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1 Data structures

1.1 Dsu

```
struct DSU {
 vector < int > ps;
 vector < int > size;
 DSU(int N) : ps(N + 1), size(N + 1, 1) { iota(ps.begin(), ps.end(), 0); }
 int find_set(int x) { return ps[x] == x ? x : ps[x] = find_set(ps[x]); }
 bool same_set(int x, int y) { return find_set(x) == find_set(y); }
 void union_set(int x, int y) {
    if (same_set(x, y)) return;
   int px = find_set(x);
    int py = find_set(y);
    if (size[px] < size[py]) swap(px, py);</pre>
   ps[py] = px;
    size[px] += size[py];
};
     Dsu (Python)
class DSU:
    def init (self. n):
        self.n = n
        self.p = [x for x in range(0, n + 1)]
        self.size = [0 for i in range(0, n + 1)]
    def find_set(self, x): # log n
        if self.p[x] == x:
            return x
        else:
            self.p[x] = self.find_set(self.p[x])
            return self.p[x]
    def same_set(self, x, y): # log n
        return bool(self.find_set(x) == self.find_set(y))
    def union_set(self, x, y): # log n
        px = self.find set(x)
        py = self.find_set(y)
        if px == py:
           return
        size x = self.size[px]
        size_y = self.size[py]
        if size_x > size_y:
            self.p[pv] = self.p[px]
            self.size[px] += self.size[py]
        else:
            self.p[px] = self.p[py]
```

self.size[py] += self.size[px]

1.3 Ordered Set Gnu Pbds

1.4 Segtree Point Rmq

```
#include <bits/stdc++.h>
using namespace std;
#ifdef DEBUG
#include "debug.cpp"
#else
#define dbg(...) 666
#endif
#define endl '\n'
#define fastio
 ios_base::sync_with_stdio(false); \
 cin.tie(0):
 cout.tie(0);
#define len(__x) (ll) __x.size()
using ll = long long;
using vll = vector<ll>;
using pll = pair<ll, ll>;
using v112d = vector < v11 >;
using vi = vector<int>;
using vi2d = vector < vi>;
using pii = pair <int, int>;
using vii = vector<pii>;
using vc = vector < char >:
#define all(a) a.begin(), a.end()
#define snd second
#define fst first
#define pb(___x) push_back(___x)
#define mp(__a, __b) make_pair(__a, __b)
#define eb(___x) emplace_back(___x)
const ll INF = 1e18;
void run() {}
int32_t main(void) {
 fastio;
 int t:
 t = 1;
 // cin >> t;
  while (t--) run();
class SegTree {
public:
 int n;
 vector<1l> st;
```

```
SegTree(const vector<11> &v) : n((int)v.size()), st(n * 4 + 1, LLONG_MAX) {
   for (int i = 0; i < n; ++i) update(i, v[i]);</pre>
 void update(int p, ll v) { update(1, 0, n - 1, p, v); }
 11 RMQ(int 1, int r) { return RMQ(1, 0, n - 1, 1, r); }
 private:
 void update(int node, int 1, int r, int p, 11 v) {
    if (p < l or p > r) return; // fora do intervalo.
    if (1 == r) {
      st[node] = v;
     return;
    int mid = 1 + (r - 1) / 2;
    update(node * 2, 1, mid, p, v);
    update(node * 2 + 1, mid + 1, r, p, v);
    st[node] = min(st[node * 2], st[node * 2 + 1]);
 11 RMQ(int node, int L, int R, int l, int r) {
   if (1 <= L and r >= R) return st[node];
   if (L > r or R < 1) return LLONG_MAX;</pre>
    if (L == R) return st[node];
   int mid = L + (R - L) / 2;
   return min(RMQ(node * 2, L, mid, 1, r),
               RMQ(node * 2 + 1, mid + 1, R, 1, r));
 }
};
     Segtree Rming Rsu
template <typename t = 11>
struct segtree {
 int n:
```

```
t nu;
t nq;
vector < t> st, lazy;
segtree(const vector<t> &xs)
 : n(len(xs)),
    nu(0),
    nq(numeric_limits <t>::max()),
    st(4 * n, nu),
    lazy(4 * n, nu) {
 for (int i = 0; i < len(xs); ++i) update(i, i, xs[i]);
segtree(int n) : n(n), st(4 * n, nu), lazy(4 * n, nu) {}
void update(int 1, int r, 11 value) { update(1, 0, n - 1, 1, r, value); }
t query(int 1, int r) { return query(1, 0, n - 1, 1, r); }
```

```
void update(int node, int nl, int nr, int ql, int qr, ll v) {
    propagation(node, nl, nr);
    if (ql > nr or qr < nl) return;</pre>
    if (ql <= nl and nr <= qr) {</pre>
      st[node] += (nr - nl + 1) * v:
      if (nl < nr) {
        lazy[left(node)] += v;
        lazy[right(node)] += v;
      return:
    update(left(node), nl, mid(nl, nr), ql, qr, v);
    update(right(node), mid(nl, nr) + 1, nr, ql, qr, v);
    st[node] = min(st[left(node)], st[right(node)]);
  }
  t query(int node, int nl, int nr, int ql, int qr) {
    propagation(node, nl, nr);
    if (ql > nr or qr < nl) return nq;
    if (ql <= nl and nr <= qr) return st[node];</pre>
    t x = query(left(node), nl, mid(nl, nr), ql, qr);
    t y = query(right(node), mid(nl, nr) + 1, nr, ql, qr);
    return min(x, y);
  void propagation(int node, int nl, int nr) {
    if (lazy[node]) {
      st[node] += lazy[node];
      if (nl < nr) {
        lazy[left(node)] += lazy[node];
        lazy[right(node)] += lazy[node];
      lazy[node] = nu;
  int left(int p) { return p << 1; }</pre>
  int right(int p) { return (p << 1) + 1; }</pre>
  int mid(int 1, int r) { return (r - 1) / 2 + 1; }
};
```

Segtree Rmq Lazy Max Update

```
#include <bits/stdc++.h>
using namespace std;
#ifdef DEBUG
```

```
#include "debug.cpp"
#else
#define dbg(...) 666
#endif
#define endl '\n'
#define fastio
 ios base::svnc with stdio(false): \
 cin.tie(0);
 cout.tie(0):
#define len(__x) (ll) __x.size()
using 11 = long long;
using vll = vector<ll>;
using pll = pair<11, 11>;
using v112d = vector<v11>;
using vi = vector<int>:
using vi2d = vector < vi>;
using pii = pair<int, int>;
using vii = vector<pii>;
using vc = vector < char >;
#define all(a) a.begin(), a.end()
#define snd second
#define fst first
#define pb(___x) push_back(___x)
#define mp(__a, __b) make_pair(__a, __b)
#define eb(___x) emplace_back(___x)
const 11 INF = 1e18:
void run() {}
struct SegmentTree {
 int N;
 vll ns. lazv:
 SegmentTree(const v11 &xs) : N(xs.size()), ns(4 * N, 0), lazy(4 * N, 0) {
   for (size_t i = 0; i < xs.size(); ++i) {</pre>
      update(i, i, xs[i]);
   }
 }
 void update(int a, int b, ll value) { update(1, 0, N - 1, a, b, value); }
 void update(int node, int L, int R, int a, int b, ll value) {
    if (lazy[node]) {
      ns[node] = max(ns[node], lazy[node]);
     if (L < R) {
       lazv[2 * node] = max(lazv[2 * node], lazv[node]):
        lazy[2 * node + 1] = max(lazy[2 * node + 1], lazy[node]);
      lazy[node] = 0;
    if (a > R or b < L) return:
    if (a \le L \text{ and } R \le b) {
     ns[node] = max(ns[node], value);
     if (L < R) {
       lazv[2 * node] = max(value, lazv[2 * node]);
       lazy[2 * node + 1] = max(value, lazy[2 * node + 1]);
     }
      return;
    update(2 * node, L, (L + R) / 2, a, b, value);
```

```
update(2 * node + 1, (L + R) / 2 + 1, R, a, b, value):
    ns[node] = max(ns[node * 2], ns[node * 2 + 1]);
 }
  11 RMQ(int a, int b) { return RMQ(1, 0, N - 1, a, b); }
  11 RMQ(int node, int L, int R, int a, int b) {
    if (lazv[node]) {
      ns[node] = max(ns[node], lazy[node]);
      if (L < R) {
        lazy[node * 2] = max(lazy[node * 2], lazy[node]);
        lazy[node * 2 + 1] = max(lazy[node * 2 + 1], lazy[node]);
      lazy[node] = 0;
    if (a > R \text{ or } b < L) \text{ return } 0;
    if (a <= L and R <= b) return ns[node];</pre>
    11 x = RMQ(2 * node, L, (L + R) / 2, a, b);
    11 \text{ y} = RMQ(2 * node + 1, (L + R) / 2 + 1, R, a, b);
    return max(x, v):
 }
}:
int32 t main(void) {
 fastio;
  int t:
  t = 1;
 // cin >> t:
 while (t--) run();
1.7 Segtree Rsq Rsu
template <typename T = 11>
struct SegTree {
  int N:
  vector <T> st, lazy;
  T nu = 0:
  T nq = 0;
  SegTree(const vector<T> &xs) : N(len(xs)), st(4 * N, nu), lazy(4 * N, nu) {
    for (int i = 0; i < len(xs); ++i) update(i, i, xs[i]);</pre>
  SegTree(int n): N(n), st(4 * N, nu), lazy(4 * N, nu) {}
  void update(int 1, int r, 11 value) { update(1, 0, N - 1, 1, r, value); }
  T query(int 1, int r) { return query(1, 0, N - 1, 1, r); }
  void update(int node, int nl, int nr, int ql, int qr, ll v) {
    propagation(node, nl, nr);
    if (ql > nr or qr < nl) return;
    if (ql <= nl and nr <= qr) {</pre>
      st[node] += (nr - nl + 1) * v;
      if (n1 < nr) {
```

