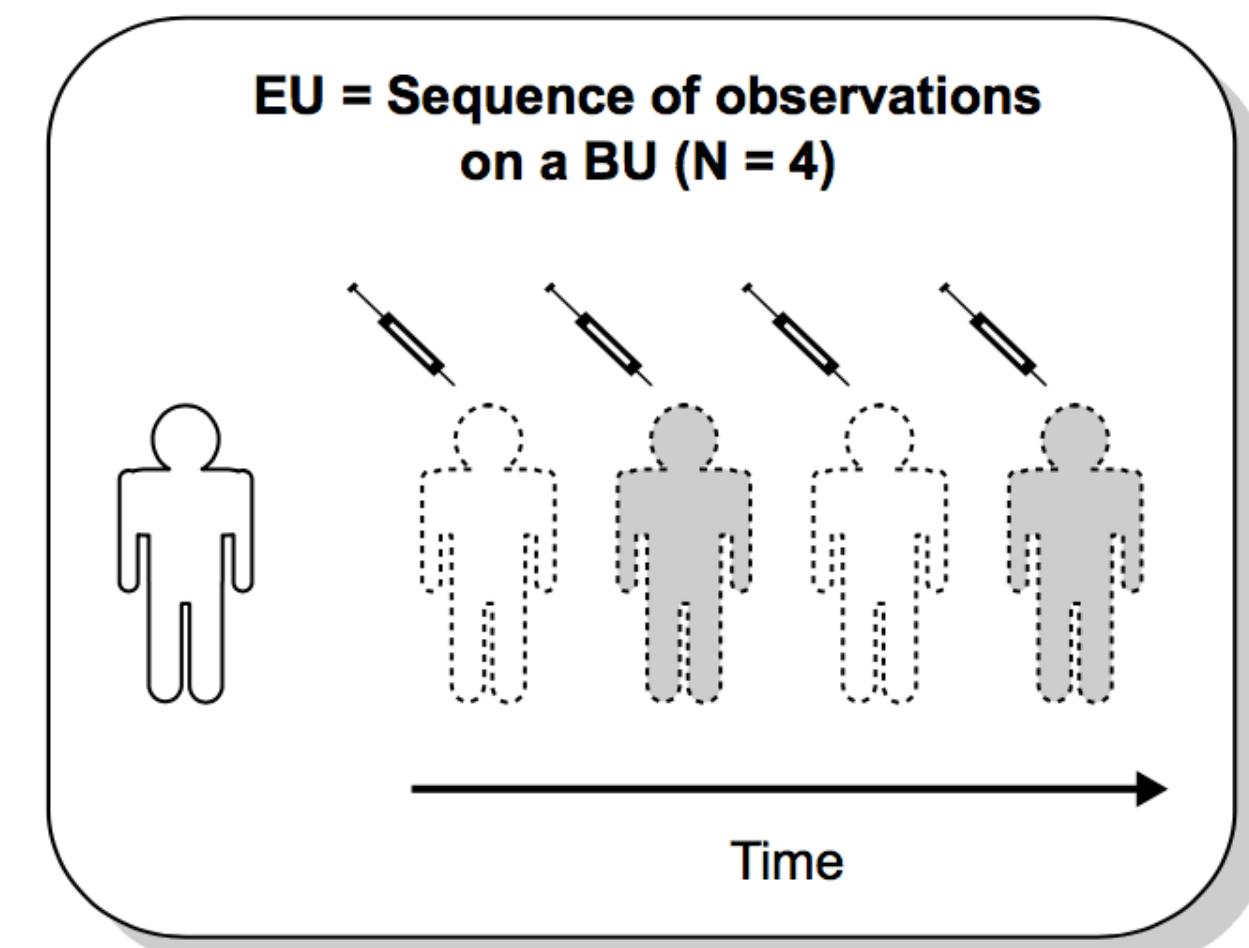
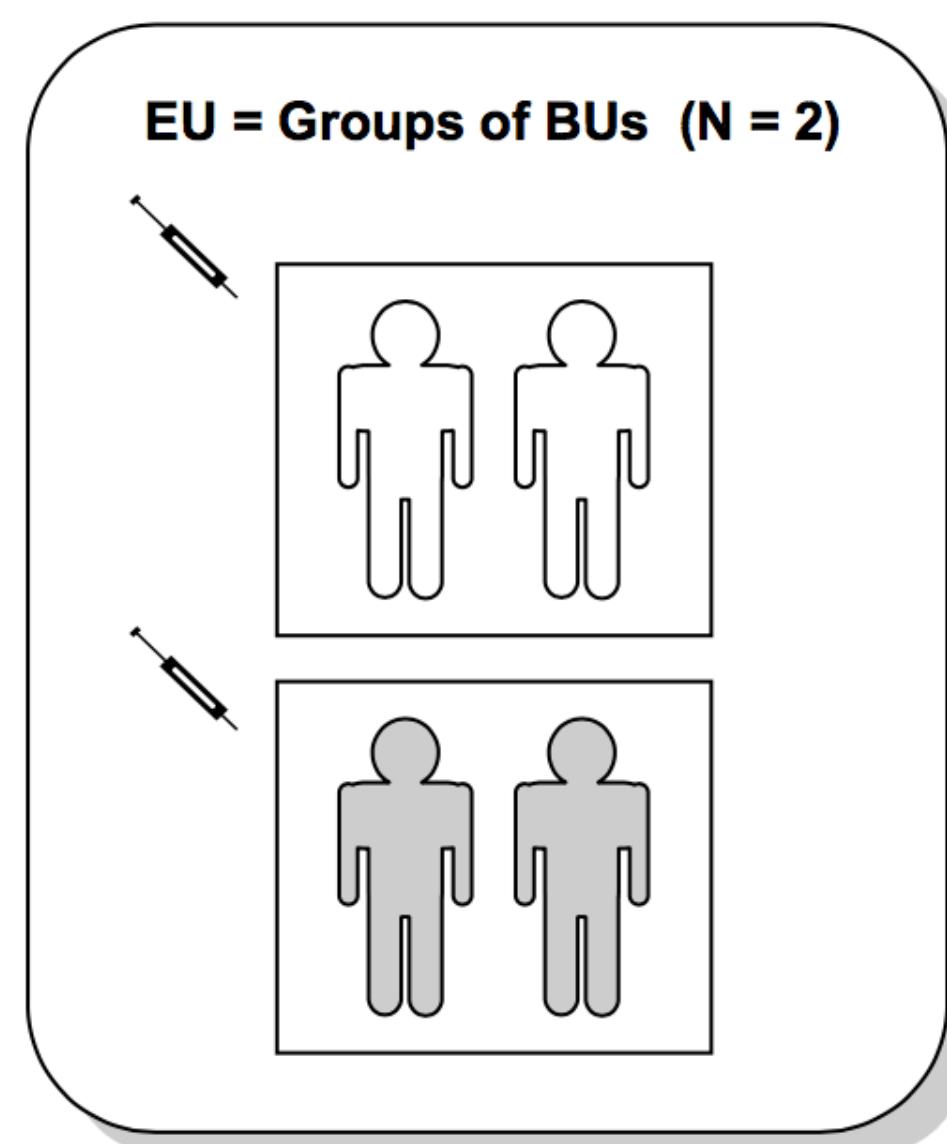
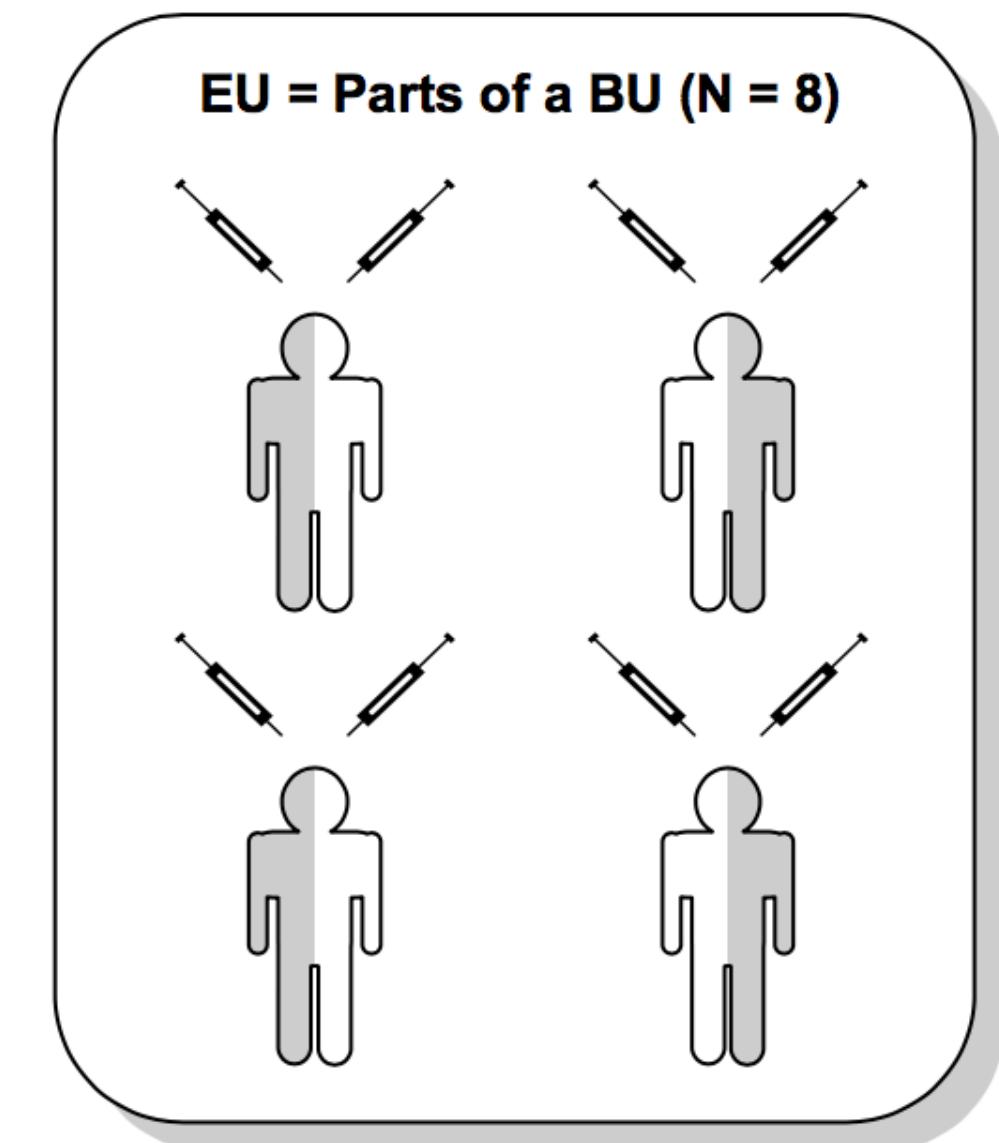
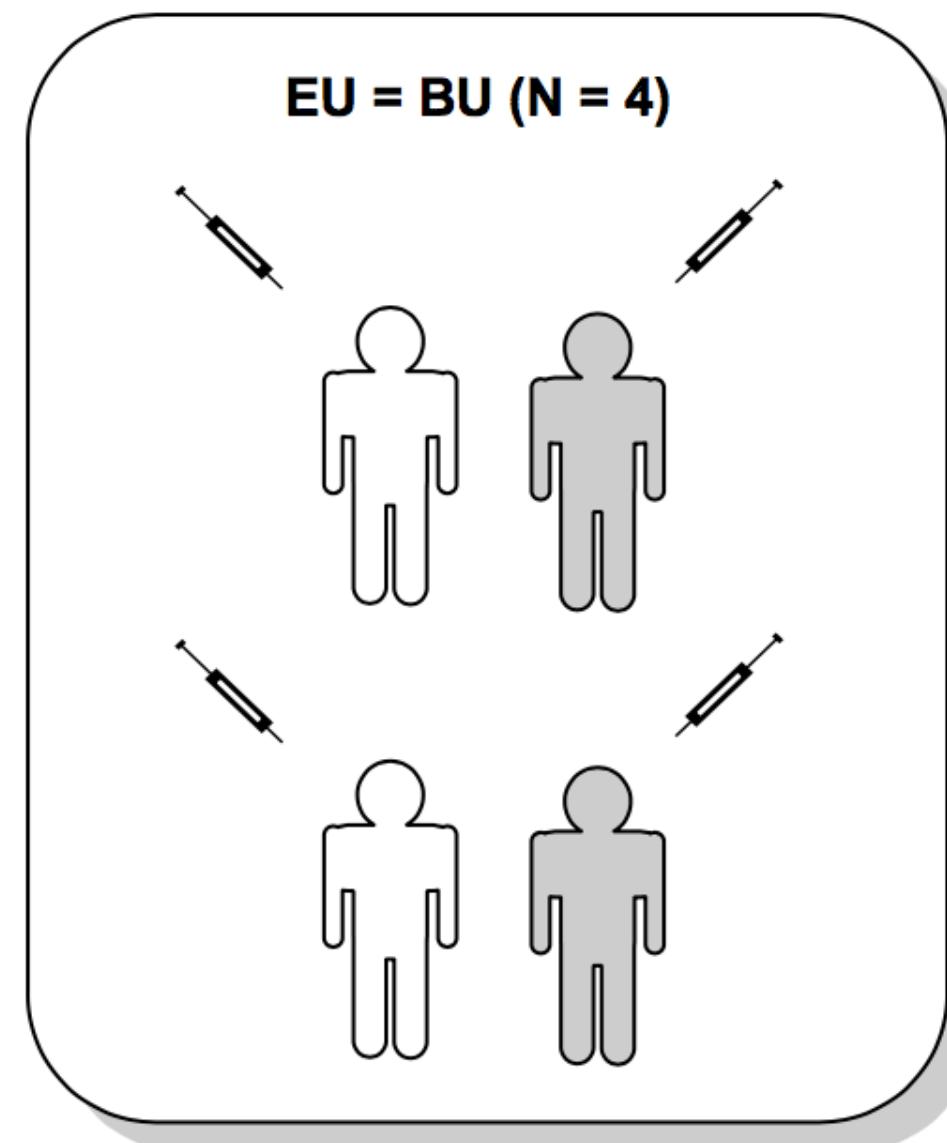
- Replicates are **necessary** to estimate within-condition variability.
- Variability estimates are, in turn, **vital** for statistical testing.



