# ICPC - Notebook

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# data structures

### 1.1 Ordered Set Gnu Pbds

```
1 #include <ext/pb_ds/assoc_container.hpp>
2 #include <ext/pb_ds/tree_policy.hpp>
3 using namespace __gnu_pbds;
4 template < typename T >
5 // using ordered_set = tree<T, null_type, less<T>,
      rb_tree_tag, tree_order_statistics_node_update>;
_{7} // if you want to find the elements less or equal :p _{55}
s using ordered_set = tree<T, null_type, less_equal<T>, _{56}
        rb_tree_tag, tree_order_statistics_node_update>;
      Segtree Rmq Lazy Max Update
                                                             59
                                                             60
struct SegmentTree
2 {
                                                             62
           int N:
                                                             63
           vll ns, lazy;
                                                             64
           SegmentTree (const vll &xs)
               : N (xs.size ()), ns (4 * N, 0), lazy (4
           {
                    for (size_t i = 0; i < xs.size (); ++</pre>
      i)
                             {
                                     update (i, i, xs[i]); 69
           }
12
           void
           update (int a, int b, ll value)
14
           {
                    update (1, 0, N - 1, a, b, value);
16
           }
           void
           update (int node, int L, int R, int a, int b,
19
        11 value)
20
           {
                                                             76
                    if (lazy[node])
21
                                                             77
22
                                     ns[node] = max (ns[
      node], lazy[node]);
                                                             80
                                      if (L < R)
24
                                                             81
26
                                                       lazy
       [2 * node]
                                                             83
       max (lazy[2 * node],
                                                             84
                                                             85 };
             lazy[node]);
                                                       lazy
29
       [2 * node + 1]
30
        max (lazy[2 * node + 1],
             lazy[node]);
                                              }
32
                                     lazy[node] = 0;
33
                    if (a > R \text{ or } b < L)
35
                            return;
37
                    if (a \le L \text{ and } R \le b)
                             {
38
39
                                     ns[node] = max (ns[
      node], value);
                                                             10
40
                                     if (L < R)
41
                                                       lazy 12
       [2 * node] = max (
43
      value, lazy[2 * node]);
                                                       lazv
44
       [2 * node + 1] = max (
45
                                                             16
      value, lazy[2 * node + 1]);
```

```
return;
            update (2 * node, L, (L + R) / 2, a,
b, value);
            update (2 * node + 1, (L + R) / 2 +
1, R, a, b, value);
            ns[node] = max (ns[node * 2], ns[node
 * 2 + 1]);
    }
    11
    RMQ (int a, int b)
            return RMQ (1, 0, N - 1, a, b);
    }
    11
    RMQ (int node, int L, int R, int a, int b)
            if (lazy[node])
                             ns[node] = max (ns[
node], lazy[node]);
                             if (L < R)
                                              lazy[
node * 21
 max (lazy[node * 2],
      lazy[node]);
                                              lazy[
node *2 + 1]
 max (lazy[node * 2 + 1],
      lazy[node]);
                             lazy[node] = 0;
                     }
            if (a > R \text{ or } b < L)
                     return 0;
            if (a <= L and R <= b)
                     return ns[node];
            11 x = RMQ (2 * node, L, (L + R) / 2,
 a, b);
            11 y = RMQ (2 * node + 1, (L + R) / 2
 + 1. R. a. b):
            return max (x, y);
    }
  Segtree Rmq Lazy Range
```

## 1.3

```
struct SegmentTree {
         int N:
          vll ns, lazy;
          SegmentTree(const vll &xs)
                  : N(xs.size()), ns(4 * N, INT_MAX),
     lazy(4 * N, 0) {
                  for (size_t i = 0; i < xs.size(); ++i</pre>
     ) update(i, i, xs[i]);
          }
          void update(int a, int b, ll value) {
                  update(1, 0, N - 1, a, b, value);
          void update(int node, int L, int R, int a,
      int b, ll value) {
                  if (lazy[node]) {
                          ns[node] = ns[node] ==
     INT_MAX ? lazy[node]
        : ns[node] + lazy[node];
                          if (L < R) {
                                   lazy[2 * node] +=
     lazy[node];
```

13

47 48

```
lazy[2 * node + 1] += 17
                                                                          return:
       lazy[node];
                           lazy[node] = 0;
                                                                      int mid = 1 + (r - 1) / 2;
19
                   }
20
                                                          21
                                                                      update(node * 2, 1, mid, p, v);
21
                   if (a > R \text{ or } b < L) return:
                                                          22
                   if (a \le L \text{ and } R \le b) {
                                                                      update(node * 2 + 1, mid + 1, r, p, v);
                                                          23
                           ns[node] =
                                                          24
                                    ns[node] == INT_MAX ? 25
                                                                      st[node] = min(st[node * 2], st[node * 2 +
       value : ns[node] + value;
                                                                 1]);
                           if (L < R) {
25
                                                          26
26
                                    lazy[2 * node] +=
                                                          27
      value:
                                                                 11 RMQ(int node, int L, int R, int l, int r) {
                                                          28
                                    lazy[2 * node + 1] += 29
                                                                      if (1 <= L and r >= R) return st[node];
                                                                      if (L > r or R < 1) return LLONG_MAX;</pre>
       value:
                                                          30
                            }
                                                                      if (L == R) return st[node];
                                                          31
28
29
                           return;
                                                          32
                                                                      int mid = L + (R - L) / 2;
30
                                                          33
                   update(2 * node, L, (L + R) / 2, a, b_{34}
       , value);
                                                                     return min(RMQ(node * 2, L, mid, 1, r),
                   update(2 * node + 1, (L + R) / 2 + 1, 36
                                                                                 RMQ(node * 2 + 1, mid + 1, R, 1, r)
       R, a, b, value);
                                                                 ));
                   ns[node] = min(ns[2 * node], ns[2 *
                                                                 }
      node + 1]);
                                                          38 };
          }
34
          11 RMQ(int a, int b) { return RMQ(1, 0, N -
                                                                   Sparse-segment-tree
                                                             1.5
      1, a, b); }
          11 RMQ(int node, int L, int R, int a, int b)
36
                                                           #include <bits/stdc++.h>
                                                           2 #pragma GCC optimize("03")
                   if (lazy[node]) {
                                                           3 #define FOR(i, x, y) for (int i = x; i < y; i++)
                           ns[node] = ns[node] ==
                                                           4 #define MOD 100000007
      INT_MAX ? lazy[node]
                                                           5 typedef long long 11;
                                                           6 using namespace std;
        : ns[node] + lazy[node];
40
                           if (L < R) {
                                                           8 struct Node {
                                    lazy[2 * node] +=
41
                                                               int sum, lazy, tl, tr, l, r;
                                                           9
      lazy[node];
                                                               Node(): sum(0), lazy(0), l(-1), r(-1) {}
                                    lazy[2 * node + 1] += ^{10}
                                                          11 };
       lazy[node];
43
                                                          13 const int MAXN = 123456;
                            lazy[node] = 0;
                                                           14 Node segtree[64 * MAXN];
45
                                                           15 int cnt = 2;
                   if (a > R or b < L) return INT_MAX;</pre>
                                                           16 const 11 v = 10;
47
                   if (a <= L and R <= b) return ns[node]^{17}
48
                                                           18 void push_lazy(int node) {
      ];
                                                               if (segtree[node].lazy) {
                                                          19
                   11 x = RMQ(2 * node, L, (L + R) / 2,
49
                                                                 segtree[node].sum = (segtree[node].tr - segtree[
      a, b);
                                                                 node].tl + 1) * v;
                   11 y = RMQ(2 * node + 1, (L + R) / 2
50
                                                                 int mid = (segtree[node].tl + segtree[node].tr) /
      + 1, R, a, b);
                                                                  2;
                   return min(x, y);
                                                                 if (segtree[node].l == -1) {
          }
52
                                                                    segtree[node].1 = cnt++;
                                                          23
53 };
                                                          24
                                                                    segtree[segtree[node].1].tl = segtree[node].tl;
                                                          25
                                                                    segtree[segtree[node].1].tr = mid;
        Segtree Point Rmq
                                                          26
                                                                 if (segtree[node].r == -1) {
                                                          27
1 class SegTree {
                                                                   segtree[node].r = cnt++;
                                                          28
                                                                    segtree[segtree[node].r].tl = mid + 1;
     public:
                                                          29
                                                                   segtree[segtree[node].r].tr = segtree[node].tr;
      int n:
                                                          30
      vector<1l> st;
                                                          31
      SegTree(const vector<ll> &v) : n((int)v.size()), 32
                                                                 segtree[segtree[node].1].lazy = segtree[segtree[
      st(n * 4 + 1, LLONG_MAX) {
                                                                 nodel.rl.lazv = v:
          for (int i = 0; i < n; ++i) update(i, v[i]); 33</pre>
                                                                  segtree[node].lazy = 0;
      void update(int p, ll v) { update(1, 0, n - 1, p, 35 }
      11 RMQ(int 1, int r) { return RMQ(1, 0, n - 1, 1, 37 void update(int node, int 1, int r) {
                                                               push_lazy(node);
                                                               if (1 == segtree[node].tl && r == segtree[node].tr)
10
11
     private:
      void update(int node, int 1, int r, int p, 11 v) 40
                                                                  segtree[node].lazy = v;
                                                                 push_lazy(node);
                                                           41
          if (p < l or p > r) return;
                                           // fora do
                                                               } else {
                                                           42
      intervalo.
                                                                 int mid = (segtree[node].tl + segtree[node].tr) /
                                                           43
          if (1 == r) {
                                                                 if (segtree[node].1 == -1) {
                                                           44
               st[node] = v;
                                                                    segtree[node].1 = cnt++;
16
                                                           45
```