lazy[left(node)] += v;

```
lazy[right(node)] += v;
      return:
    update(left(node), nl, mid(nl, nr), ql, qr, v);
    update(right(node), mid(nl, nr) + 1, nr, ql, qr, v);
    st[node] = st[left(node)] + st[right(node)];
 }
 T query(int node, int nl, int nr, int ql, int qr) {
    propagation(node, nl, nr);
   if (ql > nr or qr < nl) return nq;</pre>
    if (ql <= nl and nr <= qr) return st[node];</pre>
   T x = query(left(node), nl, mid(nl, nr), ql, qr);
   T y = query(right(node), mid(nl, nr) + 1, nr, ql, qr);
   return x + y;
 void propagation(int node, int nl, int nr) {
    if (lazy[node]) {
      st[node] += (nr - nl + 1) * lazy[node];
     if (nl < nr) {
       lazy[left(node)] += lazy[node];
       lazy[right(node)] += lazy[node];
     lazy[node] = nu;
 }
 int left(int p) { return p << 1; }</pre>
 int right(int p) { return (p << 1) + 1; }</pre>
 int mid(int 1, int r) { return (r - 1) / 2 + 1; }
};
     Segtree Rxq Lazy Range Xor
struct SegTree {
 int N:
 vector < ll > ns , lazy;
 SegTree(const vector<11> &xs) : N(xs.size()), ns(4 * N, 0), lazy(4 * N, 0) {
   for (size_t i = 0; i < xs.size(); ++i) update(i, i, xs[i]);</pre>
 void update(int a, int b, ll value) { update(1, 0, N - 1, a, b, value); }
  void update(int node, int L, int R, int a, int b, ll value) {
```

// Lazy propagation

if (lazy[node]) {

```
ns[node] ^= lazv[node]:
      if (L < R) // Se o ón ãno é uma folha, propaga
        lazy[2 * node] ^= lazy[node];
        lazy[2 * node + 1] ^= lazy[node];
      lazv[node] = 0:
    if (a > R or b < L) return;
    if (a \le L \text{ and } R \le b)
      ns[node] ^= value:
      if (L < R) {
        lazy[2 * node] ^= value;
        lazv[2 * node + 1] ^= value;
      return:
    7
    update (2 * node, L, (L + R) / 2, a, b, value);
    update(2 * node + 1, (L + R) / 2 + 1, R, a, b, value);
    ns[node] = ns[2 * node] ^ ns[2 * node + 1];
  11 rxg(int a. int b) { return RSQ(1, 0, N - 1, a, b): }
  11 rxq(int node, int L, int R, int a, int b) {
    if (lazy[node]) {
      ns[node] ^= lazy[node];
      if (L < R) {
        lazy[2 * node] ^= lazy[node];
        lazv[2 * node + 1] ^= lazv[node]:
      lazy[node] = 0;
    if (a > R \text{ or } b < L) \text{ return } 0;
    if (a <= L and R <= b) return ns[node];</pre>
    11 x = rxq(2 * node, L, (L + R) / 2, a, b);
    11 y = rxq(2 * node + 1, (L + R) / 2 + 1, R, a, b);
    return x ^ y;
};
      Sparse Table Rmq
```

/*

```
Sparse table implementation for rmq.
        build: O(NlogN)
        query: 0(1)
*/
int fastlog2(11 x) {
 ull i = x:
 return i ? __builtin_clzll(1) - __builtin_clzll(i) : -1;
template <typename T>
class SparseTable {
public:
 int N;
 int K;
 vector < vector < T >> st:
 SparseTable(vector<T> vs)
    : N((int)vs.size()), K(fastlog2(N) + 1), st(K + 1, vector < T > (N + 1)) {
    copy(vs.begin(), vs.end(), st[0].begin());
   for (int i = 1; i <= K; ++i)
     for (int j = 0; j + (1 << i) <= N; ++j)
        st[i][j] = min(st[i - 1][j], st[i - 1][j + (1 << (i - 1))]);
 T RMQ(int 1, int r) { // [1, r], 0 indexed
    int i = fastlog2(r - 1 + 1);
   return min(st[i][l], st[i][r - (1 << i) + 1]);
 }
};
```

2 Dynamic programming

2.1 Edit Distance

```
int edit_distance(const string &a, const string &b) {
 int n = a.size();
 int m = b.size():
 vector \langle vi \rangle dp(n + 1, vi(m + 1, 0));
 int ADD = 1, DEL = 1, CHG = 1;
 for (int i = 0; i <= n; ++i) {</pre>
   dp[i][0] = i * DEL;
 for (int i = 1; i <= m; ++i) {
   dp[0][i] = ADD * i;
 for (int i = 1; i <= n; ++i) {
   for (int j = 1; j <= m; ++j) {
      int add = dp[i][j - 1] + ADD;
     int del = dp[i - 1][j] + DEL;
      int chg = dp[i - 1][j - 1] + (a[i - 1] == b[j - 1]?0:1) * CHG;
      dp[i][j] = min({add, del, chg});
 }
 return dp[n][m];
```

2.2 Knapsack Dp Values 01

```
const int MAX N = 1001:
const int MAX_S = 100001;
array < array < int , MAX_S > , MAX_N > dp;
bool check[MAX_N][MAX_S];
pair < int , vi > knapsack(int S, const vector < pii > &xs) {
  int N = (int)xs.size();
  for (int i = 0; i <= N; ++i) dp[i][0] = 0;
  for (int m = 0; m \le S; ++m) dp[0][m] = 0;
  for (int i = 1; i <= N; ++i) {
    for (int m = 1; m <= S; ++m) {
      dp[i][m] = dp[i - 1][m];
      check[i][m] = false;
      auto [w, v] = xs[i - 1];
      if (w \le m \text{ and } (dp[i - 1][m - w] + v) >= dp[i][m]) {
        dp[i][m] = dp[i - 1][m - w] + v;
        check[i][m] = true;
    }
  }
  int m = S;
  vi es:
  for (int i = N; i >= 1; --i) {
   if (check[i][m]) {
      es.push_back(i);
      m -= xs[i - 1].first;
  reverse(es.begin(), es.end());
  return {dp[N][S], es};
     Money Sum Bottom Up
   find every possible sum using
   the given values only once.
set < int > money_sum(const vi &xs) {
  using vc = vector < char >:
  using vvc = vector<vc>;
  int _m = accumulate(all(xs), 0);
  int _n = xs.size();
  vvc _dp(_n + 1, vc(_m + 1, 0));
  set < int > _ans;
  _{dp}[0][xs[0]] = 1;
  for (int i = 1; i < _n; ++i) {
```