Different types of units

- Biological units (BU) - entities we want to make inferences about (e.g., animal, person)
- Experimental units (EU) - smallest entities that can be independently assigned to a treatment (e.g., animal, litter, cage, well)
- Observational units (OU) - entities at which measurements are made

Biological vs experimental units



Pseudoreplication

- “**Artificial inflation** of the sample size, that usually occurs when the biological unit of interest differs from the experimental unit or observational unit.”
- Only replication of experimental units is true replication
- To make a general statement about the effect of an intervention on a biological unit, we need to replicate the number of such units

Model formulas and design matrices

- Testing is done separately for each gene
- We must tell the packages **which model** to fit (e.g. which predictors to use)
- The design does *not* follow “automatically” from having the sample annotation table - many different designs are often possible
- Model formulas in R:

response variable ~ predictors

- Fit a separate model for each gene - response variable changes. Specify only predictors

Examples

```
## Linear model, mtcars data
lm(mpg ~ cyl, data = mtcars)

## Linear model (limma), gene expression data
lmFit(object = y, design = model.matrix(~ group))

## GLM (edgeR), RNA-seq data
fit <- glmFit(y = d, design = model.matrix(~ time))

## DESeq2, RNA-seq data
dds <- DESeqDataSetFromMatrix(countData = countData,
                               colData = DataFrame(condition),
                               design = ~ condition)
```

Testing and contrasts

- After fitting the model(s), we must decide *which* coefficient (or combination thereof) we want to apply a hypothesis test for.
- Combinations of coefficients are called *contrasts*.
- Design matrices can often be defined in many equivalent ways - important that the contrast is defined accordingly!

Examples

```
## GLM (edgeR), RNA-seq data
glmLRT(fit, coef = 2)
glmLRT(fit, contrast = c(-1, 1))

## DESeq2, RNA-seq data
results(dds, contrast = c("condition", "B", "A"))
results(dds, contrast = c(0, -1, 1))
results(dds)
```

Model formulas and design matrices

- A **design matrix** contains the values of the predictor variables for each sample

coefficients

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ y_5 \\ y_6 \end{pmatrix} = \boxed{\begin{pmatrix} 1 & 0 \\ 1 & 0 \\ 1 & 0 \\ 1 & 1 \\ 1 & 1 \\ 1 & 1 \end{pmatrix}} \begin{pmatrix} \beta_0 \\ \beta_1 \end{pmatrix} + \begin{pmatrix} \varepsilon_1 \\ \varepsilon_2 \\ \varepsilon_3 \\ \varepsilon_4 \\ \varepsilon_5 \\ \varepsilon_6 \end{pmatrix} = \boxed{X}\beta + \varepsilon$$

e.g.: (log) expression values for a given gene

$$y_i = \beta_0 + \beta_1 x_i + \varepsilon_i$$

Many ways of modeling the same expected values

Explore model matrices with <https://github.com/csoneson/ExploreModelMatrix>

- 1 predictor, 2 groups

	group 1	group 2
X	b0	b0 + b1
	$\sim X$	

	group 1	group 2
X	b0	b1
	$\sim 0 + X$	

the coefficients mean different things in the different cases!

