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1 Data structures

1.1 Dsu

```
struct DSU {
 vector < int > ps;
 vector < int > size;
 DSU(int N) : ps(N + 1), size(N + 1, 1) { iota(ps.begin(), ps.end(), 0); }
 int find_set(int x) { return ps[x] == x ? x : ps[x] = find_set(ps[x]); }
 bool same_set(int x, int y) { return find_set(x) == find_set(y); }
 void union_set(int x, int y) {
    if (same_set(x, y)) return;
   int px = find_set(x);
    int py = find_set(y);
    if (size[px] < size[py]) swap(px, py);</pre>
   ps[py] = px;
    size[px] += size[py];
};
     Dsu (Python)
class DSU:
    def init (self. n):
        self.n = n
        self.p = [x for x in range(0, n + 1)]
        self.size = [0 for i in range(0, n + 1)]
    def find_set(self, x): # log n
        if self.p[x] == x:
            return x
        else:
            self.p[x] = self.find_set(self.p[x])
            return self.p[x]
    def same_set(self, x, y): # log n
        return bool(self.find_set(x) == self.find_set(y))
    def union_set(self, x, y): # log n
        px = self.find_set(x)
        py = self.find_set(y)
        if px == py:
           return
        size x = self.size[px]
        size_y = self.size[py]
        if size_x > size_y:
            self.p[pv] = self.p[px]
            self.size[px] += self.size[py]
        else:
            self.p[px] = self.p[py]
```

self.size[py] += self.size[px]

1.3 Ordered Set Gnu Pbds

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template <typename T>
// using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
// tree_order_statistics_node_update>;
// if you want to find the elements less or equal :p
using ordered_set = tree<T, null_type, less_equal<T>, rb_tree_tag,
                         tree order statistics node update >:
1.4 Segtree Point Rmq
class SegTree {
 public:
  int n;
  vector<1l> st;
  SegTree(const vector<11> &v) : n((int)v.size()), st(n * 4 + 1, LLONG_MAX) {
    for (int i = 0; i < n; ++i) update(i, v[i]);</pre>
  void update(int p, ll v) { update(1, 0, n - 1, p, v); }
  ll RMQ(int 1, int r) { return RMQ(1, 0, n - 1, 1, r); }
 private:
  void update(int node, int 1, int r, int p, 11 v) {
    if (p < l or p > r) return; // fora do intervalo.
    if (1 == r) {
      st[node] = v:
      return;
    }
    int mid = 1 + (r - 1) / 2;
    update(node * 2, 1, mid, p, v);
    update(node * 2 + 1, mid + 1, r, p, v);
    st[node] = min(st[node * 2], st[node * 2 + 1]);
  11 RMQ(int node, int L, int R, int 1, int r) {
    if (1 <= L and r >= R) return st[node];
    if (L > r or R < 1) return LLONG_MAX;
    if (L == R) return st[node];
    int mid = L + (R - L) / 2;
    return min(RMQ(node * 2, L, mid, 1, r),
               RMQ(node * 2 + 1, mid + 1, R, 1, r));
};
```

1.5 Segtree Rmq Lazy Max Update

```
struct SegmentTree {
```

```
int N:
  vll ns, lazy;
  SegmentTree(const vll &xs) : N(xs.size()), ns(4 * N, 0), lazy(4 * N, 0) {
   for (size t i = 0: i < xs.size(): ++i) {</pre>
      update(i, i, xs[i]);
   }
 }
 void update(int a, int b, ll value) { update(1, 0, N - 1, a, b, value); }
 void update(int node, int L. int R. int a. int b. 11 value) {
   if (lazy[node]) {
      ns[node] = max(ns[node], lazy[node]);
     if (L < R) {
        lazy[2 * node] = max(lazy[2 * node], lazy[node]);
        lazy[2 * node + 1] = max(lazy[2 * node + 1], lazy[node]);
      lazy[node] = 0;
    if (a > R or b < L) return;
    if (a \le L \text{ and } R \le b) {
     ns[node] = max(ns[node], value);
     if (L < R) {
       lazv[2 * node] = max(value. lazv[2 * node]);
       lazy[2 * node + 1] = max(value, lazy[2 * node + 1]);
     }
     return;
    update(2 * node, L, (L + R) / 2, a, b, value);
    update(2 * node + 1, (L + R) / 2 + 1, R, a, b, value);
    ns[node] = max(ns[node * 2], ns[node * 2 + 1]);
 11 RMQ(int a, int b) { return RMQ(1, 0, N - 1, a, b); }
 11 RMQ(int node, int L, int R, int a, int b) {
    if (lazy[node]) {
     ns[node] = max(ns[node], lazy[node]);
     if (L < R) {
        lazv[node * 2] = max(lazv[node * 2], lazv[node]);
        lazy[node * 2 + 1] = max(lazy[node * 2 + 1], lazy[node]);
     lazy[node] = 0;
    if (a > R \text{ or } b < L) \text{ return } 0;
    if (a <= L and R <= b) return ns[node]:
    11 x = RMQ(2 * node, L, (L + R) / 2, a, b);
   11 y = RMQ(2 * node + 1, (L + R) / 2 + 1, R, a, b);
    return max(x, y);
 }
}:
      Segtree Rmq Lazy Range
struct SegmentTree {
 int N;
 vll ns, lazy;
 SegmentTree(const vll &xs)
    : N(xs.size()), ns(4 * N, INT_MAX), lazy(4 * N, 0) {
```

for (size_t i = 0; i < xs.size(); ++i) update(i, i, xs[i]);</pre>

void update(int a, int b, ll value) { update(1, 0, N - 1, a, b, value); } void update(int node, int L, int R, int a, int b, ll value) { if (lazv[node]) { ns[node] = ns[node] == INT_MAX ? lazy[node] : ns[node] + lazy[node]; if (L < R) { lazy[2 * node] += lazy[node]; lazy[2 * node + 1] += lazy[node]; lazv[node] = 0;} if (a > R or b < L) return; if $(a \le L \text{ and } R \le b)$ { ns[node] = ns[node] == INT_MAX ? value : ns[node] + value; if (L < R) { lazv[2 * node] += value; lazy[2 * node + 1] += value; return; update(2 * node, L, (L + R) / 2, a, b, value); update(2 * node + 1, (L + R) / 2 + 1, R, a, b, value); ns[node] = min(ns[2 * node], ns[2 * node + 1]);11 RMQ(int a, int b) { return RMQ(1, 0, N - 1, a, b); } 11 RMQ(int node, int L, int R, int a, int b) { if (lazy[node]) { ns[node] = ns[node] == INT_MAX ? lazy[node] : ns[node] + lazy[node]; **if** (L < R) { lazy[2 * node] += lazy[node]; lazy[2 * node + 1] += lazy[node]; lazy[node] = 0;if (a > R or b < L) return INT_MAX; if (a <= L and R <= b) return ns[node]; 11 x = RMQ(2 * node, L, (L + R) / 2, a, b);11 y = RMQ(2 * node + 1, (L + R) / 2 + 1, R, a, b);return min(x, y); }; Segtree Rsq Lazy Range Sum struct SegTree { int N: vector<ll> ns, lazy; SegTree(const vector<11> &xs) : N(xs.size()), ns(4 * N, 0), lazy(4 * N, 0) { for (size_t i = 0; i < xs.size(); ++i) update(i, i, xs[i]);</pre> void update(int a, int b, ll value) { update(1, 0, N - 1, a, b, value); }

void update(int node, int L, int R, int a, int b, ll value) {

// Lazy propagation

if (lazy[node]) {