for (int j = 0; j <= _m; ++j) {

```
if (i == 0 or dp[i - 1][i]) {
        dp[i][i + xs[i]] = 1;
       _dp[i][j] = 1;
   }
 }
 for (int i = 0; i < _n; ++i)</pre>
   for (int j = 0; j <= _m; ++j)
     if (_dp[i][j]) _ans.insert(j);
 return _ans;
2.4 Tsp
using vi = vector<int>;
vector<vi> dist;
vector < vi> memo:
/* 0 ( N^2 * 2^N )*/
int tsp(int i, int mask, int N) {
 if (mask == (1 << N) - 1) return dist[i][0]:
 if (memo[i][mask] != -1) return memo[i][mask];
 int ans = INT_MAX << 1;</pre>
 for (int j = 0; j < N; ++ j) {
   if (mask & (1 << j)) continue;
   auto t = tsp(j, mask | (1 << j), N) + dist[i][j];</pre>
   ans = min(ans, t);
 return memo[i][mask] = ans:
    Extras
3.1 Bigint
const int maxn = 1e2 + 14, 1g = 15;
const int base = 1000000000;
const int base_digits = 9;
struct bigint {
 vector < int > a;
 int sign;
 int size() {
   if (a.empty()) return 0;
    int ans = (a.size() - 1) * base_digits;
   int ca = a.back();
    while (ca) ans++, ca \neq 10;
   return ans;
 bigint operator^(const bigint &v) {
   bigint ans = 1, a = *this, b = v;
    while (!b.isZero()) {
     if (b % 2) ans *= a;
     a *= a, b /= 2;
   return ans;
```

```
string to_string() {
  stringstream ss;
  ss << *this;
  string s;
  ss >> s:
  return s;
int sumof() {
  string s = to_string();
 int ans = 0;
  for (auto c : s) ans += c - '0';
  return ans:
}
/*</arpa>*/
bigint() : sign(1) {}
bigint(long long v) { *this = v; }
bigint(const string &s) { read(s); }
void operator=(const bigint &v) {
  sign = v.sign:
  a = v.a:
}
void operator=(long long v) {
  sign = 1;
 a.clear();
 if (v < 0) sign = -1, v = -v;
  for (; v > 0; v = v / base) a.push_back(v % base);
bigint operator+(const bigint &v) const {
 if (sign == v.sign) {
    bigint res = v;
    for (int i = 0, carry = 0; i < (int)max(a.size(), v.a.size()) || carry;</pre>
         ++i) {
      if (i == (int)res.a.size()) res.a.push back(0);
      res.a[i] += carry + (i < (int)a.size() ? a[i] : 0);
      carry = res.a[i] >= base;
      if (carry) res.a[i] -= base;
    return res:
  return *this - (-v):
bigint operator-(const bigint &v) const {
 if (sign == v.sign) {
    if (abs() >= v.abs()) {
      bigint res = *this;
      for (int i = 0, carry = 0; i < (int)v.a.size() || carry; ++i) {
        res.a[i] -= carry + (i < (int)v.a.size() ? v.a[i] : 0);
        carry = res.a[i] < 0;</pre>
        if (carry) res.a[i] += base;
      res.trim();
```

```
return res:
    return -(v - *this);
  return *this + (-v);
}
void operator*=(int v) {
  if (v < 0) sign = -sign, v = -v;
  for (int i = 0, carry = 0; i < (int)a.size() || carry; ++i) {</pre>
    if (i == (int)a.size()) a.push_back(0);
    long long cur = a[i] * (long long)v + carry;
    carry = (int)(cur / base);
    a[i] = (int)(cur % base);
    // asm("divl %%ecx" : "=a"(carry), "=d"(a[i]) :
    // "A"(cur), "c"(base));
  trim();
}
bigint operator*(int v) const {
  bigint res = *this:
 res *= v:
  return res;
void operator*=(long long v) {
  if (v < 0) sign = -sign, v = -v;
  if (v > base) {
    *this = *this * (v / base) * base + *this * (v % base):
    return:
  for (int i = 0, carry = 0; i < (int)a.size() || carry; ++i) {</pre>
    if (i == (int)a.size()) a.push_back(0);
    long long cur = a[i] * (long long)v + carry;
    carry = (int)(cur / base);
    a[i] = (int)(cur \% base);
    // asm("divl %%ecx" : "=a"(carry), "=d"(a[i]) :
    // "A"(cur), "c"(base));
  trim();
}
bigint operator*(long long v) const {
  bigint res = *this;
 res *= v:
  return res;
friend pair < bigint, bigint > divmod(const bigint &a1, const bigint &b1) {
  int norm = base / (b1.a.back() + 1);
  bigint a = a1.abs() * norm;
  bigint b = b1.abs() * norm;
  bigint q, r;
  q.a.resize(a.a.size());
  for (int i = a.a.size() - 1; i \ge 0; i--) {
    r *= base;
```

```
r += a.a[i]:
    int s1 = r.a.size() <= b.a.size() ? 0 : r.a[b.a.size()];</pre>
    int s2 = r.a.size() <= b.a.size() - 1 ? 0 : r.a[b.a.size() - 1];
    int d = ((long long)base * s1 + s2) / b.a.back();
    r -= b * d:
    while (r < 0) r += b, --d;
    q.a[i] = d;
 }
  q.sign = a1.sign * b1.sign;
  r.sign = a1.sign;
  q.trim();
 r.trim();
  return make_pair(q, r / norm);
bigint operator/(const bigint &v) const { return divmod(*this, v).first; }
bigint operator%(const bigint &v) const { return divmod(*this, v).second; }
void operator/=(int v) {
 if (v < 0) sign = -sign, v = -v:
 for (int i = (int)a.size() - 1, rem = 0; i \ge 0; --i) {
    long long cur = a[i] + rem * (long long)base;
    a[i] = (int)(cur / v);
    rem = (int)(cur \% v);
  trim();
}
bigint operator/(int v) const {
 bigint res = *this;
 res /= v:
  return res;
int operator%(int v) const {
 if (v < 0) v = -v:
 int m = 0:
 for (int i = a.size() - 1; i >= 0; --i)
    m = (a[i] + m * (long long)base) % v;
  return m * sign;
void operator+=(const bigint &v) { *this = *this + v; }
void operator -=(const bigint &v) { *this = *this - v; }
void operator*=(const bigint &v) { *this = *this * v; }
void operator/=(const bigint &v) { *this = *this / v; }
bool operator < (const bigint &v) const {</pre>
  if (sign != v.sign) return sign < v.sign;</pre>
  if (a.size() != v.a.size()) return a.size() * sign < v.a.size() * v.sign;</pre>
  for (int i = a.size() - 1; i >= 0; i--)
    if (a[i] != v.a[i]) return a[i] * sign < v.a[i] * sign;</pre>
  return false:
}
bool operator>(const bigint &v) const { return v < *this; }</pre>
```

```
bool operator <= (const bigint &v) const { return !(v < *this); }</pre>
bool operator>=(const bigint &v) const { return !(*this < v); }</pre>
bool operator == (const bigint &v) const {
 return !(*this < v) && !(v < *this):
bool operator!=(const bigint &v) const { return *this < v || v < *this; }
void trim() {
  while (!a.empty() && !a.back()) a.pop_back();
  if (a.empty()) sign = 1;
}
bool isZero() const { return a.empty() || (a.size() == 1 && !a[0]); }
bigint operator - () const {
  bigint res = *this;
 res.sign = -sign;
 return res;
}
bigint abs() const {
  bigint res = *this;
 res.sign *= res.sign;
  return res;
long longValue() const {
  long long res = 0;
 for (int i = a.size() - 1; i >= 0; i--) res = res * base + a[i];
  return res * sign:
}
friend bigint gcd(const bigint &a, const bigint &b) {
  return b.isZero() ? a : gcd(b, a % b);
friend bigint lcm(const bigint &a, const bigint &b) {
  return a / gcd(a, b) * b;
void read(const string &s) {
  sign = 1;
  a.clear();
  int pos = 0;
  while (pos < (int)s.size() && (s[pos] == '-' || s[pos] == '+')) {
   if (s[pos] == '-') sign = -sign;
    ++pos;
  }
  for (int i = s.size() - 1; i >= pos; i -= base_digits) {
   for (int j = max(pos, i - base_digits + 1); j <= i; j++)
     x = x * 10 + s[j] - '0';
    a.push_back(x);
  trim();
}
friend istream & operator >> (istream & stream, bigint &v) {
  string s;
```

```
stream >> s:
  v.read(s);
  return stream;
friend ostream & operator << (ostream & stream, const bigint &v) {
  if (v.sign == -1) stream << '-':
  stream << (v.a.empty() ? 0 : v.a.back());
  for (int i = (int)v.a.size() - 2: i >= 0: --i)
    stream << setw(base_digits) << setfill('0') << v.a[i];</pre>
  return stream;
static vector <int > convert_base(const vector <int > &a, int old_digits,
                                 int new digits) {
  vector < long long > p(max(old_digits, new_digits) + 1);
  p[0] = 1:
  for (int i = 1; i < (int)p.size(); i++) p[i] = p[i - 1] * 10;
  vector < int > res;
  long long cur = 0;
  int cur_digits = 0;
  for (int i = 0; i < (int)a.size(); i++) {
    cur += a[i] * p[cur_digits];
    cur_digits += old_digits;
    while (cur_digits >= new_digits) {
      res.push_back(int(cur % p[new_digits]));
      cur /= p[new_digits];
      cur_digits -= new_digits;
  res.push_back((int)cur);
  while (!res.empty() && !res.back()) res.pop_back();
  return res:
}
typedef vector < long long > vll;
static vll karatsubaMultiply(const vll &a, const vll &b) {
 int n = a.size();
  vll res(n + n):
 if (n <= 32) {
    for (int i = 0; i < n; i++)
      for (int j = 0; j < n; j++) res[i + j] += a[i] * b[j];
    return res:
  }
  int k = n \gg 1:
  vll a1(a.begin(), a.begin() + k);
  vll a2(a.begin() + k, a.end());
  vll b1(b.begin(), b.begin() + k);
  vll b2(b.begin() + k, b.end());
  vll a1b1 = karatsubaMultiply(a1, b1);
  vll a2b2 = karatsubaMultiply(a2, b2);
  for (int i = 0; i < k; i++) a2[i] += a1[i];
  for (int i = 0; i < k; i++) b2[i] += b1[i];
```

```
vll r = karatsubaMultiply(a2, b2);
    for (int i = 0; i < (int)a1b1.size(); i++) r[i] -= a1b1[i];
    for (int i = 0; i < (int)a2b2.size(); i++) r[i] -= a2b2[i];
    for (int i = 0; i < (int)r.size(); i++) res[i + k] += r[i];
    for (int i = 0; i < (int)a1b1.size(); i++) res[i] += a1b1[i];</pre>
    for (int i = 0; i < (int)a2b2.size(); i++) res[i + n] += a2b2[i];
    return res;
 bigint operator*(const bigint &v) const {
    vector < int > a6 = convert_base(this -> a, base_digits, 6);
    vector < int > b6 = convert_base(v.a, base_digits, 6);
    vll a(a6.begin(), a6.end());
    vll b(b6.begin(), b6.end()):
    while (a.size() < b.size()) a.push_back(0);</pre>
    while (b.size() < a.size()) b.push_back(0);</pre>
    while (a.size() & (a.size() - 1)) a.push_back(0), b.push_back(0);
    vll c = karatsubaMultiply(a, b);
    bigint res:
    res.sign = sign * v.sign;
    for (int i = 0, carry = 0; i < (int)c.size(); i++) {</pre>
     long long cur = c[i] + carry;
     res.a.push_back((int)(cur % 1000000));
      carry = (int)(cur / 1000000);
    res.a = convert_base(res.a, 6, base_digits);
   res.trim();
    return res;
};
     Binary To Gray
string binToGray(string bin) {
 string gray(bin.size(), '0');
 int n = bin.size() - 1;
 grav[0] = bin[0];
 for (int i = 1: i <= n: i++) {
    gray[i] = '0' + (bin[i - 1] == '1') ^ (bin[i] == '1');
 return gray;
     Get Permutation Cicles
* receives a permutation [0, n-1]
 * returns a vector of cicles
 * for example: [1, 0, 3, 4, 2] \rightarrow [[0, 1], [2, 3, 4]]
vector < vll > getPermutationCicles(const vll &ps) {
 11 n = len(ps):
 vector < char > visited(n);
 vector <vll> cicles:
 for (int i = 0; i < n; ++i) {
   if (visited[i]) continue;
```

```
vll cicle:
    11 pos = i;
    while (!visited[pos]) {
      cicle.pb(pos):
      visited[pos] = true;
      pos = ps[pos];
    cicles.push_back(vll(all(cicle)));
  return cicles;
    Graphs
4.1 2 SAT (struct)
struct SAT2 {
  11 n:
  vll2d adj, adj_t;
  vc used;
  vll order, comp;
  vc assignment;
  bool solvable;
  SAT2(11 n)
   : n(2 * _n),
      adi(n).
      adj_t(n),
      used(n),
      order(n).
      comp(n, -1),
      assignment(n / 2) {}
  void dfs1(int v) {
    used[v] = true;
    for (int u : adj[v]) {
      if (!used[u]) dfs1(u):
    order.push_back(v);
  void dfs2(int v, int cl) {
    comp[v] = c1;
   for (int u : adj_t[v]) {
      if (comp[u] == -1) dfs2(u, cl);
  }
  bool solve_2SAT() {
    // find and label each SCC
    for (int i = 0; i < n; ++i) {
      if (!used[i]) dfs1(i);
    reverse(all(order));
    11 j = 0;
    for (auto &v : order) {
      if (comp[v] == -1) dfs2(v, j++);
```

```
assignment.assign(n / 2, false);
    for (int i = 0; i < n; i += 2) {
     // x and !x belong to the same SCC
     if (comp[i] == comp[i + 1]) {
        solvable = false;
       return false;
     }
      assignment[i / 2] = comp[i] > comp[i + 1];
    solvable = true;
   return true;
  void add_disjunction(int a, bool na, int b, bool nb) {
    a = (2 * a) ^na;
    b = (2 * b) ^ nb;
    int neg_a = a ^1;
    int neg_b = b ^ 1;
    adj[neg_a].push_back(b);
    adj[neg_b].push_back(a);
    adj_t[b].push_back(neg_a);
    adj_t[a].push_back(neg_b);
 }
};
     SCC (struct)
struct SCC {
 11 N:
 vll2d adj, tadj;
 vll todo, comps, comp;
 vector < set < ll >> sccad;;
 vchar vis;
 SCC(11 _N) : N(_N), adj(_N), tadj(_N), comp(_N, -1), sccadj(_N), vis(_N) {}
 void add_edge(ll x, ll y) { adj[x].eb(y), tadj[y].eb(x); }
  void dfs(ll x) {
    vis[x] = 1;
    for (auto &y : adj[x])
     if (!vis[y]) dfs(y);
   todo.pb(x);
 void dfs2(11 x, 11 v) {
   comp[x] = v;
   for (auto &y : tadj[x])
      if (comp[v] == -1) dfs2(v, v);
 void gen() {
   for (11 i = 0; i < N; ++i)
     if (!vis[i]) dfs(i);
    reverse(all(todo));
    for (auto &x : todo)
     if (comp[x] == -1) {
        dfs2(x, x);
        comps.pb(x);
```

```
}
  void genSCCGraph() {
    for (ll i = 0; i < N; ++i) {</pre>
      for (auto &j : adj[i]) {
        if (comp[i] != comp[j]) {
          sccadj[comp[i]].insert(comp[j]);
      }
    }
 }
};
      SCC Nodes (kosajaru)
/*
 * O(n+m)
 * Returns a pair <a, b>
        a: number of SCCs
        b: vector of size n, where b[i] is the SCC id of node i
void dfs(ll u, vchar &visited, const vll2d &g, vll &scc, bool buildScc, ll id,
         vll &sccid) {
  visited[u] = true;
  sccid[u] = id;
 for (auto &v : g[u])
    if (!visited[v]) dfs(v, visited, g, scc, buildScc, id, sccid);
  // if it's the first pass, add the node to the scc
  if (buildScc) scc.eb(u);
pair<11, vll> kosajaru(vll2d &g) {
  ll n = len(g);
  vll scc;
  vchar vis(n);
  vll sccid(n);
  for (11 i = 0; i < n; i++)
    if (!vis[i]) dfs(i, vis, g, scc, true, 0, sccid);
  // build the transposed graph
  v112d gt(n);
  for (int i = 0; i < n; ++i)
   for (auto &v : g[i]) gt[v].eb(i);
  // run the dfs on the previous scc order
  ll id = 1:
  vis.assign(n, false);
  for (ll i = len(scc) - 1; i >= 0; i--)
   if (!vis[scc[i]]) {
      dfs(scc[i], vis, gt, scc, false, id++, sccid);
  return {id - 1, sccid};
```

