

The Reference

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1 Data structures

1.1 Ordered Set Gnu Pbds

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template <typename T>
// using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
// tree_order_statistics_node_update>;

// if you want to find the elements less or equal :p
using ordered_set = tree<T, null_type, less_equal<T>, rb_tree_tag,
                        tree_order_statistics_node_update>;
```

1.2 Segtree Rmq Lazy Max Update

```
struct SegmentTree {
    int N;
    vll ns, lazy;
    SegmentTree(const vll &xs) : N(xs.size()), ns(4 * N, 0), lazy(4 * N, 0) {
        for (size_t i = 0; i < xs.size(); ++i) {
            update(i, i, xs[i]);
        }
    }
    void update(int a, int b, ll value) { update(1, 0, N - 1, a, b, value); }
    void update(int node, int L, int R, int a, int b, ll value) {
        if (lazy[node]) {
            ns[node] = max(ns[node], lazy[node]);
            if (L < R) {
                lazy[2 * node] = max(lazy[2 * node], lazy[node]);
                lazy[2 * node + 1] = max(lazy[2 * node + 1], lazy[node]);
            }
            lazy[node] = 0;
        }
        if (a > R or b < L) return;
        if (a <= L and R <= b) {
            ns[node] = max(ns[node], value);
            if (L < R) {
                lazy[2 * node] = max(value, lazy[2 * node]);
                lazy[2 * node + 1] = max(value, lazy[2 * node + 1]);
            }
            return;
        }
        update(2 * node, L, (L + R) / 2, a, b, value);
        update(2 * node + 1, (L + R) / 2 + 1, R, a, b, value);
        ns[node] = max(ns[2 * node], ns[2 * node + 1]);
    }
}

ll RMQ(int a, int b) { return RMQ(1, 0, N - 1, a, b); }
ll RMQ(int node, int L, int R, int a, int b) {
    if (lazy[node]) {
        ns[node] = max(ns[node], lazy[node]);
        if (L < R) {
            lazy[2 * node] = max(lazy[2 * node], lazy[node]);
            lazy[2 * node + 1] = max(lazy[2 * node + 1], lazy[node]);
        }
    }
}
```

```

    lazy[node] = 0;
}

if (a > R or b < L) return 0;
if (a <= L and R <= b) return ns[node];
ll x = RMQ(2 * node, L, (L + R) / 2, a, b);
ll y = RMQ(2 * node + 1, (L + R) / 2 + 1, R, a, b);
return max(x, y);
}
};

```

1.3 Segtree Rmq Lazy Range

```

struct SegmentTree {
    int N;
    vll ns, lazy;
    SegmentTree(const vll &xs)
        : N(xs.size()), ns(4 * N, INT_MAX), lazy(4 * N, 0) {
        for (size_t i = 0; i < xs.size(); ++i) update(i, i, xs[i]);
    }
    void update(int a, int b, ll value) { update(1, 0, N - 1, a, b, value); }
    void update(int node, int L, int R, int a, int b, ll value) {
        if (lazy[node]) {
            ns[node] = ns[node] == INT_MAX ? lazy[node] : ns[node] + lazy[node];
            if (L < R) {
                lazy[2 * node] += lazy[node];
                lazy[2 * node + 1] += lazy[node];
            }
            lazy[node] = 0;
        }
        if (a > R or b < L) return;
        if (a <= L and R <= b) {
            ns[node] = ns[node] == INT_MAX ? value : ns[node] + value;
            if (L < R) {
                lazy[2 * node] += value;
                lazy[2 * node + 1] += value;
            }
            return;
        }
        update(2 * node, L, (L + R) / 2, a, b, value);
        update(2 * node + 1, (L + R) / 2 + 1, R, a, b, value);
        ns[node] = min(ns[2 * node], ns[2 * node + 1]);
    }
    ll RMQ(int a, int b) { return RMQ(1, 0, N - 1, a, b); }
    ll RMQ(int node, int L, int R, int a, int b) {
        if (lazy[node]) {
            ns[node] = ns[node] == INT_MAX ? lazy[node] : ns[node] + lazy[node];
            if (L < R) {
                lazy[2 * node] += lazy[node];
                lazy[2 * node + 1] += lazy[node];
            }
            lazy[node] = 0;
        }
        if (a > R or b < L) return INT_MAX;

        if (a <= L and R <= b) return ns[node];
        ll x = RMQ(2 * node, L, (L + R) / 2, a, b);
        ll y = RMQ(2 * node + 1, (L + R) / 2 + 1, R, a, b);

```

```

        return min(x, y);
    }
};

```

1.4 Segtree Point Rmq

```

class SegTree {
public:
    int n;
    vector<ll> st;
    SegTree(const vector<ll> &v) : n((int)v.size()), st(n * 4 + 1, LLONG_MAX) {
        for (int i = 0; i < n; ++i) update(i, v[i]);
    }
    void update(int p, ll v) { update(1, 0, n - 1, p, v); }
    ll RMQ(int l, int r) { return RMQ(1, 0, n - 1, l, r); }

private:
    void update(int node, int l, int r, int p, ll v) {
        if (p < l or p > r) return; // fora do intervalo.

        if (l == r) {
            st[node] = v;
            return;
        }

        int mid = l + (r - l) / 2;

        update(node * 2, l, mid, p, v);
        update(node * 2 + 1, mid + 1, r, p, v);

        st[node] = min(st[node * 2], st[node * 2 + 1]);
    }

    ll RMQ(int node, int L, int R, int l, int r) {
        if (l <= L and r >= R) return st[node];
        if (L > r or R < l) return LLONG_MAX;
        if (L == R) return st[node];

        int mid = L + (R - L) / 2;

        return min(RMQ(node * 2, L, mid, l, r),
                   RMQ(node * 2 + 1, mid + 1, R, l, r));
    }
};

```

1.5 Segtree Rsq Lazy Range Sum

```

struct SegTree {
    int N;
    vector<ll> ns, lazy;

    SegTree(const vector<ll> &xs) : N(xs.size()), ns(4 * N, 0), lazy(4 * N, 0) {
        for (size_t i = 0; i < xs.size(); ++i) update(i, i, xs[i]);
    }

    void update(int a, int b, ll value) { update(1, 0, N - 1, a, b, value); }

    void update(int node, int L, int R, int a, int b, ll value) {

```

```

// Lazy propagation
if (lazy[node]) {
    ns[node] += (R - L + 1) * lazy[node];

    if (L < R) // Se o nó não é uma folha, propaga
    {
        lazy[2 * node] += lazy[node];
        lazy[2 * node + 1] += lazy[node];
    }

    lazy[node] = 0;
}

if (a > R or b < L) return;

if (a <= L and R <= b) {
    ns[node] += (R - L + 1) * value;

    if (L < R) {
        lazy[2 * node] += value;
        lazy[2 * node + 1] += value;
    }

    return;
}

update(2 * node, L, (L + R) / 2, a, b, value);
update(2 * node + 1, (L + R) / 2 + 1, R, a, b, value);

ns[node] = ns[2 * node] + ns[2 * node + 1];
}

ll RSQ(int a, int b) { return RSQ(1, 0, N - 1, a, b); }

ll RSQ(int node, int L, int R, int a, int b) {
    if (lazy[node]) {
        ns[node] += (R - L + 1) * lazy[node];

        if (L < R) {
            lazy[2 * node] += lazy[node];
            lazy[2 * node + 1] += lazy[node];
        }

        lazy[node] = 0;
    }

    if (a > R or b < L) return 0;

    if (a <= L and R <= b) return ns[node];

    ll x = RSQ(2 * node, L, (L + R) / 2, a, b);
    ll y = RSQ(2 * node + 1, (L + R) / 2 + 1, R, a, b);

    return x + y;
}
};

```

1.6 Segtree Rxq Lazy Range Xor

```

struct SegTree {
    int N;
    vector<ll> ns, lazy;

