

# Modifications

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## 1)Change of t,k-term: Rescue Annealed Local-Table move

**Previous Formula:**

$$\begin{aligned}
 & -\log p(x, z|\lambda) \\
 & = \\
 & \text{(t-term)} \log \frac{\Gamma(m_{..} + \gamma)}{\Gamma(\gamma)} + \sum_{j=1}^J \{ \log \frac{\Gamma(n_{j..} + \alpha)}{\Gamma(\alpha)} - \sum_{t=1}^{m_{j.}} [\log(\Gamma(n_{jt.})) + \log \alpha] \} \\
 & + \text{(k-term)} \sum_{k=1}^K [ \log \left( \frac{\Gamma(n_{..k} + W\phi_0)}{\prod_{w=1}^W \Gamma(\phi_0 + n_{..k}^w)} \right) + \log \left( \frac{\Gamma(\phi_0)^W}{\Gamma(W\phi_0)} \right) - \log(\Gamma(m_{.k})) - \log \gamma ]
 \end{aligned}$$

(underlined part come from Hierarchical Dirichlet Process)

**New Formula:**

$$\begin{aligned}
 & -\log p(x, z|\lambda) \\
 & = \\
 & \text{(t-term)} + \sum_{j=1}^J \{ \log \frac{\Gamma(n_{j..} + \alpha)}{\Gamma(\alpha)} - \sum_{t=1}^{m_{j.}} [\log(\Gamma(n_{jt.})) + \log \alpha] \} \\
 & + \text{(k-term)} \log \frac{\Gamma(m_{..} + \gamma)}{\Gamma(\gamma)} + \sum_{k=1}^K [ \log \left( \frac{\Gamma(n_{..k} + W\phi_0)}{\prod_{w=1}^W \Gamma(\phi_0 + n_{..k}^w)} \right) + \log \left( \frac{\Gamma(\phi_0)^W}{\Gamma(W\phi_0)} \right) - \log(\Gamma(m_{.k})) - \log \gamma ]
 \end{aligned}$$

1) Previously, t-term wants only 1 table per restaurant while k-term wants every word forms a dish, which requires subtle annealing schedule.

By putting the restriction of  $\Gamma(m_{..} + \gamma)$  down to k-term, we now can anneal local-table move avoiding creating too many tables.

Annealing Schedule:  $[0.2, 0.4, 0.6, 0.8, 1]^p$

Fixing other parameters ( $p=0.5$ ), Figure 1 is the comparison of the annealing results for different formulae (anneal both local-table and merge-table)

2) Other Strategies:

- i) no anneal m-t, anneal l-t: doesn't work
- ii) anneal m-t, no anneal l-t: WORKS
- iii) no anneal m-t, no anneal l-t: doesn't work

{Tests from now on use the new formula}

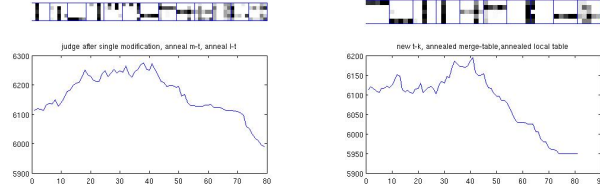


Figure 1: aneal m-t,aneal l-t left: Previous t,k-term, right: new t,k-term

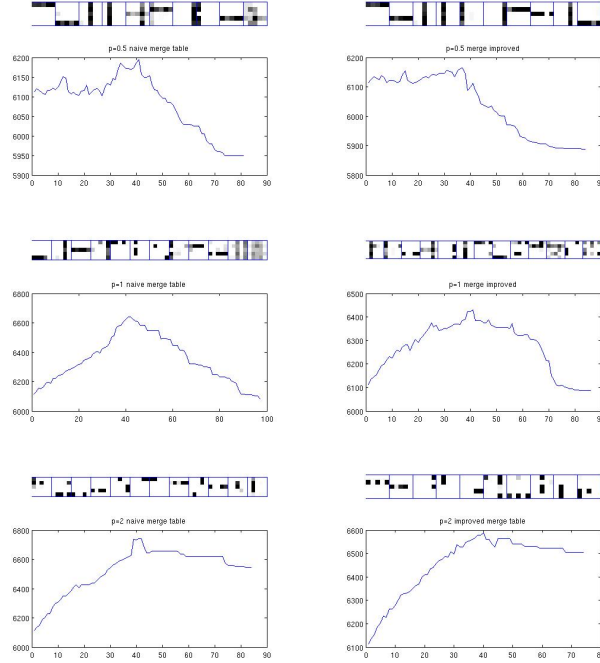


Figure 2: left: old merge-table; right: new merge-table; first row:  $T=0.5$ ; second row:  $T=1$ ; third row:  $T=2$ ;

## 2) New merge-table

- 1) Previously, in restaurant  $j$ , merge-table only tries find the best table  $t^*$  for certain table  $t$  to merge while serving  $k_{jt^*}$
- 2) A better merge-table should also search for the best  $k$  for the new merged table.

Fixing other parameters, Figure 2 is the comparison of the merge-table for different Annealing power  $p \in [0.5, 1, 2]$ .