```
ns[node] += (R - L + 1) * lazv[node];
      if (L < R) // Se o ón ãno é uma folha, propaga
        lazy[2 * node] += lazy[node];
       lazy[2 * node + 1] += lazy[node];
     lazv[node] = 0:
    if (a > R or b < L) return;
    if (a <= L and R <= b) {
      ns[node] += (R - L + 1) * value:
      if (L < R) {
       lazy[2 * node] += value;
        lazv[2 * node + 1] += value;
      return:
    update (2 * node, L, (L + R) / 2, a, b, value);
    update(2 * node + 1, (L + R) / 2 + 1, R, a, b, value);
    ns[node] = ns[2 * node] + ns[2 * node + 1];
 }
 11 RSQ(int a. int b) { return RSQ(1. 0. N - 1. a. b): }
 11 RSQ(int node, int L, int R, int a, int b) {
    if (lazy[node]) {
      ns[node] += (R - L + 1) * lazy[node];
      if (L < R) {
       lazy[2 * node] += lazy[node];
       lazy[2 * node + 1] += lazy[node];
      lazy[node] = 0;
    if (a > R \text{ or } b < L) \text{ return } 0;
    if (a <= L and R <= b) return ns[node];</pre>
    11 x = RSQ(2 * node, L, (L + R) / 2, a, b);
    11 \text{ v} = RSQ(2 * node + 1, (L + R) / 2 + 1, R, a, b);
    return x + y;
 }
};
```

Segtree Rxq Lazy Range Xor

```
struct SegTree {
```

```
int N:
vector<ll> ns, lazy;
SegTree(const vector<11> &xs) : N(xs.size()), ns(4 * N, 0), lazy(4 * N, 0) {
  for (size_t i = 0; i < xs.size(); ++i) update(i, i, xs[i]);</pre>
7
void update(int a, int b, ll value) { update(1, 0, N - 1, a, b, value); }
void update(int node, int L, int R, int a, int b, 11 value) {
 // Lazy propagation
 if (lazy[node]) {
   ns[node] ^= lazy[node];
    if (L < R) // Se o ón ano é uma folha, propaga
     lazy[2 * node] ^= lazy[node];
     lazy[2 * node + 1] ^= lazy[node];
    lazy[node] = 0;
  if (a > R or b < L) return;
  if (a \le L \text{ and } R \le b) {
    ns[node] ^= value;
    if (L < R) {
     lazy[2 * node] ^= value;
     lazv[2 * node + 1] ^= value:
    return;
  update (2 * node, L, (L + R) / 2, a, b, value);
  update(2 * node + 1, (L + R) / 2 + 1, R, a, b, value);
  ns[node] = ns[2 * node] ^ ns[2 * node + 1];
ll rxq(int a, int b) { return RSQ(1, 0, N - 1, a, b); }
ll rxq(int node, int L, int R, int a, int b) {
 if (lazv[node]) {
    ns[node] ^= lazy[node];
    if (L < R) {
      lazy[2 * node] ^= lazy[node];
     lazy[2 * node + 1] ^= lazy[node];
    lazy[node] = 0;
  if (a > R \text{ or } b < L) return 0:
```

```
if (a <= L and R <= b) return ns[node]:
   11 x = rxq(2 * node, L, (L + R) / 2, a, b);
   11 y = rxq(2 * node + 1, (L + R) / 2 + 1, R, a, b);
   return x ^ y;
 }
};
     Sparse Table Rmq
        Sparse table implementation for rmq.
        build: O(NlogN)
        query: 0(1)
int fastlog2(ll x) {
 ull i = x:
 return i ? __builtin_clzll(1) - __builtin_clzll(i) : -1;
template <typename T>
class SparseTable {
public:
 int N:
 int K;
 vector < vector < T >> st:
 SparseTable(vector<T> vs)
   : N((int)vs.size()), K(fastlog2(N) + 1), st(K + 1, vector < T > (N + 1)) {
    copy(vs.begin(), vs.end(), st[0].begin());
```

2 Dynamic programming

for (int i = 1; i <= K; ++i)

int i = fastlog2(r - l + 1);

for (int j = 0; j + (1 << i) <= N; ++j)

return min(st[i][l], st[i][r - (1 << i) + 1]);

T RMQ(int 1, int r) { // [1, r], 0 indexed

st[i][j] = min(st[i - 1][j], st[i - 1][j + (1 << (i - 1))]);

2.1 Edit Distance

};

```
int edit_distance(const string &a, const string &b) {
   int n = a.size();
   int m = b.size();
   vector < vi > dp(n + 1, vi(m + 1, 0));

   int ADD = 1, DEL = 1, CHG = 1;
   for (int i = 0; i <= n; ++i) {
      dp[i][0] = i * DEL;
   }
   for (int i = 1; i <= m; ++i) {
      dp[0][i] = ADD * i;
   }</pre>
```

```
for (int i = 1: i <= n: ++i) {
   for (int j = 1; j <= m; ++j) {
      int add = dp[i][j - 1] + ADD;
      int del = dp[i - 1][j] + DEL;
      int chg = dp[i - 1][j - 1] + (a[i - 1] == b[j - 1]?0:1) * CHG;
      dp[i][j] = min({add, del, chg});
 }
 return dp[n][m];
     Knapsack Dp Values 01
const int MAX N = 1001:
const int MAX_S = 100001;
array < array < int , MAX_S > , MAX_N > dp;
bool check[MAX_N][MAX_S];
pair < int , vi > knapsack(int S, const vector < pii > &xs) {
 int N = (int)xs.size():
 for (int i = 0; i \le N; ++i) dp[i][0] = 0;
 for (int m = 0; m \le S; ++m) dp[0][m] = 0;
 for (int i = 1: i <= N: ++i) {
   for (int m = 1; m <= S; ++m) {
      dp[i][m] = dp[i - 1][m];
      check[i][m] = false;
      auto [w, v] = xs[i - 1];
      if (w \le m \text{ and } (dp[i - 1][m - w] + v) >= dp[i][m]) {
        dp[i][m] = dp[i - 1][m - w] + v;
        check[i][m] = true;
   }
  int m = S;
  vi es:
 for (int i = N; i >= 1; --i) {
   if (check[i][m]) {
      es.push_back(i);
      m -= xs[i - 1].first;
 }
 reverse(es.begin(), es.end());
 return {dp[N][S], es};
     Money Sum Bottom Up
```

find every possible sum using

```
the given values only once.
set < int > money_sum(const vi &xs) {
  using vc = vector < char >;
  using vvc = vector < vc >;
  int _m = accumulate(all(xs), 0);
  int _n = xs.size();
  vvc _dp(_n + 1, vc(_m + 1, 0));
  set < int > _ans;
  _{dp}[0][xs[0]] = 1;
  for (int i = 1; i < _n; ++i) {
    for (int j = 0; j <= _m; ++j) {
      if (j == 0 or _dp[i - 1][j]) {
        _{dp[i][j + xs[i]] = 1;}
        _{dp[i][j]} = 1;
   }
  }
  for (int i = 0; i < _n; ++i)
    for (int j = 0; j \le m; ++j)
      if (_dp[i][j]) _ans.insert(j);
  return _ans;
2.4 Tsp
using vi = vector<int>;
vector < vi> dist:
vector < vi > memo;
/* 0 ( N^2 * 2^N )*/
int tsp(int i, int mask, int N) {
  if (mask == (1 << N) - 1) return dist[i][0];</pre>
  if (memo[i][mask] != -1) return memo[i][mask];
  int ans = INT MAX << 1:</pre>
  for (int j = 0; j < N; ++ j) {
    if (mask & (1 << j)) continue;
    auto t = tsp(j, mask | (1 << j), N) + dist[i][j];</pre>
    ans = min(ans. t):
  return memo[i][mask] = ans;
    Extras
3.1 Bigint
const int maxn = 1e2 + 14, lg = 15;
const int base = 1000000000:
const int base_digits = 9;
struct bigint {
  vector < int > a;
  int sign;
  int size() {
    if (a.empty()) return 0;
```

int ans = (a.size() - 1) * base_digits;