4.4 Check Bipartite

```
// O(V)
bool checkBipartite(const ll n, const vector < vll > & adj) {
 queue <11> q;
 q.push(s);
 vll color(n, INF);
 color[s] = 0;
 bool isBipartite = true;
 while (!q.empty() && isBipartite) {
   11 u = q.front();
   q.pop();
   for (auto &v : adj[u]) {
     if (color[v] == INF) {
        color[v] = 1 - color[u];
        q.push(v);
     } else if (color[v] == color[u]) {
        return false;
     }
 return true;
     Count SCC (kosajaru)
void dfs(ll u, vchar &visited, const vll2d &g, vll &scc, bool buildScc) {
  visited[u] = true;
 for (auto &v : g[u])
    if (!visited[v]) dfs(v, visited, g, scc, buildScc);
 // if it's the first pass, add the node to the scc
 if (buildScc) scc.eb(u);
11 kosajaru(v112d &g) {
 ll n = len(g):
 vll scc;
 vchar vis(n);
 for (ll i = 0; i < n; i++)
   if (!vis[i]) dfs(i, vis, g, scc, true);
 // build the transposed graph
 vll2d gt(n):
 for (int i = 0; i < n; ++i)
   for (auto &v : g[i]) gt[v].eb(i);
 // run the dfs on the previous scc order
 11 \ \text{scccnt} = 0;
 vis.assign(n, false);
 for (ll i = len(scc) - 1; i >= 0; i--)
    if (!vis[scc[i]]) dfs(scc[i], vis, gt, scc, false), scccnt++;
 return scccnt:
     Dijkstra
11 __inf = LLONG_MAX >> 5;
vll dijkstra(const vector<vector<pll>>> &g, ll n) {
```

```
priority_queue < pll , vector < pll > , greater < pll >> pq;
 vll dist(n, __inf);
 vector < char > vis(n);
 pq.emplace(0, 0);
 dist[0] = 0;
 while (!pq.empty()) {
   auto [d1, v] = pq.top();
   pq.pop();
   if (vis[v]) continue;
   vis[v] = true;
   for (auto [d2, u] : g[v]) {
     if (dist[u] > d1 + d2) {
        dist[u] = d1 + d2:
       pq.emplace(dist[u], u);
   }
 }
 return dist;
    Floyd Warshall
vector < vll > floyd_warshall(const vector < vll > & adj, ll n) {
 auto dist = adj;
 for (int i = 0; i < n; ++i) {
   for (int j = 0; j < n; ++ j) {
     for (int k = 0; k < n; ++k) {
        dist[j][k] = min(dist[j][k], dist[j][i] + dist[i][k]);
   }
 }
 return dist;
     Kruskal (Python)
class DSU:
   def __init__(self, n):
        self.n = n
        self.p = [x for x in range(0, n + 1)]
        self.size = [0 for i in range(0, n + 1)]
   def find_set(self, x):
        if self.p[x] == x:
            return x
        else:
            self.p[x] = self.find_set(self.p[x])
            return self.p[x]
   def same_set(self, x, y):
        return bool(self.find_set(x) == self.find_set(y))
   def union_set(self, x, y):
        px = self.find_set(x)
        py = self.find_set(y)
```

```
if px == py:
           return
        size x = self.size[px]
       size_y = self.size[py]
        if size_x > size_y:
           self.p[py] = self.p[px]
            self.size[px] += self.size[py]
            self.p[px] = self.p[py]
           self.size[py] += self.size[px]
def kruskal(gv. n):
   Receives te list of edges as a list of tuple in the form:
       d: distance between u and v
   And also n as the total of verties.
   dsu = DSU(n)
   c = 0
   for e in gv:
       d, u, v = e
       if not dsu.same_set(u, v):
           c += d
           dsu.union_set(u, v)
   return c
```

