ICPC - Notebook

Contents					Fast Exp	
	data structures 1.1 Ordered Set Gnu Pbds	2 2 2 2 2 3 3 4 4 4		7.10 7.11 7.12 7.13 7.14 7.15 7.16 7.17 7.18 7.19	Lcm-using-factorization 1 Euler-phi 1 Polynomial 1 Integer Mod 1 Count Divisors Memo 1 Lcm 1 Factorial-factorization 1 Factorization-with-primes 1 Modular-inverse-using-phi 1 Factorization 1 Gcd 1 Combinatorics With Repetitions 1	14 14 15 15 15 16 16
2	graphs 2.1 Scc-nodes-(kosajaru) 2.2 2-sat-(struct) 2.3 Floyd Warshall 2.4 Topological-sorting 2.5 Lowest Common Ancestor Sparse Table 2.6 Count-scc-(kosajaru) 2.7 Kruskal 2.8 Scc-(struct) 2.9 Check-bipartite 2.10 Dijkstra	4 5 5 6 6 7 7	8	8.2	gs 1 Rabin-karp 1 Trie-naive 1 String-psum 1	16
3	extras 3.1 Binary To Gray	7 7 7 10				
4	dynamic programming4.1 Edit Distance4.2 Money Sum Bottom Up4.3 Knapsack Dp Values 014.4 Tsp	10 11				
5	trees 5.1 Binary-lifting	11 11 11 12 12				
6	searching 6.1 Ternary Search Recursive	13 13				
7	math7.1 Power-sum7.2 Sieve-list-primes7.3 Factorial7.4 Permutation-count7.5 N-choose-k-count7.6 Gcd-using-factorization					

data structures

struct SegmentTree {

Ordered Set Gnu Pbds

```
1 #include <ext/pb_ds/assoc_container.hpp>
2 #include <ext/pb_ds/tree_policy.hpp>
3 using namespace __gnu_pbds;
4 template <typename T>
5 // using ordered_set = tree<T, null_type, less<T>,
     rb_tree_tag,
6 // tree_order_statistics_node_update>;
8 // if you want to find the elements less or equal :p
9 using ordered_set = tree<T, null_type, less_equal<T>,
      rb_tree_tag,
     tree_order_statistics_node_update>;
```

1.2 Segtree Rmq Lazy Max Update

```
int N:
      vll ns, lazy;
      SegmentTree(const vll &xs) : N(xs.size()), ns(4 * ^{10}
       N, 0), lazy(4 * N, 0) {
           for (size_t i = 0; i < xs.size(); ++i) {</pre>
               update(i, i, xs[i]);
      }
      void update(int a, int b, ll value) { update(1,
9
      0, N - 1, a, b, value); }
      void update(int node, int L, int R, int a, int b,
       ll value) {
          if (lazy[node]) {
               ns[node] = max(ns[node], lazy[node]);
               if (L < R) {
                   lazy[2 * node] = max(lazy[2 * node],
14
      lazy[node]);
                   lazy[2 * node + 1] = max(lazy[2 *
      node + 1], lazy[node]);
16
               lazy[node] = 0;
           }
           if (a > R or b < L) return;</pre>
19
           if (a \le L \text{ and } R \le b) {
               ns[node] = max(ns[node], value);
21
               if (L < R) {
23
                   lazy[2 * node] = max(value, lazy[2 *
      node]);
                   lazy[2 * node + 1] = max(value, lazy
      [2 * node + 1]);
               return;
26
           }
           update(2 * node, L, (L + R) / 2, a, b, value)
           update(2 * node + 1, (L + R) / 2 + 1, R, a, b^{36}
        value):
           ns[node] = max(ns[node * 2], ns[node * 2 +
30
      1]);
      }
31
33
      11 RMQ(int a, int b) { return RMQ(1, 0, N - 1, a,
       b); }
      11 RMQ(int node, int L, int R, int a, int b) {
           if (lazy[node]) {
35
36
               ns[node] = max(ns[node], lazy[node]);
               if (L < R) {
37
                   lazy[node * 2] = max(lazy[node * 2],
      lazy[node]);
                   lazy[node * 2 + 1] = max(lazy[node *
      2 + 1], lazy[node]);
40
               lazy[node] = 0;
          }
42
43
```

```
if (a > R \text{ or } b < L) \text{ return } 0;
            if (a <= L and R <= b) return ns[node];</pre>
            11 x = RMQ(2 * node, L, (L + R) / 2, a, b);
            11 y = RMQ(2 * node + 1, (L + R) / 2 + 1, R,
          b);
           return max(x, y);
50 };
```

Segtree Rmq Lazy Range 1.3

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```
struct SegmentTree {
     int N;
      vll ns, lazy;
      SegmentTree(const vll &xs)
         : N(xs.size()), ns(4 * N, INT_MAX), lazy(4 *
        0) {
          for (size_t i = 0; i < xs.size(); ++i) update</pre>
      (i, i, xs[i]);
     void update(int a, int b, ll value) { update(1,
     0, N - 1, a, b, value); }
      void update(int node, int L, int R, int a, int b,
      11 value) {
          if (lazy[node]) {
              ns[node] = ns[node] == INT_MAX ? lazy[
      node] : ns[node] + lazy[node];
              if (L < R) {
                  lazy[2 * node] += lazy[node];
                  lazy[2 * node + 1] += lazy[node];
              lazy[node] = 0;
          if (a > R or b < L) return;
          if (a <= L and R <= b) \{
              ns[node] = ns[node] == INT_MAX ? value :
     ns[node] + value;
              if (L < R) {</pre>
                  lazy[2 * node] += value;
                  lazy[2 * node + 1] += value;
              }
              return;
          update(2 * node, L, (L + R) / 2, a, b, value)
          update(2 * node + 1, (L + R) / 2 + 1, R, a, b
      , value);
          ns[node] = min(ns[2 * node], ns[2 * node +
     11):
     ll RMQ(int a, int b) { return RMQ(1, 0, N - 1, a,
      b): }
      11 RMQ(int node, int L, int R, int a, int b) {
          if (lazy[node]) {
              ns[node] = ns[node] == INT_MAX ? lazy[
      node] : ns[node] + lazy[node];
              if (L < R) {
                  lazy[2 * node] += lazy[node];
                  lazy[2 * node + 1] += lazy[node];
              lazy[node] = 0;
          if (a > R or b < L) return INT_MAX;</pre>
          if (a <= L and R <= b) return ns[node];</pre>
          11 x = RMQ(2 * node, L, (L + R) / 2, a, b);
          11 y = RMQ(2 * node + 1, (L + R) / 2 + 1, R,
     a, b);
          return min(x, y);
```

Segtree Point Rmq 1.4

```
1 class SegTree {
    public:
     int n;
```

48 }:

```
vector<ll> st:
       SegTree(const vector<11> &v) : n((int)v.size()), 29
       st(n * 4 + 1, LLONG_MAX) {
           for (int i = 0; i < n; ++i) update(i, v[i]); 31</pre>
       void update(int p, ll v) { update(1, 0, n - 1, p, 33
       11 RMQ(int 1, int r) { return RMQ(1, 0, n - 1, 1, 35
10
     private:
12
       void update(int node, int 1, int r, int p, 11 v)
           if (p < l or p > r) return; // fora do
       \verb"intervalo".
                                                             40
                                                             41
14
           if (1 == r) {
                                                             42
               st[node] = v;
16
                                                             43
                return;
                                                             44
           }
18
19
                                                             45
           int mid = 1 + (r - 1) / 2;
                                                             46
20
21
                                                             47
           update(node * 2, 1, mid, p, v);
           update(node * 2 + 1, mid + 1, r, p, v);
23
                                                             49
                                                             50
           st[node] = min(st[node * 2], st[node * 2 +
25
                                                             51
       1]);
                                                             52
26
       }
                                                             53
27
                                                             54
       11 RMQ(int node, int L, int R, int l, int r) {
                                                             55
           if (1 <= L and r >= R) return st[node];
29
                                                             56
           if (L > r or R < 1) return LLONG_MAX;</pre>
                                                             57
30
           if (L == R) return st[node];
                                                             58
31
                                                             59
32
           int mid = L + (R - L) / 2;
34
                                                             61
           return min(RMQ(node * 2, L, mid, 1, r),
                       RMQ(node * 2 + 1, mid + 1, R, 1, r_{63})
36
       ));
       }
38 };
                                                             65
                                                             66
                                                             67 };
```

Segtree Rsq Lazy Range Sum

```
1 struct SegTree {
      int N:
      vector <11> ns, lazy;
      SegTree(const vector<1l> &xs) : N(xs.size()), ns
       (4 * N, 0), lazy(4 * N, 0) {
          for (size_t i = 0; i < xs.size(); ++i) update 5</pre>
       (i, i, xs[i]);
      }
       void update(int a, int b, ll value) { update(1,
      0, N - 1, a, b, value); }
      void update(int node, int L, int R, int a, int b,
11
       11 value) {
                                                            10
           // Lazy propagation
           if (lazy[node]) {
               ns[node] += (R - L + 1) * lazy[node];
               if (L < R) // Se o ón ano é uma folha,
16
                                                            14
      propaga
                                                            15
                                                            16
                    lazy[2 * node] += lazy[node];
                   lazy[2 * node + 1] += lazy[node];
19
                                                            17
20
                                                            18
                                                            19
               lazy[node] = 0;
                                                            20
           }
                                                            21
24
                                                            22
           if (a > R or b < L) return;
26
                                                            24
           if (a \le L \text{ and } R \le b) {
                                                            25
```