**{Tests from now on use the new merge-table}**

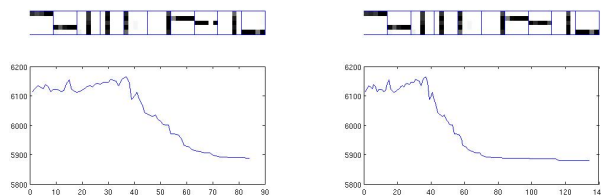


Figure 3: left: Get Stuck; right: Better config by local dish

### 3) Local Dish

#### i) Background

So far, for tables, we have:

- 1) Local-Table-Refinement
- 2) Local-Search-Dish
- 3) Merge-Table

But for dishes, we only have:

- 1) Merge-Dish

#### ii) Local Maxima

On the left of Figure 3, we expect the third to last dish to be a bar, which shares the word, say  $w$ , with the second to last dish.

But, in decompose restaurant, we will never see word  $w$  magically go to the third to last dish since the (k-term)sampling likelihood is almost 0, while merge-dish is too cumbersome to help.

It's not a perfect config since word  $w$  in ground truth comes from those two dishes. In some restaurants, it will cause small tables serving the second to last dish while the third to last dish is around.

#### iii) Welcome: Local Dish

Now we only have the building block "table", which forms restaurants and dishes.

There is another key fundamental part——**Word**

We can do Local-Dish-Refinement by greedily deciding the allocation of one certain word in the dish.(exchange it with another dish)

(Detail is in the pseudo-code description)

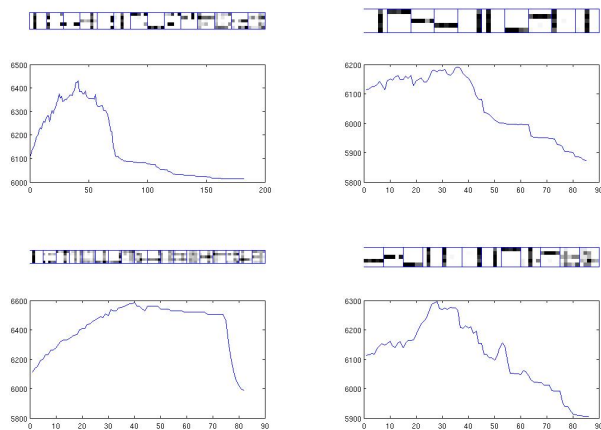


Figure 4: left: Anneal local-table; right: No Anneal local-table first row:  $p=1$ ; second row:  $p=2$ ;

## 4) Remarks

1) I still think it a bad idea to anneal local-table.

Though annealing local-table works for  $p=0.5$  (Temperature Schedule:  $[0.2, 0.4, 0.6, 0.8, 1]^p$ )

It fails (figure 4, left) for  $p=1, 2$  while it would still work (figure 4, right) if we do not anneal local-table. Maybe we can make up other stories for it.

From Above ( $p < 1$  is better than others, only anneal merge-table is better than anneal both m-t, l-t), we can see that, we do not need those much annealing to get out of the dominance of t-term.

It is only the "merge-table" that is doing bad without annealing, which is too greedy while the dish config is still vague.

Also, I did not anneal merge-dish and local-dish, which were doing right things without annealing.

If we anneal them, dishes will be less likely to merge or to refine, leading to bad config.

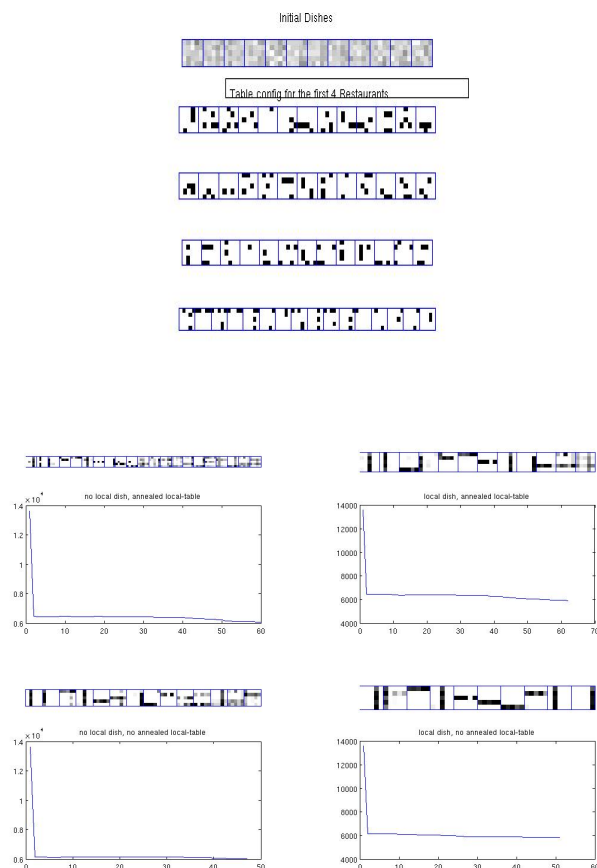


Figure 5: left: No local-dish; right: local-dish first row: annealed local-table;second row: no annealed local-table;

2) Local-Dish move can really make a change:)

Above, it seems local-dish is just for further, minor refinement.

Figure 5 shows that Local-Dish is **"indispensable"**.

I use the same initialization with that from Teh's Gibbs Sampling.(Every Restaurant has 12 tables and there are 12 random flat dish).

i) We still need annealing, since getting t-term better is a lot easier(simply merge-table) than improving k-term.

ii) Again, no anneal local-table is much better

iii) Without Local-Dish, we can still solve it with other annealing schedule. But the point is that with Local-Dish, our algorithm becomes more robust.

3) By now, we've almost figure out for small(40 5 by5 res) and medium(200 5 by5 res) toy data. I'm still debugging mex to see what will happen for larger datas.