```
int ca = a.back();
  while (ca) ans++, ca \neq 10;
  return ans;
bigint operator (const bigint &v) {
  bigint ans = 1, a = *this, b = v;
  while (!b.isZero()) {
   if (b % 2) ans *= a;
    a *= a. b /= 2:
  return ans;
string to_string() {
  stringstream ss;
  ss << *this:
  string s;
  ss >> s;
  return s;
int sumof() {
  string s = to_string();
 int ans = 0:
 for (auto c : s) ans += c - '0';
  return ans;
/*</arpa>*/
bigint() : sign(1) {}
bigint(long long v) { *this = v; }
bigint(const string &s) { read(s); }
void operator=(const bigint &v) {
  sign = v.sign;
  a = v.a;
}
void operator=(long long v) {
 sign = 1:
  a.clear();
 if (v < 0) sign = -1, v = -v;
  for (; v > 0; v = v / base) a.push_back(v % base);
bigint operator+(const bigint &v) const {
 if (sign == v.sign) {
    bigint res = v;
    for (int i = 0, carry = 0; i < (int)max(a.size(), v.a.size()) || carry;</pre>
      if (i == (int)res.a.size()) res.a.push_back(0);
      res.a[i] += carry + (i < (int)a.size() ? a[i] : 0);
      carry = res.a[i] >= base;
      if (carry) res.a[i] -= base;
    return res;
  return *this - (-v);
```

```
}
bigint operator-(const bigint &v) const {
  if (sign == v.sign) {
    if (abs() >= v.abs()) {
      bigint res = *this;
      for (int i = 0, carry = 0; i < (int)v.a.size() || carry; ++i) {
        res.a[i] -= carry + (i < (int)v.a.size() ? v.a[i] : 0);
        carrv = res.a[i] < 0:</pre>
        if (carry) res.a[i] += base;
      res.trim();
      return res;
    return -(v - *this):
  return *this + (-v);
}
void operator*=(int v) {
  if (v < 0) sign = -sign, v = -v;
  for (int i = 0, carry = 0; i < (int)a.size() || carry; ++i) {
    if (i == (int)a.size()) a.push_back(0);
    long long cur = a[i] * (long long)v + carry;
    carry = (int)(cur / base);
    a[i] = (int)(cur \% base);
    // asm("divl %%ecx" : "=a"(carry), "=d"(a[i]) :
    // "A"(cur), "c"(base));
  trim();
}
bigint operator*(int v) const {
  bigint res = *this;
  res *= v;
  return res;
}
void operator*=(long long v) {
  if (v < 0) sign = -sign, v = -v;
  if (v > base) {
    *this = *this * (v / base) * base + *this * (v % base);
    return;
  for (int i = 0, carry = 0; i < (int)a.size() || carry; ++i) {</pre>
    if (i == (int)a.size()) a.push_back(0);
    long long cur = a[i] * (long long)v + carry;
    carry = (int)(cur / base);
    a[i] = (int)(cur % base);
    // asm("divl %%ecx" : "=a"(carry), "=d"(a[i]) :
    // "A"(cur), "c"(base));
 trim();
bigint operator*(long long v) const {
  bigint res = *this:
  res *= v;
```

```
return res:
friend pair < bigint , bigint > divmod(const bigint &a1, const bigint &b1) {
  int norm = base / (b1.a.back() + 1);
  bigint a = a1.abs() * norm;
  bigint b = b1.abs() * norm;
  bigint q, r;
  g.a.resize(a.a.size()):
  for (int i = a.a.size() - 1; i >= 0; i--) {
    r *= base:
    r += a.a[i];
    int s1 = r.a.size() \le b.a.size() ? 0 : r.a[b.a.size()]:
    int s2 = r.a.size() \le b.a.size() - 1 ? 0 : r.a[b.a.size() - 1]:
    int d = ((long long)base * s1 + s2) / b.a.back();
    r -= b * d:
    while (r < 0) r += b, --d;
    q.a[i] = d;
  q.sign = a1.sign * b1.sign;
  r.sign = a1.sign;
  q.trim();
 r.trim();
  return make_pair(q, r / norm);
bigint operator/(const bigint &v) const { return divmod(*this, v).first; }
bigint operator%(const bigint &v) const { return divmod(*this, v).second; }
void operator/=(int v) {
  if (v < 0) sign = -sign, v = -v;
  for (int i = (int)a.size() - 1, rem = 0; i \ge 0; --i) {
    long long cur = a[i] + rem * (long long)base;
    a[i] = (int)(cur / v);
    rem = (int)(cur % v);
 }
  trim();
bigint operator/(int v) const {
 bigint res = *this;
  res /= v;
  return res:
int operator%(int v) const {
 if (v < 0) v = -v;
 int m = 0;
 for (int i = a.size() - 1; i >= 0; --i)
    m = (a[i] + m * (long long)base) % v;
  return m * sign;
}
void operator+=(const bigint &v) { *this = *this + v; }
void operator -= (const bigint &v) { *this = *this - v; }
```

```
void operator*=(const bigint &v) { *this = *this * v; }
void operator/=(const bigint &v) { *this = *this / v; }
bool operator < (const bigint &v) const {</pre>
  if (sign != v.sign) return sign < v.sign;</pre>
  if (a.size() != v.a.size()) return a.size() * sign < v.a.size() * v.sign;</pre>
  for (int i = a.size() - 1; i >= 0; i--)
    if (a[i] != v.a[i]) return a[i] * sign < v.a[i] * sign;</pre>
  return false:
}
bool operator>(const bigint &v) const { return v < *this; }</pre>
bool operator <= (const bigint &v) const { return !(v < *this); }</pre>
bool operator>=(const bigint &v) const { return !(*this < v); }</pre>
bool operator == (const bigint &v) const {
  return !(*this < v) && !(v < *this);
bool operator!=(const bigint &v) const { return *this < v || v < *this; }
void trim() {
  while (!a.empty() && !a.back()) a.pop_back();
  if (a.empty()) sign = 1;
bool isZero() const { return a.empty() || (a.size() == 1 && !a[0]); }
bigint operator-() const {
  bigint res = *this;
  res.sign = -sign;
  return res:
}
bigint abs() const {
  bigint res = *this;
  res.sign *= res.sign;
  return res:
}
long longValue() const {
  long long res = 0;
 for (int i = a.size() - 1; i >= 0; i--) res = res * base + a[i];
  return res * sign;
}
friend bigint gcd(const bigint &a, const bigint &b) {
 return b.isZero() ? a : gcd(b, a % b);
friend bigint lcm(const bigint &a, const bigint &b) {
  return a / gcd(a, b) * b;
void read(const string &s) {
  sign = 1;
  a.clear();
  int pos = 0:
  while (pos < (int)s.size() && (s[pos] == '-' || s[pos] == '+')) {
   if (s[pos] == '-') sign = -sign;
    ++pos;
```