```
ns[node] += (R - L + 1) * value;
        if (L < R) {</pre>
            lazy[2 * node] += value;
            lazy[2 * node + 1] += value;
        return;
    update(2 * node, L, (L + R) / 2, a, b, value)
    update(2 * node + 1, (L + R) / 2 + 1, R, a, b)
, value);
    ns[node] = ns[2 * node] + ns[2 * node + 1];
}
ll RSQ(int a, int b) { return RSQ(1, 0, N - 1, a,
b): }
11 RSQ(int node, int L, int R, int a, int b) {
    if (lazy[node]) {
        ns[node] += (R - L + 1) * lazy[node];
        if (L < R) {</pre>
            lazy[2 * node] += lazy[node];
             lazy[2 * node + 1] += lazy[node];
        lazy[node] = 0;
    if (a > R \text{ or } b < L) \text{ return } 0;
    if (a <= L and R <= b) return ns[node];</pre>
    11 x = RSQ(2 * node, L, (L + R) / 2, a, b);
    11 y = RSQ(2 * node + 1, (L + R) / 2 + 1, R,
a, b);
    return x + v;
```

Segtree Rxq Lazy Range Xor

```
struct SegTree {
     int N;
     vector<1l> ns, lazy;
     SegTree(const vector<11> &xs) : N(xs.size()), ns
     (4 * N, 0), lazy(4 * N, 0) {
         for (size_t i = 0; i < xs.size(); ++i) update</pre>
     (i, i, xs[i]);
     void update(int a, int b, ll value) { update(1,
     0, N - 1, a, b, value); }
     void update(int node, int L, int R, int a, int b,
      ll value) {
          // Lazy propagation
          if (lazy[node]) {
              ns[node] ^= lazy[node];
              if (L < R) // Se o ón ano é uma folha,
     propaga
                  lazy[2 * node] ^= lazy[node];
                  lazy[2 * node + 1] ^= lazy[node];
             lazy[node] = 0;
          if (a > R or b < L) return;
```

```
self.p[py] = self.p[px]
          if (a \le L \text{ and } R \le b) {
                                                                          self.size[px] += self.size[py]
                                                           29
              ns[node] ^= value;
28
                                                           30
                                                                      else:
                                                                          self.p[px] = self.p[py]
                                                          31
               if (L < R) {
                                                                          self.size[py] += self.size[px]
30
                   lazy[2 * node] ^= value;
31
                   lazy[2 * node + 1] ^= value;
                                                             1.8
                                                                   Dsu
33
                                                           1 struct DSU {
               return:
                                                           2
                                                                vector < int > ps;
          }
36
                                                                 vector<int> size;
                                                           3
                                                                 DSU(int N) : ps(N + 1), size(N + 1, 1) { iota(ps.)}
           update(2 * node, L, (L + R) / 2, a, b, value)
38
                                                                 begin(), ps.end(), 0); }
                                                                 int find_set(int x) { return ps[x] == x ? x : ps[
          update (2 * node + 1, (L + R) / 2 + 1, R, a, b)
39
                                                                 x] = find_set(ps[x]); }
      , value);
                                                                 bool same_set(int x, int y) { return find_set(x)
40
                                                                 == find_set(y); }
          ns[node] = ns[2 * node] ^ ns[2 * node + 1];
41
                                                                 void union_set(int x, int y) {
42
                                                                      if (same_set(x, y)) return;
43
      ll rxq(int a, int b) { return RSQ(1, 0, N - 1, a,
44
                                                                      int px = find_set(x);
       b); }
                                                                      int py = find_set(y);
45
      ll rxq(int node, int L, int R, int a, int b) {
                                                                      if (size[px] < size[py]) swap(px, py);</pre>
47
          if (lazy[node]) {
                                                           14
               ns[node] ^= lazy[node];
48
                                                                      ps[py] = px;
                                                           15
49
                                                                      size[px] += size[py];
                                                           16
               if (L < R) {
50
                                                           17
                   lazy[2 * node] ^= lazy[node];
                                                          18 };
                   lazy[2 * node + 1] ^= lazy[node];
                                                                    Sparse Table Rmq
                                                             1.9
54
               lazy[node] = 0;
          }
                                                           1 /*
56
57
                                                                      Sparse table implementation for rmg.
                                                           2
          if (a > R \text{ or } b < L) \text{ return } 0;
                                                                      build: O(NlogN)
                                                           3
                                                                      query: 0(1)
59
          if (a <= L and R <= b) return ns[node];</pre>
                                                           5 */
                                                           6 int fastlog2(ll x) {
61
          11 x = rxq(2 * node, L, (L + R) / 2, a, b);
                                                                 ull i = x;
62
          11 y = rxq(2 * node + 1, (L + R) / 2 + 1, R,
                                                                  return i ? __builtin_clzll(1) - __builtin_clzll(i
63
      a, b);
                                                                 ) : -1:
                                                           9 }
65
          return x ^ y;
                                                          10 template <typename T>
                                                           11 class SparseTable {
66
67 };
                                                           12
                                                                public:
                                                                 int N:
                                                           13
        Dsu
                                                           14
                                                                 int K;
                                                           15
                                                                 vector < vector < T >> st;
                                                                  SparseTable(vector <T> vs)
                                                           16
1 class DSU:
                                                                      : N((int)vs.size()), K(fastlog2(N) + 1), st(K
                                                           17
      def __init__(self, n):
                                                                   + 1, vector < T > (N + 1)) {
          self.n = n
                                                                      copy(vs.begin(), vs.end(), st[0].begin());
           self.p = [x for x in range(0, n + 1)]
                                                           19
          self.size = [0 for i in range(0, n + 1)]
                                                                      for (int i = 1; i <= K; ++i)</pre>
                                                           20
                                                                          for (int j = 0; j + (1 << i) <= N; ++j)
                                                           21
      def find_set(self, x): # log n
                                                                              st[i][j] = min(st[i - 1][j], st[i -
                                                           22
          if self.p[x] == x:
                                                                 1][j + (1 << (i - 1))]);
              return x
                                                           23
10
           else:
                                                                 T RMQ(int 1, int r) { // [1, r], 0 indexed
                                                           24
               self.p[x] = self.find_set(self.p[x])
11
                                                                      int i = fastlog2(r - l + 1);
                                                           25
               return self.p[x]
                                                                      return min(st[i][1], st[i][r - (1 << i) + 1])
                                                           26
13
      def same_set(self, x, y): # log n
14
          return bool(self.find_set(x) == self.find_set
28 };
16
                                                                  graphs
                                                             \mathbf{2}
      def union_set(self, x, y): # log n
17
          px = self.find_set(x)
19
          py = self.find_set(y)
                                                             2.1 Scc-nodes-(kosajaru)
20
           if px == py:
21
              return
                                                           1 /*
                                                           2 * 0(n+m)
           size_x = self.size[px]
                                                           3 * Returns a pair <a, b>
24
           size_y = self.size[py]
                                                                      a: number of SCCs
                                                                      b: vector of size n, where b[i] is the SCC id
26
          if size_x > size_y:
                                                                  of node i
```

26

```
7 void dfs(ll u, vchar &visited, const vll2d &g, vll & 37
                                                                    11 j = 0;
      scc, bool buildScc, ll id,
                                                                    for (auto &v : order) {
           vll &sccid) {
                                                                        if (comp[v] == -1) dfs2(v, j++);
9
      visited[u] = true;
10
      sccid[u] = id;
                                                         41
      for (auto &v : g[u])
                                                                    assignment.assign(n / 2, false);
         if (!visited[v]) dfs(v, visited, g, scc,
                                                                    for (int i = 0; i < n; i += 2) {
12
                                                         43
                                                                        // x and !x belong to the same SCC
      buildScc, id, sccid);
13
                                                         45
                                                                        if (comp[i] == comp[i + 1]) {
      // if it's the first pass, add the node to the
                                                                            solvable = false;
14
                                                         46
                                                         47
                                                                             return false;
      if (buildScc) scc.eb(u);
15
                                                         48
16 }
                                                                         assignment[i / 2] = comp[i] > comp[i +
17
                                                         50
18 pair<11, vll> kosajaru(vll2d &g) {
                                                                1];
19
      ll n = len(g);
                                                         51
      vll scc;
                                                                    solvable = true;
                                                         52
20
      vchar vis(n);
                                                                    return true;
      vll sccid(n);
22
                                                         54
      for (ll i = 0; i < n; i++)</pre>
                                                         55
23
          if (!vis[i]) dfs(i, vis, g, scc, true, 0,
                                                                void add_disjunction(int a, bool na, int b, bool
24
                                                         56
      sccid):
                                                                nb) {
25
                                                                    a = (2 * a) ^na;
                                                                    b = (2 * b) ^n b;
      // build the transposed graph
26
                                                         58
                                                                    int neg_a = a ^ 1;
      v112d gt(n);
                                                         59
                                                                    int neg_b = b ^ 1;
      for (int i = 0; i < n; ++i)</pre>
28
                                                         60
          for (auto &v : g[i]) gt[v].eb(i);
                                                                    adj[neg_a].push_back(b);
29
                                                         61
30
                                                         62
                                                                    adj[neg_b].push_back(a);
      // run the dfs on the previous scc order
                                                                    adj_t[b].push_back(neg_a);
                                                         63
31
      11 id = 1;
                                                         64
                                                                    adj_t[a].push_back(neg_b);
      vis.assign(n, false);
33
                                                         65
      for (ll i = len(scc) - 1; i \ge 0; i--)
34
                                                         66 };
          if (!vis[scc[i]]) {
35
                                                          2.3 Floyd Warshall
36
              dfs(scc[i], vis, gt, scc, false, id++,
      sccid);
        }
                                                          vector <vll> floyd_warshall(const vector <vll> &adj, ll
      return {id - 1, sccid};
                                                                 n) {
39 }
                                                          2
                                                                auto dist = adj;
  2.2 2-sat-(struct)
                                                                for (int i = 0; i < n; ++i) {
                                                                    for (int j = 0; j < n; ++j) {
                                                          5
                                                                        for (int k = 0; k < n; ++k) {
                                                          6
struct SAT2 {
                                                                            dist[j][k] = min(dist[j][k], dist[j][
                                                          7
      11 n;
                                                                i] + dist[i][k]);
      vll2d adj, adj_t;
                                                                        }
      vc used:
                                                                    }
                                                          9
      vll order, comp;
                                                         10
      vc assignment;
                                                         11
                                                                return dist;
      bool solvable:
                                                         12 }
      SAT2(11 _n)
9
          : n(2 * _n),
                                                            2.4 Topological-sorting
            adj(n),
10
11
            adj_t(n),
            used(n),
                                                          1 /*
12
            order(n),
                                                          2 * O(V)
13
            comp(n, -1),
14
                                                          3 * assumes:
            assignment(n / 2) {}
                                                                  * vertices have index [0, n-1]
15
      void dfs1(int v) {
                                                          s * if is a DAG:
16
                                                          6 * returns a topological sorting
          used[v] = true;
17
          for (int u : adj[v]) {
                                                          7 * else:
18
               if (!used[u]) dfs1(u);
                                                                  * returns an empty vector
19
                                                          9 * */
20
                                                         10 enum class state { not_visited, processing, done };
          order.push_back(v);
22
      }
                                                         11 bool dfs(const vector < vll> &adj, ll s, vector < state>
                                                                &states, vll &order) {
23
      void dfs2(int v, int cl) {
24
                                                                states[s] = state::processing;
          comp[v] = cl;
                                                                for (auto &v : adj[s]) {
25
                                                         13
          for (int u : adj_t[v]) {
                                                         14
                                                                    if (states[v] == state::not_visited) {
              if (comp[u] == -1) dfs2(u, cl);
                                                                        if (not dfs(adj, v, states, order))
27
                                                         15
28
                                                                return false:
                                                                    } else if (states[v] == state::processing)
29
      }
                                                         16
                                                         17
                                                                        return false;
30
      bool solve_2SAT() {
                                                         18
          // find and label each SCC
                                                                states[s] = state::done;
32
                                                         19
          for (int i = 0; i < n; ++i) {
                                                         20
                                                                order.pb(s);
              if (!used[i]) dfs1(i);
34
                                                         21
                                                                return true;
```

reverse(all(order));

6 * */

35

22 }