Lowest Common Ancestor Sparse Table

```
int fastlog2(ll x) {
 ull i = x:
 return i ? __builtin_clzll(1) - __builtin_clzll(i) : -1;
template <typename T>
class SparseTable {
public:
 int N:
 int K;
 vector < vector < T >> st:
 SparseTable(vector<T> vs)
    : N((int)vs.size()), K(fastlog2(N) + 1), st(K + 1, vector < T > (N + 1)) {
    copy(vs.begin(), vs.end(), st[0].begin());
   for (int i = 1; i <= K; ++i)
     for (int j = 0; j + (1 << i) <= N; ++j)
        st[i][j] = min(st[i - 1][j], st[i - 1][j + (1 << (i - 1))]);
 SparseTable() {}
 T RMQ(int 1, int r) {
   int i = fastlog2(r - l + 1);
    return min(st[i][1], st[i][r - (1 << i) + 1]);
};
```

```
class LCA {
 public:
  int p;
  int n:
  vi first:
  vector < char > visited;
  vi vertices:
  vi height;
  SparseTable < int > st:
  LCA(const vector < vi> &g)
    : p(0), n((int)g.size()), first(n + 1), visited(n + 1, 0), height(n + 1) {
    build_dfs(g, 1, 1);
    st = SparseTable < int > (vertices);
  void build_dfs(const vector<vi> &g, int u, int hi) {
    visited[u] = true;
    height[u] = hi;
    first[u] = vertices.size();
    vertices.push_back(u);
    for (auto uv : g[u]) {
      if (!visited[uv]) {
        build_dfs(g, uv, hi + 1);
        vertices.push_back(u);
    }
  }
  int lca(int a, int b) {
    int l = min(first[a], first[b]);
    int r = max(first[a], first[b]);
    return st.RMQ(1, r):
 }
};
       Topological Sorting
4.10
```

```
/*
* 0(V)
* assumes:
       * vertices have index [0, n-1]
* if is a DAG:
      * returns a topological sorting
* else:
     * returns an empty vector
enum class state { not_visited, processing, done };
bool dfs(const vector<vll> &adj, ll s, vector<state> &states, vll &order) {
 states[s] = state::processing;
 for (auto &v : adj[s]) {
   if (states[v] == state::not_visited) {
     if (not dfs(adj, v, states, order)) return false;
   } else if (states[v] == state::processing)
     return false:
 states[s] = state::done;
 order.pb(s);
```

```
return true:
vll topologicalSorting(const vector<vll> &adj) {
 11 n = len(adi):
 vll order:
 vector < state > states(n, state::not_visited);
 for (int i = 0: i < n: ++i) {
   if (states[i] == state::not_visited) {
      if (not dfs(adj, i, states, order)) return {};
 }
 reverse(all(order));
 return order;
    Math
    Combinatorics With Repetitions
void combinations_with_repetition(int n, int k,
                                  function < void (const vector < int > &) > process)
 vector < int > v(k, 1);
 int pos = k - 1;
 while (true) {
   process(v);
   v[pos]++;
    while (pos > 0 and v[pos] > n) {
      --pos:
     v[pos]++;
   if (pos == 0 and v[pos] > n) break;
    for (int i = pos + 1; i < k; ++i) v[i] = v[pos];
   pos = k - 1;
      Count Divisors Memo
const 11 mod = 1073741824;
const ll maxd = 100 * 100 * 100 + 1;
vector<11> memo(maxd, -1);
ll countdivisors(ll x) {
 11 ox = x;
 11 \text{ ans} = 1;
 for (11 i = 2; i <= x; ++i) {
   if (memo[x] != -1) {
     ans *= memo[x];
     break;
```