```
for (int i = s.size() - 1; i >= pos; i -= base_digits) {
    for (int j = max(pos, i - base_digits + 1); j <= i; j++)
      x = x * 10 + s[i] - '0';
    a.push_back(x);
  trim();
friend istream & operator >> (istream & stream, bigint &v) {
  string s;
  stream >> s;
  v.read(s):
  return stream:
}
friend ostream & operator << (ostream & stream, const bigint &v) {
  if (v.sign == -1) stream << '-';
  stream << (v.a.empty() ? 0 : v.a.back());
 for (int i = (int)v.a.size() - 2; i >= 0; --i)
    stream << setw(base digits) << setfill('0') << v.a[i]:
  return stream:
}
static vector <int > convert_base(const vector <int > &a, int old_digits,
                                 int new_digits) {
  vector < long long > p(max(old_digits, new_digits) + 1);
 p[0] = 1;
  for (int i = 1; i < (int)p.size(); i++) p[i] = p[i - 1] * 10;
  vector<int> res:
  long long cur = 0;
 int cur_digits = 0;
 for (int i = 0; i < (int)a.size(); i++) {</pre>
    cur += a[i] * p[cur_digits];
    cur_digits += old_digits;
    while (cur_digits >= new_digits) {
      res.push_back(int(cur % p[new_digits]));
      cur /= p[new digits]:
      cur_digits -= new_digits;
 }
  res.push_back((int)cur);
  while (!res.empty() && !res.back()) res.pop_back();
  return res;
typedef vector<long long> vll;
static vll karatsubaMultiply(const vll &a, const vll &b) {
 int n = a.size();
 vll res(n + n):
 if (n \le 32) {
   for (int i = 0; i < n; i++)
      for (int j = 0; j < n; j++) res[i + j] += a[i] * b[j];
    return res;
```

```
int k = n \gg 1:
    vll a1(a.begin(), a.begin() + k);
    vll a2(a.begin() + k, a.end());
    vll b1(b.begin(), b.begin() + k);
    vll b2(b.begin() + k, b.end());
    vll a1b1 = karatsubaMultiply(a1, b1);
    vll a2b2 = karatsubaMultiply(a2, b2);
    for (int i = 0; i < k; i++) a2[i] += a1[i];</pre>
    for (int i = 0; i < k; i++) b2[i] += b1[i];
    vll r = karatsubaMultiply(a2, b2);
    for (int i = 0; i < (int)a1b1.size(); i++) r[i] -= a1b1[i];
    for (int i = 0: i < (int)a2b2.size(): i++) r[i] -= a2b2[i]:
    for (int i = 0; i < (int)r.size(); i++) res[i + k] += r[i];</pre>
    for (int i = 0; i < (int)a1b1.size(); i++) res[i] += a1b1[i];
    for (int i = 0; i < (int)a2b2.size(); i++) res[i + n] += a2b2[i];
    return res:
 }
  bigint operator*(const bigint &v) const {
    vector < int > a6 = convert_base(this - > a, base_digits, 6);
    vector < int > b6 = convert_base(v.a, base_digits, 6);
    vll a(a6.begin(), a6.end());
    vll b(b6.begin(), b6.end());
    while (a.size() < b.size()) a.push_back(0);</pre>
    while (b.size() < a.size()) b.push_back(0);</pre>
    while (a.size() & (a.size() - 1)) a.push_back(0), b.push_back(0);
    vll c = karatsubaMultiply(a, b);
    bigint res;
    res.sign = sign * v.sign;
    for (int i = 0, carry = 0; i < (int)c.size(); i++) {</pre>
      long long cur = c[i] + carry;
      res.a.push_back((int)(cur % 1000000));
      carry = (int)(cur / 1000000);
    res.a = convert_base(res.a, 6, base_digits);
    res.trim();
    return res;
 }
};
     Binary To Gray
string binToGray(string bin) {
  string gray(bin.size(), '0');
 int n = bin.size() - 1;
  grav[0] = bin[0];
  for (int i = 1; i <= n; i++) {</pre>
    gray[i] = '0' + (bin[i - 1] == '1') ^ (bin[i] == '1');
 }
 return gray;
```

3.3 Get Permutation Cicles

```
* receives a permutation [0, n-1]
 * returns a vector of cicles
 * for example: [ 1, 0, 3, 4, 2] -> [[0, 1], [2, 3, 4]]
vector<vll> getPermutationCicles(const vll &ps) {
  ll n = len(ps):
  vector < char > visited(n);
  vector < vll> cicles:
  for (int i = 0; i < n; ++i) {
    if (visited[i]) continue;
    vll cicle;
    11 pos = i;
    while (!visited[pos]) {
      cicle.pb(pos);
      visited[pos] = true;
      pos = ps[pos];
    cicles.push_back(vll(all(cicle)));
  return cicles;
4 Graphs
4.1 2 Sat (struct)
struct SAT2 {
  11 n;
  vll2d adj, adj_t;
  vc used;
  vll order, comp;
  vc assignment;
  bool solvable:
  SAT2(11 _n)
   : n(2 * _n),
      adj(n),
      adi_t(n)
      used(n).
      order(n),
      comp(n, -1),
      assignment(n / 2) {}
  void dfs1(int v) {
    used[v] = true;
    for (int u : adj[v]) {
      if (!used[u]) dfs1(u);
    order.push_back(v);
  void dfs2(int v, int cl) {
```

comp[v] = c1;

for (int u : adj_t[v]) {

if (comp[u] == -1) dfs2(u, c1);

```
}
 bool solve_2SAT() {
    // find and label each SCC
    for (int i = 0; i < n; ++i) {
     if (!used[i]) dfs1(i);
    reverse(all(order));
   11 j = 0;
    for (auto &v : order) {
     if (comp[v] == -1) dfs2(v, j++);
    assignment.assign(n / 2, false);
    for (int i = 0; i < n; i += 2) {
      // x and !x belong to the same SCC
     if (comp[i] == comp[i + 1]) {
       solvable = false;
       return false;
     }
      assignment[i / 2] = comp[i] > comp[i + 1];
    solvable = true;
    return true;
 }
 void add_disjunction(int a, bool na, int b, bool nb) {
    a = (2 * a) ^na;
   b = (2 * b) ^ nb;
    int neg_a = a ^ 1;
    int neg_b = b^1;
    adj[neg_a].push_back(b);
    adj[neg_b].push_back(a);
    adj_t[b].push_back(neg_a);
    adj_t[a].push_back(neg_b);
 }
};
     Scc (struct)
struct SCC {
 11 N;
 vll2d adj, tadj;
 vll todo, comps, comp;
 vector<set<ll>> sccadj;
 vchar vis:
 SCC(11 _N) : N(_N), adj(_N), tadj(_N), comp(_N, -1), sccadj(_N), vis(_N) {}
 void add_edge(11 x, 11 y) { adj[x].eb(y), tadj[y].eb(x); }
 void dfs(ll x) {
   vis[x] = 1:
   for (auto &y : adj[x])
     if (!vis[y]) dfs(y);
   todo.pb(x);
 void dfs2(11 x, 11 v) {
```

```
comp[x] = v;
   for (auto &y : tadj[x])
      if (comp[y] == -1) dfs2(y, v);
  void gen() {
   for (11 i = 0; i < N; ++i)</pre>
      if (!vis[i]) dfs(i);
    reverse(all(todo));
   for (auto &x : todo)
      if (comp[x] == -1) {
        dfs2(x, x);
        comps.pb(x);
 }
  void genSCCGraph() {
   for (11 i = 0; i < N; ++i) {</pre>
      for (auto &j : adj[i]) {
        if (comp[i] != comp[j]) {
          sccadj[comp[i]].insert(comp[j]);
   }
};
     Scc Nodes (kosajaru)
/*
* O(n+m)
 * Returns a pair <a, b>
        a: number of SCCs
        b: vector of size n, where b[i] is the SCC id of node i
void dfs(ll u, vchar &visited, const vll2d &g, vll &scc, bool buildScc, ll id,
         vll &sccid) {
 visited[u] = true:
  sccid[u] = id;
 for (auto &v : g[u])
   if (!visited[v]) dfs(v, visited, g, scc, buildScc, id, sccid);
 // if it's the first pass, add the node to the scc
  if (buildScc) scc.eb(u);
pair <11, vll > kosajaru(vll2d &g) {
 ll n = len(g);
  vll scc;
  vchar vis(n);
  vll sccid(n):
 for (ll i = 0; i < n; i++)
    if (!vis[i]) dfs(i, vis, g, scc, true, 0, sccid);
 // build the transposed graph
 v112d gt(n);
 for (int i = 0; i < n; ++i)
   for (auto &v : g[i]) gt[v].eb(i);
```