```
23 vll topologicalSorting(const vector < vll > & adj) {
                                                          57
      11 n = len(adj);
                                                                 int lca(int a, int b) {
24
      vll order;
                                                                     int 1 = min(first[a], first[b]);
25
                                                          59
      vector < state > states(n, state::not_visited);
                                                                      int r = max(first[a], first[b]);
                                                          60
      for (int i = 0; i < n; ++i) {
                                                                      return st.RMQ(1, r);
                                                          61
          if (states[i] == state::not_visited) {
28
                                                          62
               if (not dfs(adj, i, states, order))
                                                          63 };
      return {};
                                                             2.6 Count-scc-(kosajaru)
          }
31
      }
      reverse(all(order));
32
                                                           void dfs(ll u, vchar &visited, const vll2d &g, vll &
33
      return order;
                                                                 scc, bool buildScc) {
34 }
                                                                 visited[u] = true;
                                                                 for (auto &v : g[u])
  2.5 Lowest Common Ancestor Sparse Table
                                                                      if (!visited[v]) dfs(v, visited, g, scc,
                                                                 buildScc);
1 int fastlog2(11 x) {
                                                                 // if it's the first pass, add the node to the
      ull i = x;
                                                                 SCC
      return i ? __builtin_clzll(1) - __builtin_clzll(i
3
                                                                 if (buildScc) scc.eb(u);
      ) : -1;
                                                           8 }
4 }
5 template <typename T>
                                                          10 ll kosajaru(vll2d &g) {
6 class SparseTable {
                                                                 ll n = len(g);
                                                          11
     public:
                                                                 vll scc;
                                                          12
      int N;
                                                                 vchar vis(n):
                                                          13
      int K;
9
                                                                 for (ll i = 0; i < n; i++)
       vector < vector < T >> st;
                                                                     if (!vis[i]) dfs(i, vis, g, scc, true);
                                                          15
      SparseTable(vector <T> vs)
11
          : N((int)vs.size()), K(fastlog2(N) + 1), st(K^{16}
                                                                 // build the transposed graph
       + 1, vector <T > (N + 1)) {
                                                                 v112d gt(n);
          copy(vs.begin(), vs.end(), st[0].begin());
13
                                                                 for (int i = 0; i < n; ++i)</pre>
                                                                     for (auto &v : g[i]) gt[v].eb(i);
                                                          20
          for (int i = 1; i <= K; ++i)</pre>
15
                                                          21
               for (int j = 0; j + (1 << i) <= N; ++j)
                                                          22
                                                                 // run the dfs on the previous scc order
                   st[i][j] = min(st[i - 1][j], st[i -
                                                                 11 \ \text{scccnt} = 0;
                                                          23
      1][j + (1 << (i - 1))]);
                                                                 vis.assign(n, false);
                                                                 for (ll i = len(scc) - 1; i \ge 0; i--)
      SparseTable() {}
                                                          25
19
                                                                      if (!vis[scc[i]]) dfs(scc[i], vis, gt, scc,
      T RMQ(int 1, int r) {
                                                                 false), scccnt++;
          int i = fastlog2(r - l + 1);
21
                                                                 return scccnt;
          return min(st[i][1], st[i][r - (1 << i) + 1]) ^{27}
23
                                                             2.7
                                                                  Kruskal
24 };
25 class LCA {
     public:
                                                           1 class DSU:
27
      int p;
                                                                 def __init__(self, n):
      int n;
                                                                     self.n = n
28
                                                           3
29
      vi first;
                                                           4
                                                                      self.p = [x for x in range(0, n + 1)]
                                                                      self.size = [0 for i in range(0, n + 1)]
      vector < char > visited;
30
                                                           5
      vi vertices;
      vi height;
                                                                 def find_set(self, x):
32
      SparseTable < int > st;
                                                           8
                                                                     if self.p[x] == x:
33
                                                                         return x
                                                           9
34
      LCA(const vector < vi> &g)
                                                                      else:
                                                          10
35
          : p(0),
                                                                          self.p[x] = self.find_set(self.p[x])
                                                          11
37
            n((int)g.size()),
                                                          12
                                                                          return self.p[x]
            first(n + 1),
                                                          13
38
            visited(n + 1, 0),
39
                                                          14
                                                                 def same_set(self, x, y):
            height(n + 1) {
                                                                      return bool(self.find_set(x) == self.find_set
40
                                                          15
           build_dfs(g, 1, 1);
                                                                 (y))
41
           st = SparseTable <int > (vertices);
42
      }
                                                                 def union_set(self, x, y):
44
                                                                     px = self.find_set(x)
      void build_dfs(const vector<vi> &g, int u, int hi 19
                                                                     py = self.find_set(y)
45
          visited[u] = true;
                                                                      if px == py:
                                                          21
46
          height[u] = hi;
                                                          22
                                                                         return
          first[u] = vertices.size();
48
                                                          23
49
           vertices.push_back(u);
                                                          24
                                                                      size_x = self.size[px]
           for (auto uv : g[u]) {
                                                          25
                                                                      size_y = self.size[py]
50
               if (!visited[uv]) {
51
                                                          26
                   build_dfs(g, uv, hi + 1);
                                                                      if size_x > size_y:
                                                          27
                                                                          self.p[py] = self.p[px]
                   vertices.push_back(u);
53
                                                          28
                                                                          self.size[px] += self.size[py]
          }
55
                                                          30
                                                                      else:
      }
                                                                          self.p[px] = self.p[py]
56
                                                          31
```