#### segtree[segtree[node].1].tl = segtree[node].tl;121 46 segtree[segtree[node].1].tr = mid; 123 } 48 if (segtree[node].r == -1) { 49 50 segtree[node].r = cnt++; segtree[segtree[node].r].tl = mid + 1; 51 segtree[segtree[node].r].tr = segtree[node].tr; 52 54 **if** (1 > mid) update(segtree[node].r, 1, r); 56 else if (r <= mid)</pre> update(segtree[node].1, 1, r); 58 59 update(segtree[node].1, 1, mid); 60 61 update(segtree[node].r, mid + 1, r); 62 63 10 push\_lazy(segtree[node].1); 64 push\_lazy(segtree[node].r); 65 12 segtree[node].sum = 66 ${\tt segtree[segtree[node].1].sum + segtree[segtree[}^{13}$ 67 nodel.rl.sum: 68 } 69 } 16 70 17 71 int query(int node, int 1, int r) { push\_lazy(node); 72 if (1 == segtree[node].tl && r == segtree[node].tr) $^{18}$ 73 return segtree[node].sum; 74 int mid = (segtree[node].tl + segtree[node].tr) / $^{20}$ 76 if (segtree[node].l == -1) { 77 78 segtree[node].1 = cnt++; segtree[segtree[node].1].tl = segtree[node].tl; 79 segtree[segtree[node].l].tr = mid; 80 81 82 if (segtree[node].r == -1) { segtree[node].r = cnt++; 83 27 segtree[segtree[node].r].tl = mid + 1; 84 segtree[segtree[node].r].tr = segtree[node].tr; 85 29 86 30 87 **if** (1 > mid) 88 return query(segtree[node].r, 1, r); 89 else if (r <= mid)</pre> 90 33 return query(segtree[node].1, 1, r); 91 34 else 92 return query(segtree[node].1, 1, mid) + 93 35 query(segtree[node].r, mid + 1, r); 94 95 96 } 37 97 int main() { 38 iostream::sync\_with\_stdio(false); 39 99 cin.tie(0): 40 100 41 cout << "enter m: ";</pre> 101 cin >> m; 42 segtree[1].sum = 0;104 43 segtree[1].lazy = 0; 44 106 segtree[1].tl = 1; segtree[1].tr = 1e9;107 45 108 46 int c = 0; 109 47 FOR(\_, 0, m) { 110 int d, x, y; 48 cout << "enter d, x, y:";</pre> 49 cin >> d >> x >> y; **if** (d == 1) { 114 50 c = query(1, x, y); 51 cout << "c: "; 116 cout << c << '\n'; 117 118 } else { 53 update(1, x, y); 119 54 }

# 1.6 Segtree Rsq Lazy Range Sum

return 0:

```
1 struct SegTree {
          int N;
          vector <11> ns, lazy;
          SegTree(const vector<11> &xs)
                  : N(xs.size()), ns(4 * N, 0), lazy(4
     * N. 0) {
                  for (size_t i = 0; i < xs.size(); ++i</pre>
     ) update(i, i, xs[i]);
          }
          void update(int a, int b, ll value) {
                  update(1, 0, N - 1, a, b, value);
          void update(int node, int L, int R, int a,
      int b, ll value) {
                  // Lazy propagation
                  if (lazy[node]) {
                          ns[node] += (R - L + 1) *
      lazy[node];
                          if (L < R) // Se o ón ãno é
     uma folha, propaga
                          {
                                   lazy[2 * node] +=
     lazv[node]:
                                   lazy[2 * node + 1] +=
      lazy[node];
                          lazy[node] = 0;
                  }
                  if (a > R or b < L) return;
                  if (a <= L and R <= b) {
                          ns[node] += (R - L + 1) *
      value:
                          if (L < R) {</pre>
                                   lazy[2 * node] +=
      value:
                                   lazy[2 * node + 1] +=
       value;
                          }
                          return:
                  update(2 * node, L, (L + R) / 2, a, b
      , value);
                  update(2 * node + 1, (L + R) / 2 + 1,
      R, a, b, value);
                  ns[node] = ns[2 * node] + ns[2 * node
       + 1];
          11 RSQ(int a, int b) { return RSQ(1, 0, N -
     1, a, b); }
          11 RSQ(int node, int L, int R, int a, int b)
                  if (lazy[node]) {
                          ns[node] += (R - L + 1) *
     lazy[node];
                          if (L < R) {
                                   lazy[2 * node] +=
     lazy[node];
```

```
+ 1];
                                     lazy[2 * node + 1] +=
        lazy[node];
                                                                       11 rxq(int a, int b) { return RSQ(1, 0, N -
                                                            47
                            lazy[node] = 0;
                                                                   1, a, b); }
                   }
59
                                                            48
                                                                       11 rxq(int node, int L, int R, int a, int b)
60
                   if (a > R \text{ or } b < L) \text{ return } 0;
                                                                                if (lazy[node]) {
                                                                                        ns[node] ^= lazy[node];
                   if (a <= L and R <= b) return ns[node 51
      ];
                                                                                        if (L < R) {</pre>
                   11 x = RSQ(2 * node, L, (L + R) / 2, 54
                                                                                                 lazy[2 * node] ^=
65
      a, b);
                                                                   lazy[node];
                   ll y = RSQ(2 * node + 1, (L + R) / 2 55
                                                                                                 lazy[2 * node + 1] ^=
66
      + 1, R, a, b);
                                                                    lazy[node];
67
                   return x + y;
                                                            57
68
           }
                                                                                        lazy[node] = 0;
69
70 };
                                                                                }
                                                            59
                                                            60
        Segtree Rxq Lazy Range Xor
                                                                                if (a > R \text{ or } b < L) \text{ return } 0;
                                                            61
                                                            62
                                                                                if (a <= L and R <= b) return ns[node
struct SegTree {
                                                                   1:
          int N:
           vector <11> ns, lazy;
3
                                                                                11 x = rxq(2 * node, L, (L + R) / 2,
                                                                   a, b);
           SegTree(const vector<11> &xs)
                                                                                11 y = rxq(2 * node + 1, (L + R) / 2
                   : N(xs.size()), ns(4 * N, 0), lazy(4)
                                                                   + 1, R, a, b);
      * N. 0) {
                   for (size_t i = 0; i < xs.size(); ++i
68</pre>
                                                                                return x ^ y;
      ) update(i, i, xs[i]);
                                                                       }
           }
                                                            70 };
           void update(int a, int b, ll value) {
                                                              1.8
                                                                     Dsu
                   update(1, 0, N - 1, a, b, value);
                                                            1 class DSU:
           void update(int node, int L, int R, int a,
14
                                                                   def __init__(self, n):
      int b, ll value) {
                                                                       self.n = n
                    // Lazy propagation
                                                                       self.p = [x for x in range(0, n + 1)]
                   if (lazy[node]) {
16
                                                                       self.size = [0 for i in range(0, n + 1)]
                            ns[node] ^= lazy[node];
                                                                   def find_set(self, x): # log n
                            if (L < R) // Se o ón ãno é
19
                                                                       if self.p[x] == x:
      uma folha, propaga
                                                                           return x
20
                                                                       else:
                                                            10
                                     lazy[2 * node] ^=
                                                                           self.p[x] = self.find_set(self.p[x])
      lazy[node];
                                                                           return self.p[x]
                                                            12
                                     lazy[2 * node + 1] ^{-}= _{13}
22
        lazy[node];
                                                            14
                                                                   def same_set(self, x, y): # log n
                            }
                                                                       return bool(self.find_set(x) == self.find_set
                                                            15
                                                                   (V)
                            lazy[node] = 0;
25
                                                            16
26
                                                                   def union_set(self, x, y): # log n
                                                            17
                                                                       px = self.find_set(x)
                                                            18
                   if (a > R or b < L) return;
                                                                       py = self.find_set(y)
                                                            19
                                                            20
                   if (a \le L \text{ and } R \le b) {
30
                                                                       if px == py:
                                                            21
                            ns[node] ^= value;
31
                                                                           return
                                                            23
                            if (L < R) {
33
                                                                       size_x = self.size[px]
                                                            24
                                     lazy[2 * node] ^=
                                                                       size_y = self.size[py]
                                                            25
      value;
                                     lazy[2 * node + 1] ^{=}_{27}
35
                                                                       if size_x > size_y:
        value;
                                                                           self.p[py] = self.p[px]
                                                            28
                            }
36
                                                                           self.size[px] += self.size[py]
37
                                                            30
                                                                       else:
38
                            return;
                                                            31
                                                                           self.p[px] = self.p[py]
                   }
39
                                                                           self.size[py] += self.size[px]
40
                    update(2 * node, L, (L + R) / 2, a, b
                                                              1.9
                                                                     Dsu
       , value);
                   update(2 * node + 1, (L + R) / 2 + 1,
42
                                                            1 struct DSU {
        R, a, b, value);
                                                                vector < int > ps;
                   ns[node] = ns[2 * node] ^ ns[2 * node 3
                                                                vector < int > size;
44
```