11 count = 0;

```
x /= i;
      count++;
    ans *= (count + 1);
  memo[ox] = ans:
  return ans;
     Euler Phi
5.3
const ll MAXN = 1e5;
vll list_primes(ll n) { // Nlog * log N
  vll ps;
  bitset < MAXN > sieve;
  sieve.set();
  sieve.reset(1);
  for (11 i = 2; i <= n; ++i) {
    if (sieve[i]) ps.push_back(i);
   for (11 j = i * 2; j <= n; j += i) {
      sieve.reset(j);
 }
  return ps;
vector<pll> factorization(ll n, const vll &primes) {
  vector < pll > ans;
 for (auto &p : primes) {
    if (n == 1) break;
    11 cnt = 0;
    while (n % p == 0) {
      cnt++;
      n /= p;
    if (cnt) ans.emplace_back(p, cnt);
  return ans:
11 phi(ll n, vector<pll> factors) {
  if (n == 1) return 1;
 11 \text{ ans} = n:
 for (auto [p, k] : factors) {
    ans /= p;
    ans *= (p - 1);
  return ans;
5.4 Factorial Factorization
// O(logN) greater k that p^k | n
```

ll E(ll n, ll p) {

11 k = 0, b = p;

while (x and x % i == 0) {

```
while (b \le n) {
   k += n / b;
   b *= p;
 return k;
// lsit every prime until MAXN O(Nlog * log N)
const 11 MAXN = 1e5:
vll list_primes(ll n) {
  vll ps;
 bitset < MAXN > sieve;
 sieve.set();
  sieve.reset(1);
 for (11 i = 2: i \le n: ++i) {
   if (sieve[i]) ps.push_back(i);
   for (ll j = i * 2; j <= n; j += i) sieve.reset(j);
 return ps;
// O(pi(N)*logN)
map<11, 11> factorial_factorization(11 n, const v11 &primes) {
 map < 11, 11 > fs;
 for (const auto &p : primes) {
   if (p > n) break;
   fs[p] = E(n, p);
  return fs;
    Factorial
const ll MAX = 18;
vll fv(MAX, -1);
ll factorial(ll n) {
 if (fv[n] != -1) return fv[n];
 if (n == 0) return 1;
 return n * factorial(n - 1);
     Factorization With Primes
// Nlog * log N
const ll MAXN = 1e5;
vll list_primes(ll n) {
 vll ps;
 bitset < MAXN > sieve;
 sieve.set();
 sieve.reset(1):
 for (11 i = 2; i <= n; ++i) {
   if (sieve[i]) ps.push_back(i);
   for (11 j = i * 2; j <= n; j += i) sieve.reset(j);</pre>
 }
  return ps;
// O(pi(sqrt(n)))
```

```
map<ll, 11> factorization(ll n, const vll &primes) {
  map<11, 11> ans;
  for (auto p : primes) {
   if (p * p > n) break;
   11 count = 0;
   for (; n % p == 0; count++, n /= p)
    if (count) ans[p] = count;
  return ans;
      Factorization
// O(sqrt(n))
map<ll, ll> factorization(ll n) {
  map<11, 11> ans;
  for (11 i = 2; i * i <= n; i++) {
   11 count = 0;
   for (; n % i == 0; count++, n /= i)
    if (count) ans[i] = count;
  }
  if (n > 1) ans[n]++;
  return ans:
     Fast Exp
 Fast exponentiation algorithm,
 compute a^n in O(log(n))
ll fexp(ll a, int n) {
 if (n == 0) return 1:
  if (n == 1) return a;
 11 x = fexp(a, n / 2);
  return x * x * (n & 1 ? a : 1);
     Gcd Using Factorization
// O(sqrt(n))
map<ll, ll> factorization(ll n) {
  map<11, 11> ans;
 for (ll i = 2; i * i <= n; i++) {
   11 count = 0;
   for (; n % i == 0; count++, n /= i)
    if (count) ans[i] = count;
  if (n > 1) ans[n]++;
  return ans;
ll gcd_with_factorization(ll a, ll b) {
  map<ll, ll> fa = factorization(a);
```

```
map<ll. 11> fb = factorization(b):
 ll ans = 1;
 for (auto fai : fa) {
   11 k = min(fai.second, fb[fai.first]);
   while (k--) ans *= fai.first;
 return ans;
5.10 Gcd
11 gcd(11 a, 11 b) { return b ? gcd(b, a % b) : a; }
5.11 Integer Mod
const ll INF = 1e18;
const 11 mod = 998244353;
template <11 MOD = mod>
struct Modular {
 ll value:
 static const 11 MOD value = MOD:
 Modular(11 v = 0) {
   value = v % MOD;
   if (value < 0) value += MOD;</pre>
 Modular(ll a, ll b) : value(0) {
   *this += a:
   *this /= b;
 }
 Modular& operator+=(Modular const& b) {
    value += b.value;
   if (value >= MOD) value -= MOD;
   return *this;
  Modular& operator -= (Modular const& b) {
    value -= b.value;
   if (value < 0) value += MOD:</pre>
   return *this;
 Modular& operator*=(Modular const& b) {
    value = (11)value * b.value % MOD;
   return *this:
 friend Modular mexp(Modular a, 11 e) {
    Modular res = 1;
    while (e) {
     if (e & 1) res *= a:
     a *= a;
      e >>= 1:
   return res;
 friend Modular inverse (Modular a) { return mexp(a, MOD - 2); }
 Modular& operator/=(Modular const& b) { return *this *= inverse(b); }
```

```
friend Modular operator+(Modular a, Modular const b) { return a += b; }
  Modular operator++(int) { return this->value = (this->value + 1) % MOD; }
  Modular operator++() { return this->value = (this->value + 1) % MOD; }
  friend Modular operator - (Modular a, Modular const b) { return a -= b; }
  friend Modular operator - (Modular const a) { return 0 - a; }
  Modular operator -- (int) {
    return this->value = (this->value - 1 + MOD) % MOD:
  }
  Modular operator -- () { return this -> value = (this -> value - 1 + MOD) % MOD; }
  friend Modular operator*(Modular a, Modular const b) { return a *= b; }
  friend Modular operator/(Modular a, Modular const b) { return a /= b; }
  friend std::ostream& operator << (std::ostream& os, Modular const& a) {
    return os << a.value:
  friend bool operator == (Modular const& a, Modular const& b) {
    return a.value == b.value:
  friend bool operator!=(Modular const& a, Modular const& b) {
    return a.value != b.value:
 }
}:
5.12 Is Prime
bool isprime(ll n) { // O(sqrt(n))
  if (n < 2) return false;
  if (n == 2) return true:
  if (n % 2 == 0) return false:
 for (11 i = 3; i * i < n; i += 2)
   if (n % i == 0) return false:
  return true;
5.13 Lcm Using Factorization
map<ll. 11> factorization(11 n) {
  map<11, 11> ans;
 for (11 i = 2: i * i <= n: i++) {
   11 count = 0:
   for (; n % i == 0; count++, n /= i)
    if (count) ans[i] = count;
  if (n > 1) ans[n]++;
  return ans;
11 lcm_with_factorization(ll a, ll b) {
  map<11, 11> fa = factorization(a):
  map<11, 11> fb = factorization(b);
  ll ans = 1:
 for (auto fai : fa) {
   11 k = max(fai.second, fb[fai.first]);
    while (k--) ans *= fai.first:
 7
  return ans;
```