```
// run the dfs on the previous scc order
 11 id = 1;
 vis.assign(n, false);
 for (ll i = len(scc) - 1: i >= 0: i--)
   if (!vis[scc[i]]) {
      dfs(scc[i], vis, gt, scc, false, id++, sccid);
 return {id - 1, sccid};
4.4 Check Bipartite
// O(V)
bool checkBipartite(const ll n, const vector<vll> &adj) {
 11 s = 0:
 queue <11> q;
 q.push(s);
 vll color(n, INF);
 color[s] = 0;
 bool isBipartite = true;
 while (!q.empty() && isBipartite) {
   11 u = q.front();
   q.pop();
   for (auto &v : adj[u]) {
     if (color[v] == INF) {
        color[v] = 1 - color[u];
       q.push(v);
     } else if (color[v] == color[u]) {
       return false:
  return true;
     Count Scc (kosajaru)
void dfs(ll u, vchar &visited, const vll2d &g, vll &scc, bool buildScc) {
 visited[u] = true:
 for (auto &v : g[u])
   if (!visited[v]) dfs(v, visited, g, scc, buildScc);
 // if it's the first pass, add the node to the scc
 if (buildScc) scc.eb(u):
11 kosajaru(v112d &g) {
 ll n = len(g);
 vll scc;
 vchar vis(n):
 for (ll i = 0; i < n; i++)
   if (!vis[i]) dfs(i, vis, g, scc, true);
 // build the transposed graph
 v112d gt(n);
 for (int i = 0; i < n; ++i)
   for (auto &v : g[i]) gt[v].eb(i);
```

```
// run the dfs on the previous scc order
 11 \ \text{scccnt} = 0;
  vis.assign(n, false);
 for (ll i = len(scc) - 1; i \ge 0; i--)
    if (!vis[scc[i]]) dfs(scc[i], vis, gt, scc, false), scccnt++;
 return scccnt;
4.6
    Dijkstra
11 __inf = LLONG_MAX >> 5;
vll dijkstra(const vector<vector<pll>>> &g, ll n) {
  priority_queue < pll , vector < pll > , greater < pll >> pq;
  vll dist(n, __inf);
  vector < char > vis(n);
  pq.emplace(0, 0);
  dist[0] = 0;
  while (!pq.empty()) {
   auto [d1, v] = pq.top();
   pq.pop();
   if (vis[v]) continue:
    vis[v] = true;
    for (auto [d2, u] : g[v]) {
      if (dist[u] > d1 + d2) {
        dist[u] = d1 + d2:
        pq.emplace(dist[u], u);
    }
  return dist;
4.7 Floyd Warshall
vector<vll> floyd_warshall(const vector<vll> &adj, ll n) {
  auto dist = adj;
 for (int i = 0; i < n; ++i) {
   for (int j = 0; j < n; ++ j) {
      for (int k = 0; k < n; ++k) {
        dist[j][k] = min(dist[j][k], dist[j][i] + dist[i][k]);
   }
  return dist;
    Kruskal (Python)
class DSU:
    def __init__(self, n):
        self.n = n
        self.p = [x for x in range(0, n + 1)]
        self.size = [0 for i in range(0, n + 1)]
    def find_set(self, x):
```

```
if self.p[x] == x:
            return x
        else:
            self.p[x] = self.find_set(self.p[x])
            return self.p[x]
   def same_set(self, x, y):
       return bool(self.find_set(x) == self.find_set(y))
   def union_set(self, x, y):
       px = self.find_set(x)
       py = self.find_set(y)
       if px == py:
           return
        size_x = self.size[px]
        size_v = self.size[pv]
       if size_x > size_y:
           self.p[py] = self.p[px]
            self.size[px] += self.size[py]
            self.p[px] = self.p[py]
           self.size[py] += self.size[px]
def kruskal(gv, n):
   Receives te list of edges as a list of tuple in the form:
       d. u. v
       d: distance between u and v
   And also n as the total of verties.
   dsu = DSU(n)
   c = 0
   for e in gv:
       d. u. v = e
       if not dsu.same_set(u, v):
           c += d
           dsu.union_set(u, v)
   return c
```

4.9 Lowest Common Ancestor Sparse Table

```
int fastlog2(11 x) {
  ull i = x;
  return i ? __builtin_clzll(1) - __builtin_clzll(i) : -1;
}
template <typename T>
class SparseTable {
  public:
    int N;
    int K;
  vector<vector<T>> st;
    SparseTable(vector<T> vs)
```

```
: N((int)vs.size()), K(fastlog2(N) + 1), st(K + 1, vector < T > (N + 1)) {
    copy(vs.begin(), vs.end(), st[0].begin());
    for (int i = 1: i <= K: ++i)
      for (int j = 0; j + (1 << i) <= N; ++j)
        st[i][j] = min(st[i - 1][j], st[i - 1][j + (1 << (i - 1))]);
  SparseTable() {}
  T RMO(int 1, int r) {
    int i = fastlog2(r - 1 + 1);
    return min(st[i][1], st[i][r - (1 << i) + 1]);
};
class LCA {
 public:
 int p;
 int n:
  vi first:
  vector < char > visited;
  vi vertices:
  vi height;
  SparseTable < int > st:
  LCA(const vector <vi> &g)
    : p(0), n((int)g.size()), first(n + 1), visited(n + 1, 0), height(n + 1) {
    build_dfs(g, 1, 1);
    st = SparseTable < int > (vertices);
  void build_dfs(const vector < vi > &g, int u, int hi) {
    visited[u] = true:
    height[u] = hi;
    first[u] = vertices.size():
    vertices.push_back(u);
    for (auto uv : g[u]) {
      if (!visited[uv]) {
        build_dfs(g, uv, hi + 1);
        vertices.push_back(u);
      7
    }
  }
  int lca(int a, int b) {
   int l = min(first[a], first[b]);
    int r = max(first[a], first[b]);
    return st.RMQ(1, r):
 }
};
       Topological Sorting
* (V)
* * vertices have index [0, n-1]
* if is a DAG:
```

* returns a topological sorting

* else:

```
* returns an empty vector
enum class state { not_visited, processing, done };
bool dfs(const vector < vll > &adj, ll s, vector < state > &states, vll &order) {
 states[s] = state::processing;
 for (auto &v : adj[s]) {
   if (states[v] == state::not_visited) {
     if (not dfs(adj, v, states, order)) return false;
   } else if (states[v] == state::processing)
      return false;
 states[s] = state::done;
 order.pb(s);
 return true:
vll topologicalSorting(const vector<vll> &adj) {
 ll n = len(adj);
 vll order;
 vector < state > states(n, state::not_visited);
 for (int i = 0; i < n; ++i) {
   if (states[i] == state::not_visited) {
     if (not dfs(adj, i, states, order)) return {};
   }
 reverse(all(order));
 return order;
```

5 Math

5.1 Combinatorics With Repetitions

5.2 Count Divisors Memo

```
const 11 mod = 1073741824:
const ll maxd = 100 * 100 * 100 + 1;
vector < 11 > memo(maxd, -1);
11 countdivisors(11 x) {
  11 \text{ ox} = x:
  ll ans = 1;
  for (11 i = 2; i <= x; ++i) {
    if (memo[x] != -1) {
      ans *= memo[x]:
      break;
    11 count = 0;
    while (x \text{ and } x \% i == 0)  {
      x /= i:
      count++:
    ans *= (count + 1);
  memo[ox] = ans;
  return ans:
5.3
      Euler Phi
const ll MAXN = 1e5;
vll list_primes(ll n) { // Nlog * log N
  vll ps;
  bitset < MAXN > sieve:
  sieve.set();
  sieve.reset(1);
  for (11 i = 2; i <= n; ++i) {
    if (sieve[i]) ps.push_back(i);
    for (11 j = i * 2; j <= n; j += i) {
      sieve.reset(j);
  }
  return ps;
vector<pll> factorization(ll n, const vll &primes) {
  vector < pll > ans;
 for (auto &p : primes) {
    if (n == 1) break;
    11 cnt = 0:
    while (n \% p == 0) {
      cnt++;
      n /= p;
    if (cnt) ans.emplace_back(p, cnt);
  return ans;
11 phi(ll n, vector<pll> factors) {
 if (n == 1) return 1;
  ll ans = n;
  for (auto [p, k] : factors) {
```