57

58

61

62

21

24

28

41

```
sccid[u] = id;
      begin(), ps.end(), 0); }
                                                                    for (auto &v : g[u])
    int find_set(int x) { return ps[x] == x ? x : ps[x]_{12}
                                                                            if (!visited[v]) dfs(v, visited, g,
       = find_set(ps[x]); }
                                                                scc, buildScc, id, sccid);
    bool same_set(int x, int y) { return find_set(x) == 13
       find_set(y); }
                                                                    // if it's the first pass, add the node to
    void union_set(int x, int y) {
                                                                the scc
      if (same_set(x, y))
                                                                    if (buildScc) scc.eb(u);
                                                         15
                                                         16 }
10
                                                         17
      int px = find_set(x);
                                                         18 pair<11, vll> kosajaru(vll2d &g) {
12
      int py = find_set(y);
                                                         19
                                                                    ll n = len(g);
                                                                    vll scc:
13
                                                         20
      if (size[px] < size[py])</pre>
                                                                    vchar vis(n);
1.5
       swap(px, py);
                                                         22
                                                                    vll sccid(n);
                                                                    for (11 i = 0; i < n; i++)</pre>
16
                                                         23
                                                                            if (!vis[i]) dfs(i, vis, g, scc, true
17
      ps[py] = px;
                                                         24
      size[px] += size[py];
                                                                , 0, sccid);
18
    }
19
20 }:
                                                                    // build the transposed graph
                                                         26
                                                         27
                                                                    v112d gt(n);
  1.10 Sparse Table Rmq
                                                                    for (int i = 0; i < n; ++i)</pre>
                                                         28
                                                                            for (auto &v : g[i]) gt[v].eb(i);
                                                         29
1 /*
                                                                    // run the dfs on the previous scc order
                                                         31
          Sparse table implementation for rmq.
2
                                                         32
                                                                    11 id = 1;
3
          build: O(NlogN)
                                                         33
                                                                    vis.assign(n, false);
          query: 0(1)
                                                                    for (11 i = len(scc) - 1; i \ge 0; i--)
                                                         34
5 */
                                                         35
                                                                            if (!vis[scc[i]]) {
6 int fastlog2(ll x) {
                                                                                     dfs(scc[i], vis, gt, scc,
                                                         36
          ull i = x:
                                                                false, id++, sccid);
          return i ? __builtin_clzll(1) -
      __builtin_clzll(i) : -1;
                                                         37
                                                         38
                                                                    return {id - 1, sccid};
9 }
                                                         39 }
10 template <typename T>
11 class SparseTable {
                                                            2.2
                                                                  2-sat-(struct)
         public:
13
          int N:
          int K;
14
                                                         1 struct SAT2 {
15
          vector < vector < T >> st;
                                                          2
                                                               11 n:
          SparseTable(vector < T > vs)
16
                                                                vll2d adj, adj_t;
                                                          3
                  : N((int)vs.size()),
                                                                vc used;
                     K(fastlog2(N) + 1),
18
                                                                vll order, comp;
                     st(K + 1, vector < T > (N + 1)) {
19
                                                                vc assignment;
20
                   copy(vs.begin(), vs.end(), st[0].
                                                                bool solvable;
      begin());
                                                                SAT2(11 _n)
21
                                                                   : n(2 * _n),
                   for (int i = 1; i <= K; ++i)
22
                                                         10
                                                                      adj(n),
                           for (int j = 0; j + (1 << i)
                                                                      adi_t(n)
                                                         11
      \leq N; ++j
                                   st[i][j] = min(st[i - \frac{12}{13})
                                                                      used(n),
                                                                      order(n),
       1][j],
                                                                      comp(n, -1),
                                                   st[i - 15
25
                                                                      assignment(n / 2) {}
       1][j + (1 << (i - 1))]);
                                                         16
                                                                void dfs1(int v) {
26
                                                                    used[v] = true;
          T RMQ(int 1, int r) { // [1, r], 0 indexed
                                                                    for (int u : adj[v]) {
                                                         18
                  int i = fastlog2(r - 1 + 1);
28
                                                                        if (!used[u]) dfs1(u);
                                                         19
                  return min(st[i][1], st[i][r - (1 << \frac{1}{20}
      i) + 1]);
                                                         21
                                                                    order.push_back(v);
          }
30
                                                         22
31 };
                                                         23
                                                                void dfs2(int v, int cl) {
                                                         24
       graphs
                                                                    comp[v] = cl:
                                                         25
                                                                    for (int u : adj_t[v]) {
                                                         27
                                                                        if (comp[u] == -1) dfs2(u, cl);
      Scc-nodes-(kosajaru)
                                                         28
                                                         29
                                                                }
1 /*
                                                         30
2 * 0(n+m)
                                                                bool solve_2SAT() {
3 * Returns a pair <a, b>
                                                                    // find and label each SCC
                                                                    for (int i = 0; i < n; ++i) {</pre>
          a: number of SCCs
                                                         33
                                                                        if (!used[i]) dfs1(i);
          b: vector of size n, where b[i] is the SCC id 34
       of node i
6 * */
                                                                    reverse(all(order));
_{7} void dfs(ll u, vchar &visited, const vll2d &g, vll & _{37}
                                                                    11 j = 0;
      scc, bool buildScc, ll id,
                                                                    for (auto &v : order) {
                                                                        if (comp[v] == -1) dfs2(v, j++);
           vll &sccid) {
                                                         39
          visited[u] = true;
                                                         40
```

```
11 n = len(adj);
41
                                                           24
           assignment.assign(n / 2, false);
                                                                      vll order;
42
                                                           25
          for (int i = 0; i < n; i += 2) {
43
                                                           26
                                                                      vector < state > states(n, state::not_visited);
               // x and !x belong to the same SCC
                                                                      for (int i = 0; i < n; ++i) {</pre>
                                                           27
                                                                              if (states[i] == state::not_visited)
               if (comp[i] == comp[i + 1]) {
45
                   solvable = false;
46
                                                                 {
                   return false;
                                                                                       if (not dfs(adj, i, states,
48
                                                                 order)) return {};
49
                                                                              }
50
               assignment[i / 2] = comp[i] > comp[i +
                                                           31
                                                                      }
      1];
                                                                      reverse(all(order));
                                                           32
          }
                                                           33
                                                                      return order;
                                                           34 }
           solvable = true:
           return true;
                                                                   Lowest Common Ancestor Sparse Table
54
      void add_disjunction(int a, bool na, int b, bool
56
                                                           1 int fastlog2(ll x) {
      nb) {
                                                                      ull i = x;
           a = (2 * a) ^na;
                                                                      return i ?
                                                                                  __builtin_clzll(1) -
                                                           3
          b = (2 * b) ^n b;
58
                                                                 __builtin_clzll(i) : -1;
           int neg_a = a ^ 1;
59
                                                           4 }
           int neg_b = b ^1;
60
                                                           5 template <typename T>
           adj[neg_a].push_back(b);
61
                                                           6 class SparseTable {
           adj[neg_b].push_back(a);
                                                                    public:
63
           adj_t[b].push_back(neg_a);
                                                                     int N;
           adj_t[a].push_back(neg_b);
                                                                      int K;
                                                           9
65
                                                                      vector < vector < T >> st;
                                                           10
66 };
                                                           11
                                                                      SparseTable(vector<T> vs)
                                                                              : N((int)vs.size()),
                                                           12
  2.3 Floyd Warshall
                                                                                K(fastlog2(N) + 1),
                                                                                st(K + 1, vector < T > (N + 1)) {
_{\rm 1} vector<vll> floyd_warshall(const vector<vll> &adj, ll _{\rm 15}
                                                                              copy(vs.begin(), vs.end(), st[0].
       n) {
                                                                 begin());
          auto dist = adj;
                                                           17
                                                                              for (int i = 1; i <= K; ++i)
           for (int i = 0; i < n; ++i) {
                                                                                       for (int j = 0; j + (1 << i)
                                                           18
                   for (int j = 0; j < n; ++j) {
                                                                  <= N; ++j)
                           for (int k = 0; k < n; ++k) {
                                                                                               st[i][j] = min(st[i -
                                    dist[j][k] = min(dist
                                                                  1][j],
      [j][k],
                                                                                                               st[i -
                                                      dist
                                                                  1][j + (1 << (i - 1))]);
      [j][i] + dist[i][k]);
                                                          21
9
                                                                      SparseTable() {}
                                                          22
10
                   }
                                                                      T RMQ(int 1, int r) {
                                                          23
          }
11
                                                                              int i = fastlog2(r - 1 + 1);
                                                          24
          return dist;
12
                                                                              return min(st[i][1], st[i][r - (1 <<</pre>
13 }
                                                                 i) + 1]);
                                                                     }
                                                          26
  2.4
        Topological-sorting
                                                          27 };
                                                          28 class LCA {
                                                           29
                                                                     public:
  * O(V)
                                                           30
                                                                     int p;
3 * assumes:
                                                          31
                                                                      int n;
        * vertices have index [0, n-1]
                                                                      vi first;
                                                          32
  * if is a DAG:
                                                                      vector < char > visited;
5
                                                          33
                                                                      vi vertices;
         * returns a topological sorting
   * else:
                                                                      vi height;
                                                          35
                                                                      SparseTable <int> st;
         * returns an empty vector
9 * */
10 enum class state { not_visited, processing, done };
                                                                      LCA(const vector < vi> &g)
                                                          38
11 bool dfs(const vector<vll> &adj, ll s, vector<state> 39
                                                                              : p(0),
      &states, vll &order) {
                                                                                n((int)g.size()),
                                                           40
           states[s] = state::processing;
                                                                                first(n + 1),
                                                                                visited(n + 1, 0),
          for (auto &v : adj[s]) {
                   if (states[v] == state::not_visited) 43
                                                                                height(n + 1) {
14
                                                                              build_dfs(g, 1, 1);
                           if (not dfs(adj, v, states,
                                                                              st = SparseTable < int > (vertices);
                                                           45
      order)) return false;
                                                                      }
                   } else if (states[v] == state::
16
                                                           47
                                                                      void build_dfs(const vector<vi> &g, int u,
      processing)
                                                           48
                           return false;
                                                                 int hi) {
                                                                              visited[u] = true;
18
                                                           49
          states[s] = state::done;
                                                                              height[u] = hi;
19
                                                           50
          order.pb(s);
                                                                              first[u] = vertices.size();
20
                                                           51
          return true;
                                                                              vertices.push_back(u);
22 }
                                                                              for (auto uv : g[u]) {
                                                           53
vll topologicalSorting(const vector<vll> &adj) {
                                                                                       if (!visited[uv]) {
                                                           54
```

```
build_dfs(g, uv, hi +24
                                                                       size_x = self.size[px]
        1);
                                                                       size_y = self.size[py]
                                     vertices.push_back(u) 26
56
                                                                       if size_x > size_y:
                            }
                                                                           self.p[py] = self.p[px]
                   }
                                                                           self.size[px] += self.size[py]
58
                                                           29
           }
59
                                                           30
                                                                           self.p[px] = self.p[py]
60
                                                           31
           int lca(int a, int b) {
                                                                           self.size[py] += self.size[px]
61
62
                   int l = min(first[a], first[b]);
                                                           33
                    int r = max(first[a], first[b]);
                                                           34
63
64
                    return st.RMQ(1, r);
                                                           35 def kruskal(gv, n):
           }
                                                           36
65
66 };
                                                                  Receives te list of edges as a list of tuple in
                                                                  the form:
  2.6
         Count-scc-(kosajaru)
                                                                       d, u, v
                                                           38
                                                                       d: distance between u and v
                                                           39
                                                                  And also n as the total of verties.
                                                            40
void dfs(ll u, vchar &visited, const vll2d &g, vll &
      scc, bool buildScc) {
                                                                  dsu = DSU(n)
                                                            42
           visited[u] = true;
           for (auto &v : g[u])
                                                            43
                                                                  c = 0
                                                            44
                   if (!visited[v]) dfs(v, visited, g,
                                                                  for e in gv:
                                                            45
      scc, buildScc);
                                                            46
                                                                       d, u, v = e
5
                                                                       if not dsu.same_set(u, v):
                                                            47
           // if it's the first pass, add the node to
6
                                                                           c += d
      the scc
                                                           49
                                                                           dsu.union_set(u, v)
           if (buildScc) scc.eb(u);
                                                           50
8 }
                                                           51
                                                                  return c
9
10 ll kosajaru(vll2d &g) {
                                                                   Scc-(struct)
                                                              2.8
           11 n = len(g);
11
           vll scc;
12
           vchar vis(n):
13
                                                            1 struct SCC {
           for (ll i = 0; i < n; i++)</pre>
14
                                                                       11 N;
                   if (!vis[i]) dfs(i, vis, g, scc, true
                                                                       vll2d adj, tadj;
                                                                       vll todo, comps, comp;
16
                                                                       vector < set < 11 >> sccadj;
           // build the transposed graph
17
                                                                       vchar vis;
                                                            6
18
           v112d gt(n);
                                                                       SCC(11 _N)
           for (int i = 0; i < n; ++i)
                                                                               : N(_N), adj(_N), tadj(_N), comp(_N,
                   for (auto &v : g[i]) gt[v].eb(i);
20
                                                                  -1), sccadj(_N), vis(_N) {}
21
           // run the dfs on the previous scc order
                                                                       void add_edge(ll x, ll y) { adj[x].eb(y),
                                                            10
           11 \ \text{scccnt} = 0;
                                                                  tadj[y].eb(x); }
           vis.assign(n, false);
24
           for (ll i = len(scc) - 1; i >= 0; i--)
25
                                                                       void dfs(ll x) {
                   if (!vis[scc[i]]) dfs(scc[i], vis, gt _{\rm 13}
26
                                                                               vis[x] = 1;
       , scc, false), scccnt++;
                                                                               for (auto &y : adj[x])
                                                            14
           return scccnt;
                                                                                        if (!vis[y]) dfs(y);
28 }
                                                                               todo.pb(x);
                                                           16
                                                           17
                                                                       }
  2.7 Kruskal
                                                                       void dfs2(11 x, 11 v) \{
                                                           18
                                                           19
                                                                               comp[x] = v;
1 class DSU:
                                                                               for (auto &y : tadj[x])
                                                           20
      def __init__(self, n):
                                                           21
                                                                                        if (comp[y] == -1) dfs2(y, v)
2
           self.n = n
           self.p = [x for x in range(0, n + 1)]
                                                                       }
                                                           22
           self.size = [0 for i in range(0, n + 1)]
                                                                       void gen() {
                                                           23
                                                                               for (11 i = 0; i < N; ++i)
                                                           24
                                                                                        if (!vis[i]) dfs(i);
      def find_set(self, x):
           if self.p[x] == x:
                                                                               reverse(all(todo));
                                                           26
                                                                               for (auto &x : todo)
9
               return x
                                                           27
           else:
                                                                                        if (comp[x] == -1) {
                                                                                                dfs2(x, x);
               self.p[x] = self.find_set(self.p[x])
               return self.p[x]
                                                                                                 comps.pb(x);
12
                                                                                        }
13
                                                           31
       def same_set(self, x, y):
14
           return bool(self.find_set(x) == self.find_set 33
                                                                       void genSCCGraph() {
                                                           34
                                                                               for (11 i = 0; i < N; ++i) {</pre>
16
                                                           35
                                                                                        for (auto &j : adj[i]) {
17
       def union_set(self, x, y):
                                                           36
           px = self.find_set(x)
                                                           37
                                                                                                if (comp[i] != comp[j
18
           py = self.find_set(y)
                                                                  1) {
19
                                                                                                         sccadj[comp[i
20
                                                           38
           if px == py:
                                                                  ]].insert(comp[j]);
                                                                                                }
22
               return
                                                           39
                                                                                        }
23
                                                            40
```

```
}
                                                            1 const int maxn = 1e2 + 14, lg = 15;
41
           }
                                                            2 const int base = 1000000000;
42
43 };
                                                            3 const int base_digits = 9;
                                                            4 struct bigint {
  2.9
        Check-bipartite
                                                                      vector < int > a;
                                                                      int sign;
1 // O(V)
                                                                      int size() {
2 bool checkBipartite(const ll n, const vector<vll> &
                                                                               if (a.empty()) return 0;
      adj) {
                                                                               int ans = (a.size() - 1) *
          11 s = 0;
                                                                  base_digits;
           queue <11> q;
                                                                               int ca = a.back();
           q.push(s);
                                                                               while (ca) ans++, ca /= 10;
           vll color(n, INF);
                                                                               return ans;
           color[s] = 0;
                                                           14
           bool isBipartite = true;
                                                                      bigint operator^(const bigint &v) {
           while (!q.empty() && isBipartite) {
                                                                               bigint ans = 1, a = *this, b = v;
                                                           16
                   11 u = q.front();
                                                                               while (!b.isZero()) {
                                                           17
                   q.pop();
                                                                                       if (b % 2) ans *= a;
12
                   for (auto &v : adj[u]) {
                                                                                       a *= a, b /= 2;
                                                           19
                            if (color[v] == INF) {
                                                                               }
                                     color[v] = 1 - color[
                                                                               return ans;
      u];
                                                           22
                                    q.push(v);
                                                                      string to_string() {
                           } else if (color[v] == color[
16
                                                                               stringstream ss;
                                                           24
      u]) {
                                                                               ss << *this;
                                                           25
                                    return false;
17
                                                           26
                                                                               string s;
                           }
18
                                                                               ss >> s;
                                                           27
                   }
19
                                                           28
                                                                               return s;
           }
20
                                                                      }
                                                           29
21
           return true;
                                                                      int sumof() {
22 }
                                                                               string s = to_string();
                                                           31
                                                                               int ans = 0;
                                                           32
  2.10
          Dijkstra
                                                                               for (auto c : s) ans += c - '0';
                                                                               return ans;
1 11 __inf = LLONG_MAX >> 5;
vll dijkstra(const vector<vector<pll>>> &g, ll n) {
                                                                       /*</arpa>*/
          priority_queue<pll, vector<pll>, greater<pll 37</pre>
                                                                      bigint() : sign(1) {}
      >> pq;
                                                                      bigint(long long v) { *this = v; }
           vll dist(n, __inf);
                                                           39
           vector < char > vis(n);
                                                           40
           pq.emplace(0, 0);
                                                                      bigint(const string &s) { read(s); }
                                                           41
           dist[0] = 0;
                                                                      void operator=(const bigint &v) {
           while (!pq.empty()) {
                                                           43
                   auto [d1, v] = pq.top();
                                                                               sign = v.sign;
                                                           44
9
                   pq.pop();
                                                           45
                                                                               a = v.a;
                   if (vis[v]) continue;
11
                                                           46
                   vis[v] = true;
                                                                      void operator=(long long v) {
                                                           48
                   for (auto [d2, u] : g[v]) {
                                                           49
                                                                               sign = 1;
14
                            if (dist[u] > d1 + d2) {
                                                           50
                                                                               a.clear();
                                    dist[u] = d1 + d2;
                                                                               if (v < 0) sign = -1, v = -v;
                                                           51
16
                                    pq.emplace(dist[u], u52
                                                                               for (; v > 0; v = v / base) a.
      );
                                                                  push_back(v % base);
                            }
                                                                      }
                                                           53
18
                   }
                                                           54
19
                                                                      bigint operator+(const bigint &v) const {
                                                           55
20
           return dist;
                                                           56
                                                                               if (sign == v.sign) {
21
                                                                                       bigint res = v;
22 }
                                                           57
                                                           58
                                                                                       for (int i = 0, carry = 0;
  3
                                                           59
       extras
                                                                                             i < (int)max(a.size(), v</pre>
                                                           60
                                                                  .a.size()) || carry; ++i) {
        Binary To Gray
                                                                                                if (i == (int)res.a.
                                                           61
                                                                  size()) res.a.push_back(0);
                                                                                                res.a[i] +=
                                                           62
string binToGray(string bin){
                                                                                                         carry + (i <
                                                           63
      string gray(bin.size(), '0');
                                                                  (int)a.size() ? a[i] : 0);
      int n = bin.size()-1;
                                                                                                carry = res.a[i] >=
                                                           64
      gray[0] = bin[0];
                                                                  base:
      for(int i = 1; i <= n; i++){</pre>
                                                                                                if (carry) res.a[i]
           gray[i] = '0'+(bin[i-1]=='1')^(bin[i]=='1');
                                                                  -= base;
                                                                                       }
      return gray;
                                                           67
                                                                                       return res;
9 }
                                                           68
                                                                               return *this - (-v);
                                                           69
  3.2
        Bigint
                                                                      }
```

```
}
    bigint operator-(const bigint &v) const {
                                                               friend pair < bigint , bigint > divmod(const
            if (sign == v.sign) {
                                                    134
                     if (abs() >= v.abs()) {
                                                           bigint &a1, const bigint &b1) {
                             bigint res = *this;
                                                                        int norm = base / (b1.a.back() + 1);
                                                                        bigint a = a1.abs() * norm;
                             for (int i = 0, carry 136
 = 0:
                                                                        bigint b = b1.abs() * norm;
                                   i < (int)v.a.
                                                                        bigint q, r;
                                                   138
size() || carry; ++i) {
                                                                        q.a.resize(a.a.size());
                                      res.a[i] -=
                                                   140
carry + (i < (int)v.a.size()</pre>
                                                                        for (int i = a.a.size() - 1; i >= 0;
                                                    141
                                                           i--) {
                 ? v.a[i]
                                                                                r *= base;
                                                    142
                                                                                r += a.a[i];
                                                                                int s1 = r.a.size() <= b.a.</pre>
                 : 0):
                                                    144
                                      carry = res.a
                                                           size() ? 0 : r.a[b.a.size()];
[i] < 0;
                                                                                int s2 = r.a.size() \le b.a.
                                      if (carry)
                                                           size() - 1
res.a[i] += base;
                                                                                                  ? 0
                                                    146
                                                                                                  : r.a[b.a.
                                                    147
                             res.trim();
                                                           size() - 1];
                                                                                int d = ((long long)base * s1
                             return res;
                                                    148
                     }
                                                            + s2) / b.a.back();
                     return -(v - *this);
                                                    149
                                                                                r -= b * d;
            }
                                                                                while (r < 0) r += b, --d;
                                                    150
            return *this + (-v);
                                                                                q.a[i] = d;
    7
                                                                        7
                                                   153
    void operator*=(int v) {
                                                    154
                                                                        q.sign = a1.sign * b1.sign;
            if (v < 0) sign = -sign, v = -v;
                                                                        r.sign = a1.sign;
                                                   155
                                                                        q.trim();
            for (int i = 0, carry = 0; i < (int)a156
.size() || carry; ++i) {
                                                                        r.trim();
                     if (i == (int)a.size()) a.
                                                    158
                                                                        return make_pair(q, r / norm);
push_back(0);
                                                   159
                                                               7
                     long long cur = a[i] * (long 160
long)v + carry;
                                                               bigint operator/(const bigint &v) const {
                     carry = (int)(cur / base);
                                                                        return divmod(*this, v).first;
                                                    162
                     a[i] = (int)(cur % base);
                     // asm("divl %%ecx" : "=a"(
                                                   164
carry), "=d"(a[i]) :
                                                               bigint operator%(const bigint &v) const {
                     // "A"(cur), "c"(base));
                                                                        return divmod(*this, v).second;
                                                    166
            }
                                                   167
            trim();
    }
                                                               void operator/=(int v) {
                                                    169
                                                                        if (v < 0) sign = -sign, v = -v;
    bigint operator*(int v) const {
                                                                        for (int i = (int)a.size() - 1, rem =
                                                    171
            bigint res = *this;
                                                            0; i >= 0; --i) {
            res *= v;
                                                                                long long cur = a[i] + rem *
            return res:
                                                           (long long)base;
    }
                                                                                a[i] = (int)(cur / v);
                                                    173
                                                                                rem = (int)(cur % v);
                                                    174
    void operator*=(long long v) {
                                                                        }
                                                    175
            if (v < 0) sign = -sign, v = -v;
                                                                        trim();
            if (v > base) {
                                                    177
                     *this = *this * (v / base) * 178
                                                               bigint operator/(int v) const {
base + *this * (v % base);
                                                    179
                                                                        bigint res = *this;
                     return;
                                                    180
                                                                        res /= v;
            for (int i = 0, carry = 0; i < (int)a_{182}
                                                                        return res:
.size() || carry; ++i) {
                                                               }
                     if (i == (int)a.size()) a.
                                                    184
push_back(0);
                                                   185
                                                               int operator%(int v) const {
                     long long cur = a[i] * (long 186
                                                                        if (v < 0) v = -v;
                                                                        int m = 0;
long)v + carry;
                                                   187
                     carry = (int)(cur / base);
                                                                        for (int i = a.size() - 1; i >= 0; --
                     a[i] = (int)(cur % base);
                                                           i)
                     // asm("divl %%ecx" : "=a"(
                                                                                m = (a[i] + m * (long long))
carry), "=d"(a[i]) :
                                                           base) % v;
                     // "A"(cur), "c"(base));
                                                                        return m * sign;
                                                    190
            }
                                                               }
                                                    191
            trim();
    }
                                                               void operator+=(const bigint &v) { *this = *
                                                           this + v; }
    bigint operator*(long long v) const {
                                                               void operator -=(const bigint &v) { *this = *
                                                    194
            bigint res = *this;
                                                           this - v; }
            res *= v;
                                                               void operator*=(const bigint &v) { *this = *
                                                    195
            return res;
                                                           this * v; }
```