5.14 Lcm

```
11 gcd(l1 a, l1 b) { return b ? gcd(b, a % b) : a; }
11 lcm(l1 a, l1 b) { return a / gcd(a, b) * b; }
```

5.15 Modular Inverse Using Phi

```
map<11, 11> factorization(11 n) {
 map < 11, 11 > ans;
 for (ll i = 2; i * i <= n; i++) {
   11 count = 0;
   for (; n % i == 0; count++, n /= i)
   if (count) ans[i] = count:
 if (n > 1) ans [n]++;
 return ans:
ll phi(ll n) {
 if (n == 1) return 1;
 auto fs = factorization(n):
 auto res = n;
 for (auto [p, k] : fs) {
   res /= p;
   res *= (p - 1);
 return res:
11 fexp(ll a, ll n, ll mod) {
 if (n == 0) return 1;
 if (n == 1) return a:
 11 x = fexp(a, n / 2, mod);
 return x * x * (n & 1 ? a : 1) % mod:
11 inv(ll a, ll mod) { return fexp(a, phi(mod) - 1, mod); }
```

5.16 N Choose K Count

```
/*
 * 0(nm) time, 0(m) space
 * equal to n choose k
 * */
11 binom(11 n, 11 k) {
   if (k > n) return 0;
   vll dp(k + 1, 0);
   dp[0] = 1;
   for (11 i = 1; i <= n; i++)
      for (11 j = k; j > 0; j--) dp[j] = dp[j] + dp[j - 1];
   return dp[k];
}
```

5.17 Permutation Count

}

```
const 11 MAX = 18;
vll fv(MAX, -1):
ll factorial(ll n) {
 if (fv[n] != -1) return fv[n];
 if (n == 0) return 1;
  return n * factorial(n - 1);
template <typename T>
11 permutation_count(vector <T> xs) {
  map < T, 11 > h;
  for (auto xi : xs) h[xi]++;
  11 ans = factorial((11)xs.size());
  dbg(ans);
 for (auto [v, cnt] : h) {
    dbg(cnt):
    ans /= cnt;
  return ans;
5.18 Polynomial
using polynomial = vector<11>;
int degree(const polynomial &xs) { return xs.size() - 1; }
ll horner_evaluate(const polynomial &xs, ll x) {
 11 \text{ ans} = 0;
 11 n = degree(xs);
 for (int i = n; i >= 0; --i) {
    ans *= x;
    ans += xs[i];
 }
  return ans;
polynomial operator+(const polynomial &a, const polynomial &b) {
 int n = degree(a);
 int m = degree(b);
  polynomial r(max(n, m) + 1, 0);
  for (int i = 0; i <= n; ++i) r[i] += a[i];
  for (int j = 0; j \le m; ++j) r[j] += b[j];
  while (!r.empty() and r.back() == 0) r.pop_back();
  if (r.empty()) r.push_back(0);
  return r:
polynomial operator*(const polynomial &p, const polynomial &q) {
 int n = degree(p);
  int m = degree(q);
  polynomial r(n + m + 1, 0);
 for (int i = 0; i <= n; ++i)
    for (int j = 0; j \le m; ++j) r[i + j] += (p[i] * q[j]);
```

5.19 Power Sum

```
// calculates K^0 + K^1 ... + K^n
ll fastpow(ll a, int n) {
   if (n == 1) return a;
    ll x = fastpow(a, n / 2);
   return x * x * (n & 1 ? a : 1);
}
ll powersum(ll n, ll k) { return (fastpow(n, k + 1) - 1) / (n - 1); }
```

5.20 Sieve List Primes

```
// lsit every prime until MAXN
const ll MAXN = 1e5;
vll list_primes(ll n) { // Nlog * log N
  vll ps;
  bitset<MAXN> sieve;
  sieve.set();
  sieve.reset(l);
  for (ll i = 2; i <= n; ++i) {
    if (sieve[i]) ps.push_back(i);
    for (ll j = i * 2; j <= n; j += i) {
       sieve.reset(j);
    }
}
return ps;
}</pre>
```

6 Searching

6.1 Ternary Search Recursive

```
const double eps = 1e-6;

// IT MUST BE AN UNIMODAL FUNCTION
double f(int x) { return x * x + 2 * x + 4; }

double ternary_search(double 1, double r) {
   if (fabs(f(1) - f(r)) < eps) return f((1 + (r - 1) / 2.0));

   auto third = (r - 1) / 3.0;
   auto m1 = 1 + third;
   auto m2 = r - third;

   // change the signal to find the maximum point.
   return m1 < m2 ? ternary_search(m1, r) : ternary_search(1, m2);
}</pre>
```

7 Strings

7.1 Rabin Karp

```
vi rabin_karp(string const &s, string const &t) {
    ll p = 31;
    ll m = 1e9 + 9;
```

```
int S = s.size(), T = t.size();
  vll p_pow(max(S, T));
  p_pow[0] = 1;
  for (int i = 1; i < (int)p_pow.size(); i++) p_pow[i] = (p_pow[i - 1] * p) %
  vll h(T + 1, 0);
  for (int i = 0; i < T; i++)
   h[i + 1] = (h[i] + (t[i] - 'a' + 1) * p_pow[i]) % m;
  11 h_s = 0:
  for (int i = 0; i < S; i++) h_s = (h_s + (s[i] - 'a' + 1) * p_pow[i]) % m;
  vi occurences:
  for (int i = 0; i + S - 1 < T; i++) {
   ll cur_h = (h[i + S] + m - h[i]) % m;
    // IT DON'T CONSIDERE CONLISIONS !
    if (cur_h == h_s * p_pow[i] % m) occurences.push_back(i);
  return occurences;
7.2 String Psum
struct strPsum {
 11 n;
  11 k;
  vector < vll > psum;
  strPsum(const string \&s) : n(s.size()), k(100), psum(k, vll(n + 1)) {
    for (ll i = 1; i <= n; ++i) {
      for (11 j = 0; j < k; ++j) {
        psum[j][i] = psum[j][i - 1];
      psum[s[i - 1]][i]++;
  }
  ll qtd(ll l, ll r, char c) { // [0,n-1]
    return psum[c][r + 1] - psum[c][1];
      Trie Naive
// time: O(n^2) memory: O(n^2)
using Node = map < char, int >;
using vi = vector<int>;
using Trie = vector < Node >;
Trie build(const string &s) {
  int n = (int)s.size();
  Trie trie(1);
  string suffix;
  for (int i = n - 1; i \ge 0; --i) {
    suffix = s.substr(i) + '#';
    int v = 0; // root
```

```
for (auto c : suffix) {
     if (c == '#') {  // makrs the poistion of an occurence
        trie[v][c] = i;
        break:
     if (trie[v][c])
       v = trie[v][c]:
      else {
       trie.push_back({});
        trie[v][c] = trie.size() - 1;
        v = trie.size() - 1;
   }
 return trie:
}
vi search(Trie &trie, string s) {
 int p = 0;
 vi occ:
 for (auto &c : s) {
   p = trie[p][c];
   if (!p) return occ;
 }
 queue < int > q;
 q.push(0);
 while (!q.empty()) {
   auto cur = q.front();
   q.pop();
   for (auto [c, v] : trie[cur]) {
     if (c == '#')
        occ.push_back(v);
      else
        q.push(v);
 return occ;
11 distinct substr(const Trie &trie) {
 11 cnt = 0;
 queue < int > q;
 q.push(0);
 while (!q.empty()) {
   auto u = q.front();
   q.pop();
    for (auto [c, v] : trie[u]) {
     if (c != '#') {
       cnt++;
        q.push(v);
   }
 }
 return cnt;
```