- 2 predictors, 2*2 groups

	Y	
X	b0	b0+b1
	b0+b2	b0+b1+ b2+b3

$\sim X^*Y$
 $\sim X + Y + X:Y$

	Y	
X	b0	b1
	b2	b3

$\sim 0 + XY$

New variable,
combining X
and Y

	Y	
X	b0	b0+b1
	b0+b2	b0+b2+ b3

$\sim X + X:Y$

Model formulas and design matrices - example 1

One predictor, two levels (without intercept)

Sample table:

	sample	treatment
1	s1	control
2	s2	control
3	s3	control
4	s4	treated
5	s5	treated
6	s6	treated

Design matrix:

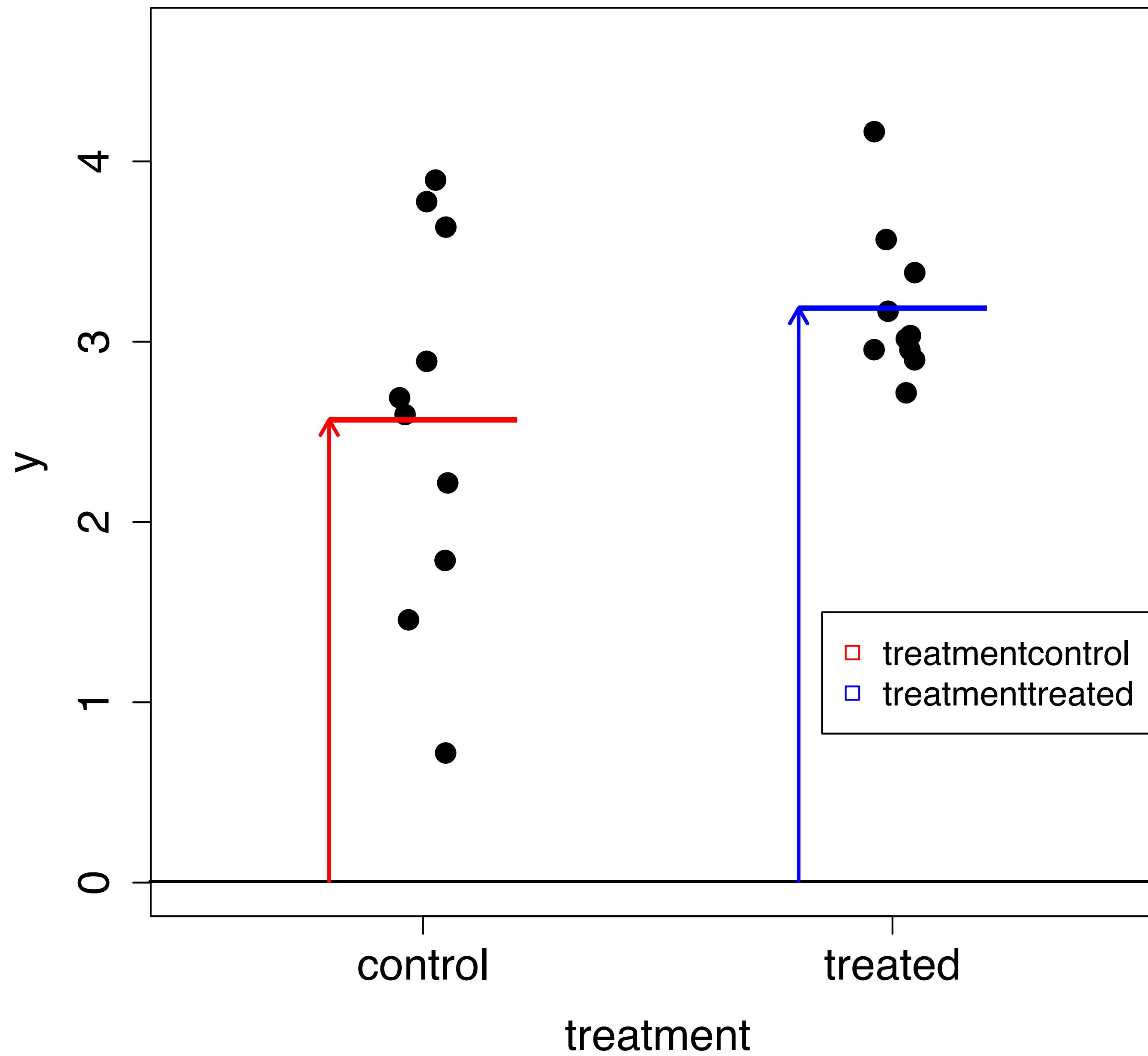
	<u>treatmentcontrol</u>	<u>treatmenttreated</u>
1	1	0
2	1	0
3	1	0
4	0	1
5	0	1
6	0	1

Formula:

$\sim 0 + \text{treatment}$

Modeled values:

	control	treated
treatmentcontrol		treatmenttreated



Model formulas and design matrices - example 1

One predictor, two levels (with intercept)

Sample table:

	sample	treatment
1	s1	control
2	s2	control
3	s3	control
4	s4	treated
5	s5	treated
6	s6	treated

Design matrix:

	(Intercept)	treatmenttreated
1	1	0
2	1	0
3	1	0
4	1	1
5	1	1
6	1	1

Formula:

\sim treatment

Modeled values:

control	treated
$1 * \text{Intercept} + 0 * \text{treatmenttreated}$	$1 * \text{Intercept} + 1 * \text{treatmenttreated}$

Model formulas and design matrices - example 1

One predictor, two levels (with intercept)

Sample table:

	sample	treatment
1	s1	control
2	s2	control
3	s3	control
4	s4	treated
5	s5	treated
6	s6	treated

Design matrix:

	(Intercept)	treatmenttreated
1	1	0
2	1	0
3	1	0
4	1	1
5	1	1
6	1	1

Formula:

\sim treatment

Modeled values:

	control	treated
	$1 * \text{Intercept} + 0 * \text{treatmenttreated}$	$1 * \text{Intercept} + 1 * \text{treatmenttreated}$