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```
void operator/=(const bigint &v) { *this = * 257
this / v; }
                                                                         for (int i = s.size() - 1; i >= pos;
                                                            i -= base_digits) {
    bool operator < (const bigint &v) const {</pre>
                                                                                  int x = 0:
             if (sign != v.sign) return sign < v. 260
                                                                                  for (int j = max(pos, i -
sign;
                                                            base_digits + 1); j <= i; j++)
             if (a.size() != v.a.size())
                                                                                           x = x * 10 + s[j] - 
                                                            0::
                     return a.size() * sign < v.a.</pre>
size() * v.sign;
                                                                                  a.push_back(x);
             for (int i = a.size() - 1: i >= 0: i 263
                                                                         }
--)
                                                                         trim();
                                                     264
                     if (a[i] != v.a[i]) return a[265
                                                                 }
i] * sign < v.a[i] * sign;
                                                     266
             return false;
                                                                 friend istream &operator>>(istream &stream,
    }
                                                            bigint &v) {
                                                                         string s;
                                                    268
    bool operator>(const bigint &v) const {
                                                                         stream >> s;
                                                    269
return v < *this; }</pre>
                                                                         v.read(s);
                                                    270
    bool operator <= (const bigint &v) const {</pre>
                                                    271
                                                                         return stream;
return !(v < *this); }</pre>
                                                                }
                                                    272
    bool operator >= (const bigint &v) const {
                                                    273
                                                                 friend ostream &operator << (ostream &stream,</pre>
return !(*this < v); }
                                                    274
    bool operator == (const bigint &v) const {
                                                            const bigint &v) {
             return !(*this < v) && !(v < *this); 275
                                                                         if (v.sign == -1) stream << '-';</pre>
    }
                                                                         stream << (v.a.empty() ? 0 : v.a.back
                                                    276
    bool operator!=(const bigint &v) const {
                                                             ());
             return *this < v || v < *this;
                                                                         for (int i = (int)v.a.size() - 2; i
    }
                                                            >= 0: --i)
                                                     278
                                                                                  stream << setw(base_digits)</pre>
    void trim() {
                                                            << setfill('0') << v.a[i];
             while (!a.empty() && !a.back()) a.
                                                     279
                                                                         return stream;
pop_back();
                                                                 }
                                                     280
             if (a.empty()) sign = 1;
                                                     281
    }
                                                                 static vector<int> convert_base(const vector<</pre>
                                                     282
                                                            int> &a, int old_digits,
    bool isZero() const { return a.empty() || (a.283
size() == 1 && !a[0]); }
                                                            new_digits) {
                                                                         vector < long long > p(max(old_digits,
    bigint operator-() const {
                                                            new_digits) + 1);
                                                                         p[0] = 1;
             bigint res = *this;
                                                    285
             res.sign = -sign;
                                                                         for (int i = 1; i < (int)p.size(); i</pre>
                                                     286
                                                            ++) p[i] = p[i - 1] * 10;
             return res;
    }
                                                                         vector < int > res;
                                                    287
                                                                         long long cur = 0;
                                                    288
    bigint abs() const {
                                                                         int cur_digits = 0;
                                                    289
                                                                         for (int i = 0; i < (int)a.size(); i</pre>
             bigint res = *this;
                                                     290
             res.sign *= res.sign;
                                                            ++) {
                                                                                  cur += a[i] * p[cur_digits];
             return res;
                                                     291
                                                                                  cur_digits += old_digits;
    }
                                                    292
                                                                                  while (cur_digits >=
                                                    293
    long longValue() const {
                                                            new_digits) {
             long long res = 0;
                                                                                           res.push_back(int(cur
                                                    294
             for (int i = a.size() - 1; i >= 0; i
                                                             % p[new_digits]));
                                                                                           cur /= p[new_digits];
--) res = res * base + a[i]:
                                                    295
                                                                                           cur_digits -=
             return res * sign;
                                                            new_digits;
                                                                                  }
                                                    297
    friend bigint gcd(const bigint &a, const
                                                    298
bigint &b) {
                                                                         res.push_back((int)cur);
                                                     299
             return b.isZero() ? a : gcd(b, a % b)300
                                                                         while (!res.empty() && !res.back())
                                                            res.pop_back();
    }
                                                                         return res;
                                                     301
                                                                 }
    friend bigint lcm(const bigint &a, const
                                                    302
bigint &b) {
                                                    303
             return a / gcd(a, b) * b;
                                                                 typedef vector < long long > vll;
                                                     304
    }
                                                    305
                                                                 static vll karatsubaMultiply(const vll &a,
    void read(const string &s) {
                                                            const vll &b) {
             sign = 1;
                                                                         int n = a.size();
                                                    307
             a.clear();
                                                                         vll res(n + n);
                                                     308
                                                                         if (n <= 32) {
             int pos = 0;
                                                    309
             while (pos < (int)s.size() &&</pre>
                                                                                  for (int i = 0; i < n; i++)</pre>
                                                     310
                    (s[pos] == '-' || s[pos] == '+311
                                                                                           for (int j = 0; j < n
,)) {
                                                            ; j++)
                     if (s[pos] == '-') sign = - 312
                                                                                                   res[i + j] +=
                                                             a[i] * b[j];
sign;
                     ++pos;
                                                                                  return res;
```

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253

254