    SegTree(const vector<ll> &xs) : N(xs.size()), ns(4 * N, 0), lazy(4 * N, 0) {
        for (size_t i = 0; i < xs.size(); ++i) update(i, i, xs[i]);
    }

    void update(int a, int b, ll value) { update(1, 0, N - 1, a, b, value); }

    void update(int node, int L, int R, int a, int b, ll value) {
        // Lazy propagation
        if (lazy[node]) {
            ns[node] ^= lazy[node];

            if (L < R) // Se o nó não é uma folha, propaga
            {
                lazy[2 * node] ^= lazy[node];
                lazy[2 * node + 1] ^= lazy[node];
            }

            lazy[node] = 0;
        }

        if (a > R or b < L) return;

        if (a <= L and R <= b) {
            ns[node] ^= value;

            if (L < R) {
                lazy[2 * node] ^= value;
                lazy[2 * node + 1] ^= value;
            }

            return;
        }

        update(2 * node, L, (L + R) / 2, a, b, value);
        update(2 * node + 1, (L + R) / 2 + 1, R, a, b, value);

        ns[node] = ns[2 * node] ^ ns[2 * node + 1];
    }

    ll rxq(int a, int b) { return RSQ(1, 0, N - 1, a, b); }

    ll rxq(int node, int L, int R, int a, int b) {
        if (lazy[node]) {
            ns[node] ^= lazy[node];

            if (L < R) {
                lazy[2 * node] ^= lazy[node];
                lazy[2 * node + 1] ^= lazy[node];
            }

            lazy[node] = 0;
        }
    }
};

```

```

    if (a > R or b < L) return 0;

    if (a <= L and R <= b) return ns[node];

    ll x = rxq(2 * node, L, (L + R) / 2, a, b);
    ll y = rxq(2 * node + 1, (L + R) / 2 + 1, R, a, b);

    return x ^ y;
}
};

```

1.7 Dsu (Python)

```

class DSU:
    def __init__(self, n):
        self.n = n
        self.p = [x for x in range(0, n + 1)]
        self.size = [0 for i in range(0, n + 1)]

    def find_set(self, x): # log n
        if self.p[x] == x:
            return x
        else:
            self.p[x] = self.find_set(self.p[x])
            return self.p[x]

    def same_set(self, x, y): # log n
        return bool(self.find_set(x) == self.find_set(y))

    def union_set(self, x, y): # log n
        px = self.find_set(x)
        py = self.find_set(y)

        if px == py:
            return

        size_x = self.size[px]
        size_y = self.size[py]

        if size_x > size_y:
            self.p[py] = self.p[px]
            self.size[px] += self.size[py]
        else:
            self.p[px] = self.p[py]
            self.size[py] += self.size[px]

```

1.8 Dsu

```

struct DSU {
    vector<int> ps;
    vector<int> size;
    DSU(int N) : ps(N + 1), size(N + 1, 1) { iota(ps.begin(), ps.end(), 0); }
    int find_set(int x) { return ps[x] == x ? x : ps[x] = find_set(ps[x]); }
    bool same_set(int x, int y) { return find_set(x) == find_set(y); }
    void union_set(int x, int y) {
        if (same_set(x, y)) return;

```

```

        int px = find_set(x);
        int py = find_set(y);

        if (size[px] < size[py]) swap(px, py);

        ps[py] = px;
        size[px] += size[py];
    }
};

```

1.9 Sparse Table Rmq

```

/*
    Sparse table implementation for rmq.
    build: O(NlogN)
    query: O(1)
*/

int fastlog2(ll x) {
    ull i = x;
    return i ? __builtin_clzll(1) - __builtin_clzll(i) : -1;
}

template <typename T>
class SparseTable {
public:
    int N;
    int K;
    vector<vector<T>> st;
    SparseTable(vector<T> vs)
        : N((int)vs.size()), K(fastlog2(N) + 1), st(K + 1, vector<T>(N + 1)) {
        copy(vs.begin(), vs.end(), st[0].begin());

        for (int i = 1; i <= K; ++i)
            for (int j = 0; j + (1 << i) <= N; ++j)
                st[i][j] = min(st[i - 1][j], st[i - 1][j + (1 << (i - 1))]);
    }

    T RMQ(int l, int r) { // [l, r], 0 indexed
        int i = fastlog2(r - l + 1);
        return min(st[i][l], st[i][r - (1 << i) + 1]);
    }
};

```

2 Graphs

2.1 Scc Nodes (kosajaru)

```

/*
    * O(n+m)
    * Returns a pair <a, b>
    *     a: number of SCCs
    *     b: vector of size n, where b[i] is the SCC id of node i
    */
void dfs(ll u, vchar &visited, const vll2d &g, vll &scc, bool buildScc, ll id,
        vll &sccid) {
    visited[u] = true;
    sccid[u] = id;
    for (auto &v : g[u])
        if (!visited[v]) dfs(v, visited, g, scc, buildScc, id, sccid);

```

```

    // if it's the first pass, add the node to the scc
    if (buildScc) scc.eb(u);
}

pair<ll, vll> kosajaru(vll2d &g) {
    ll n = len(g);
    vll scc;
    vchar vis(n);
    vll sccid(n);
    for (ll i = 0; i < n; i++)
        if (!vis[i]) dfs(i, vis, g, scc, true, 0, sccid);

    // build the transposed graph
    vll2d gt(n);
    for (int i = 0; i < n; ++i)
        for (auto &v : g[i]) gt[v].eb(i);

    // run the dfs on the previous scc order
    ll id = 1;
    vis.assign(n, false);
    for (ll i = len(scc) - 1; i >= 0; i--)
        if (!vis[scc[i]]) {
            dfs(scc[i], vis, gt, scc, false, id++, sccid);
        }
    return {id - 1, sccid};
}

```

2.2 2 Sat (struct)

```

struct SAT2 {
    ll n;
    vll2d adj, adj_t;
    vc used;
    vll order, comp;
    vc assignment;
    bool solvable;
    SAT2(ll _n)
        : n(2 * _n),
          adj(n),
          adj_t(n),
          used(n),
          order(n),
          comp(n, -1),
          assignment(n / 2) {}
    void dfs1(int v) {
        used[v] = true;
        for (int u : adj[v]) {
            if (!used[u]) dfs1(u);
        }
        order.push_back(v);
    }

    void dfs2(int v, int c1) {
        comp[v] = c1;
        for (int u : adj_t[v]) {
            if (comp[u] == -1) dfs2(u, c1);
        }
    }
}

```

```

}

bool solve_2SAT() {
    // find and label each SCC
    for (int i = 0; i < n; ++i) {
        if (!used[i]) dfs1(i);
    }
    reverse(all(order));
    ll j = 0;
    for (auto &v : order) {
        if (comp[v] == -1) dfs2(v, j++);
    }

    assignment.assign(n / 2, false);
    for (int i = 0; i < n; i += 2) {
        // x and !x belong to the same SCC
        if (comp[i] == comp[i + 1]) {
            solvable = false;
            return false;
        }

        assignment[i / 2] = comp[i] > comp[i + 1];
    }
    solvable = true;
    return true;
}

```

```

void add_disjunction(int a, bool na, int b, bool nb) {
    a = (2 * a) ^ na;
    b = (2 * b) ^ nb;
    int neg_a = a ^ 1;
    int neg_b = b ^ 1;
    adj[neg_a].push_back(b);
    adj[neg_b].push_back(a);
    adj_t[b].push_back(neg_a);
    adj_t[a].push_back(neg_b);
}
};

```

2.3 Floyd Warshall

```

vector<vll> floyd_warshall(const vector<vll> &adj, ll n) {
    auto dist = adj;

    for (int i = 0; i < n; ++i) {
        for (int j = 0; j < n; ++j) {
            for (int k = 0; k < n; ++k) {
                dist[j][k] = min(dist[j][k], dist[j][i] + dist[i][k]);
            }
        }
    }
    return dist;
}

```

2.4 Topological Sorting