Model formulas and design matrices - example 1

One predictor, two levels (with intercept)

Sample table:

	sample	treatment
1	s1	control
2	s2	control
3	s3	control
4	s4	treated
5	s5	treated
6	s6	treated

Design matrix:

	(Intercept)	treatmenttreated
1	1	0
2	1	0
3	1	0
4	1	1
5	1	1
6	1	1

Formula:

\sim treatment

Modeled values:

	control	treated
	$1 * \text{Intercept} + 0 * \text{treatmenttreated}$	$1 * \text{Intercept} + 1 * \text{treatmenttreated}$

Model formulas and design matrices - example 1

One predictor, two levels (with intercept)

Sample table:

	sample	treatment
1	s1	control
2	s2	control
3	s3	control
4	s4	treated
5	s5	treated
6	s6	treated

Design matrix:

	(Intercept)	treatmenttreated
1	1	0
2	1	0
3	1	0
4	1	1
5	1	1
6	1	1

Formula:

\sim treatment

Modeled values:

	control	treated
	$1 * \text{Intercept} + 0 * \text{treatmenttreated}$	$1 * \text{Intercept} + 1 * \text{treatmenttreated}$

Model formulas and design matrices - example 1

One predictor, two levels (with intercept)

Sample table:

	sample	treatment
1	s1	control
2	s2	control
3	s3	control
4	s4	treated
5	s5	treated
6	s6	treated

Design matrix:

	(Intercept)	treatmenttreated
1	1	0
2	1	0
3	1	0
4	1	1
5	1	1
6	1	1

Formula:

\sim treatment

Modeled values:

	control	treated
	$1 * \text{Intercept} + 0 * \text{treatmenttreated}$	$1 * \text{Intercept} + 1 * \text{treatmenttreated}$

Model formulas and design matrices - example 1

One predictor, two levels (with intercept)

Sample table:

	sample	treatment
1	s1	control
2	s2	control
3	s3	control
4	s4	treated
5	s5	treated
6	s6	treated

Design matrix:

	(Intercept)	treatmenttreated
1	1	0
2	1	0
3	1	0
4	1	1
5	1	1
6	1	1

Formula:

\sim treatment

Modeled values:

	control	treated
	$1 * \text{Intercept} + 0 * \text{treatmenttreated}$	$1 * \text{Intercept} + 1 * \text{treatmenttreated}$

Model formulas and design matrices - example 1

One predictor, two levels (with intercept)

Sample table:

	sample	treatment
1	s1	control
2	s2	control
3	s3	control
4	s4	treated
5	s5	treated
6	s6	treated

Design matrix:

	(Intercept)	treatmenttreated
1	1	0
2	1	0
3	1	0
4	1	1
5	1	1
6	1	1

Formula:

\sim treatment

Modeled values:

	control	treated
	$1 * \text{Intercept} + 0 * \text{treatmenttreated}$	$1 * \text{Intercept} + 1 * \text{treatmenttreated}$

Model formulas and design matrices - example 1

One predictor, two levels (with intercept)

Sample table:

	sample	treatment
1	s1	control
2	s2	control
3	s3	control
4	s4	treated
5	s5	treated
6	s6	treated

Design matrix:

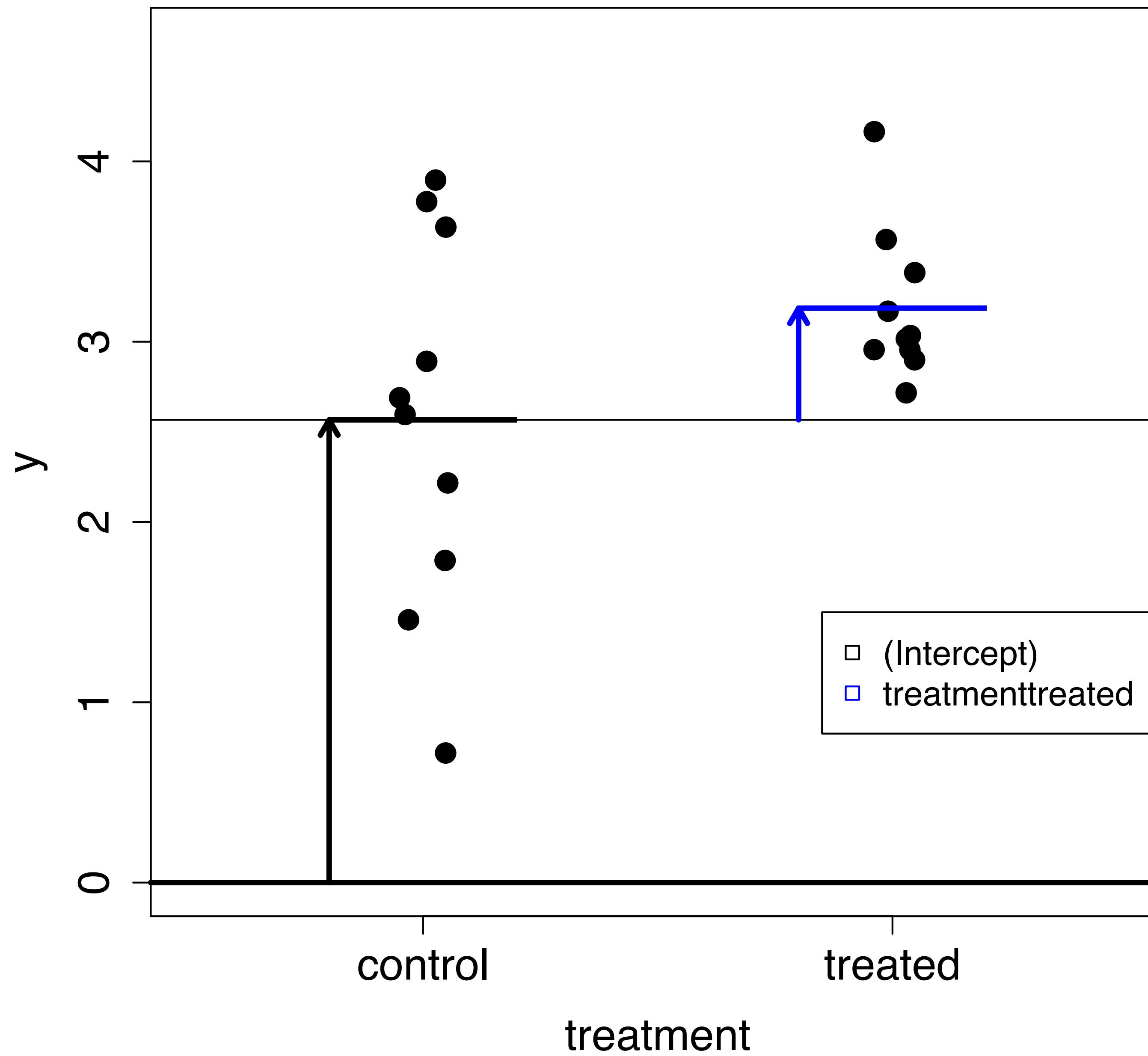
	(Intercept)	treatmenttreated
1	1	0
2	1	0
3	1	0
4	1	1
5	1	1
6	1	1