```
}
314
315
                                                              13
                     int k = n \gg 1;
316
                                                              14
                     vll a1(a.begin(), a.begin() + k);
317
                                                              15
                     vll a2(a.begin() + k, a.end());
319
                     vll b1(b.begin(), b.begin() + k);
                                                              17
                     vll b2(b.begin() + k, b.end());
320
321
                     vll a1b1 = karatsubaMultiply(a1, b1); 20
                     vll a2b2 = karatsubaMultiply(a2, b2); 21
323
324
325
                     for (int i = 0; i < k; i++) a2[i] += 23
                                                              24 }
       a1[i]:
                     for (int i = 0; i < k; i++) b2[i] +=
       b1[i]:
327
328
                     vll r = karatsubaMultiply(a2, b2);
                     for (int i = 0; i < (int)a1b1.size();</pre>
         i++) r[i] -= a1b1[i];
330
         i++) r[i] -= a2b2[i];
331
                     for (int i = 0; i < (int)r.size(); i</pre>
332
        ++) res[i + k] += r[i];
                     for (int i = 0; i < (int)a1b1.size();</pre>
333
         i++) res[i] += a1b1[i];
                     for (int i = 0; i < (int)a2b2.size();</pre>
335
                             res[i + n] += a2b2[i];
                     return res:
336
            }
                                                              12
338
                                                              13
            bigint operator*(const bigint &v) const {
339
                                                              14
                     vector < int > a6 = convert_base(this->a 15
340
        , base_digits, 6);
                                                              16
                     vector < int > b6 = convert_base(v.a,
                                                              17
       base_digits, 6);
                                                              18
                     vll a(a6.begin(), a6.end());
                                                              19
343
                     vll b(b6.begin(), b6.end());
                     while (a.size() < b.size()) a.</pre>
344
       push_back(0);
                     while (b.size() < a.size()) b.
345
                                                              21
       push_back(0);
                                                              22
                     while (a.size() & (a.size() - 1))
346
                                                              23
                             a.push_back(0), b.push_back
347
                                                              24
        (0);
                                                              25 }
                     vll c = karatsubaMultiply(a, b);
348
                     bigint res;
                     res.sign = sign * v.sign;
350
351
                     for (int i = 0, carry = 0; i < (int)c
        .size(); i++) {
                              long long cur = c[i] + carry;
352
                             res.a.push_back((int)(cur %
       1000000));
                              carry = (int)(cur / 1000000);
355
                     }
                     res.a = convert_base(res.a, 6,
356
       base_digits);
                     res.trim():
357
                                                              10
                     return res;
                                                              11
            }
359
                                                              12
360 }:
                                                              13
                                                              14
```

### 3.3 Get-permutation-cicles

# 4 dynamic programming

### 4.1 Edit Distance