```

/*
 * O(V)

```

```

* assumes:
*     * vertices have index [0, n-1]
* if is a DAG:
*     * returns a topological sorting
* else:
*     * returns an empty vector
* */
enum class state { not_visited, processing, done };
bool dfs(const vector<vll> &adj, ll s, vector<state> &states, vll &order) {
    states[s] = state::processing;
    for (auto &v : adj[s]) {
        if (states[v] == state::not_visited) {
            if (not dfs(adj, v, states, order)) return false;
        } else if (states[v] == state::processing)
            return false;
    }
    states[s] = state::done;
    order.pb(s);
    return true;
}
vll topologicalSorting(const vector<vll> &adj) {
    ll n = len(adj);
    vll order;
    vector<state> states(n, state::not_visited);
    for (int i = 0; i < n; ++i) {
        if (states[i] == state::not_visited) {
            if (not dfs(adj, i, states, order)) return {};
        }
    }
    reverse(all(order));
    return order;
}

```

2.5 Lowest Common Ancestor Sparse Table

```

int fastlog2(ll x) {
    ull i = x;
    return i ? __builtin_clzll(1) - __builtin_clzll(i) : -1;
}
template <typename T>
class SparseTable {
public:
    int N;
    int K;
    vector<vector<T>> st;
    SparseTable(vector<T> vs)
        : N((int)vs.size()), K(fastlog2(N) + 1), st(K + 1, vector<T>(N + 1)) {
        copy(vs.begin(), vs.end(), st[0].begin());

        for (int i = 1; i <= K; ++i)
            for (int j = 0; j + (1 << i) <= N; ++j)
                st[i][j] = min(st[i - 1][j], st[i - 1][j + (1 << (i - 1))]);
    }
    SparseTable() {}
    T RMQ(int l, int r) {
        int i = fastlog2(r - l + 1);
        return min(st[i][l], st[i][r - (1 << i) + 1]);
    }
}

```

```

};
class LCA {
public:
    int p;
    int n;
    vi first;
    vector<char> visited;
    vi vertices;
    vi height;
    SparseTable<int> st;

    LCA(const vector<vi> &g)
        : p(0), n((int)g.size()), first(n + 1), visited(n + 1, 0), height(n + 1) {
        build_dfs(g, 1, 1);
        st = SparseTable<int>(vertices);
    }

    void build_dfs(const vector<vi> &g, int u, int hi) {
        visited[u] = true;
        height[u] = hi;
        first[u] = vertices.size();
        vertices.push_back(u);
        for (auto uv : g[u]) {
            if (!visited[uv]) {
                build_dfs(g, uv, hi + 1);
                vertices.push_back(u);
            }
        }
    }

    int lca(int a, int b) {
        int l = min(first[a], first[b]);
        int r = max(first[a], first[b]);
        return st.RMQ(l, r);
    }
};

```

2.6 Count Scc (kosajaru)

```

void dfs(ll u, vchar &visited, const vll2d &g, vll &scc, bool buildScc) {
    visited[u] = true;
    for (auto &v : g[u])
        if (!visited[v]) dfs(v, visited, g, scc, buildScc);

    // if it's the first pass, add the node to the scc
    if (buildScc) scc.pb(u);
}

ll kosajaru(vll2d &g) {
    ll n = len(g);
    vll scc;
    vchar vis(n);
    for (ll i = 0; i < n; i++)
        if (!vis[i]) dfs(i, vis, g, scc, true);

    // build the transposed graph
    vll2d gt(n);
    for (int i = 0; i < n; ++i)

```

```

    for (auto &v : g[i]) gt[v].eb(i);

// run the dfs on the previous scc order
ll scccnt = 0;
vis.assign(n, false);
for (ll i = len(scc) - 1; i >= 0; i--)
    if (!vis[scc[i]]) dfs(scc[i], vis, gt, scc, false), scccnt++;
return scccnt;
}

```

2.7 Kruskal (Python)

```

class DSU:
    def __init__(self, n):
        self.n = n
        self.p = [x for x in range(0, n + 1)]
        self.size = [0 for i in range(0, n + 1)]

    def find_set(self, x):
        if self.p[x] == x:
            return x
        else:
            self.p[x] = self.find_set(self.p[x])
            return self.p[x]

    def same_set(self, x, y):
        return bool(self.find_set(x) == self.find_set(y))

    def union_set(self, x, y):
        px = self.find_set(x)
        py = self.find_set(y)

        if px == py:
            return

        size_x = self.size[px]
        size_y = self.size[py]

        if size_x > size_y:
            self.p[py] = self.p[px]
            self.size[px] += self.size[py]
        else:
            self.p[px] = self.p[py]
            self.size[py] += self.size[px]

def kruskal(gv, n):
    """
    Receives te list of edges as a list of tuple in the form:
        d, u, v
        d: distance between u and v
    And also n as the total of verties.
    """
    dsu = DSU(n)

    c = 0
    for e in gv:
        d, u, v = e

```

```

        if not dsu.same_set(u, v):
            c += d
            dsu.union_set(u, v)

    return c

```

2.8 Scc (struct)

```

struct SCC {
    ll N;
    vll2d adj, tadj;
    vll todo, comps, comp;
    vector<set<ll>> sccadj;
    vchar vis;
    SCC(ll _N) : N(_N), adj(_N), tadj(_N), comp(_N, -1), sccadj(_N), vis(_N) {}

    void add_edge(ll x, ll y) { adj[x].eb(y), tadj[y].eb(x); }

    void dfs(ll x) {
        vis[x] = 1;
        for (auto &y : adj[x])
            if (!vis[y]) dfs(y);
        todo.pb(x);
    }

    void dfs2(ll x, ll v) {
        comp[x] = v;
        for (auto &y : tadj[x])
            if (comp[y] == -1) dfs2(y, v);
    }

    void gen() {
        for (ll i = 0; i < N; ++i)
            if (!vis[i]) dfs(i);
        reverse(all(todo));
        for (auto &x : todo)
            if (comp[x] == -1) {
                dfs2(x, x);
                comps.pb(x);
            }
    }

    void genSCCGraph() {
        for (ll i = 0; i < N; ++i) {
            for (auto &j : adj[i]) {
                if (comp[i] != comp[j]) {
                    sccadj[comp[i]].insert(comp[j]);
                }
            }
        }
    }
};

```

2.9 Check Bipartite

```

// O(V)
bool checkBipartite(const ll n, const vector<vll> &adj) {
    ll s = 0;
    queue<ll> q;
    q.push(s);

```



```

vll color(n, INF);
color[s] = 0;
bool isBipartite = true;
while (!q.empty() && isBipartite) {
    ll u = q.front();
    q.pop();
    for (auto &v : adj[u]) {
        if (color[v] == INF) {
            color[v] = 1 - color[u];
            q.push(v);
        } else if (color[v] == color[u]) {
            return false;
        }
    }
}
return true;
}

```

2.10 Dijkstra

```

ll __inf = LLONG_MAX >> 5;
vll dijkstra(const vector<vector<pll>> &g, ll n) {
    priority_queue<pll, vector<pll>, greater<pll>> pq;
    vll dist(n, __inf);
    vector<char> vis(n);
    pq.emplace(0, 0);
    dist[0] = 0;
    while (!pq.empty()) {
        auto [d1, v] = pq.top();
        pq.pop();
        if (vis[v]) continue;
        vis[v] = true;

        for (auto [d2, u] : g[v]) {
            if (dist[u] > d1 + d2) {
                dist[u] = d1 + d2;
                pq.emplace(dist[u], u);
            }
        }
    }
    return dist;
}

```

3 Extras

3.1 Binary To Gray

```

string binToGray(string bin) {
    string gray(bin.size(), '0');
    int n = bin.size() - 1;
    gray[0] = bin[0];
    for (int i = 1; i <= n; i++) {
        gray[i] = '0' + (bin[i - 1] == '1') ^ (bin[i] == '1');
    }
    return gray;
}

```

3.2 Bigint

```

const int maxn = 1e2 + 14, lg = 15;
const int base = 1000000000;
const int base_digits = 9;
struct bigint {
    vector<int> a;
    int sign;

    int size() {
        if (a.empty()) return 0;
        int ans = (a.size() - 1) * base_digits;
        int ca = a.back();
        while (ca) ans++, ca /= 10;
        return ans;
    }

    bigint operator^(const bigint &v) {
        bigint ans = 1, a = *this, b = v;
        while (!b.isZero()) {
            if (b % 2) ans *= a;
            a *= a, b /= 2;
        }
        return ans;
    }

    string to_string() {
        stringstream ss;
        ss << *this;
        string s;
        ss >> s;
        return s;
    }

    int sumof() {
        string s = to_string();
        int ans = 0;
        for (auto c : s) ans += c - '0';
        return ans;
    }