```
self.size[py] += self.size[px]
                                                                 vll color(n, INF);
                                                           6
32
                                                                 color[s] = 0;
                                                                 bool isBipartite = true;
34
                                                                 while (!q.empty() && isBipartite) {
35 def kruskal(gv, n):
36
                                                                     11 u = q.front();
                                                                     q.pop();
37
      Receives te list of edges as a list of tuple in
                                                          11
      the form:
                                                                     for (auto &v : adj[u]) {
                                                                         if (color[v] == INF) {
          d, u, v
                                                          13
          d: distance between u and v
                                                                              color[v] = 1 - color[u];
40
      And also n as the total of verties.
                                                          15
                                                                              q.push(v);
                                                                         } else if (color[v] == color[u]) {
41
                                                          16
      dsu = DSU(n)
                                                          17
                                                                              return false;
43
                                                          18
      c = 0
                                                                     }
                                                                 }
45
      for e in gv:
                                                          20
          d, u, v = e
                                                          21
                                                                 return true;
46
          if not dsu.same_set(u, v):
47
                                                          22 }
              c += d
48
                                                             2.10 Dijkstra
               dsu.union_set(u, v)
50
      return c
                                                           1 11 __inf = LLONG_MAX >> 5;
                                                           vll dijkstra(const vector<vector<pll>>> &g, ll n) {
  2.8 Scc-(struct)
                                                                 priority_queue < pll , vector < pll > , greater < pll >> pq
1 struct SCC {
                                                                 vll dist(n, __inf);
                                                           4
      11 N;
                                                                 vector < char > vis(n);
                                                           5
      vll2d adj, tadj;
                                                                 pq.emplace(0, 0);
      vll todo, comps, comp;
                                                                 dist[0] = 0;
      vector<set<11>> sccadj;
                                                                 while (!pq.empty()) {
      vchar vis:
                                                                     auto [d1, v] = pq.top();
      SCC(11 _N) : N(_N), adj(_N), tadj(_N), comp(_N,
                                                                     pq.pop();
      -1), sccadj(_N), vis(_N) {}
                                                                     if (vis[v]) continue;
                                                                     vis[v] = true;
      void add_edge(ll x, ll y) { adj[x].eb(y), tadj[y _{13}
9
      ].eb(x); }
                                                                     for (auto [d2, u] : g[v]) {
                                                          14
                                                                         if (dist[u] > d1 + d2) {
      void dfs(ll x) {
                                                                             dist[u] = d1 + d2;
                                                          16
          vis[x] = 1:
12
                                                                              pq.emplace(dist[u], u);
          for (auto &y : adj[x])
                                                                         }
                                                          18
              if (!vis[y]) dfs(y);
14
                                                                     }
                                                          19
           todo.pb(x);
                                                          20
                                                                 }
                                                          21
                                                                 return dist;
      void dfs2(11 x, 11 v) {
17
                                                          22 }
           comp[x] = v;
          for (auto &y : tadj[x])
19
                                                             3
                                                                  extras
              if (comp[y] == -1) dfs2(y, v);
20
21
      void gen() {
22
                                                             3.1
                                                                   Binary To Gray
          for (11 i = 0; i < N; ++i)
23
              if (!vis[i]) dfs(i);
24
                                                           string binToGray(string bin) {
          reverse(all(todo));
                                                              string gray(bin.size(), '0');
26
          for (auto &x : todo)
                                                           3
                                                                 int n = bin.size() - 1;
              if (comp[x] == -1) {
                                                                 gray[0] = bin[0];
                                                           4
                   dfs2(x, x);
                                                                 for (int i = 1; i <= n; i++) {</pre>
                                                           5
                   comps.pb(x);
29
                                                                     gray[i] = '0' + (bin[i - 1] == '1') ^ (bin[i]
      }
31
                                                                 }
32
                                                                 return gray;
      void genSCCGraph() {
33
                                                           9 }
          for (ll i = 0; i < N; ++i) {</pre>
34
               for (auto &j : adj[i]) {
                                                             3.2 Bigint
                   if (comp[i] != comp[j]) {
36
                       sccadj[comp[i]].insert(comp[j]);
38
                                                           1 const int maxn = 1e2 + 14, lg = 15;
              }
39
                                                           2 const int base = 1000000000;
          }
40
                                                           3 const int base_digits = 9;
      }
41
                                                           4 struct bigint {
42 };
                                                                 vector<int> a;
                                                                 int sign;
        Check-bipartite
                                                                 int size() {
1 // O(V)
                                                                     if (a.empty()) return 0;
2 bool checkBipartite(const ll n, const vector<vll> &
                                                                     int ans = (a.size() - 1) * base_digits;
      adi) {
                                                                     int ca = a.back();
                                                          11
      11 s = 0;
                                                                     while (ca) ans++, ca \neq 10;
      queue <11> q;
                                                          13
                                                                     return ans;
      q.push(s);
                                                          14
```

```
bigint operator^(const bigint &v) {
                                                    86
    bigint ans = 1, a = *this, b = v;
    while (!b.isZero()) {
                                                           void operator*=(int v) {
                                                    88
        if (b % 2) ans *= a;
                                                               if (v < 0) sign = -sign, v = -v;
                                                    89
                                                               for (int i = 0, carry = 0; i < (int)a.size()</pre>
        a *= a, b /= 2;
                                                    90
    }
                                                           || carry; ++i) {
    return ans;
                                                                    if (i == (int)a.size()) a.push_back(0);
                                                    91
                                                                    long long cur = a[i] * (long long)v +
                                                    92
string to_string() {
                                                           carrv:
    stringstream ss;
                                                    93
                                                                    carry = (int)(cur / base);
    ss << *this;
                                                                    a[i] = (int)(cur % base);
                                                    94
                                                                    // asm("divl %%ecx" : "=a"(carry), "=d"(a
    string s;
                                                    95
    ss >> s;
                                                           [i]) :
    return s;
                                                                    // "A"(cur), "c"(base));
                                                               }
}
                                                    97
int sumof() {
                                                    98
                                                               trim();
    string s = to_string();
                                                    99
    int ans = 0;
                                                    100
    for (auto c : s) ans += c - '0';
                                                           bigint operator*(int v) const {
    return ans:
                                                               bigint res = *this;
}
                                                               res *= v;
/*</arpa>*/
                                                    104
                                                               return res;
bigint() : sign(1) {}
                                                   105
                                                   106
                                                           void operator*=(long long v) {
bigint(long long v) { *this = v; }
                                                   107
                                                               if (v < 0) sign = -sign, v = -v;
                                                    108
bigint(const string &s) { read(s); }
                                                               if (v > base) {
                                                    109
                                                                    *this = *this * (v / base) * base + *this
                                                    110
                                                            * (v % base);
void operator=(const bigint &v) {
    sign = v.sign;
                                                                    return:
                                                    111
    a = v.a;
                                                               }
                                                               for (int i = 0, carry = 0; i < (int)a.size()</pre>
                                                           || carry; ++i) {
void operator=(long long v) {
                                                   114
                                                                    if (i == (int)a.size()) a.push_back(0);
    sign = 1;
                                                    115
                                                                    long long cur = a[i] * (long long)v +
    a.clear();
                                                           carry;
    if (v < 0) sign = -1, v = -v;
                                                                    carry = (int)(cur / base);
    for (; v > 0; v = v / base) a.push_back(v %
                                                                    a[i] = (int)(cur % base);
                                                                    // asm("divl %%ecx" : "=a"(carry), "=d"(a
base);
                                                    118
                                                            [i]) :
                                                                    // "A"(cur), "c"(base));
                                                    119
bigint operator+(const bigint &v) const {
                                                               }
                                                    120
    if (sign == v.sign) {
                                                               trim();
                                                    121
        bigint res = v;
        for (int i = 0, carry = 0;
                                                           bigint operator*(long long v) const {
                                                    124
             i < (int)max(a.size(), v.a.size())</pre>
                                                               bigint res = *this;
|| carry; ++i) {
                                                               res *= v;
            if (i == (int)res.a.size()) res.a.
                                                               return res:
                                                    127
push_back(0);
                                                    128
            res.a[i] += carry + (i < (int)a.size 129
() ? a[i] : 0);
                                                           friend pair < bigint , bigint > divmod(const bigint &
                                                   130
            carry = res.a[i] >= base;
                                                           a1, const bigint &b1) {
                                                               int norm = base / (b1.a.back() + 1);
            if (carry) res.a[i] -= base;
                                                   131
        }
                                                               bigint a = a1.abs() * norm;
                                                               bigint b = b1.abs() * norm;
        return res:
                                                    133
    }
                                                               bigint q, r;
                                                   134
    return *this - (-v);
                                                    135
                                                               q.a.resize(a.a.size());
}
                                                    136
                                                               for (int i = a.a.size() - 1; i >= 0; i--) {
                                                    137
bigint operator-(const bigint &v) const {
                                                                   r *= base;
                                                    138
    if (sign == v.sign) {
                                                    139
                                                                    r += a.a[i];
                                                                    int s1 = r.a.size() <= b.a.size() ? 0 : r</pre>
        if (abs() >= v.abs()) {
                                                   140
            bigint res = *this;
                                                           .a[b.a.size()];
            for (int i = 0, carry = 0; i < (int)v_{141}
                                                                    int s2 = r.a.size() <= b.a.size() - 1 ? 0</pre>
.a.size() || carry; ++i) {
                                                            : r.a[b.a.size() - 1];
                 res.a[i] -= carry + (i < (int)v.a_{142}
                                                                    int d = ((long long)base * s1 + s2) / b.a
.size() ? v.a[i] : 0);
                                                           .back();
                 carry = res.a[i] < 0;</pre>
                                                                    r \rightarrow b * d;
                                                    143
                 if (carry) res.a[i] += base;
                                                                    while (r < 0) r += b, --d;
                                                    144
            }
                                                                    q.a[i] = d;
                                                   145
            res.trim();
                                                               }
                                                    146
            return res;
                                                   147
        }
                                                               q.sign = a1.sign * b1.sign;
                                                    148
        return -(v - *this);
                                                    149
                                                               r.sign = a1.sign;
                                                               q.trim();
                                                    150
    return *this + (-v);
                                                               r.trim();
```

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84