Formula:

\sim treatment

Modeled values:

	control	treated
	Intercept	Intercept + treatmenttreated



Model formulas and design matrices - example 2

One continuous predictor

Sample table:

	sample	age
1	s1	21
2	s2	12
3	s3	64
4	s4	44
5	s5	19
6	s6	26

Design matrix:

	(Intercept)	age
1	1	21
2	1	12
3	1	64
4	1	44
5	1	19
6	1	26

Formula:

$\sim \text{age}$

Modeled values:

	s1	s2	s3	s4	s5	s6
	Intercept + 21 * age	Intercept + 12 * age	Intercept + 64 * age	Intercept + 44 * age	Intercept + 19 * age	Intercept + 26 * age

Model formulas and design matrices - example 3

One predictor, three levels

Sample table:

	sample	treatment
1	s1	control
2	s2	control
3	s3	treatA
4	s4	treatA
5	s5	treatB
6	s6	treatB

Design matrix:

	(Intercept)	treatmenttreatA	treatmenttreatB
1	1	1	0
2	2	1	0
3	3	1	1
4	4	1	1
5	5	1	0
6	6	1	0

Formula:

\sim treatment

Modeled values:

	control	treatA	treatB
Intercept	Intercept	Intercept + treatmenttreatA	Intercept + treatmenttreatB

Model formulas and design matrices - example 4

One predictor, paired data (or two predictors)

Sample table:

	sample	treatment
1	s1	control
2	s1	treated
3	s2	control
4	s2	treated
5	s3	control
6	s3	treated

Design matrix:

	(Intercept)	samples2	samples3	treatmenttreated
1	1	1	0	0
2	2	1	0	1
3	3	1	1	0
4	4	1	1	1
5	5	1	0	1
6	6	1	0	1

Formula:

$\sim \text{sample} + \text{treatment}$

Modeled values:

	s1	s2	s3
control	Intercept	Intercept + samples2	Intercept + samples3
treated	Intercept + treatmenttreated	Intercept + samples2 + treatmenttreated	Intercept + samples3 + treatmenttreated

Model formulas and design matrices - example 4

One predictor, paired data (or two predictors)

Sample table:

	genotype	treatment
1	A	control
2	A	control
3	A	treated
4	A	treated
5	B	control
6	B	control
7	B	treated
8	B	treated

Design matrix:

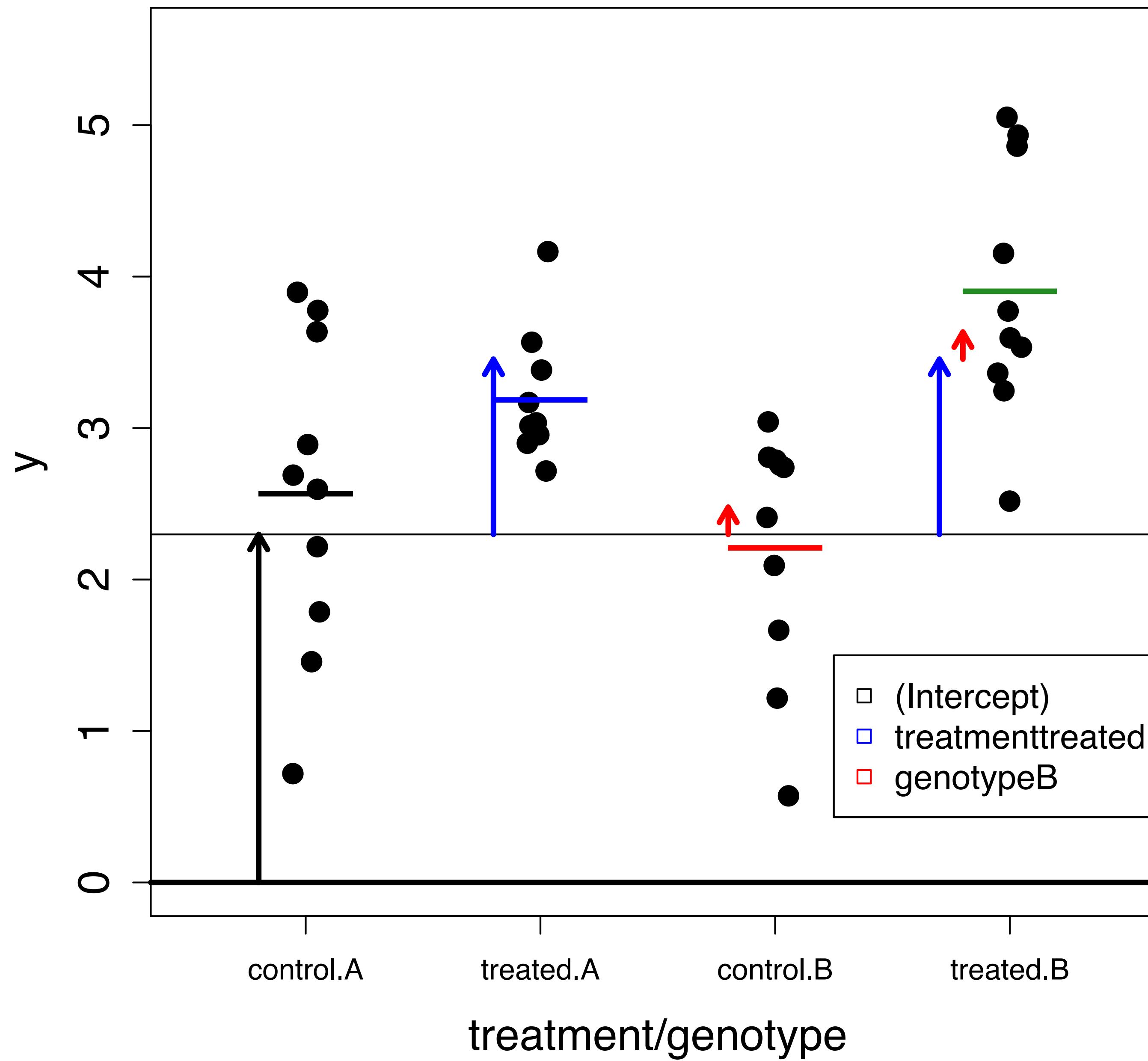
	(Intercept)	genotypeB	treatmenttreated
1	1	0	0
2	2	0	0
3	3	0	1
4	4	0	1
5	5	1	0
6	6	1	0
7	7	1	1
8	8	1	1