    /*</arpa>*/
    bigint() : sign(1) {}

    bigint(long long v) { *this = v; }

    bigint(const string &s) { read(s); }

    void operator=(const bigint &v) {
        sign = v.sign;
        a = v.a;
    }

    void operator=(long long v) {
        sign = 1;
        a.clear();
        if (v < 0) sign = -1, v = -v;
        for (; v > 0; v = v / base) a.push_back(v % base);
    }

    bigint operator+(const bigint &v) const {
        if (sign == v.sign) {

```

```

bigint res = v;

for (int i = 0, carry = 0; i < (int)max(a.size(), v.a.size()) || carry; ++i) {
    if (i == (int)res.a.size()) res.a.push_back(0);
    res.a[i] += carry + (i < (int)a.size() ? a[i] : 0);
    carry = res.a[i] >= base;
    if (carry) res.a[i] -= base;
}
return res;
}
return *this - (-v);
}

bigint operator-(const bigint &v) const {
    if (sign == v.sign) {
        if (abs() >= v.abs()) {
            bigint res = *this;
            for (int i = 0, carry = 0; i < (int)v.a.size() || carry; ++i) {
                res.a[i] -= carry + (i < (int)v.a.size() ? v.a[i] : 0);
                carry = res.a[i] < 0;
                if (carry) res.a[i] += base;
            }
            res.trim();
            return res;
        }
        return -(v - *this);
    }
    return *this + (-v);
}

void operator*=(int v) {
    if (v < 0) sign = -sign, v = -v;
    for (int i = 0, carry = 0; i < (int)a.size() || carry; ++i) {
        if (i == (int)a.size()) a.push_back(0);
        long long cur = a[i] * (long long)v + carry;
        carry = (int)(cur / base);
        a[i] = (int)(cur % base);
        // asm("divl %%ecx" : "=a"(carry), "=d"(a[i]) :
        // "A"(cur), "c"(base));
    }
    trim();
}

bigint operator*(int v) const {
    bigint res = *this;
    res *= v;
    return res;
}

void operator*=(long long v) {
    if (v < 0) sign = -sign, v = -v;
    if (v > base) {
        *this = *this * (v / base) * base + *this * (v % base);
        return;
    }
    for (int i = 0, carry = 0; i < (int)a.size() || carry; ++i) {
        if (i == (int)a.size()) a.push_back(0);

```

```

        long long cur = a[i] * (long long)v + carry;
        carry = (int)(cur / base);
        a[i] = (int)(cur % base);
        // asm("divl %%ecx" : "=a"(carry), "=d"(a[i]) :
        // "A"(cur), "c"(base));
    }
    trim();
}

bigint operator*(long long v) const {
    bigint res = *this;
    res *= v;
    return res;
}

friend pair<bigint, bigint> divmod(const bigint &a1, const bigint &b1) {
    int norm = base / (b1.a.back() + 1);
    bigint a = a1.abs() * norm;
    bigint b = b1.abs() * norm;
    bigint q, r;
    q.a.resize(a.a.size());

    for (int i = a.a.size() - 1; i >= 0; i--) {
        r *= base;
        r += a.a[i];
        int s1 = r.a.size() <= b.a.size() ? 0 : r.a[b.a.size()];
        int s2 = r.a.size() <= b.a.size() - 1 ? 0 : r.a[b.a.size() - 1];
        int d = ((long long)base * s1 + s2) / b.a.back();
        r -= b * d;
        while (r < 0) r += b, --d;
        q.a[i] = d;
    }

    q.sign = a1.sign * b1.sign;
    r.sign = a1.sign;
    q.trim();
    r.trim();
    return make_pair(q, r / norm);
}

bigint operator/(const bigint &v) const { return divmod(*this, v).first; }

bigint operator%(const bigint &v) const { return divmod(*this, v).second; }

void operator/=(int v) {
    if (v < 0) sign = -sign, v = -v;
    for (int i = (int)a.size() - 1, rem = 0; i >= 0; --i) {
        long long cur = a[i] + rem * (long long)base;
        a[i] = (int)(cur / v);
        rem = (int)(cur % v);
    }
    trim();
}

bigint operator/(int v) const {
    bigint res = *this;
    res /= v;
    return res;
}

```

```

}

int operator%(int v) const {
    if (v < 0) v = -v;
    int m = 0;
    for (int i = a.size() - 1; i >= 0; --i)
        m = (a[i] + m * (long long)base) % v;
    return m * sign;
}

void operator+=(const bigint &v) { *this = *this + v; }
void operator-=(const bigint &v) { *this = *this - v; }
void operator*=(const bigint &v) { *this = *this * v; }
void operator/=(const bigint &v) { *this = *this / v; }

bool operator<(const bigint &v) const {
    if (sign != v.sign) return sign < v.sign;
    if (a.size() != v.a.size()) return a.size() * sign < v.a.size() * v.sign;
    for (int i = a.size() - 1; i >= 0; i--)
        if (a[i] != v.a[i]) return a[i] * sign < v.a[i] * v.sign;
    return false;
}

bool operator>(const bigint &v) const { return v < *this; }
bool operator<=(const bigint &v) const { return !(v < *this); }
bool operator>=(const bigint &v) const { return !(*this < v); }
bool operator==(const bigint &v) const {
    return !(*this < v) && !(v < *this);
}

bool operator!=(const bigint &v) const { return *this < v || v < *this; }

void trim() {
    while (!a.empty() && !a.back()) a.pop_back();
    if (a.empty()) sign = 1;
}

bool isZero() const { return a.empty() || (a.size() == 1 && !a[0]); }

bigint operator-() const {
    bigint res = *this;
    res.sign = -sign;
    return res;
}

bigint abs() const {
    bigint res = *this;
    res.sign *= res.sign;
    return res;
}

long long longValue() const {
    long long res = 0;
    for (int i = a.size() - 1; i >= 0; i--) res = res * base + a[i];
    return res * sign;
}

friend bigint gcd(const bigint &a, const bigint &b) {
    return b.isZero() ? a : gcd(b, a % b);
}

```

```

}

friend bigint lcm(const bigint &a, const bigint &b) {
    return a / gcd(a, b) * b;
}

void read(const string &s) {
    sign = 1;
    a.clear();
    int pos = 0;
    while (pos < (int)s.size() && (s[pos] == '-' || s[pos] == '+')) {
        if (s[pos] == '-') sign = -sign;
        ++pos;
    }
    for (int i = s.size() - 1; i >= pos; i -= base_digits) {
        int x = 0;
        for (int j = max(pos, i - base_digits + 1); j <= i; j++)
            x = x * 10 + s[j] - '0';
        a.push_back(x);
    }
    trim();
}

friend istream &operator>>(istream &stream, bigint &v) {
    string s;
    stream >> s;
    v.read(s);
    return stream;
}

friend ostream &operator<<(ostream &stream, const bigint &v) {
    if (v.sign == -1) stream << '-';
    stream << (v.a.empty() ? 0 : v.a.back());
    for (int i = (int)v.a.size() - 2; i >= 0; --i)
        stream << setw(base_digits) << setfill('0') << v.a[i];
    return stream;
}

static vector<int> convert_base(const vector<int> &a, int old_digits,
                                int new_digits) {
    vector<long long> p(max(old_digits, new_digits) + 1);
    p[0] = 1;
    for (int i = 1; i < (int)p.size(); i++) p[i] = p[i - 1] * 10;
    vector<int> res;
    long long cur = 0;
    int cur_digits = 0;
    for (int i = 0; i < (int)a.size(); i++) {
        cur += a[i] * p[cur_digits];
        cur_digits += old_digits;
        while (cur_digits >= new_digits) {
            res.push_back((int)(cur % p[new_digits]));
            cur /= p[new_digits];
            cur_digits -= new_digits;
        }
    }
    res.push_back((int)cur);
    while (!res.empty() && !res.back()) res.pop_back();
    return res;
}

```