```
ans /= p;
   ans *= (p - 1);
 return ans;
    Factorial Factorization
// O(logN) greater k that p^k | n
11 E(11 n, 11 p) {
 11 k = 0, b = p;
 while (b <= n) {
   k += n / b;
   b *= p;
 return k;
// lsit every prime until MAXN O(Nlog * log N)
const ll MAXN = 1e5;
vll list_primes(ll n) {
 vll ps;
 bitset < MAXN > sieve;
 sieve.set():
 sieve.reset(1);
 for (ll i = 2; i <= n; ++i) {
   if (sieve[i]) ps.push_back(i);
   for (ll j = i * 2; j <= n; j += i) sieve.reset(j);
 return ps;
// O(pi(N)*logN)
map<11, 11> factorial_factorization(11 n, const v11 &primes) {
 map<11, 11> fs;
 for (const auto &p : primes) {
   if (p > n) break;
   fs[p] = E(n, p);
 return fs;
5.5 Factorial
const 11 MAX = 18:
vll fv(MAX, -1);
ll factorial(ll n) {
 if (fv[n] != -1) return fv[n];
 if (n == 0) return 1;
 return n * factorial(n - 1);
     Factorization With Primes
// Nlog * log N
const ll MAXN = 1e5;
```

```
vll list_primes(ll n) {
  bitset < MAXN > sieve;
  sieve.set():
  sieve.reset(1);
 for (11 i = 2; i <= n; ++i) {
   if (sieve[i]) ps.push_back(i);
   for (11 j = i * 2; j <= n; j += i) sieve.reset(j);</pre>
  return ps;
// O(pi(sqrt(n)))
map<ll, ll> factorization(ll n, const vll &primes) {
  map<11. 11> ans:
 for (auto p : primes) {
   if (p * p > n) break;
   11 count = 0;
   for (; n % p == 0; count++, n /= p)
    if (count) ans[p] = count;
  return ans;
     Factorization
// O(sqrt(n))
map<ll, ll> factorization(ll n) {
  map<11, 11> ans;
  for (ll i = 2; i * i <= n; i++) {
   11 count = 0;
   for (; n % i == 0; count++, n /= i)
    if (count) ans[i] = count;
  if (n > 1) ans[n]++;
  return ans;
5.8
     Fast Exp
 Fast exponentiation algorithm,
  compute a^n in O(log(n))
ll fexp(ll a, int n) {
 if (n == 0) return 1;
  if (n == 1) return a;
 11 x = fexp(a, n / 2);
  return x * x * (n & 1 ? a : 1);
     Gcd Using Factorization
// O(sqrt(n))
map<ll, ll> factorization(ll n) {
```

```
map<11. 11> ans:
  for (ll i = 2; i * i <= n; i++) {
   11 count = 0;
   for (: n % i == 0: count++, n /= i)
    if (count) ans[i] = count;
 if (n > 1) ans [n]++;
 return ans:
ll gcd_with_factorization(ll a, ll b) {
 map<11, 11> fa = factorization(a);
 map<11, 11> fb = factorization(b);
 ll ans = 1:
 for (auto fai : fa) {
   11 k = min(fai.second, fb[fai.first]);
   while (k--) ans *= fai.first;
 return ans:
5.10 Gcd
11 gcd(ll a, ll b) { return b ? gcd(b, a % b) : a; }
5.11 Integer Mod
const ll INF = 1e18:
const 11 mod = 998244353;
template <11 MOD = mod>
struct Modular {
 ll value:
 static const 11 MOD_value = MOD;
 Modular(11 v = 0) {
   value = v % MOD:
    if (value < 0) value += MOD;</pre>
 Modular(ll a, ll b) : value(0) {
   *this += a;
    *this /= b;
 Modular& operator+=(Modular const& b) {
    value += b.value;
   if (value >= MOD) value -= MOD;
   return *this;
  Modular& operator -= (Modular const& b) {
    value -= b.value;
   if (value < 0) value += MOD;</pre>
   return *this;
 Modular& operator*=(Modular const& b) {
    value = (11)value * b.value % MOD;
   return *this;
```

```
friend Modular mexp(Modular a, ll e) {
    Modular res = 1;
    while (e) {
     if (e & 1) res *= a;
      a *= a:
      e >>= 1:
    return res:
  friend Modular inverse (Modular a) { return mexp(a, MOD - 2); }
  Modular& operator/=(Modular const& b) { return *this *= inverse(b); }
  friend Modular operator+(Modular a, Modular const b) { return a += b; }
  Modular operator++(int) { return this->value = (this->value + 1) % MOD: }
  Modular operator++() { return this->value = (this->value + 1) % MOD; }
  friend Modular operator - (Modular a, Modular const b) { return a -= b; }
  friend Modular operator - (Modular const a) { return 0 - a; }
  Modular operator -- (int) {
    return this->value = (this->value - 1 + MOD) % MOD:
  }
  Modular operator -- () { return this -> value = (this -> value - 1 + MOD) % MOD; }
  friend Modular operator*(Modular a, Modular const b) { return a *= b; }
  friend Modular operator/(Modular a, Modular const b) { return a /= b; }
  friend std::ostream& operator << (std::ostream& os, Modular const& a) {
    return os << a.value:
  friend bool operator == (Modular const& a, Modular const& b) {
    return a.value == b.value;
  friend bool operator!=(Modular const& a, Modular const& b) {
    return a.value != b.value:
  }
};
5.12 Is Prime
bool isprime(ll n) { // O(sgrt(n))
  if (n < 2) return false;
  if (n == 2) return true:
  if (n % 2 == 0) return false:
  for (11 i = 3; i * i < n; i += 2)
    if (n % i == 0) return false:
  return true;
5.13 Lcm Using Factorization
map<ll, ll> factorization(ll n) {
  map<11, 11> ans;
 for (11 i = 2; i * i <= n; i++) {
   11 count = 0:
    for (; n % i == 0; count++, n /= i)
    if (count) ans[i] = count;
  if (n > 1) ans[n]++;
```

```
return ans:
ll lcm with factorization(ll a. ll b) {
  map<11, 11> fa = factorization(a);
 map<11, 11> fb = factorization(b);
 ll ans = 1:
 for (auto fai : fa) {
   11 k = max(fai.second, fb[fai.first]);
    while (k--) ans *= fai.first;
 }
 return ans;
5.14 Lcm
11 gcd(ll a, ll b) { return b ? gcd(b, a % b) : a; }
11 lcm(ll a, ll b) { return a / gcd(a, b) * b; }
5.15 Modular Inverse Using Phi
map<ll, ll> factorization(ll n) {
  map<11, 11> ans;
  for (11 i = 2; i * i <= n; i++) {
   11 count = 0:
    for (; n % i == 0; count++, n /= i)
    if (count) ans[i] = count:
 if (n > 1) ans [n]++;
  return ans;
ll phi(ll n) {
 if (n == 1) return 1;
  auto fs = factorization(n);
  auto res = n:
 for (auto [p, k] : fs) {
   res /= p;
   res *= (p - 1);
 return res;
11 fexp(ll a, ll n, ll mod) {
 if (n == 0) return 1:
 if (n == 1) return a;
 11 x = fexp(a, n / 2, mod);
 return x * x * (n & 1 ? a : 1) % mod;
11 inv(11 a, 11 mod) { return fexp(a, phi(mod) - 1, mod); }
```

5.16 N Choose K Count