```
for (int i = 0; i < (int)a2b2.size(); _{1} int edit_distance(const string &a, const string &b) {
                                                  int n = a.size();
                                                  int m = b.size();
                                                  vector < vi > dp(n + 1, vi(m + 1, 0));
                                                  int ADD = 1, DEL = 1, CHG = 1;
                                                  for (int i = 0; i <= n; ++i) {</pre>
                                                          dp[i][0] = i * DEL;
                                                  for (int i = 1; i <= m; ++i) {</pre>
                                                          dp[0][i] = ADD * i;
                                                  for (int i = 1; i <= n; ++i) {
                                                          for (int j = 1; j <= m; ++j) {
                                                                   int add = dp[i][j - 1] + ADD;
                                                                   int del = dp[i - 1][j] + DEL;
                                                                   int chg = dp[i - 1][j - 1] +
                                                                              (a[i - 1] == b[j -
                                              1] ? 0 : 1) * CHG;
                                                                   dp[i][j] = min({add, del, chg
                                              });
                                                          }
                                                  return dp[n][m];
```

# 4.2 Money Sum Bottom Up

```
find every possible sum using
  the given values only once.
set < int > money_sum(const vi &xs) {
        using vc = vector < char >;
        using vvc = vector < vc >;
        int _m = accumulate(all(xs), 0);
        int _n = xs.size();
        vvc _dp(_n + 1, vc(_m + 1, 0));
        set < int > _ans;
         _{dp}[0][xs[0]] = 1;
        for (int i = 1; i < _n; ++i) {</pre>
                 for (int j = 0; j <= _m; ++j) {</pre>
                          if (j == 0 or _dp[i - 1][j])
    {
                                   _{dp[i][j + xs[i]] =}
    1:
                                   _{dp[i][j]} = 1;
                          }
                 }
        for (int i = 0; i < _n; ++i)</pre>
                 for (int j = 0; j \le _m; ++j)
                          if (_dp[i][j]) _ans.insert(j)
        return _ans;
```

21

23

```
4 pll mostDistantFrom(const vector <vll> &adj, ll n, ll
                                                                  root) {
        Knapsack Dp Values 01
                                                                      // O indexed
  4.3
                                                                      11 mostDistantNode = root;
                                                            6
                                                                      11 nodeDistance = 0;
_{1} const int MAX_N = 1001;
                                                                      queue <pll> q;
2 const int MAX_S = 100001;
                                                                      vector < char > vis(n);
3 array < array < int , MAX_S > , MAX_N > dp;
                                                                      q.emplace(root, 0);
                                                           10
4 bool check[MAX_N][MAX_S];
                                                                      vis[root] = true;
5 pair<int, vi> knapsack(int S, const vector<pii> &xs)
                                                                      while (!q.empty()) {
      {
                                                                               auto [node, dist] = q.front();
           int N = (int)xs.size();
                                                                               q.pop();
                                                                               if (dist > nodeDistance) {
          for (int i = 0; i \le N; ++i) dp[i][0] = 0;
                                                                                       nodeDistance = dist;
                                                                                       mostDistantNode = node;
                                                           17
          for (int m = 0; m <= S; ++m) dp[0][m] = 0;</pre>
10
                                                           18
                                                           19
                                                                               for (auto u : adj[node]) {
           for (int i = 1; i <= N; ++i) {</pre>
12
                                                                                       if (!vis[u]) {
                                                           20
                   for (int m = 1; m <= S; ++m) {</pre>
                                                                                                vis[u] = true;
                                                           21
14
                            dp[i][m] = dp[i - 1][m];
                                                                                                q.emplace(u, dist +
                            check[i][m] = false;
                                                                  1);
16
                                                                                       }
                            auto [w, v] = xs[i - 1];
                                                           24
18
                            if (w <= m and (dp[i - 1][m - 25
                                                                      }
                                                                      return {mostDistantNode, nodeDistance};
       w] + v) >= dp[i][m]) {
                                    dp[i][m] = dp[i - 1][_{00}^{27}]
20
      m - w] + v;
                                                           29 ll twoNodesDist(const vector < vll > & adj, ll n, ll a,
                                    check[i][m] = true;
21
                                                                  11 b) {
                            }
                                                                      queue <pll> q;
                                                           30
                   }
23
                                                           31
                                                                      vector < char > vis(n);
24
           }
                                                                      q.emplace(a, 0);
                                                           32
25
                                                                      while (!q.empty()) {
                                                           33
           int m = S;
26
                                                                               auto [node, dist] = q.front();
                                                           34
27
          vi es;
                                                           35
                                                                               q.pop();
28
                                                                               if (node == b) return dist;
           for (int i = N; i >= 1; --i) {
                                                                               for (auto u : adj[node]) {
                                                           37
                  if (check[i][m]) {
30
                                                                                       if (!vis[u]) {
                            es.push_back(i);
                                                                                                vis[u] = true;
                                                           39
                            m -= xs[i - 1].first;
32
                                                                                                q.emplace(u, dist +
                                                           40
                   }
33
                                                                  1);
          }
34
                                                                                       }
                                                           41
35
                                                                               }
           reverse(es.begin(), es.end());
                                                                      }
                                                           43
37
                                                           44
                                                                      return -1;
          return {dp[N][S], es};
38
                                                           45 }
39 }
                                                           46
                                                           47 tuple <11, 11, 11> tree_diameter(const vector <v11> &
        Tsp
  4.4
                                                                  adj, 11 n) {
                                                                      // returns two points of the diameter and the
                                                           48
                                                                   diameter itself
using vi = vector<int>;
vector < vi > dist;
                                                                      auto [node1, dist1] = mostDistantFrom(adj, n,
                                                           49
3 vector < vi > memo;
                                                                      auto [node2, dist2] = mostDistantFrom(adj, n,
4 /* 0 ( N^2 * 2^N )*/
5 int tsp(int i, int mask, int N) {
           if (mask == (1 << N) - 1) return dist[i][0]; 51</pre>
                                                                      auto diameter = twoNodesDist(adj, n, node1,
           if (memo[i][mask] != -1) return memo[i][mask
                                                                  node2);
                                                                      return make_tuple(node1, node2, diameter);
                                                           53 }
           int ans = INT_MAX << 1;</pre>
          for (int j = 0; j < N; ++j) {
                                                           54
9
                   if (mask & (1 << j)) continue;</pre>
                                                           55 vll everyDistanceFromNode(const vector < vll> &adj, ll
10
                                                                  n, ll root) {
                   auto t = tsp(j, mask | (1 << j), N) +
       dist[i][j];
                                                                      // Single Source Shortest Path, from a given
                                                                  root
12
                   ans = min(ans, t);
                                                                      queue<pair<11, 11>> q;
13
                                                                      vll ans(n, -1);
           return memo[i][mask] = ans;
                                                           58
14
                                                                      ans[root] = 0;
15 }
                                                                      q.emplace(root, 0);
                                                           60
                                                                      while (!q.empty()) {
                                                           61
       trees
                                                                               auto [u, d] = q.front();
                                                           62
                                                           63
                                                                               q.pop();
       Maximum-distances
  5.1
                                                           65
                                                                               for (auto w : adj[u]) {
                                                           66
                                                                                       if (ans[w] != -1) continue;
1 /*
                                                                                       ans[w] = d + 1;
                                                           67
   * Returns the maximum distance from every node to
                                                                                       q.emplace(w, d + 1);
                                                           68
      any other node in the tree.
                                                                               }
```

26 }

```
sizes[u] = sz:
70
                                                          56
                                                                 }
71
          return ans;
                                                          57
72 }
                                                                 void decompose(int u, int p) {
                                                          58
                                                                     groups[u] = p;
                                                          59
74 vll maxDistances(const vector<vll> &adj, ll n) {
                                                                     for (auto &v : g[u])
                                                                         if (v != p) {
          auto [node1, node2, diameter] = tree_diameter 61
                                                                             if (v == heavy[u])
      (adj, n);
          auto distances1 = everyDistanceFromNode(adj,
                                                                                 decompose(v, p);
          auto distances2 = everyDistanceFromNode(adj,
                                                                                  decompose(v, v);
      n, node2);
                                                          66
           vll ans(n);
          for (int i = 0; i < n; ++i) ans[i] = max(</pre>
                                                          68 };
79
      distances1[i], distances2[i]);
                                                          69 void run() {}
                                                          70 int32_t main(void) {
80
          return ans;
81 }
                                                          71
                                                                 fastio;
                                                          72
                                                                 int t:
        Heavy-light-decomposition
                                                                 t = 1;
                                                          73
                                                                 // cin >> t;
                                                                 while (t--) run();
                                                          75
1 // iagorrr ;)
2 #include <bits/stdc++.h>
3 using namespace std;
                                                             5.3 Tree Diameter
4 #ifdef DEBUG
5 #include "debug.cpp"
                                                          pll mostDistantFrom(const vector < vll > & adj, ll n, ll
6 #else
7 #define dbg(...) 666
                                                                 root) {
                                                                     // 0 indexed
8 #endif
                                                                     11 mostDistantNode = root;
9 #define endl '\n'
10 #define fastio
                                                                     11 nodeDistance = 0;
      ios_base::sync_with_stdio(false);
                                                                     queue <pll> q;
      cin.tie(0);
                                                                     vector < char > vis(n);
12
      cout.tie(0);
                                                                     q.emplace(root, 0);
14 #define rep(i, l, r) for (int i = (l); i < (r); i++)
                                                                     vis[root] = true:
15 #define len(__x) (ll) __x.size()
                                                                     while (!q.empty()) {
16 using ll = long long;
                                                          10
                                                                             auto [node, dist] = q.front();
17 using vll = vector<ll>;
                                                                             q.pop();
                                                          11
18 using pll = pair<11, 11>;
                                                                             if (dist > nodeDistance) {
                                                          12
19 using v112d = vector<v11>;
                                                                                      nodeDistance = dist;
                                                          13
20 using vi = vector<int>;
                                                                                      mostDistantNode = node;
using vi2d = vector < vi>;
22 using pii = pair<int, int>;
                                                                             for (auto u : adj[node]) {
                                                          16
23 using vii = vector<pii>;
                                                          17
                                                                                      if (!vis[u]) {
24 using vc = vector<char>;
                                                                                              vis[u] = true;
                                                          18
25 #define all(a) a.begin(), a.end()
                                                                                              q.emplace(u, dist +
26 #define INV(xxxx) \
                                                                 1):
      for (auto &xxx : xxxx) cin >> xxx;
                                                                                      }
28 #define PRINTV(___x) \
                                                                             }
      for_each(all(___x), [](ll &___x) { cout << ___x 22
       << ''; }), cout << '\n';
                                                                     return {mostDistantNode, nodeDistance};
30 #define snd second
                                                          24 }
31 #define fst first
                                                          25 ll twoNodesDist(const vector < vll> & adj, ll n, ll a,
32 #define pb(___x) push_back(___x)
                                                                 11 b) {
33 #define mp(__a, __b) make_pair(__a, __b)
                                                                     // 0 indexed
34 #define eb(___x) emplace_back(___x)
                                                                     queue <pl1> q;
                                                          27
35 #define rsz(__x, __n) resize(__x, __n)
                                                                     vector < char > vis(n);
                                                          28
                                                                     q.emplace(a, 0);
37 const ll INF = 1e18;
                                                                     while (!q.empty()) {
                                                          30
                                                                             auto [node, dist] = q.front();
                                                          31
39 struct HLD {
                                                          32
                                                                             q.pop();
      int n:
                                                                             if (node == b) {
40
                                                          33
      vi sizes;
                                                                                      return dist;
41
      vi2d g;
42
                                                                              for (auto u : adj[node]) {
      vi groups;
      vi heavy;
44
                                                                                      if (!vis[u]) {
      HLD(int n) : n(n), sizes(n + 1), g(n + 1), groups 38
                                                                                              vis[u] = true;
45
      (n + 1), heavy(n + 1) {}
                                                                                              q.emplace(u, dist +
      void get_sizes(int u, int p) {
                                                                 1);
46
          int sz = 1;
                                                                                      }
           int bigc = -1;
                                                                             }
48
                                                          41
                                                                     }
49
           for (auto &v : g[u])
               if (v != p) {
50
                                                          43
                                                                     return -1;
                                                          44 }
51
                   get_sizes(p, u);
                   if (bigc == -1 or sizes[bigc] < sizes 45 ll tree_diameter(const vector<vll> &adj, ll n) {
      [v]
                                                                     // 0 indexed !!!
                                                          46
                       bigc = v, heavy[u] = v;
                                                                     auto [node1, dist1] = mostDistantFrom(adj, n,
53
                   sz += sizes[v];
54
               }
                                                                     auto [node2, dist2] = mostDistantFrom(adj, n,
```