```

typedef vector<long long> vll;

static vll karatsubaMultiply(const vll &a, const vll &b) {
    int n = a.size();
    vll res(n + n);
    if (n <= 32) {
        for (int i = 0; i < n; i++)
            for (int j = 0; j < n; j++) res[i + j] += a[i] * b[j];
        return res;
    }

    int k = n >> 1;
    vll a1(a.begin(), a.begin() + k);
    vll a2(a.begin() + k, a.end());
    vll b1(b.begin(), b.begin() + k);
    vll b2(b.begin() + k, b.end());

    vll a1b1 = karatsubaMultiply(a1, b1);
    vll a2b2 = karatsubaMultiply(a2, b2);

    for (int i = 0; i < k; i++) a2[i] += a1[i];
    for (int i = 0; i < k; i++) b2[i] += b1[i];

    vll r = karatsubaMultiply(a2, b2);
    for (int i = 0; i < (int)a1b1.size(); i++) r[i] -= a1b1[i];
    for (int i = 0; i < (int)a2b2.size(); i++) r[i] -= a2b2[i];

    for (int i = 0; i < (int)r.size(); i++) res[i + k] += r[i];
    for (int i = 0; i < (int)a1b1.size(); i++) res[i] += a1b1[i];
    for (int i = 0; i < (int)a2b2.size(); i++) res[i + n] += a2b2[i];
    return res;
}

bigint operator*(const bigint &v) const {
    vector<int> a6 = convert_base(this->a, base_digits, 6);
    vector<int> b6 = convert_base(v.a, base_digits, 6);
    vll a(a6.begin(), a6.end());
    vll b(b6.begin(), b6.end());
    while (a.size() < b.size()) a.push_back(0);
    while (b.size() < a.size()) b.push_back(0);
    while (a.size() & (a.size() - 1)) a.push_back(0), b.push_back(0);
    vll c = karatsubaMultiply(a, b);
    bigint res;
    res.sign = sign * v.sign;
    for (int i = 0, carry = 0; i < (int)c.size(); i++) {
        long long cur = c[i] + carry;
        res.a.push_back((int)(cur % 1000000));
        carry = (int)(cur / 1000000);
    }
    res.a = convert_base(res.a, 6, base_digits);
    res.trim();
    return res;
}
};

```

3.3 Get Permutation Cicles

```

/*
 * receives a permutation [0, n-1]
 * returns a vector of cicles
 * for example: [ 1, 0, 3, 4, 2] -> [[0, 1], [2, 3, 4]]
 */
vector<vll> getPermutationCicles(const vll &ps) {
    ll n = len(ps);
    vector<char> visited(n);
    vector<vll> cicles;
    for (int i = 0; i < n; ++i) {
        if (visited[i]) continue;

        vll cicle;
        ll pos = i;
        while (!visited[pos]) {
            cicle.pb(pos);
            visited[pos] = true;
            pos = ps[pos];
        }

        cicles.push_back(vll(all(cicle)));
    }
    return cicles;
}

```

4 Dynamic programming

4.1 Edit Distance

```

int edit_distance(const string &a, const string &b) {
    int n = a.size();
    int m = b.size();
    vector<vi> dp(n + 1, vi(m + 1, 0));

    int ADD = 1, DEL = 1, CHG = 1;
    for (int i = 0; i <= n; ++i) {
        dp[i][0] = i * DEL;
    }
    for (int i = 1; i <= m; ++i) {
        dp[0][i] = ADD * i;
    }

    for (int i = 1; i <= n; ++i) {
        for (int j = 1; j <= m; ++j) {
            int add = dp[i][j - 1] + ADD;
            int del = dp[i - 1][j] + DEL;
            int chg = dp[i - 1][j - 1] + (a[i - 1] == b[j - 1] ? 0 : 1) * CHG;
            dp[i][j] = min({add, del, chg});
        }
    }

    return dp[n][m];
}

```

4.2 Money Sum Bottom Up

/*

```

    find every possible sum using
    the given values only once.
*/
set<int> money_sum(const vi &xs) {
    using vc = vector<char>;
    using vvc = vector<vc>;
    int _m = accumulate(all(xs), 0);
    int _n = xs.size();
    vvc _dp(_n + 1, vc(_m + 1, 0));
    set<int> _ans;
    _dp[0][xs[0]] = 1;
    for (int i = 1; i < _n; ++i) {
        for (int j = 0; j <= _m; ++j) {
            if (j == 0 or _dp[i - 1][j]) {
                _dp[i][j + xs[i]] = 1;
                _dp[i][j] = 1;
            }
        }
    }

    for (int i = 0; i < _n; ++i)
        for (int j = 0; j <= _m; ++j)
            if (_dp[i][j]) _ans.insert(j);
    return _ans;
}

```

4.3 Knapsack Dp Values 01

```

const int MAX_N = 1001;
const int MAX_S = 100001;
array<array<int, MAX_S>, MAX_N> dp;
bool check[MAX_N][MAX_S];
pair<int, vi> knapsack(int S, const vector<pii> &xs) {
    int N = (int)xs.size();

    for (int i = 0; i <= N; ++i) dp[i][0] = 0;

    for (int m = 0; m <= S; ++m) dp[0][m] = 0;

    for (int i = 1; i <= N; ++i) {
        for (int m = 1; m <= S; ++m) {
            dp[i][m] = dp[i - 1][m];
            check[i][m] = false;

            auto [w, v] = xs[i - 1];

            if (w <= m and (dp[i - 1][m - w] + v) >= dp[i][m]) {
                dp[i][m] = dp[i - 1][m - w] + v;
                check[i][m] = true;
            }
        }
    }

    int m = S;
    vi es;

    for (int i = N; i >= 1; --i) {
        if (check[i][m]) {

```

```

            es.push_back(i);
            m -= xs[i - 1].first;
        }
    }

    reverse(es.begin(), es.end());

    return {dp[N][S], es};
}

```

4.4 Tsp

```

using vi = vector<int>;
vector<vi> dist;
vector<vi> memo;
/* 0 ( N^2 * 2^N ) */
int tsp(int i, int mask, int N) {
    if (mask == (1 << N) - 1) return dist[i][0];
    if (memo[i][mask] != -1) return memo[i][mask];
    int ans = INT_MAX << 1;
    for (int j = 0; j < N; ++j) {
        if (mask & (1 << j)) continue;
        auto t = tsp(j, mask | (1 << j), N) + dist[i][j];
        ans = min(ans, t);
    }
    return memo[i][mask] = ans;
}

```

5 Trees

5.1 Binary Lifting

```

/*
 * far[h][i] = the node that 2^h far from node i
 * sometimes is useful invert the order of loops
 * time : O(nlogn)
 * */
const int maxlog = 20;
int far[maxlog + 1][n + 1];
int n;
for (int h = 1; h <= maxlog; h++) {
    for (int i = 1; i <= n; i++) {
        far[h][i] = far[h - 1][far[h - 1][i]];
    }
}

```

5.2 Maximum Distances

```

/*
 * Returns the maximum distance from every node to any other node in the tree.
 * */
pll mostDistantFrom(const vector<vll> &adj, ll n, ll root) {
    // 0 indexed
    ll mostDistantNode = root;
    ll nodeDistance = 0;
    queue<pll> q;

```