```
res.sign = -sign;
           return make_pair(q, r / norm);
                                                            214
       }
                                                                        return res;
153
                                                            215
154
                                                            216
       bigint operator/(const bigint &v) const { return 217
       divmod(*this, v).first; }
                                                                    bigint abs() const {
                                                                        bigint res = *this;
156
                                                            219
                                                                        res.sign *= res.sign;
       bigint operator%(const bigint &v) const { return 220
       divmod(*this, v).second; }
                                                            221
                                                                        return res;
159
       void operator/=(int v) {
                                                            223
           if (v < 0) sign = -sign, v = -v;
                                                                    long longValue() const {
                                                            224
            for (int i = (int)a.size() - 1, rem = 0; i >=225
161
                                                                        long long res = 0;
        0; --i) {
                                                                        for (int i = a.size() - 1; i >= 0; i--) res =
                long long cur = a[i] + rem * (long long)
                                                                     res * base + a[i];
       base:
                                                            227
                                                                        return res * sign;
                a[i] = (int)(cur / v);
163
                                                            228
                rem = (int)(cur % v);
164
                                                            229
           }
                                                                    friend bigint gcd(const bigint &a, const bigint &
                                                            230
            trim();
166
       }
                                                                        return b.isZero() ? a : gcd(b, a % b);
167
                                                            231
                                                            232
168
       bigint operator/(int v) const {
                                                                    friend bigint lcm(const bigint &a, const bigint &
169
                                                            233
           bigint res = *this;
170
171
            res /= v;
                                                            234
                                                                        return a / gcd(a, b) * b;
            return res;
172
                                                            235
                                                                    void read(const string &s) {
174
                                                            237
       int operator%(int v) const {
                                                                        sign = 1;
175
                                                            238
176
            if (v < 0) v = -v;
                                                            239
                                                                        a.clear();
            int m = 0;
                                                                        int pos = 0;
177
                                                            240
            for (int i = a.size() - 1; i >= 0; --i)
                                                                        while (pos < (int)s.size() && (s[pos] == '-'</pre>
               m = (a[i] + m * (long long)base) % v;
                                                                    || s[pos] == '+')) {
179
                                                                            if (s[pos] == '-') sign = -sign;
180
            return m * sign;
       7
181
                                                            243
                                                                            ++pos;
                                                            244
182
       void operator+=(const bigint &v) { *this = *this 245
                                                                        for (int i = s.size() - 1; i >= pos; i -=
       + v: }
                                                                    base_digits) {
       void operator -=(const bigint &v) { *this = *this 246
                                                                            int x = 0;
       - v; }
                                                                            for (int j = max(pos, i - base_digits +
       void operator*=(const bigint &v) { *this = *this
                                                                    1); j <= i; j++)
185
       * v; }
                                                                                 x = x * 10 + s[j] - '0';
       void operator/=(const bigint &v) { *this = *this 249
                                                                            a.push_back(x);
186
       / v; }
                                                                        }
                                                            250
187
                                                            251
                                                                        trim():
       bool operator < (const bigint &v) const {</pre>
                                                            252
188
189
           if (sign != v.sign) return sign < v.sign;</pre>
                                                            253
            if (a.size() != v.a.size())
                                                                    friend istream &operator>>(istream &stream,
                                                            254
190
                return a.size() * sign < v.a.size() * v.</pre>
                                                                    bigint &v) {
191
                                                                        string s;
       sign:
                                                            255
            for (int i = a.size() - 1; i >= 0; i--)
192
                                                            256
                                                                        stream >> s;
               if (a[i] != v.a[i]) return a[i] * sign < 257
193
                                                                        v.read(s):
       v.a[i] * sign;
                                                                        return stream;
                                                            258
           return false;
                                                                   }
194
                                                            259
195
                                                            260
                                                                    friend ostream &operator << (ostream &stream, const
197
       bool operator>(const bigint &v) const { return v
                                                                     bigint &v) {
       < *this: }
                                                                        if (v.sign == -1) stream << '-';</pre>
                                                            262
       bool operator <= (const bigint &v) const { return 263
                                                                        stream << (v.a.empty() ? 0 : v.a.back());
198
       !(v < *this); }
                                                                        for (int i = (int)v.a.size() - 2; i >= 0; --i
                                                            264
       bool operator>=(const bigint &v) const { return
                                                                   )
199
       !(*this < v); }
                                                                            stream << setw(base_digits) << setfill('0</pre>
                                                            265
       bool operator == (const bigint &v) const {
                                                                    ') << v.a[i];
200
201
            return !(*this < v) && !(v < *this);
                                                            266
                                                                        return stream;
202
                                                            267
       bool operator!=(const bigint &v) const { return
203
                                                           *268
       this < v || v < *this; }
                                                                    static vector<int> convert_base(const vector<int>
                                                            269
                                                                     &a, int old_digits,
       void trim() {
205
                                                            270
                                                                                                      int new_digits) {
            while (!a.empty() && !a.back()) a.pop_back();271
                                                                        vector < long long > p(max(old_digits,
206
            if (a.empty()) sign = 1;
                                                                   new_digits) + 1);
207
                                                                        p[0] = 1;
208
                                                                        for (int i = 1; i < (int)p.size(); i++) p[i]</pre>
209
                                                                    = p[i - 1] * 10;
       bool isZero() const { return a.empty() || (a.size
       () == 1 && !a[0]); }
                                                            274
                                                                        vector < int > res;
                                                            275
                                                                        long long cur = 0;
       bigint operator-() const {
                                                                        int cur_digits = 0;
212
                                                            276
213
            bigint res = *this;
                                                                        for (int i = 0; i < (int)a.size(); i++) {</pre>
```

```
cur += a[i] * p[cur_digits];
                                                              return res:
                                                   342
        cur_digits += old_digits;
                                                   343
        while (cur_digits >= new_digits) {
                                                   344 };
            res.push_back(int(cur % p[new_digits
]));
                                                            Get-permutation-cicles
                                                      3.3
             cur /= p[new_digits];
             cur_digits -= new_digits;
        }
                                                    _{2} * receives a permutation [0, n-1]
    }
                                                    3 * returns a vector of cicles
    res.push_back((int)cur);
                                                    4 * for example: [1, 0, 3, 4, 2] -> [[0, 1], [2, 3, 4]]
    while (!res.empty() && !res.back()) res.
pop_back();
                                                    5 * */
    return res:
                                                    6 vector < vll > getPermutationCicles(const vll &ps) {
                                                          ll n = len(ps);
                                                          vector < char > visited(n);
typedef vector<long long> vll;
                                                          vector < vll > cicles;
                                                    9
                                                          for (int i = 0; i < n; ++i) {</pre>
static vll karatsubaMultiply(const vll &a, const
                                                              if (visited[i]) continue;
                                                    11
vll &b) {
                                                    12
    int n = a.size();
                                                              vll cicle:
                                                    13
    vll res(n + n);
                                                              11 pos = i;
                                                    14
    if (n <= 32) {
                                                               while (!visited[pos]) {
                                                    15
        for (int i = 0; i < n; i++)</pre>
                                                                   cicle.pb(pos);
            for (int j = 0; j < n; j++) res[i + j
                                                                   visited[pos] = true;
] += a[i] * b[j];
                                                                   pos = ps[pos];
                                                   18
        return res;
                                                    19
                                                   20
                                                               cicles.push_back(vll(all(cicle)));
                                                   21
    int k = n >> 1;
                                                          }
                                                   22
    vll a1(a.begin(), a.begin() + k);
                                                          return cicles:
                                                   23
    vll a2(a.begin() + k, a.end());
                                                   24 }
    vll b1(b.begin(), b.begin() + k);
    vll b2(b.begin() + k, b.end());
                                                           dynamic programming
    vll a1b1 = karatsubaMultiply(a1, b1);
    vll a2b2 = karatsubaMultiply(a2, b2);
                                                      4.1 Edit Distance
    for (int i = 0; i < k; i++) a2[i] += a1[i];</pre>
    for (int i = 0; i < k; i++) b2[i] += b1[i];</pre>
                                                    int edit_distance(const string &a, const string &b) {
                                                          int n = a.size();
    vll r = karatsubaMultiply(a2, b2);
                                                          int m = b.size();
    for (int i = 0; i < (int)a1b1.size(); i++) r[ 4</pre>
                                                          vector < vi > dp(n + 1, vi(m + 1, 0));
i] -= a1b1[i];
    for (int i = 0; i < (int)a2b2.size(); i++) r[ 6</pre>
                                                          int ADD = 1, DEL = 1, CHG = 1;
i] -= a2b2[i];
                                                          for (int i = 0; i <= n; ++i) {</pre>
                                                               dp[i][0] = i * DEL;
    for (int i = 0; i < (int)r.size(); i++) res[i 9</pre>
 + k] += r[i];
                                                          for (int i = 1; i <= m; ++i) {</pre>
                                                   10
    for (int i = 0; i < (int)a1b1.size(); i++)</pre>
                                                               dp[0][i] = ADD * i;
                                                    11
res[i] += a1b1[i];
                                                   12
    for (int i = 0; i < (int)a2b2.size(); i++)</pre>
                                                    13
                                                          for (int i = 1; i <= n; ++i) {
res[i + n] += a2b2[i];
                                                   14
    return res;
                                                               for (int j = 1; j \le m; ++j) {
                                                   15
                                                                   int add = dp[i][j - 1] + ADD;
                                                   16
                                                                   int del = dp[i - 1][j] + DEL;
                                                   17
bigint operator*(const bigint &v) const {
                                                                   int chg = dp[i - 1][j - 1] + (a[i - 1] ==
   vector < int > a6 = convert_base(this - >a,
                                                           b[j - 1] ? 0 : 1) * CHG;
base_digits, 6);
                                                                   dp[i][j] = min({add, del, chg});
    vector < int > b6 = convert_base(v.a,
                                                               }
                                                   20
base_digits, 6);
                                                   21
    vll a(a6.begin(), a6.end());
    vll b(b6.begin(), b6.end());
                                                          return dp[n][m];
                                                   23
    while (a.size() < b.size()) a.push_back(0);</pre>
    while (b.size() < a.size()) b.push_back(0);</pre>
    while (a.size() & (a.size() - 1)) a.push_back 4.2 Money Sum Bottom Up
(0), b.push_back(0);
    vll c = karatsubaMultiply(a, b);
    bigint res;
                                                    find every possible sum using
    res.sign = sign * v.sign;
                                                         the given values only once.
    for (int i = 0, carry = 0; i < (int)c.size(); 3</pre>
 i++) {
                                                    5 set <int > money_sum(const vi &xs) {
        long long cur = c[i] + carry;
                                                    using vc = vector < char >;
        res.a.push_back((int)(cur % 1000000));
                                                          using vvc = vector < vc>;
        carry = (int)(cur / 1000000);
                                                          int _m = accumulate(all(xs), 0);
                                                          int _n = xs.size();
    res.a = convert_base(res.a, 6, base_digits);
                                                          vvc _dp(_n + 1, vc(_m + 1, 0));
                                                    10
    res.trim();
                                                          set < int > _ans;
                                                    11
```

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339

340