```
node1):
                                                        1 const 11 MAX = 18;
         auto diameter = twoNodesDist(adj, n, node1, 2 vll fv(MAX, -1);
      node2);
                                                        3 ll factorial(ll n) {
                                                                  if (fv[n] != -1) return fv[n];
         return diameter;
50
51 }
                                                                  if (n == 0) return 1;
                                                        6
                                                                  return n * factorial(n - 1);
                                                        7 }
      searching
                                                        9 template <typename T>
                                                      10 ll permutation_count(vector <T> xs) {
  6.1
        Ternary Search Recursive
                                                                  map < T , ll > h;
                                                       11
                                                        12
                                                                  for (auto xi : xs) h[xi]++;
1 const double eps = 1e-6;
                                                                  11 ans = factorial((11)xs.size());
                                                        13
                                                                  dbg(ans);
3 // IT MUST BE AN UNIMODAL FUNCTION
                                                                  for (auto [v, cnt] : h) {
                                                        1.5
4 double f(int x) { return x * x + 2 * x + 4; }
                                                        16
                                                                          dbg(cnt);
                                                        17
                                                                          ans /= cnt;
6 double ternary_search(double 1, double r) {
         if (fabs(f(1) - f(r)) < eps) return f((1 + (r_{19})
       -1) / 2.0));
                                                                  return ans:
          auto third = (r - 1) / 3.0;
9
          auto m1 = 1 + third;
                                                          7.5 N-choose-k-count
          auto m2 = r - third;
11
          // change the signal to find the maximum
                                                        2 * O(nm) time, O(m) space
        return m1 < m2 ? ternary_search(m1, r) :</pre>
                                                       3 * equal to n choose k
                                                        4 * */
      ternary_search(1, m2);
                                                        5 ll binom(ll n, ll k) {
                                                                 if (k > n) return 0;
                                                                  vll dp(k + 1, 0);
      \mathbf{math}
                                                                  dp[0] = 1;
                                                                  for (ll i = 1; i <= n; i++)
                                                        9
                                                                          for (11 j = k; j > 0; j--) dp[j] = dp
  7.1 Power-sum
                                                              [j] + dp[j - 1];
                                                                  return dp[k];
                                                        11
_{\text{1}} // calculates K^0 + K^1 ... + K^n
                                                        12 }
2 ll fastpow(ll a, int n) {
         if (n == 1) return a;
                                                          7.6 Gcd-using-factorization
          11 x = fastpow(a, n / 2);
          return x * x * (n & 1 ? a : 1);
                                                        1 // O(sqrt(n))
6 }
_7 ll powersum(ll n, ll k) { return (fastpow(n, k + 1) - 2 map<ll, ll> factorization(ll n) {
                                                                  map<11, 11> ans;
       1) / (n - 1); }
                                                                  for (11 i = 2; i * i <= n; i++) {
                                                                          11 count = 0;
  7.2 Sieve-list-primes
                                                                           for (; n % i == 0; count++, n /= i)
1 // lsit every prime until MAXN
                                                                          if (count) ans[i] = count;
const ll MAXN = 1e5;
                                                        9
                                                                  }
3 vll list_primes(ll n) { // Nlog * log N
                                                                  if (n > 1) ans[n]++;
                                                        10
          vll ps;
                                                        11
                                                                  return ans;
          bitset < MAXN > sieve;
                                                        12 }
         sieve.set();
                                                        13
                                                        14 ll gcd_with_factorization(ll a, ll b) {
          sieve.reset(1);
          for (11 i = 2; i <= n; ++i) {
                                                             map<ll, ll> fa = factorization(a);
                                                       15
                  if (sieve[i]) ps.push_back(i);
                                                                  map<11, 11> fb = factorization(b);
9
                                                        16
                  for (11 j = i * 2; j <= n; j += i) { <sub>17</sub>
                                                                  ll ans = 1;
10
                          sieve.reset(j);
                                                                  for (auto fai : fa) {
                                                        18
                  }
12
                                                                          11 k = min(fai.second, fb[fai.first])
                                                        19
13
14
          return ps;
                                                                          while (k--) ans *= fai.first;
15 }
                                                        21
                                                        22
                                                                  return ans;
  7.3 Factorial
                                                        23 }
                                                          7.7 Is-prime
1 const 11 MAX = 18;
vll fv(MAX, -1);
3 ll factorial(ll n) {
                                                        1 bool isprime(ll n) { // O(sqrt(n))
         if (fv[n] != -1) return fv[n];
                                                                  if (n < 2) return false;
          if (n == 0) return 1;
                                                                  if (n == 2) return true;
                                                        3
          return n * factorial(n - 1);
                                                                  if (n % 2 == 0) return false;
7 }
                                                                  for (11 i = 3; i * i < n; i += 2)
                                                        5
                                                                          if (n % i == 0) return false;
                                                        6
  7.4 Permutation-count
                                                                  return true;
                                                        8 }
```

#### 7.8 Fast Exp ans \*= (p - 1); 36 38 return ans; 39 2 Fast exponentiation algorithm, 40 } 3 compute a^n in O(log(n)) **Polynomial** 7.115 ll fexp(ll a, int n){ if(n == 0) return 1; using polynomial = vector<11>; if (n==1) return a; 11 x = fexp(a, n/2);2 int degree(const polynomial &xs) { return xs.size() -1; } return x\*x\*(n&1?a:1); 3 ll horner\_evaluate(const polynomial &xs, ll x) { 10 } 11 ans = 0;4 11 n = degree(xs); Lcm-using-factorization 5 for (int i = n; i >= 0; --i) { ans \*= x;1 map<ll, ll> factorization(ll n) { ans += xs[i]; map<ll, ll> ans; } 9 for (11 i = 2; i \* i <= n; i++) {</pre> 10 return ans; 11 count = 0; 11 **}** for (; n % i == 0; count++, n /= i) 5 12 polynomial operator+(const polynomial &a, const polynomial &b) { if (count) ans[i] = count; int n = degree(a); 13 } 14 int m = degree(b); if (n > 1) ans[n]++; 9 polynomial r(max(n, m) + 1, 0);1.5 10 return ans; 16 11 } for (int i = 0; i <= n; ++i) r[i] += a[i]; 17 for (int j = 0; $j \le m$ ; ++j) r[j] += b[j]; 18 13 ll lcm\_with\_factorization(ll a, ll b) { while (!r.empty() and r.back() == 0) r.map < ll, ll > fa = factorization(a);14 pop\_back(); 15 map<ll, ll> fb = factorization(b); if (r.empty()) r.push\_back(0); ll ans = 1; 16 21 return r; for (auto fai : fa) { 17 22 } 11 k = max(fai.second, fb[fai.first]) 23 polynomial operator\*(const polynomial &p, const polynomial &q) { while (k--) ans \*= fai.first; int n = degree(p); } 20 25 int m = degree(q); return ans; 21 polynomial r(n + m + 1, 0); 26 22 } for (int i = 0; i <= n; ++i)</pre> 27 for (int j = 0; j <= m; ++j) r[i + j]28 7.10 Euler-phi += (p[i] \* q[j]); return r; 29 1 const ll MAXN = 1e5; 2 vll list\_primes(ll n) { // Nlog \* log N 7.12 Integer Mod vll ps; bitset < MAXN > sieve; const ll INF = 1e18; sieve.set(); sieve.reset(1); 2 const 11 mod = 998244353; for (ll i = 2; i <= n; ++i) { 3 template <11 MOD = mod> if (sieve[i]) ps.push\_back(i); 4 struct Modular { 9 for (11 $j = i * 2; j \le n; j += i$ ) { ll value; static const 11 MOD\_value = MOD; 10 sieve.reset(j); } Modular(ll v = 0) { return ps; value = v % MOD; 13 9 14 } if (value < 0) value += MOD;</pre> 15 16 vector<pll> factorization(ll n, const vll &primes) { 12 Modular(ll a, ll b) : value(0) { vector <pll> ans; \*this += a; 17 for (auto &p : primes) { \*this /= b; 18 14 if (n == 1) break; } 19 15 11 cnt = 0; 20 16 while $(n \% p == 0) {$ Modular& operator+=(Modular const& b) { 17 22 cnt++; 18 value += b.value; n /= p; if (value >= MOD) value -= MOD; 23 19 } 24 20 return \*this; if (cnt) ans.emplace\_back(p, cnt); 25 21 } Modular& operator -= (Modular const& b) { value -= b.value; 27 return ans; 23 if (value < 0) value += MOD;</pre> 24 25 return \*this; 30 ll phi(ll n, vector<pll> factors) { 26 if (n == 1) return 1; Modular& operator\*=(Modular const& b) { 27 value = (11)value \* b.value % MOD; 11 ans = n;32 28 return \*this; for (auto [p, k] : factors) { } 34 30 ans /= p;31 35

#### 7.14 Lcm friend Modular mexp(Modular a, ll e) { 32 Modular res = 1; 33 34 while (e) { 1 ll gcd(ll a, ll b) { return b ? gcd(b, a % b) : a; } if (e & 1) res \*= a; 2 11 1cm(11 a, 11 b) { return a / gcd(a, b) \* b; } a \*= a; 37 e >>= 1:7.15 Factorial-factorization } 39 return res; } $_{\mbox{\scriptsize 1}}$ // O(logN) greater k that p^k | n 41 friend Modular inverse(Modular a) { return 2 ll E(ll n, ll p) { mexp(a, MOD - 2); } 11 k = 0, b = p;42 while $(b \le n)$ { Modular& operator/=(Modular const& b) { 43 k += n / b;return \*this \*= inverse(b); } b \*= p;friend Modular operator+(Modular a, Modular 44 } const b) { return a += b; } return k: Modular operator++(int) { 45 9 } return this->value = (this->value + 46 1) % MOD; $_{\rm 11}$ // lsit every prime until MAXN O(Nlog \* log N) } 47 Modular operator++() { return this->value = (12 const ll MAXN = 1e5; 13 vll list\_primes(ll n) { 48 this->value + 1) % MOD; } vll ps; 14 friend Modular operator-(Modular a, Modular 49 15 bitset < MAXN > sieve; const b) { return a -= b; } sieve.set(); 16 friend Modular operator-(Modular const a) { 50 17 sieve.reset(1); return 0 - a; } for (11 i = 2; i <= n; ++i) { 18 Modular operator --(int) { if (sieve[i]) ps.push\_back(i); return this->value = (this->value - 1 20 for (11 j = i \* 2; j <= n; j += i) + MOD) % MOD; sieve.reset(i): } } 54 22 return ps; Modular operator --() { return this->value = (this->value - 1 56 + MOD) % MOD; 25 // O(pi(N)\*logN) 57 } 26 map<ll, ll> factorial\_factorization(ll n, const vll & friend Modular operator\*(Modular a, Modular primes) { const b) { return a \*= b; } map<11, 11> fs; friend Modular operator/(Modular a, Modular 28 for (const auto &p : primes) { const b) { return a /= b; } if (p > n) break; 29 friend std::ostream& operator << (std::ostream&</pre> 60 30 fs[p] = E(n, p);os, Modular const& a) { 31 return os << a.value; 61 return fs; 33 } friend bool operator == (Modular const& a, 63 Modular const& b) { 7.16 Factorization-with-primes return a.value == b.value; 65 friend bool operator!=(Modular const& a, 1 // Nlog \* log N Modular const& b) { const ll MAXN = 1e5; 67 return a.value != b.value; 3 vll list\_primes(ll n) { 68 4 vll ps; 69 }; bitset < MAXN > sieve; 5 sieve.set(); 6 7.13 Count Divisors Memo 7 sieve.reset(1): for (11 i = 2; i <= n; ++i) {</pre> 8 9 if (sieve[i]) ps.push\_back(i); 1 const 11 mod = 1073741824; for (11 $j = i * 2; j \le n; j += i$ ) 10 2 const ll maxd = 100 \* 100 \* 100 + 1; sieve.reset(j); 3 vector<ll> memo(maxd, -1); } 11 4 ll countdivisors(ll x) { 12 return ps; 11 ox = x;13 } ll ans = 1;14 for (11 i = 2; i <= x; ++i) {</pre> 15 // O(pi(sqrt(n))) if (memo[x] != -1) { 16 map<ll, ll> factorization(ll n, const vll &primes) { ans \*= memo[x]; 9 17 map<ll, ll> ans; break: 10 for (auto p : primes) { 18 7 if (p \* p > n) break; 19 11 count = 0;20 11 count = 0; while (x and x % i == 0) { for (; n % p == 0; count++, n /= p) 21 x /= i; 14 count++: if (count) ans[p] = count; 23 } 16 24 } 17 ans \*= (count + 1); 25 return ans; } 26 } memo[ox] = ans:19 20 return ans; Modular-inverse-using-phi 21 } 7.17