```
* O(nm) time, O(m) space
* equal to n choose k
ll binom(ll n, ll k) {
 if (k > n) return 0;
  vll dp(k + 1, 0);
  dp[0] = 1;
  for (ll i = 1; i <= n; i++)
    for (11 j = k; j > 0; j--) dp[j] = dp[j] + dp[j - 1];
 return dp[k];
5.17
      Permutation Count
const 11 MAX = 18:
vll fv(MAX, -1);
11 factorial(ll n) {
  if (fv[n] != -1) return fv[n];
  if (n == 0) return 1:
  return n * factorial(n - 1);
template <typename T>
11 permutation_count(vector <T> xs) {
  map < T. 11 > h:
  for (auto xi : xs) h[xi]++;
  11 ans = factorial((11)xs.size());
  dbg(ans);
 for (auto [v, cnt] : h) {
   dbg(cnt);
    ans /= cnt;
  return ans;
5.18 Polynomial
using polynomial = vector<11>;
int degree(const polynomial &xs) { return xs.size() - 1; }
ll horner_evaluate(const polynomial &xs, ll x) {
 ll ans = 0;
 11 n = degree(xs);
 for (int i = n; i >= 0; --i) {
    ans *= x;
    ans += xs[i];
 }
  return ans;
polynomial operator+(const polynomial &a, const polynomial &b) {
 int n = degree(a);
  int m = degree(b);
  polynomial r(max(n, m) + 1, 0);
  for (int i = 0; i <= n; ++i) r[i] += a[i];
  for (int j = 0; j \le m; ++j) r[j] += b[j];
  while (!r.empty() and r.back() == 0) r.pop_back();
```

```
if (r.empty()) r.push_back(0);
 return r;
}
polynomial operator*(const polynomial &p, const polynomial &q) {
  int n = degree(p);
 int m = degree(q);
 polynomial r(n + m + 1, 0);
 for (int i = 0; i <= n; ++i)
   for (int j = 0; j \le m; ++j) r[i + j] += (p[i] * q[j]);
5.19 Power Sum
// calculates K^0 + K^1 ... + K^n
11 fastpow(ll a, int n) {
 if (n == 1) return a;
 11 x = fastpow(a, n / 2);
 return x * x * (n & 1 ? a : 1);
ll powersum(ll n, ll k) { return (fastpow(n, k + 1) - 1) / (n - 1); }
5.20 Sieve List Primes
// lsit every prime until MAXN
const ll MAXN = 1e5;
vll list_primes(ll n) { // Nlog * log N
  vll ps:
 bitset < MAXN > sieve;
 sieve.set();
  sieve.reset(1);
  for (ll i = 2; i <= n; ++i) {
   if (sieve[i]) ps.push_back(i);
   for (11 j = i * 2; j <= n; j += i) {
      sieve.reset(j);
   }
 }
  return ps;
    Searching
    Ternary Search Recursive
const double eps = 1e-6;
// IT MUST BE AN UNIMODAL FUNCTION
double f(int x) { return x * x + 2 * x + 4; }
double ternary_search(double 1, double r) {
 if (fabs(f(1) - f(r)) < eps) return f((1 + (r - 1) / 2.0));
  auto third = (r - 1) / 3.0;
```

auto m1 = 1 + third; auto m2 = r - third;

```
// change the signal to find the maximum point.
 return m1 < m2 ? ternary_search(m1, r) : ternary_search(1, m2);</pre>
    Strings
7.1 Rabin Karp
vi rabin_karp(string const &s, string const &t) {
 11 p = 31;
 11 m = 1e9 + 9;
 int S = s.size(), T = t.size();
  vll p_pow(max(S, T));
  p_pow[0] = 1;
 for (int i = 1; i < (int)p_pow.size(); i++) p_pow[i] = (p_pow[i - 1] * p) %
  vll h(T + 1, 0);
  for (int i = 0; i < T; i++)
   h[i + 1] = (h[i] + (t[i] - 'a' + 1) * p_pow[i]) % m;
  for (int i = 0; i < S; i++) h_s = (h_s + (s[i] - 'a' + 1) * p_pow[i]) % m;
  vi occurences;
 for (int i = 0; i + S - 1 < T; i++) {
   ll cur_h = (h[i + S] + m - h[i]) \% m;
   // IT DON'T CONSIDERE CONLISIONS !
    if (cur_h == h_s * p_pow[i] % m) occurences.push_back(i);
  return occurences;
     String Psum
struct strPsum {
 11 n:
 11 k;
 vector < vll > psum;
  strPsum(const string &s): n(s.size()), k(100), psum(k, vll(n + 1)) {
   for (ll i = 1; i <= n; ++i) {
     for (11 j = 0; j < k; ++j) {
        psum[j][i] = psum[j][i - 1];
      psum[s[i - 1]][i]++:
   }
 }
 ll qtd(ll l, ll r, char c) { // [0,n-1]
    return psum[c][r + 1] - psum[c][1];
     Trie Naive
// time: O(n^2) memory: O(n^2)
```

```
using Node = map < char, int >;
using vi = vector<int>;
using Trie = vector < Node >;
Trie build(const string &s) {
 int n = (int)s.size();
 Trie trie(1):
 string suffix;
 for (int i = n - 1; i \ge 0; --i) {
    suffix = s.substr(i) + '#';
   int v = 0; // root
    for (auto c : suffix) {
     if (c == '#') { // makrs the poistion of an occurence
        trie[v][c] = i;
       break:
     }
     if (trie[v][c])
       v = trie[v][c]:
      else {
       trie.push back({});
       trie[v][c] = trie.size() - 1;
        v = trie.size() - 1;
 return trie;
vi search(Trie &trie, string s) {
 int p = 0;
 vi occ:
 for (auto &c : s) {
   p = trie[p][c];
   if (!p) return occ;
 queue < int > q;
 q.push(0);
 while (!q.empty()) {
   auto cur = q.front();
   q.pop();
   for (auto [c, v] : trie[cur]) {
     if (c == '#')
       occ.push_back(v);
     else
        q.push(v);
 }
 return occ;
11 distinct_substr(const Trie &trie) {
 ll cnt = 0:
 queue < int > q;
 q.push(0);
 while (!q.empty()) {
```

```
auto u = q.front():
    q.pop();
    for (auto [c, v] : trie[u]) {
     if (c != '#') {
        cnt++;
        q.push(v);
  }
  return cnt;
    Trees
8.1 Binary Lifting
* far[h][i] = the node that 2^h far from node i
 * sometimes is useful invert the order of loops
* time : O(nlogn)
 * */
const int maxlog = 20;
int far[maxlog + 1][n + 1];
int n;
for (int h = 1; h <= maxlog; h++) {</pre>
 for (int i = 1; i <= n; i++) {
    far[h][i] = far[h - 1][far[h - 1][i]];
      Maximum Distances
* Returns the maximum distance from every node to any other node in the tree.
pll mostDistantFrom(const vector<vll> &adj, ll n, ll root) {
 // 0 indexed
  11 mostDistantNode = root;
  11 nodeDistance = 0;
  queue <pll> q;
  vector < char > vis(n);
  q.emplace(root, 0);
  vis[root] = true;
  while (!q.empty()) {
   auto [node, dist] = q.front();
    q.pop();
    if (dist > nodeDistance) {
      nodeDistance = dist:
      mostDistantNode = node;
   for (auto u : adj[node]) {
     if (!vis[u]) {
        vis[u] = true:
        q.emplace(u, dist + 1);
    }
```