```
dp[0][xs[0]] = 1;
                                                                                                15 }
12
           for (int i = 1; i < _n; ++i) {
13
                 for (int j = 0; j <= _m; ++j) {</pre>
14
                                                                                                    5
                                                                                                             trees
                        if (j == 0 or _dp[i - 1][j]) {
                                _{dp[i][j + xs[i]] = 1;}
                                                                                                               Binary-lifting
                                                                                                    5.1
                                _dp[i][j] = 1;
17
                        }
                 }
19
                                                                                                 1 /*
           }
                                                                                                 * far[h][i] = the node that 2^h far from node i
21
                                                                                                 _{3} * sometimes is useful invert the order of loops
           for (int i = 0; i < _n; ++i)</pre>
22
                                                                                                 4 * time : O(nlogn)
                 for (int j = 0; j \le m; ++j)
23
                                                                                                 5 * */
                       if (_dp[i][j]) _ans.insert(j);
24
                                                                                                 6 const int maxlog = 20;
                                                                                                 7 int far[maxlog + 1][n + 1];
26 }
                                                                                                 8 int n;
                                                                                                 9 for (int h = 1; h <= maxlog; h++) {</pre>
    4.3 Knapsack Dp Values 01
                                                                                                           for (int i = 1; i <= n; i++) {
                                                                                                                   far[h][i] = far[h - 1][far[h - 1][i]];
                                                                                                11
 1 const int MAX_N = 1001;
                                                                                                12
 2 const int MAX_S = 100001;
                                                                                                13 }
 3 array<array<int, MAX_S>, MAX_N> dp;
                                                                                                    5.2 Maximum-distances
 4 bool check[MAX_N][MAX_S];
 5 pair < int , vi > knapsack(int S, const vector < pii > &xs)
           int N = (int)xs.size();
                                                                                                  2 * Returns the maximum distance from every node to
                                                                                                          any other node in the tree.
           for (int i = 0; i <= N; ++i) dp[i][0] = 0;</pre>
                                                                                                 4 pll mostDistantFrom(const vector<vll> &adj, ll n, ll
 9
           for (int m = 0; m <= S; ++m) dp[0][m] = 0;</pre>
                                                                                                          root) {
11
                                                                                                           // 0 indexed
           for (int i = 1; i <= N; ++i) {</pre>
12
                                                                                                           11 mostDistantNode = root;
                                                                                                 6
                 for (int m = 1; m <= S; ++m) {
13
                                                                                                           11 nodeDistance = 0;
                        dp[i][m] = dp[i - 1][m];
14
                                                                                                           queue < pll > q;
                         check[i][m] = false;
                                                                                                           vector < char > vis(n);
16
                                                                                                10
                                                                                                           q.emplace(root, 0);
                         auto [w, v] = xs[i - 1];
                                                                                                           vis[root] = true;
                                                                                                11
18
                                                                                                           while (!q.empty()) {
                                                                                                12
                         if (w \le m \text{ and } (dp[i - 1][m - w] + v) >=
19
                                                                                                                  auto [node, dist] = q.front();
                                                                                                13
           dp[i][m]) {
                                                                                                                  q.pop();
                                dp[i][m] = dp[i - 1][m - w] + v;
20
                                                                                                                  if (dist > nodeDistance) {
                                                                                                15
                                check[i][m] = true;
                                                                                                16
                                                                                                                          nodeDistance = dist:
                        }
22
                                                                                                17
                                                                                                                          mostDistantNode = node;
                 }
23
                                                                                                18
           }
24
                                                                                                                   for (auto u : adj[node]) {
                                                                                                19
25
                                                                                                                         if (!vis[u]) {
                                                                                                20
           int m = S;
                                                                                                21
                                                                                                                                vis[u] = true:
           vi es;
27
                                                                                                22
                                                                                                                                q.emplace(u, dist + 1);
28
                                                                                                23
           for (int i = N; i >= 1; --i) {
29
                                                                                                24
                                                                                                                  }
                 if (check[i][m]) {
30
                                                                                                25
                        es.push_back(i);
31
                                                                                                26
                                                                                                            return {mostDistantNode, nodeDistance};
                        m -= xs[i - 1].first;
32
                                                                                                27 }
                 }
33
                                                                                                28
34
                                                                                                29 ll twoNodesDist(const vector < vll> & adj, ll n, ll a,
35
                                                                                                           11 b) {
36
           reverse(es.begin(), es.end());
                                                                                                            queue < pll > q;
37
                                                                                                           vector < char > vis(n);
                                                                                                31
38
           return {dp[N][S], es};
                                                                                                           q.emplace(a, 0);
                                                                                                32
39 }
                                                                                                            while (!q.empty()) {
                                                                                                33
                                                                                                34
                                                                                                                  auto [node, dist] = q.front();
   4.4 Tsp
                                                                                                                   q.pop();
                                                                                                35
                                                                                                                  if (node == b) return dist;
                                                                                                36
 using vi = vector<int>;
                                                                                                                   for (auto u : adj[node]) {
                                                                                                                         if (!vis[u]) {
 vector < vi > dist;
                                                                                                38
 3 vector < vi > memo;
                                                                                                                                vis[u] = true;
                                                                                                39
 4 /* 0 ( N^2 * 2^N )*/
                                                                                                40
                                                                                                                                q.emplace(u, dist + 1);
 5 int tsp(int i, int mask, int N) {
                                                                                                41
           if (mask == (1 << N) - 1) return dist[i][0];</pre>
                                                                                                                  }
           if (memo[i][mask] != -1) return memo[i][mask];
                                                                                                           }
                                                                                                43
           int ans = INT_MAX << 1;</pre>
                                                                                                44
                                                                                                           return -1;
                                                                                                45 }
 9
           for (int j = 0; j < N; ++j) {
                 if (mask & (1 << j)) continue;</pre>
10
                                                                                                46
                  auto t = tsp(j, mask | (1 << j), N) + dist[i 47 tuple < 11, 11, 11 > tree_diameter(const vector < v11 > & tree_diameter(
          ][j];
                                                                                                           adj, 11 n) {
                 ans = min(ans, t);
                                                                                                            // returns two points of the diameter and the
                                                                                                           diameter itself
13
           return memo[i][mask] = ans;
                                                                                                            auto [node1, dist1] = mostDistantFrom(adj, n, 0);
14
                                                                                                49
```

```
auto [node2, dist2] = mostDistantFrom(adj, n,
                                                           35 #define rsz(__x, __n) resize(__x, __n)
50
      auto diameter = twoNodesDist(adj, n, node1, node2 37 const 11 INF = 1e18;
      return make_tuple(node1, node2, diameter);
                                                           39 struct HLD {
52
53 }
                                                           40
                                                                 int n:
                                                                  vi sizes;
_{55} vll everyDistanceFromNode(const vector<vll> &adj, ll _{42}
                                                                 vi2d g;
      n. 11 root) {
                                                                  vi groups;
56
      // Single Source Shortest Path, from a given root 44
                                                                  vi heavy;
      queue <pair <11, 11>> q;
                                                                  \mathtt{HLD}(\mathtt{int}\ \mathtt{n})\ :\ \mathtt{n(n)}, \mathtt{sizes(n+1)}, \mathtt{g(n+1)}, groups
      vll ans(n, -1);
                                                                  (n + 1), heavy(n + 1) {}
      ans[root] = 0;
                                                                  void get_sizes(int u, int p) {
59
                                                           46
      q.emplace(root, 0);
                                                                      int sz = 1;
      while (!q.empty()) {
                                                                      int bigc = -1;
61
                                                          48
          auto [u, d] = q.front();
                                                           49
                                                                      for (auto &v : g[u])
62
                                                                          if (v != p) {
63
           q.pop();
                                                           50
                                                                              get_sizes(p, u);
                                                          51
64
           for (auto w : adj[u]) {
                                                                              if (bigc == -1 or sizes[bigc] < sizes</pre>
               if (ans[w] != -1) continue;
                                                                  [v])
66
               ans[w] = d + 1;
                                                           53
                                                                                   bigc = v, heavy[u] = v;
                                                                              sz += sizes[v];
68
               q.emplace(w, d + 1);
                                                           54
                                                                          }
69
                                                           55
70
      }
                                                                      sizes[u] = sz;
71
      return ans;
                                                           57
                                                                  void decompose(int u, int p) {
                                                                      groups[u] = p;
74 vll maxDistances(const vector < vll > & adj, ll n) {
                                                                      for (auto &v : g[u])
                                                           60
      auto [node1, node2, diameter] = tree_diameter(adj 61
                                                                          if (v != p) {
                                                                              if (v == heavy[u])
       , n);
76
      auto distances1 = everyDistanceFromNode(adj, n,
                                                                                   decompose(v, p);
      node1);
                                                                               else
      auto distances2 = everyDistanceFromNode(adj, n,
                                                           65
                                                                                   decompose(v, v);
      node2);
78
      vll ans(n);
                                                           67
      for (int i = 0; i < n; ++i) ans[i] = max(</pre>
                                                           68 };
      distances1[i], distances2[i]);
                                                           69 void run() {}
                                                           70 int32_t main(void) {
      return ans:
81 }
                                                           71
                                                                fastio;
                                                           72
                                                                  int t;
  5.3 Heavy-light-decomposition
                                                                  t = 1;
                                                           73
                                                                 // cin >> t;
                                                           74
                                                                  while (t--) run();
                                                           75
1 // iagorrr ;)
                                                           76 }
2 #include <bits/stdc++.h>
3 using namespace std;
                                                                    Tree Diameter
4 #ifdef DEBUG
5 #include "debug.cpp"
                                                           pll mostDistantFrom(const vector<vll> &adj, 11 n, 11
6 #else
7 #define dbg(...) 666
                                                                  root) {
                                                                  // 0 indexed
8 #endif
                                                            2
9 #define endl '\n'
                                                            3
                                                                  11 mostDistantNode = root;
10 #define fastio
                                                                 11 nodeDistance = 0;
11
     ios_base::sync_with_stdio(false); \
                                                                 queue < pll > q;
      cin.tie(0);
                                                                 vector < char > vis(n);
      cout.tie(0);
                                                                 q.emplace(root, 0);
14 #define rep(i, 1, r) for (int i = (1); i < (r); i++)
                                                                  vis[root] = true;
15 #define len(__x) (ll) __x.size()
                                                                  while (!q.empty()) {
                                                            9
16 using ll = long long;
                                                                      auto [node, dist] = q.front();
                                                           10
using vll = vector<1l>;
                                                           11
                                                                      q.pop();
18 using pll = pair<11, 11>;
                                                           12
                                                                      if (dist > nodeDistance) {
19 using vll2d = vector<vll>;
                                                                          nodeDistance = dist;
                                                           13
20 using vi = vector<int>;
                                                                          mostDistantNode = node:
                                                           14
21 using vi2d = vector < vi>;
                                                                      }
22 using pii = pair < int , int >;
                                                           16
                                                                      for (auto u : adj[node]) {
23 using vii = vector<pii>;
                                                                          if (!vis[u]) {
                                                           17
24 using vc = vector<char>;
                                                           18
                                                                              vis[u] = true;
25 #define all(a) a.begin(), a.end()
                                                                               q.emplace(u, dist + 1);
                                                           19
26 #define INV(xxxx) \
                                                                          }
                                                                      }
      for (auto &xxx : xxxx) cin >> xxx;
28 #define PRINTV(___x) \
      for_each(all(___x), [](ll &___x) { cout << ___x23
                                                                  return {mostDistantNode, nodeDistance};
        << '' '; }), cout << '\n';
                                                          24 }
30 #define snd second
                                                           25 ll twoNodesDist(const vector < vll> & adj, ll n, ll a,
31 #define fst first
                                                                 11 b) {
32 #define pb(___x) push_back(___x)
                                                                  // 0 indexed
33 #define mp(__a, __b) make_pair(__a, __b)
                                                           27
                                                                  queue < pll > q;
34 #define eb(___x) emplace_back(___x)
                                                                  vector < char > vis(n);
                                                           28
```