```

vector<char> vis(n);
q.emplace(root, 0);
vis[root] = true;
while (!q.empty()) {
    auto [node, dist] = q.front();
    q.pop();
    if (dist > nodeDistance) {
        nodeDistance = dist;
        mostDistantNode = node;
    }
    for (auto u : adj[node]) {
        if (!vis[u]) {
            vis[u] = true;
            q.emplace(u, dist + 1);
        }
    }
}
return {mostDistantNode, nodeDistance};
}

ll twoNodesDist(const vector<vll> &adj, ll n, ll a, ll b) {
    queue<pll> q;
    vector<char> vis(n);
    q.emplace(a, 0);
    while (!q.empty()) {
        auto [node, dist] = q.front();
        q.pop();
        if (node == b) return dist;
        for (auto u : adj[node]) {
            if (!vis[u]) {
                vis[u] = true;
                q.emplace(u, dist + 1);
            }
        }
    }
    return -1;
}

tuple<ll, ll, ll> tree_diameter(const vector<vll> &adj, ll n) {
    // returns two points of the diameter and the diameter itself
    auto [node1, dist1] = mostDistantFrom(adj, n, 0);
    auto [node2, dist2] = mostDistantFrom(adj, n, node1);
    auto diameter = twoNodesDist(adj, n, node1, node2);
    return make_tuple(node1, node2, diameter);
}

vll everyDistanceFromNode(const vector<vll> &adj, ll n, ll root) {
    // Single Source Shortest Path, from a given root
    queue<pair<ll, ll>> q;
    vll ans(n, -1);
    ans[root] = 0;
    q.emplace(root, 0);
    while (!q.empty()) {
        auto [u, d] = q.front();
        q.pop();

        for (auto w : adj[u]) {
            if (ans[w] != -1) continue;

```

```

            ans[w] = d + 1;
            q.emplace(w, d + 1);
        }
    }
    return ans;
}

vll maxDistances(const vector<vll> &adj, ll n) {
    auto [node1, node2, diameter] = tree_diameter(adj, n);
    auto distances1 = everyDistanceFromNode(adj, n, node1);
    auto distances2 = everyDistanceFromNode(adj, n, node2);
    vll ans(n);
    for (int i = 0; i < n; ++i) ans[i] = max(distances1[i], distances2[i]);
    return ans;
}

```

5.3 Tree Diameter

```

pll mostDistantFrom(const vector<vll> &adj, ll n, ll root) {
    // 0 indexed
    ll mostDistantNode = root;
    ll nodeDistance = 0;
    queue<pll> q;
    vector<char> vis(n);
    q.emplace(root, 0);
    vis[root] = true;
    while (!q.empty()) {
        auto [node, dist] = q.front();
        q.pop();
        if (dist > nodeDistance) {
            nodeDistance = dist;
            mostDistantNode = node;
        }
        for (auto u : adj[node]) {
            if (!vis[u]) {
                vis[u] = true;
                q.emplace(u, dist + 1);
            }
        }
    }
    return {mostDistantNode, nodeDistance};
}

ll twoNodesDist(const vector<vll> &adj, ll n, ll a, ll b) {
    // 0 indexed
    queue<pll> q;
    vector<char> vis(n);
    q.emplace(a, 0);
    while (!q.empty()) {
        auto [node, dist] = q.front();
        q.pop();
        if (node == b) {
            return dist;
        }
        for (auto u : adj[node]) {
            if (!vis[u]) {
                vis[u] = true;
                q.emplace(u, dist + 1);
            }
        }
    }
}

```

```

    }
}
return -1;
}
ll tree_diameter(const vector<vll> &adj, ll n) {
    // 0 indexed !!!
    auto [node1, dist1] = mostDistantFrom(adj, n, 0);
    auto [node2, dist2] = mostDistantFrom(adj, n, node1);
    auto diameter = twoNodesDist(adj, n, node1, node2);
    return diameter;
}

```

6 Searching

6.1 Ternary Search Recursive

```

const double eps = 1e-6;

// IT MUST BE AN UNIMODAL FUNCTION
double f(int x) { return x * x + 2 * x + 4; }

double ternary_search(double l, double r) {
    if (fabs(f(l) - f(r)) < eps) return f((l + (r - l) / 2.0));

    auto third = (r - l) / 3.0;
    auto m1 = l + third;
    auto m2 = r - third;

    // change the signal to find the maximum point.
    return m1 < m2 ? ternary_search(m1, r) : ternary_search(l, m2);
}

```

7 Math

7.1 Power Sum

```

// calculates K^0 + K^1 ... + K^n
ll fastpow(ll a, int n) {
    if (n == 1) return a;
    ll x = fastpow(a, n / 2);
    return x * x * (n & 1 ? a : 1);
}
ll powersum(ll n, ll k) { return (fastpow(n, k + 1) - 1) / (n - 1); }

```

7.2 Sieve List Primes

```

// list every prime until MAXN
const ll MAXN = 1e5;
vll list_primes(ll n) { // Nlog * log N
    vll ps;
    bitset<MAXN> sieve;
    sieve.set();
    sieve.reset(1);
    for (ll i = 2; i <= n; ++i) {
        if (sieve[i]) ps.push_back(i);
    }
}

```

```

    for (ll j = i * 2; j <= n; j += i) {
        sieve.reset(j);
    }
}
return ps;
}

```

7.3 Factorial

```

const ll MAX = 18;
vll fv(MAX, -1);
ll factorial(ll n) {
    if (fv[n] != -1) return fv[n];
    if (n == 0) return 1;
    return n * factorial(n - 1);
}

```

7.4 Permutation Count

```

const ll MAX = 18;
vll fv(MAX, -1);
ll factorial(ll n) {
    if (fv[n] != -1) return fv[n];
    if (n == 0) return 1;
    return n * factorial(n - 1);
}

```

```

template <typename T>
ll permutation_count(vector<T> xs) {
    map<T, ll> h;
    for (auto xi : xs) h[xi]++;
    ll ans = factorial((ll)xs.size());
    dbg(ans);
    for (auto [v, cnt] : h) {
        dbg(cnt);
        ans /= cnt;
    }

    return ans;
}

```

7.5 N Choose K Count

```

/*
 * O(nm) time, O(m) space
 * equal to n choose k
 * */
ll binom(ll n, ll k) {
    if (k > n) return 0;
    vll dp(k + 1, 0);
    dp[0] = 1;
    for (ll i = 1; i <= n; i++)
        for (ll j = k; j > 0; j--) dp[j] = dp[j] + dp[j - 1];
    return dp[k];
}

```

7.6 Gcd Using Factorization

```
// O(sqrt(n))
map<ll, ll> factorization(ll n) {
    map<ll, ll> ans;
    for (ll i = 2; i * i <= n; i++) {
        ll count = 0;
        for (; n % i == 0; count++, n /= i)
            ;
        if (count) ans[i] = count;
    }
    if (n > 1) ans[n]++;
    return ans;
}

ll gcd_with_factorization(ll a, ll b) {
    map<ll, ll> fa = factorization(a);
    map<ll, ll> fb = factorization(b);
    ll ans = 1;
    for (auto fai : fa) {
        ll k = min(fai.second, fb[fai.first]);
        while (k--) ans *= fai.first;
    }
    return ans;
}
```

7.7 Is Prime

```
bool isprime(ll n) { // O(sqrt(n))
    if (n < 2) return false;
    if (n == 2) return true;
    if (n % 2 == 0) return false;
    for (ll i = 3; i * i < n; i += 2)
        if (n % i == 0) return false;
    return true;
}
```

7.8 Fast Exp

```
/*
    Fast exponentiation algorithm,
    compute a^n in O(log(n))
*/
ll fexp(ll a, int n) {
    if (n == 0) return 1;
    if (n == 1) return a;
    ll x = fexp(a, n / 2);
    return x * x * (n & 1 ? a : 1);
}
```

7.9 Lcm Using Factorization

```
map<ll, ll> factorization(ll n) {
    map<ll, ll> ans;
    for (ll i = 2; i * i <= n; i++) {
        ll count = 0;
        for (; n % i == 0; count++, n /= i)
            ;
        if (count) ans[i] = count;
    }
}
```

```

    }
    if (n > 1) ans[n]++;
    return ans;
}

ll lcm_with_factorization(ll a, ll b) {
    map<ll, ll> fa = factorization(a);
    map<ll, ll> fb = factorization(b);
    ll ans = 1;
    for (auto fai : fa) {
        ll k = max(fai.second, fb[fai.first]);
        while (k--) ans *= fai.first;
    }
    return ans;
}
```

7.10 Euler Phi