```
return {mostDistantNode, nodeDistance};
11 twoNodesDist(const vector < vll > & adj, 11 n, 11 a, 11 b) {
  queue <pll> q;
 vector < char > vis(n):
 q.emplace(a, 0);
 while (!q.empty()) {
   auto [node, dist] = q.front();
   q.pop();
   if (node == b) return dist;
   for (auto u : adj[node]) {
     if (!vis[u]) {
       vis[u] = true:
        q.emplace(u, dist + 1);
   }
 return -1:
tuple < 11, 11, 11> tree_diameter(const vector < v11> & adj, 11 n) {
 // returns two points of the diameter and the diameter itself
 auto [node1, dist1] = mostDistantFrom(adj, n, 0);
 auto [node2, dist2] = mostDistantFrom(adj, n, node1);
 auto diameter = twoNodesDist(adj, n, node1, node2);
 return make_tuple(node1, node2, diameter);
vll everyDistanceFromNode(const vector < vll > & adj, ll n, ll root) {
 // Single Source Shortest Path, from a given root
 queue <pair <11, 11>> q;
 vll ans(n, -1);
 ans[root] = 0;
 q.emplace(root, 0);
 while (!q.empty()) {
   auto [u, d] = q.front();
   q.pop();
    for (auto w : adj[u]) {
     if (ans[w] != -1) continue;
      ans[w] = d + 1;
     q.emplace(w, d + 1);
  return ans;
vll maxDistances(const vector<vll> &adj, ll n) {
  auto [node1, node2, diameter] = tree_diameter(adj, n);
 auto distances1 = everyDistanceFromNode(adj, n, node1);
 auto distances2 = everyDistanceFromNode(adj, n, node2);
 for (int i = 0: i < n: ++i) ans[i] = max(distances1[i]. distances2[i]):
 return ans;
```

8.3 Tree Diameter

```
pll mostDistantFrom(const vector < vll > & adi. ll n. ll root) {
  // O indexed
 11 mostDistantNode = root:
 11 nodeDistance = 0;
  queue <pll> q;
  vector < char > vis(n):
  q.emplace(root, 0);
  vis[root] = true;
  while (!q.empty()) {
    auto [node, dist] = q.front();
    if (dist > nodeDistance) {
      nodeDistance = dist;
      mostDistantNode = node:
    for (auto u : adj[node]) {
      if (!vis[u]) {
        vis[u] = true;
        q.emplace(u, dist + 1);
   }
  return {mostDistantNode, nodeDistance};
11 twoNodesDist(const vector < vll> &adj, ll n, ll a, ll b) {
 // O indexed
  aueue < pll > a:
  vector < char > vis(n);
  q.emplace(a, 0);
  while (!q.empty()) {
    auto [node, dist] = q.front();
    q.pop();
    if (node == b) {
      return dist;
    for (auto u : adj[node]) {
     if (!vis[u]) {
        vis[u] = true:
        q.emplace(u, dist + 1);
   }
 }
  return -1;
ll tree_diameter(const vector < vll > & adj, ll n) {
 // 0 indexed !!!
  auto [node1, dist1] = mostDistantFrom(adj, n, 0);
  auto [node2, dist2] = mostDistantFrom(adj, n, node1);
  auto diameter = twoNodesDist(adi. n. node1. node2):
  return diameter;
```

9 Settings and macros

9.1 .vimrc

```
set ts=4 sw=4 sta nu rnu sc cindent
set bg=dark ruler clipboard=unnamed,unnamedplus, timeoutlen=100
colorscheme default
nnoremap <C-j> :botright belowright term bash <CR>
syntax on
    degug.cpp
#include <bits/stdc++.h>
using namespace std;
/****** Debug Code ******/
template <typename T>
concept Printable = requires(T t) {
    { std::cout << t } -> std::same as<std::ostream &>:
};
template <Printable T>
void __print(const T &x) {
    cerr << x;
template <size t T>
void __print(const bitset<T> &x) {
    cerr << x:
}
template <typename A, typename B>
void __print(const pair<A, B> &p);
template <typename... A>
void __print(const tuple < A... > &t);
template <typename T>
void __print(stack<T> s);
template <typename T>
void __print(queue < T > q);
template <typename T, typename... U>
void __print(priority_queue < T, U... > q);
template <typename A>
void __print(const A &x) {
    bool first = true:
    cerr << '{';
    for (const auto &i : x) {
        cerr << (first ? "" : ","), __print(i);</pre>
        first = false;
    cerr << '}';
}
template <typename A, typename B>
void __print(const pair<A, B> &p) {
    cerr << '(';
    __print(p.first);
    cerr << ',';
    __print(p.second);
    cerr << ')';
}
template <typename... A>
void __print(const tuple < A... > &t) {
    bool first = true;
    cerr << '(';
    apply(
        [&first](const auto &...args) {
```

```
((cerr << (first ? "" : ","), __print(args), first = false), ...);</pre>
        },
        t);
    cerr << ')':
template <typename T>
void __print(stack<T> s) {
    vector <T> debugVector;
    while (!s.empty()) {
        T t = s.top();
        debugVector.push_back(t);
        s.pop();
    reverse(debugVector.begin(), debugVector.end());
    __print(debugVector);
template <typename T>
void __print(queue < T > q) {
    vector <T> debugVector;
    while (!q.empty()) {
        T t = q.front();
        debugVector.push_back(t);
        q.pop();
    __print(debugVector);
template <typename T, typename... U>
void __print(priority_queue < T, U... > q) {
    vector <T> debugVector;
    while (!q.empty()) {
        T t = q.top();
        debugVector.push_back(t);
        q.pop();
    __print(debugVector);
void _print() { cerr << "]\n"; }</pre>
template <typename Head, typename... Tail>
void _print(const Head &H, const Tail &...T) {
    __print(H);
    if (sizeof...(T)) cerr << ", ";</pre>
    _print(T...);
#define dbg(x...)
    cerr << "[" << #x << "] = [": \
    _print(x)
9.3 .bashrc
cpp() {
  echo ">> COMPILING <<" 1>&2
  g++ -std=c++17 \
      -02 \
      -g \
      -g3 \
      -Wextra \
      -Wshadow \
```

```
-Wformat=2 \
      -Wconversion \
      -fsanitize=address,undefined \
      -fno-sanitize-recover \
      -Wfatal-errors \
      -DDEBUG $1 \
  if [ $? -ne 0 ]; then
      echo ">> FAILED <<" 1>&2
      return 1
  fi
  echo ">> DONE << " 1>&2
  time ./a.out ${0:2}
prepare() {
    for i in {a..z}
       cp macro.cpp $i.cpp
       touch $i.py
    done
    for i in {1..10}
        touch in${i}
        touch out${i}
        touch ans${i}
    done
9.4 macro.cpp
#include <bits/stdc++.h>
```

using namespace std;

#include "debug.cpp"

#ifdef DEBUG

#else

```
#define dbg(...) 666
#endif
#define endl '\n'
#define fastio
   ios_base::sync_with_stdio(false); \
   cin.tie(0);
   cout.tie(0):
#define len(__x) (ll) __x.size()
using ll = long long;
using vll = vector<11>;
using pll = pair<11, 11>;
using v112d = vector < v11 >;
using vi = vector<int>;
using vi2d = vector<vi>;
using pii = pair <int, int>;
using vii = vector<pii>;
using vc = vector < char >;
#define all(a) a.begin(), a.end()
#define snd second
#define fst first
#define pb(___x) push_back(___x)
#define mp(__a, __b) make_pair(__a, __b)
#define eb(___x) emplace_back(___x)
const ll INF = 1e18:
void run() {
int32_t main(void) {
   fastio:
   int t;
   t = 1:
   // cin >> t;
    while (t--) run();
```