```
q.emplace(a, 0);
29
                                                       12
      while (!q.empty()) {
                                                              }
30
                                                       13
         auto [node, dist] = q.front();
31
                                                       14
                                                              return ps;
          q.pop();
         if (node == b) {
                                                        7.3
                                                                Factorial
34
             return dist;
36
          for (auto u : adj[node]) {
                                                       const ll MAX = 18;
              if (!vis[u]) {
                                                       2 vll fv(MAX, -1);
                  vis[u] = true;
                                                       3 ll factorial(ll n) {
                  q.emplace(u, dist + 1);
39
                                                             if (fv[n] != -1) return fv[n];
40
                                                             if (n == 0) return 1;
          }
41
                                                              return n * factorial(n - 1);
      }
43
      return -1;
44 }
                                                          7.4 Permutation-count
45 ll tree_diameter(const vector < vll > & adj, ll n) {
      // 0 indexed !!!
46
      auto [node1, dist1] = mostDistantFrom(adj, n, 0); 1 const ll MAX = 18;
      auto [node2, dist2] = mostDistantFrom(adj, n,
                                                        vll fv(MAX, -1);
48
                                                        3 ll factorial(ll n) {
       auto \ diameter = twoNodesDist(adj, n, node1, node2 \ ^{4} \qquad if \ (fv[n] \ != -1) \ return \ fv[n]; 
49
                                                             if (n == 0) return 1;
                                                              return n * factorial(n - 1);
                                                        6
50
      return diameter;
                                                        7 }
51 }
                                                        9 template <typename T>
      searching
  6
                                                       10 ll permutation_count(vector <T> xs) {
                                                       11
                                                             map < T, ll > h;
                                                              for (auto xi : xs) h[xi]++;
      Ternary Search Recursive
                                                       12
                                                            ll ans = factorial((ll)xs.size());
                                                       13
                                                      14
                                                              dbg(ans);
1 const double eps = 1e-6;
                                                              for (auto [v, cnt] : h) {
                                                       1.5
                                                       16
                                                                  dbg(cnt);
3 // IT MUST BE AN UNIMODAL FUNCTION
                                                       17
                                                                  ans /= cnt;
4 double f(int x) { return x * x + 2 * x + 4; }
                                                      18
6 double ternary_search(double 1, double r) {
                                                              return ans;
      if (fabs(f(1) - f(r)) < eps) return f((1 + (r - 1_{21}))
      ) / 2.0));
                                                          7.5 N-choose-k-count
      auto third = (r - 1) / 3.0;
9
      auto m1 = 1 + third;
10
      auto m2 = r - third;
                                                        2 * O(nm) time, O(m) space
12
                                                      3 * equal to n choose k
      // change the signal to find the maximum point.
                                                       4 * */
      return m1 < m2 ? ternary_search(m1, r) :</pre>
14
                                                        5 ll binom(ll n, ll k) {
      ternary_search(1, m2);
                                                             if (k > n) return 0;
15 }
                                                             vll dp(k + 1, 0);
                                                             dp[0] = 1;
      \mathbf{math}
                                                             for (ll i = 1; i <= n; i++)
                                                        9
                                                                 for (ll j = k; j > 0; j--) dp[j] = dp[j] + dp
                                                       10
                                                              [j - 1];
  7.1 Power-sum
                                                              return dp[k];
                                                       11
                                                       12 }
_1 // calculates K^0 + K^1 ... + K^n
2 ll fastpow(ll a, int n) {
                                                        7.6 Gcd-using-factorization
      if (n == 1) return a;
      11 x = fastpow(a, n / 2);
                                                       1 // O(sqrt(n))
      return x * x * (n & 1 ? a : 1);
                                                        2 map<ll, ll> factorization(ll n) {
                                                             map<11, 11> ans;
7 ll powersum(ll n, ll k) { return (fastpow(n, k + 1) - ^3
                                                              for (11 i = 2; i * i <= n; i++) {
       1) / (n - 1); }
                                                                  11 count = 0;
                                                                  for (; n % i == 0; count++, n /= i)
  7.2 Sieve-list-primes
                                                        7
                                                                  if (count) ans[i] = count;
1 // lsit every prime until MAXN
                                                        9
2 const ll MAXN = 1e5;
                                                       10
                                                             if (n > 1) ans [n] ++;
_3 vll list_primes(ll n) { // Nlog * log N \,
                                                      11
                                                              return ans;
      vll ps;
                                                       12 }
      bitset < MAXN > sieve;
                                                       13
      sieve.set();
                                                       14 ll gcd_with_factorization(ll a, ll b) {
      sieve.reset(1);
                                                             map<ll, ll> fa = factorization(a);
                                                      15
      for (11 i = 2; i <= n; ++i) {
                                                              map<11, 11> fb = factorization(b);
                                                      16
          if (sieve[i]) ps.push_back(i);
                                                              ll ans = 1;
                                                       17
          for (11 j = i * 2; j <= n; j += i) {
                                                      18
                                                              for (auto fai : fa) {
10
              sieve.reset(j);
                                                                  11 k = min(fai.second, fb[fai.first]);
11
                                                       19
```