```
const ll MAXN = 1e5;
vll list_primes(ll n) { // Nlog * log N
    vll ps;
    bitset<MAXN> sieve;
    sieve.set();
    sieve.reset(1);
    for (ll i = 2; i <= n; ++i) {
        if (sieve[i]) ps.push_back(i);
        for (ll j = i * 2; j <= n; j += i) {
            sieve.reset(j);
        }
    }
    return ps;
}

vector<p11> factorization(ll n, const vll &primes) {
    vector<p11> ans;
    for (auto &p : primes) {
        if (n == 1) break;
        ll cnt = 0;
        while (n % p == 0) {
            cnt++;
            n /= p;
        }
        if (cnt) ans.emplace_back(p, cnt);
    }
    return ans;
}

ll phi(ll n, vector<p11> factors) {
    if (n == 1) return 1;
    ll ans = n;

    for (auto [p, k] : factors) {
        ans /= p;
        ans *= (p - 1);
    }

    return ans;
}
```


7.11 Polynomial

```
using polynomial = vector<ll>;
int degree(const polynomial &xs) { return xs.size() - 1; }
ll horner_evaluate(const polynomial &xs, ll x) {
    ll ans = 0;
    ll n = degree(xs);
    for (int i = n; i >= 0; --i) {
        ans *= x;
        ans += xs[i];
    }
    return ans;
}

polynomial operator+(const polynomial &a, const polynomial &b) {
    int n = degree(a);
    int m = degree(b);
    polynomial r(max(n, m) + 1, 0);

    for (int i = 0; i <= n; ++i) r[i] += a[i];
    for (int j = 0; j <= m; ++j) r[j] += b[j];
    while (!r.empty() and r.back() == 0) r.pop_back();
    if (r.empty()) r.push_back(0);
    return r;
}

polynomial operator*(const polynomial &p, const polynomial &q) {
    int n = degree(p);
    int m = degree(q);
    polynomial r(n + m + 1, 0);
    for (int i = 0; i <= n; ++i)
        for (int j = 0; j <= m; ++j) r[i + j] += (p[i] * q[j]);
    return r;
}
```

7.12 Integer Mod

```
const ll INF = 1e18;
const ll mod = 998244353;
template <ll MOD = mod>
struct Modular {
    ll value;
    static const ll MOD_value = MOD;

    Modular(ll v = 0) {
        value = v % MOD;
        if (value < 0) value += MOD;
    }

    Modular(ll a, ll b) : value(0) {
        *this += a;
        *this /= b;
    }

    Modular& operator+=(Modular const& b) {
        value += b.value;
        if (value >= MOD) value -= MOD;
        return *this;
    }

    Modular& operator-=(Modular const& b) {
        value -= b.value;
```

```
        if (value < 0) value += MOD;
        return *this;
    }

    Modular& operator*=(Modular const& b) {
        value = (ll)value * b.value % MOD;
        return *this;
    }

    friend Modular mexp(Modular a, ll e) {
        Modular res = 1;
        while (e) {
            if (e & 1) res *= a;
            a *= a;
            e >>= 1;
        }
        return res;
    }

    friend Modular inverse(Modular a) { return mexp(a, MOD - 2); }

    Modular& operator/=(Modular const& b) { return *this *= inverse(b); }
    friend Modular operator+(Modular a, Modular const b) { return a += b; }
    Modular operator++(int) { return this->value = (this->value + 1) % MOD; }
    Modular operator++() { return this->value = (this->value + 1) % MOD; }
    friend Modular operator-(Modular a, Modular const b) { return a -= b; }
    friend Modular operator-(Modular const a) { return 0 - a; }
    Modular operator--(int) {
        return this->value = (this->value - 1 + MOD) % MOD;
    }

    Modular operator--() { return this->value = (this->value - 1 + MOD) % MOD; }
    friend Modular operator*(Modular a, Modular const b) { return a *= b; }
    friend Modular operator/(Modular a, Modular const b) { return a /= b; }
    friend std::ostream& operator<<(std::ostream& os, Modular const& a) {
        return os << a.value;
    }

    friend bool operator==(Modular const& a, Modular const& b) {
        return a.value == b.value;
    }

    friend bool operator!=(Modular const& a, Modular const& b) {
        return a.value != b.value;
    }
};
```

7.13 Count Divisors Memo

```
const ll mod = 1073741824;
const ll maxd = 100 * 100 * 100 + 1;
vector<ll> memo(maxd, -1);
ll countdivisors(ll x) {
    ll ox = x;
    ll ans = 1;
    for (ll i = 2; i <= x; ++i) {
        if (memo[x] != -1) {
            ans *= memo[x];
            break;
        }
        ll count = 0;
        while (x and x % i == 0) {
```

```

        x /= i;
        count++;
    }
    ans *= (count + 1);
}
memo[ox] = ans;
return ans;
}

```

7.14 Lcm

```

ll gcd(ll a, ll b) { return b ? gcd(b, a % b) : a; }
ll lcm(ll a, ll b) { return a / gcd(a, b) * b; }

```

7.15 Factorial Factorization

```

// O(logN) greater k that p^k | n
ll E(ll n, ll p) {
    ll k = 0, b = p;
    while (b <= n) {
        k += n / b;
        b *= p;
    }
    return k;
}

// list every prime until MAXN O(Nlog * log N)
const ll MAXN = 1e5;
vll list_primes(ll n) {
    vll ps;
    bitset<MAXN> sieve;
    sieve.set();
    sieve.reset(1);
    for (ll i = 2; i <= n; ++i) {
        if (sieve[i]) ps.push_back(i);
        for (ll j = i * 2; j <= n; j += i) sieve.reset(j);
    }
    return ps;
}

// O(pi(N)*logN)
map<ll, ll> factorial_factorization(ll n, const vll &primes) {
    map<ll, ll> fs;
    for (const auto &p : primes) {
        if (p > n) break;
        fs[p] = E(n, p);
    }
    return fs;
}

```

7.16 Factorization With Primes

```

// Nlog * log N
const ll MAXN = 1e5;
vll list_primes(ll n) {
    vll ps;
    bitset<MAXN> sieve;

```

```

    sieve.set();
    sieve.reset(1);
    for (ll i = 2; i <= n; ++i) {
        if (sieve[i]) ps.push_back(i);
        for (ll j = i * 2; j <= n; j += i) sieve.reset(j);
    }
    return ps;
}

```

```

// O(pi(sqrt(n)))
map<ll, ll> factorization(ll n, const vll &primes) {
    map<ll, ll> ans;
    for (auto p : primes) {
        if (p * p > n) break;
        ll count = 0;
        for (; n % p == 0; count++, n /= p)
            ;
        if (count) ans[p] = count;
    }
    return ans;
}

```

7.17 Modular Inverse Using Phi

```

map<ll, ll> factorization(ll n) {
    map<ll, ll> ans;
    for (ll i = 2; i * i <= n; i++) {
        ll count = 0;
        for (; n % i == 0; count++, n /= i)
            ;
        if (count) ans[i] = count;
    }
    if (n > 1) ans[n]++;
    return ans;
}

```

```

ll phi(ll n) {
    if (n == 1) return 1;

    auto fs = factorization(n);
    auto res = n;

    for (auto [p, k] : fs) {
        res /= p;
        res *= (p - 1);
    }

    return res;
}

```

```

ll fexp(ll a, ll n, ll mod) {
    if (n == 0) return 1;
    if (n == 1) return a;
    ll x = fexp(a, n / 2, mod);
    return x * x * (n & 1 ? a : 1) % mod;
}

```

```

ll inv(ll a, ll mod) { return fexp(a, phi(mod) - 1, mod); }

```

7.18 Factorization

```
// O(sqrt(n))
map<ll, ll> factorization(ll n) {
    map<ll, ll> ans;
    for (ll i = 2; i * i <= n; i++) {
        ll count = 0;
        for (; n % i == 0; count++, n /= i)
            ;
        if (count) ans[i] = count;
    }
    if (n > 1) ans[n]++;
    return ans;
}
```

7.19 Gcd

```
ll gcd(ll a, ll b) { return b ? gcd(b, a % b) : a; }
```

7.20 Combinatorics With Repetitions