8 Trees

8.1 Binary Lifting

```
/*
  * far[h][i] = the node that 2^h far from node i
  * sometimes is useful invert the order of loops
  * time : O(nlogn)
  * */
const int maxlog = 20;
int far[maxlog + 1][n + 1];
int n;
for (int h = 1; h <= maxlog; h++) {
  for (int i = 1; i <= n; i++) {
    far[h][i] = far[h - 1][far[h - 1][i]];
  }
}
8.2 Maximum Distances
/*</pre>
```

```
* Returns the maximum distance from every node to any other node in the tree.
pll mostDistantFrom(const vector<vll> &adj, ll n, ll root) {
 // 0 indexed
 11 mostDistantNode = root;
 11 nodeDistance = 0:
 queue <pll> q;
 vector < char > vis(n);
  q.emplace(root, 0);
  vis[root] = true;
  while (!q.empty()) {
    auto [node, dist] = q.front();
    q.pop();
    if (dist > nodeDistance) {
      nodeDistance = dist:
      mostDistantNode = node;
    for (auto u : adj[node]) {
      if (!vis[u]) {
        vis[u] = true;
        q.emplace(u, dist + 1);
    }
 }
 return {mostDistantNode, nodeDistance};
11 twoNodesDist(const vector < vll> &adj, ll n, ll a, ll b) {
 queue <pll> q;
 vector < char > vis(n);
 q.emplace(a, 0);
 while (!q.empty()) {
   auto [node, dist] = q.front();
   q.pop();
    if (node == b) return dist;
    for (auto u : adj[node]) {
```

```
if (!vis[u]) {
        vis[u] = true;
       q.emplace(u, dist + 1);
  return -1;
tuple < 11, 11, 11 > tree_diameter(const vector < v11 > & adj, 11 n) {
 // returns two points of the diameter and the diameter itself
 auto [node1, dist1] = mostDistantFrom(adj, n, 0);
 auto [node2, dist2] = mostDistantFrom(adj, n, node1);
 auto diameter = twoNodesDist(adj, n, node1, node2);
 return make tuple(node1, node2, diameter):
vll everyDistanceFromNode(const vector < vll > & adj, ll n, ll root) {
 // Single Source Shortest Path, from a given root
 queue < pair < ll, ll >> q;
 vll ans(n, -1);
 ans[root] = 0:
 q.emplace(root, 0);
 while (!q.empty()) {
   auto [u, d] = q.front();
   q.pop();
    for (auto w : adj[u]) {
     if (ans[w] != -1) continue;
      ans[w] = d + 1;
      q.emplace(w, d + 1);
 }
  return ans;
vll maxDistances(const vector<vll> &adj, ll n) {
 auto [node1, node2, diameter] = tree_diameter(adj, n);
 auto distances1 = everyDistanceFromNode(adj, n, node1);
 auto distances2 = everyDistanceFromNode(adj, n, node2);
 for (int i = 0; i < n; ++i) ans[i] = max(distances1[i], distances2[i]);</pre>
 return ans;
      Tree Diameter
pll mostDistantFrom(const vector<vll> &adj, ll n, ll root) {
 // 0 indexed
 11 mostDistantNode = root:
 11 nodeDistance = 0;
 queue <pll> q;
 vector < char > vis(n);
 q.emplace(root, 0);
 vis[root] = true;
 while (!q.empty()) {
   auto [node, dist] = q.front();
```

q.pop();

```
if (dist > nodeDistance) {
      nodeDistance = dist;
      mostDistantNode = node;
    for (auto u : adj[node]) {
      if (!vis[u]) {
        vis[u] = true:
        q.emplace(u, dist + 1);
    }
  return {mostDistantNode, nodeDistance};
11 twoNodesDist(const vector < vll > & adj, ll n, ll a, ll b) {
 // 0 indexed
  queue <pll> q;
  vector < char > vis(n);
  q.emplace(a, 0);
  while (!q.empty()) {
   auto [node, dist] = q.front();
    q.pop();
    if (node == b) {
      return dist:
   for (auto u : adj[node]) {
      if (!vis[u]) {
        vis[u] = true;
        q.emplace(u, dist + 1);
 }
  return -1;
ll tree_diameter(const vector < vll > & adj, ll n) {
 // 0 indexed !!!
  auto [node1, dist1] = mostDistantFrom(adj, n, 0);
  auto [node2, dist2] = mostDistantFrom(adj, n, node1);
  auto diameter = twoNodesDist(adj, n, node1, node2);
  return diameter:
    Settings and macros
9.1 .vimrc
set ts=4 sw=4 sta nu rnu sc cindent
set bg=dark ruler clipboard=unnamed,unnamedplus, timeoutlen=100
colorscheme default
nnoremap <C-j> :botright belowright term bash <CR>
syntax on
```

degug.cpp

#include <bits/stdc++.h>

/****** Debug Code ******/

using namespace std;

```
template <typename T>
concept Printable = requires(T t) {
    { std::cout << t } -> std::same_as<std::ostream &>;
template <Printable T>
void __print(const T &x) {
    cerr << x:
}
template <size t T>
void __print(const bitset<T> &x) {
    cerr << x;
template <typename A, typename B>
void __print(const pair<A, B> &p);
template <typename... A>
void __print(const tuple<A...> &t);
template <typename T>
void __print(stack<T> s);
template <typename T>
void __print(queue < T > q);
template <typename T, typename... U>
void __print(priority_queue < T, U... > q);
template <typename A>
void __print(const A &x) {
    bool first = true:
    cerr << '{';
    for (const auto &i : x) {
        cerr << (first ? "" : ","), __print(i);</pre>
        first = false;
    cerr << '}':
template <typename A, typename B>
void __print(const pair<A, B> &p) {
    cerr << '(';
    __print(p.first);
    cerr << ',';
    __print(p.second);
    cerr << ')':
template <typename... A>
void __print(const tuple<A...> &t) {
    bool first = true;
    cerr << '(':
    apply(
        [&first](const auto &...args) {
            ((cerr << (first ? "" : ","), __print(args), first = false), ...);
        },
        t):
    cerr << ')';
}
template <typename T>
void __print(stack<T> s) {
    vector <T> debugVector;
    while (!s.empty()) {
        T t = s.top();
        debugVector.push_back(t);
        s.pop();
```

```
}
    reverse(debugVector.begin(), debugVector.end());
    __print(debugVector);
template <typename T>
void __print(queue < T > q) {
    vector <T> debugVector;
    while (!q.empty()) {
        T t = q.front();
        debugVector.push_back(t);
        q.pop();
    __print(debugVector);
template <typename T, typename... U>
void __print(priority_queue < T, U... > q) {
    vector <T> debugVector;
    while (!q.empty()) {
        T t = q.top();
        debugVector.push_back(t);
        q.pop();
    __print(debugVector);
void _print() { cerr << "]\n"; }</pre>
template <typename Head, typename... Tail>
void _print(const Head &H, const Tail &...T) {
    __print(H);
    if (sizeof...(T)) cerr << ", ";
    _print(T...);
}
#define dbg(x...)
    cerr << "[" << #x << "] = ["; \
    _print(x)
9.3 .bashrc
cpp() {
  echo ">> COMPILING <<" 1>&2
  g++ -std=c++17 \
      -02 \
      -g \
      -g3 \
      -Wextra \
      -Wshadow \
      -Wformat=2 \
      -Wconversion \
      -fsanitize=address,undefined \
      -fno-sanitize-recover \
      -Wfatal-errors \
      -DDEBUG $1 \
  if [ $? -ne 0 ]; then
      echo ">> FAILED <<" 1>&2
      return 1
  fi
  echo ">> DONE << " 1>&2
```

```
time ./a.out ${@:2}
prepare() {
    for i in {a..z}
        cp macro.cpp $i.cpp
       touch $i.py
    done
    for i in {1..10}
        touch in${i}
        touch out${i}
        touch ans${i}
    done
9.4 macro.cpp
#include <bits/stdc++.h>
using namespace std;
#ifdef DEBUG
#include "debug.cpp"
#else
#define dbg(...) 666
#endif
#define endl '\n'
#define fastio
   ios_base::sync_with_stdio(false); \
```

cin.tie(0);

```
cout.tie(0);
#define len(__x) (ll) __x.size()
using ll = long long;
using vll = vector<11>;
using pll = pair<11, 11>;
using v112d = vector < v11 >;
using vi = vector<int>;
using vi2d = vector < vi>;
using pii = pair<int, int>;
using vii = vector<pii>;
using vc = vector < char >;
#define all(a) a.begin(), a.end()
#define snd second
#define fst first
#define pb(___x) push_back(___x)
#define mp(__a, __b) make_pair(__a, __b)
#define eb(___x) emplace_back(___x)
const ll INF = 1e18;
void run() {
int32_t main(void) {
   fastio;
   int t;
   t = 1;
   // cin >> t;
    while (t--) run();
```