Formula:

$\sim \text{genotype} + \text{treatment}$

Modeled values:

		genotype A	genotype B
		Intercept	Intercept + genotypeB
		Intercept + treatmenttreated	Intercept + genotypeB + treatmenttreated
control	genotype A	Intercept	Intercept + genotypeB
	genotype B	Intercept + treatmenttreated	Intercept + genotypeB + treatmenttreated
treated	genotype A	Intercept + treatmenttreated	Intercept + genotypeB + treatmenttreated
treated	genotype B	Intercept + treatmenttreated	Intercept + genotypeB + treatmenttreated



Model formulas and design matrices - example 5

Two predictors, with interaction

Sample table:

	genotype	treatment
1	A	control
2	A	control
3	A	treated
4	A	treated
5	B	control
6	B	control
7	B	treated
8	B	treated

Design matrix:

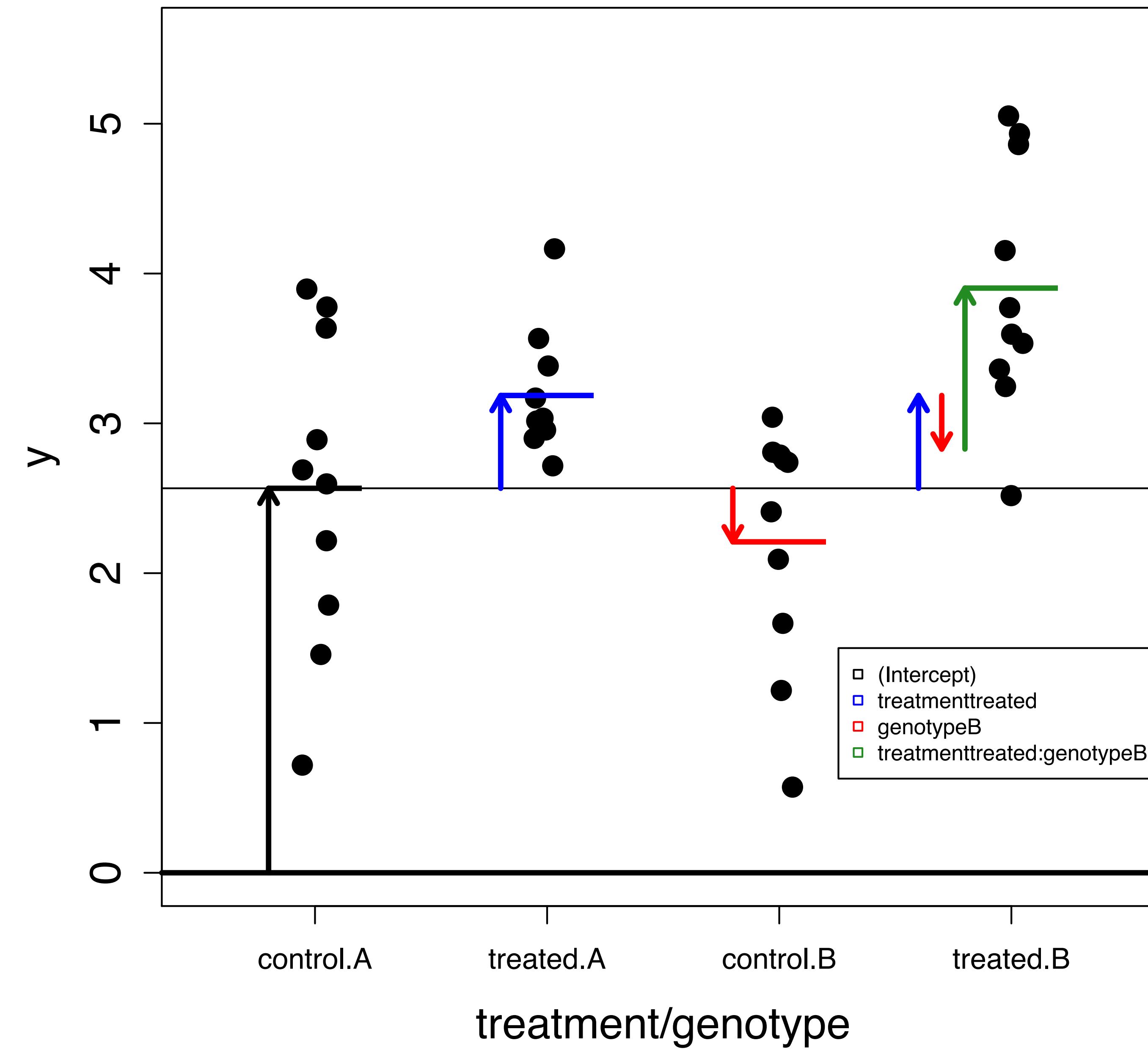
	(Intercept)	genotypeB	treatmenttreated	genotypeB:treatmenttreated
1	1	0	0	0
2	2	0	0	0
3	3	0	1	0
4	4	0	1	0
5	5	1	0	0
6	6	1	1	0
7	7	1	1	1
8	8	1	1	1