```
void combinations_with_repetition(int n, int k,
                                   function<void(const vector<int> &)> process)
{
    vector<int> v(k, 1);
    int pos = k - 1;

    while (true) {
        process(v);

        v[pos]++;

        while (pos > 0 and v[pos] > n) {
            --pos;
            v[pos]++;
        }

        if (pos == 0 and v[pos] > n) break;

        for (int i = pos + 1; i < k; ++i) v[i] = v[pos];

        pos = k - 1;
    }
}
```

8 Strings

8.1 Rabin Karp

```
vi rabin_karp(string const &s, string const &t) {
    ll p = 31;
    ll m = 1e9 + 9;
    int S = s.size(), T = t.size();

    vll p_pow(max(S, T));
    p_pow[0] = 1;
```

```
    for (int i = 1; i < (int)p_pow.size(); i++) p_pow[i] = (p_pow[i - 1] * p) % m;

    vll h(T + 1, 0);
    for (int i = 0; i < T; i++)
        h[i + 1] = (h[i] + (t[i] - 'a' + 1) * p_pow[i]) % m;
    ll h_s = 0;
    for (int i = 0; i < S; i++) h_s = (h_s + (s[i] - 'a' + 1) * p_pow[i]) % m;

    vi occurrences;
    for (int i = 0; i + S - 1 < T; i++) {
        ll cur_h = (h[i + S] + m - h[i]) % m;
        // IT DON'T CONSIDERE CONLISIONS !
        if (cur_h == h_s * p_pow[i] % m) occurrences.push_back(i);
    }
    return occurrences;
}
```

8.2 Trie Naive

```
// time: O(n^2) memory: O(n^2)
using Node = map<char, int>;
using vi = vector<int>;
using Trie = vector<Node>;

Trie build(const string &s) {
    int n = (int)s.size();
    Trie trie(1);
    string suffix;

    for (int i = n - 1; i >= 0; --i) {
        suffix = s.substr(i) + '#';

        int v = 0; // root
        for (auto c : suffix) {
            if (c == '#') { // makrs the poistion of an occurence
                trie[v][c] = i;
                break;
            }
            if (trie[v][c])
                v = trie[v][c];
            else {
                trie.push_back({});
                trie[v][c] = trie.size() - 1;
                v = trie.size() - 1;
            }
        }
    }
    return trie;
}
```

```
vi search(Trie &trie, string s) {
    int p = 0;
    vi occ;
    for (auto &c : s) {
        p = trie[p][c];
        if (!p) return occ;
    }
}
```

```

queue<int> q;
q.push(0);
while (!q.empty()) {
    auto cur = q.front();
    q.pop();
    for (auto [c, v] : trie[cur]) {
        if (c == '#')
            occ.push_back(v);
        else
            q.push(v);
    }
}
return occ;
}

```

```

11 distinct_substr(const Trie &trie) {
    11 cnt = 0;
    queue<int> q;
    q.push(0);
    while (!q.empty()) {
        auto u = q.front();
        q.pop();

        for (auto [c, v] : trie[u]) {
            if (c != '#') {
                cnt++;
                q.push(v);
            }
        }
    }
    return cnt;
}

```

8.3 String Psum

```

struct strPsum {
    11 n;
    11 k;
    vector<vll> psum;
    strPsum(const string &s) : n(s.size()), k(100), psum(k, vll(n + 1)) {
        for (11 i = 1; i <= n; ++i) {
            for (11 j = 0; j < k; ++j) {
                psum[j][i] = psum[j][i - 1];
            }
            psum[s[i - 1]][i]++;
        }
    }

    11 qtd(11 l, 11 r, char c) { // [0,n-1]
        return psum[c][r + 1] - psum[c][l];
    }
}

```

9 Settings and macros

9.1 .vimrc

```

set ts=4 sw=4 sta nu rnu sc cindent
set bg=dark ruler clipboard=unnamed,unnamedplus, timeoutlen=100
colorscheme default

nnoremap <C-j> :botright belowright term bash <CR>
syntax on

```

9.2 degug.cpp

```

#include <bits/stdc++.h>
using namespace std;
/***** Debug Code *****/
template <typename T>
concept Printable = requires(T t) {
    { std::cout << t } -> std::same_as<std::ostream &>;
};
template <Printable T>
void __print(const T &x) {
    cerr << x;
}
template <size_t T>
void __print(const bitset<T> &x) {
    cerr << x;
}
template <typename A, typename B>
void __print(const pair<A, B> &p);
template <typename... A>
void __print(const tuple<A...> &t);
template <typename T>
void __print(stack<T> s);
template <typename T>
void __print(queue<T> q);
template <typename T, typename... U>
void __print(priority_queue<T, U...> q);
template <typename A>
void __print(const A &x) {
    bool first = true;
    cerr << '{';
    for (const auto &i : x) {
        cerr << (first ? "" : ","), __print(i);
        first = false;
    }
    cerr << '}';
}
template <typename A, typename B>
void __print(const pair<A, B> &p) {
    cerr << '(';
    __print(p.first);
    cerr << ',';
    __print(p.second);
    cerr << ')';
}
template <typename... A>
void __print(const tuple<A...> &t) {
    bool first = true;
    cerr << '(';
    apply(
        [first](const auto &...args) {

```

```

        ((cerr << (first ? "" : ","), __print(args), first = false), ...);
    },
    t);
    cerr << '>';
}
template <typename T>
void __print(stack<T> s) {
    vector<T> debugVector;
    while (!s.empty()) {
        T t = s.top();
        debugVector.push_back(t);
        s.pop();
    }
    reverse(debugVector.begin(), debugVector.end());
    __print(debugVector);
}
template <typename T>
void __print(queue<T> q) {
    vector<T> debugVector;
    while (!q.empty()) {
        T t = q.front();
        debugVector.push_back(t);
        q.pop();
    }
    __print(debugVector);
}
template <typename T, typename... U>
void __print(priority_queue<T, U...> q) {
    vector<T> debugVector;
    while (!q.empty()) {
        T t = q.top();
        debugVector.push_back(t);
        q.pop();
    }
    __print(debugVector);
}
void _print() { cerr << "]\n"; }
template <typename Head, typename... Tail>
void _print(const Head &H, const Tail &...T) {
    __print(H);
    if (sizeof...(T)) cerr << ", ";
    _print(T...);
}

#define dbg(x...) \
    cerr << "[" << #x << "]" = ["; \
    _print(x)

```

9.3 .bashrc

```

cpp() {
    echo ">> COMPILING <<" 1>&2
    g++ -std=c++17 \
        -O2 \
        -g \
        -g3 \
        -Wextra \
        -Wshadow \

```

```

-Wformat=2 \
-Wconversion \
-fsanitize=address,undefined \
-fno-sanitize-recover \
-Wfatal-errors \
-DDEBUG $1 \

if [ $? -ne 0 ]; then
    echo ">> FAILED <<" 1>&2
    return 1
fi
echo ">> DONE << " 1>&2
time ./a.out ${@:2}
}

prepare() {
    for i in {a..z}
    do
        cp macro.cpp $i.cpp
        touch $i.py
    done

    for i in {1..10}
    do
        touch in${i}
        touch out${i}
        touch ans${i}
    done
}

```

9.4 macro.cpp

```

#include <bits/stdc++.h>
using namespace std;
#ifdef DEBUG
#include "debug.cpp"
#else
#define dbg(...) 666
#endif
#define endl '\n'
#define fastio \
    ios_base::sync_with_stdio(false); \
    cin.tie(0); \
    cout.tie(0);
#define len(__x) (ll) __x.size()
using ll = long long;
using vll = vector<ll>;
using pll = pair<ll, ll>;
using vll2d = vector<vll>;
using vi = vector<int>;
using vi2d = vector<vi>;
using pii = pair<int, int>;
using vii = vector<pii>;
using vc = vector<char>;
#define all(a) a.begin(), a.end()
#define snd second
#define fst first
#define pb(__x) push_back(__x)

```

```
#define mp(____a, ____b) make_pair(____a, ____b)
#define eb(____x)  emplace_back(____x)

const ll INF = 1e18;

void run() {

}

int32_t main(void) {
    fastio;
    int t;
    t = 1;
    // cin >> t;
    while (t--) run();
}
```