```
1 map<ll, ll> factorization(ll n) {
           map < 11, 11 > ans;
                                                                               pos = k - 1;
                                                           20
           for (11 i = 2; i * i <= n; i++) {
                                                                      }
                                                           21
                   11 count = 0;
                                                           22 }
                   for (; n % i == 0; count++, n /= i)
                                                                   strings
                   if (count) ans[i] = count;
           if (n > 1) ans[n]++;
                                                              8.1
                                                                    Rabin-karp
10
           return ans;
11 }
                                                            vi rabin_karp(string const &s, string const &t) {
12
                                                                      11 p = 31;
13 ll phi(ll n) {
                                                                      11 m = 1e9 + 9;
                                                            3
          if (n == 1) return 1;
                                                                      int S = s.size(), T = t.size();
                                                            4
1.5
16
           auto fs = factorization(n);
                                                                      vll p_pow(max(S, T));
                                                            6
17
           auto res = n:
                                                                      p_pow[0] = 1;
18
                                                                      for (int i = 1; i < (int)p_pow.size(); i++)</pre>
                                                            8
           for (auto [p, k] : fs) {
                                                                               p_pow[i] = (p_pow[i - 1] * p) % m;
                   res /= p;
20
                                                           10
                   res *= (p - 1);
21
                                                                      vll h(T + 1, 0);
                                                           11
           }
22
                                                           12
                                                                      for (int i = 0; i < T; i++)</pre>
23
                                                                              h[i + 1] = (h[i] + (t[i] - 'a' + 1) *
           return res;
                                                                   p_pow[i]) % m;
25 }
                                                                      11 h_s = 0;
                                                           14
26
                                                                      for (int i = 0; i < S; i++)</pre>
27 ll fexp(ll a, ll n, ll mod) {
                                                                              h_s = (h_s + (s[i] - 'a' + 1) * p_pow
                                                           16
          if (n == 0) return 1;
28
                                                                  [i]) % m;
           if (n == 1) return a;
           11 x = fexp(a, n / 2, mod);
30
                                                                      vi occurences:
                                                           18
31
           return x * x * (n & 1 ? a : 1) % mod;
                                                                      for (int i = 0; i + S - 1 < T; i++) {
                                                           19
32 }
                                                                               11 cur_h = (h[i + S] + m - h[i]) % m;
                                                           20
                                                                               // IT DON'T CONSIDERE CONLISIONS !
                                                           21
34 ll inv(ll a, ll mod) { return fexp(a, phi(mod) - 1,
                                                           22
                                                                               if (cur_h == h_s * p_pow[i] % m)
      mod); }
                                                                  occurences.push_back(i);
                                                                      }
                                                           23
  7.18 Factorization
                                                           24
                                                                      return occurences:
                                                           25 }
1 // O(sqrt(n))
2 map<ll, ll> factorization(ll n) {
                                                                    Trie-naive
           map<ll, ll> ans;
           for (ll i = 2; i * i <= n; i++) {
                                                           1 // time: O(n^2) memory: O(n^2)
                   11 count = 0;
                                                            2 using Node = map < char, int >;
                   for (; n % i == 0; count++, n /= i)
                                                            3 using vi = vector<int>;
                                                            4 using Trie = vector < Node >;
                   if (count) ans[i] = count;
9
                                                            6 Trie build(const string &s) {
           if (n > 1) ans[n]++;
10
                                                                      int n = (int)s.size();
           return ans;
11
                                                                      Trie trie(1);
12 }
                                                                      string suffix;
                                                            9
         \operatorname{Gcd}
  7.19
                                                                      for (int i = n - 1; i >= 0; --i) {
                                                                               suffix = s.substr(i) + '#';
_{\rm 1} ll gcd(ll a, ll b) { return b ? gcd(b, a % b) : a; } _{\rm 13}
                                                                               int v = 0; // root
                                                           14
  7.20
        Combinatorics With Repetitions
                                                                               for (auto c : suffix) {
                                                                                       if (c == '#') { // makrs the
                                                           16
void combinations_with_repetition(int n, int k,
                                                                   poistion of an occurence
                                       function < void (const 17
                                                                                                trie[v][c] = i:
2
        vector<int> &)> process) {
                                                                                                break;
                                                           18
           vector < int > v(k, 1);
                                                           19
           int pos = k - 1;
                                                                                       if (trie[v][c])
                                                           20
                                                                                                v = trie[v][c];
           while (true) {
                                                                                       else {
                   process(v);
                                                                                                trie.push_back({});
                                                           23
                                                           24
                                                                                                trie[v][c] = trie.
                   v[pos]++:
                                                                  size() - 1;
9
                                                                                                v = trie.size() - 1;
                   while (pos > 0 \text{ and } v[pos] > n) {
                                                                                       }
                                                           26
                                                                               }
12
                            --pos;
                                                                      }
                            v[pos]++;
                                                           28
                   }
                                                           29
                                                                      return trie;
14
                                                           30 }
                   if (pos == 0 and v[pos] > n) break;
16
                                                           31
                                                           32 vi search(Trie &trie, string s) {
                   for (int i = pos + 1; i < k; ++i) v[i33</pre>
                                                                    int p = 0;
18
      ] = v[pos];
                                                                      vi occ;
```

```
for (auto &c : s) {
35
36
                    p = trie[p][c];
                    if (!p) return occ;
37
           }
38
39
           queue < int > q;
40
            q.push(0);
           while (!q.empty()) {
42
                    auto cur = q.front();
43
44
                     q.pop();
                    for (auto [c, v] : trie[cur]) {
    if (c == '#')
45
46
                                      occ.push_back(v);
47
                              else
                                       q.push(v);
49
                     }
50
           }
51
           return occ;
52
53 }
54
55 ll distinct_substr(const Trie &trie) {
           11 cnt = 0;
56
           queue < int > q;
57
           q.push(0);
           while (!q.empty()) {
59
                     auto u = q.front();
                     q.pop();
61
62
                     for (auto [c, v] : trie[u]) {
                              if (c != '#') {
64
```

# 8.3 String-psum

```
struct strPsum {
           11 n;
2
           11 k;
 3
           vector < vll> psum;
           \verb| strPsum(const string \&s) : n(s.size()), k \\
       (100), psum(k, vll(n + 1)) {
                    for (11 i = 1; i <= n; ++i) {</pre>
                             for (11 j = 0; j < k; ++ j) {
                                     psum[j][i] = psum[j][
       i - 1];
                             psum[s[i - 1]][i]++;
10
                    }
11
           }
12
13
           ll qtd(ll l, ll r, char c) { // [0,n-1]
14
                    return psum[c][r + 1] - psum[c][1];
15
           }
16
17 }
```