Formula:

~ genotype * treatment
~ genotype + treatment + genotype:treatment

Modeled values:

		genotype A	genotype B
		control	treated
control	control	Intercept	Intercept + genotypeB
	treated	Intercept + treatmenttreated	Intercept + genotypeB + treatmenttreated + genotypeB:treatmenttreated



Model formulas and design matrices - example 6

Two predictors, with interaction

Sample table:

```
treat.gt  
1 control.A  
2 control.A  
3 treated.A  
4 treated.A  
5 control.B  
6 control.B  
7 treated.B  
8 treated.B
```

Design matrix:

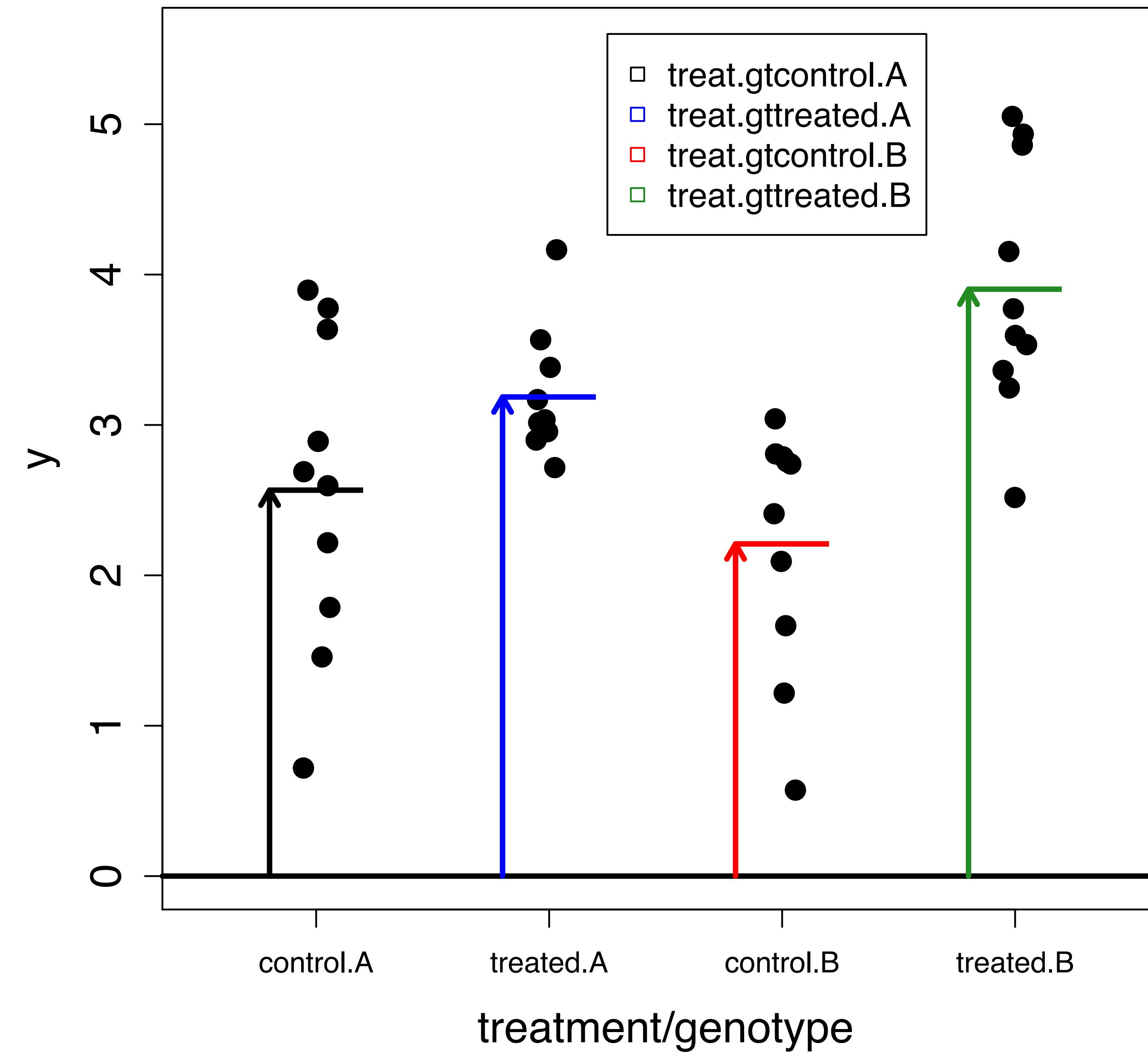
	treat.gtcontrol.A	treat.gttreated.A	treat.gtcontrol.B	treat.gttreated.B
1 control.A	1	0	0	0
2 control.A	1	0	0	0
3 treated.A	1	0	0	0
4 treated.A	0	1	0	0
5 control.B	0	1	0	0
6 control.B	0	0	1	0
7 treated.B	0	0	1	0
8 treated.B	0	0	0	1

Formula:

$\sim 0 + \text{treat.gt}$

Modeled values:

		genotype A	genotype B
		treat.gtcontrol.A	treat.gtcontrol.B
control	treat	treat.gttreated.A	treat.gttreated.B
	treated	treat.gttreated.A	treat.gttreated.B



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