```
while (k--) ans *= fai.first;
                                                                    while (n % p == 0) {
                                                         21
20
      }
                                                                        cnt++;
21
                                                                        n /= p;
22
      return ans;
                                                         23
                                                         25
                                                                    if (cnt) ans.emplace_back(p, cnt);
  7.7 Is-prime
                                                         26
                                                         27
                                                                return ans;
                                                         28 }
bool isprime(ll n) { // O(sqrt(n))
                                                         29
      if (n < 2) return false;
                                                         30 ll phi(ll n, vector<pll> factors) {
      if (n == 2) return true;
                                                                if (n == 1) return 1;
                                                         31
      if (n % 2 == 0) return false;
                                                                11 ans = n;
                                                         32
      for (11 i = 3; i * i < n; i += 2)
                                                         33
         if (n % i == 0) return false;
                                                                for (auto [p, k] : factors) {
      return true;
                                                                    ans /= p;
                                                         35
8 }
                                                         36
                                                                    ans *= (p - 1);
                                                         37
 7.8 Fast Exp
                                                         38
                                                         39
                                                                return ans;
                                                         40 }
2 Fast exponentiation algorithm,
compute a^n in O(log(n))
                                                           7.11 Polynomial
5 ll fexp(ll a, int n) {
                                                          using polynomial = vector<11>;
      if (n == 0) return 1;
                                                         2 int degree(const polynomial &xs) { return xs.size() -
      if (n == 1) return a;
                                                                1; }
      11 x = fexp(a, n / 2);
                                                        3 ll horner_evaluate(const polynomial &xs, ll x) {
      return x * x * (n & 1 ? a : 1);
                                                               11 \text{ ans} = 0:
                                                         4
                                                                11 n = degree(xs);
                                                                for (int i = n; i >= 0; --i) {
  7.9 Lcm-using-factorization
                                                                    ans *= x;
                                                                    ans += xs[i];
1 map<ll, ll> factorization(ll n) {
                                                         9
      map<11, 11> ans;
                                                         10
                                                                return ans;
      for (11 i = 2; i * i <= n; i++) {</pre>
                                                         11 }
          11 count = 0;
                                                         12 polynomial operator+(const polynomial &a, const
          for (; n % i == 0; count++, n /= i)
                                                               polynomial &b) {
                                                         13
                                                                int n = degree(a);
          if (count) ans[i] = count;
                                                                int m = degree(b);
                                                         14
                                                                polynomial r(max(n, m) + 1, 0);
                                                         15
      if (n > 1) ans[n]++;
9
10
      return ans;
                                                                for (int i = 0; i <= n; ++i) r[i] += a[i];</pre>
                                                         17
11 }
                                                                for (int j = 0; j \le m; ++j) r[j] += b[j];
                                                         18
                                                                while (!r.empty() and r.back() == 0) r.pop_back()
12
                                                         19
13 ll lcm_with_factorization(ll a, ll b) {
      map<11, 11> fa = factorization(a);
14
                                                                if (r.empty()) r.push_back(0);
15
      map<ll, ll> fb = factorization(b);
                                                                return r;
                                                         21
      ll ans = 1;
16
                                                         22 }
      for (auto fai : fa) {
17
                                                         23 polynomial operator*(const polynomial &p, const
          11 k = max(fai.second, fb[fai.first]);
                                                               polynomial &q) {
          while (k--) ans *= fai.first;
19
                                                         24
                                                                int n = degree(p);
20
                                                                int m = degree(q);
                                                         25
21
      return ans;
                                                         26
                                                                polynomial r(n + m + 1, 0);
                                                                for (int i = 0; i <= n; ++i)
22 }
                                                         27
                                                                   for (int j = 0; j <= m; ++j) r[i + j] += (p[i
                                                         28
  7.10 Euler-phi
                                                                ] * q[j]);
                                                                return r:
                                                         29
                                                         30 }
const ll MAXN = 1e5;
_2 vll list_primes(ll n) { // Nlog * log N \,
                                                           7.12 Integer Mod
      vll ps;
      bitset < MAXN > sieve;
                                                         const ll INF = 1e18;
      sieve.set():
      sieve.reset(1);
                                                        2 const 11 mod = 998244353;
      for (11 i = 2; i <= n; ++i) {
                                                        3 template <11 MOD = mod>
          if (sieve[i]) ps.push_back(i);
                                                         4 struct Modular {
          for (11 j = i * 2; j \le n; j += i) {
                                                               ll value;
              sieve.reset(j);
                                                               static const 11 MOD_value = MOD;
10
          }
      }
                                                                Modular(11 v = 0) {
12
                                                                    value = v % MOD;
13
      return ps;
14 }
                                                                    if (value < 0) value += MOD;</pre>
15
16 vector<pll> factorization(ll n, const vll &primes) { 12
                                                                Modular(ll a, ll b) : value(0) {
      vector < pll > ans;
                                                                   *this += a;
17
      for (auto &p : primes) {
                                                                    *this /= b;
          if (n == 1) break;
                                                                }
19
                                                         15
          11 cnt = 0;
20
                                                         16
```

```
Modular& operator+=(Modular const& b) {
                                                                     11 count = 0;
                                                         12
17
          value += b.value;
                                                                     while (x \text{ and } x \% i == 0) {
18
                                                          13
          if (value >= MOD) value -= MOD;
                                                                         x /= i;
19
                                                          14
          return *this;
                                                                          count++;
20
                                                          15
      7
                                                                     7
21
                                                          16
22
      Modular& operator -= (Modular const& b) {
                                                          17
                                                                     ans *= (count + 1):
           value -= b.value;
          if (value < 0) value += MOD;</pre>
                                                                 memo[ox] = ans;
24
                                                          19
          return *this;
                                                          20
                                                                 return ans:
26
                                                          21 }
      Modular& operator*=(Modular const& b) {
27
                                                             7.14 Lcm
           value = (11)value * b.value % MOD;
          return *this;
29
                                                          1 ll gcd(ll a, ll b) { return b ? gcd(b, a % b) : a; }
31
                                                           2 11 1cm(11 a, 11 b) { return a / gcd(a, b) * b; }
      friend Modular mexp(Modular a, ll e) {
32
          Modular res = 1;
33
                                                             7.15 Factorial-factorization
          while (e) {
34
              if (e & 1) res *= a;
               a *= a;
36
                                                           _{1} // O(logN) greater k that p^k | n
               e >>= 1;
                                                           2 ll E(ll n, ll p) {
          }
                                                                 11 k = 0, b = p;
38
                                                                 while (b <= n) {
          return res:
39
                                                                     k += n / b;
      friend Modular inverse (Modular a) { return mexp(a 6
41
                                                                     b *= p;
       , MOD - 2); }
                                                                 return k;
      Modular& operator/=(Modular const& b) { return * 9 }
43
      this *= inverse(b); }
       \textbf{friend Modular operator+(Modular a, Modular const}_{11} \ // \ \texttt{lsit every prime until MAXN O(Nlog * log N)} 
44
       b) { return a += b: }
                                                          12 const ll MAXN = 1e5;
      Modular operator++(int) { return this->value = ( _{13} vll list_primes(ll n) {
45
      this->value + 1) % MOD; }
                                                                 vll ps;
      Modular operator++() { return this->value = (this 15
                                                                 bitset < MAXN > sieve;
46
       ->value + 1) % MOD; }
                                                                 sieve.set();
       friend Modular operator-(Modular a, Modular const _{17}
                                                                 sieve.reset(1);
       b) { return a -= b; }
                                                                 for (11 i = 2; i <= n; ++i) {
                                                                     if (sieve[i]) ps.push_back(i);
      friend Modular operator-(Modular const a) {
                                                          19
      return 0 - a; }
                                                                     for (11 j = i * 2; j <= n; j += i) sieve.
      Modular operator --(int) {
49
                                                                 reset(j);
          return this->value = (this->value - 1 + MOD) 21
50
                                                          22
                                                                 return ps;
                                                          23 }
52
      Modular operator -- () { return this -> value = (this _{25} // O(pi(N)*logN)
      ->value - 1 + MOD) % MOD; }
                                                          26 map<ll, ll> factorial_factorization(ll n, const vll &
      friend Modular operator*(Modular a, Modular const
54
                                                                 primes) {
       b) { return a *= b; }
                                                                 map<11, 11> fs;
      friend Modular operator/(Modular a, Modular const 28
55
                                                                 for (const auto &p : primes) {
       b) { return a /= b; }
                                                                     if (p > n) break;
      friend std::ostream& operator <<(std::ostream& os, _{30}
                                                                     fs[p] = E(n, p);
56
       Modular const& a) {
                                                                 }
                                                          31
          return os << a.value;</pre>
57
                                                          32
                                                                 return fs;
58
                                                          33 }
      friend bool operator == (Modular const& a, Modular
      const& b) {
                                                             7.16 Factorization-with-primes
          return a.value == b.value;
60
61
      friend bool operator!=(Modular const& a, Modular ^{-1} // Nlog * log N
62
                                                           const ll MAXN = 1e5;
      const& b) {
                                                           3 vll list_primes(ll n) {
          return a.value != b.value;
63
                                                                 vll ps;
64
                                                                 bitset < MAXN > sieve;
                                                           5
65 };
                                                                 sieve.set();
                                                                 sieve.reset(1);
  7.13 Count Divisors Memo
                                                                 for (11 i = 2; i <= n; ++i) {</pre>
                                                           8
                                                           9
                                                                     if (sieve[i]) ps.push_back(i);
1 const ll mod = 1073741824;
                                                                     for (11 j = i * 2; j <= n; j += i) sieve.
                                                          10
                                                                 reset(j);
2 const 11 maxd = 100 * 100 * 100 + 1;
3 vector<ll> memo(maxd, -1);
                                                          1.1
4 ll countdivisors(ll x) {
                                                          12
                                                                 return ps;
                                                          13 }
      11 ox = x;
      ll ans = 1;
                                                          14
      for (11 i = 2; i <= x; ++i) {
                                                          15 // O(pi(sqrt(n)))
          if (memo[x] != -1) {
                                                          16 map<11, 11> factorization(11 n, const v11 &primes) {
               ans *= memo[x];
                                                                 map<11, 11> ans;
                                                          17
                                                                 for (auto p : primes) {
10
               break;
                                                          18
          }
                                                                     if (p * p > n) break;
11
                                                          19
```

```
11 count = 0;
                                                                    v[pos]++:
20
                                                          9
          for (; n % p == 0; count++, n /= p)
                                                         10
                                                                    while (pos > 0 \text{ and } v[pos] > n) {
22
                                                         11
          if (count) ans[p] = count;
                                                                        --pos;
                                                         12
      7
                                                         13
                                                                        v[pos]++;
25
      return ans:
                                                         14
26 }
                                                                    if (pos == 0 and v[pos] > n) break;
                                                         16
  7.17 Modular-inverse-using-phi
                                                         17
                                                         18
                                                                    for (int i = pos + 1; i < k; ++i) v[i] = v[</pre>
                                                                pos];
1 map<ll, ll> factorization(ll n) {
                                                          19
      map<ll, ll> ans;
                                                                    pos = k - 1;
                                                         20
      for (11 i = 2; i * i <= n; i++) {
                                                         21
          11 count = 0;
                                                         22 }
          for (; n % i == 0; count++, n /= i)
                                                                 strings
          if (count) ans[i] = count;
      }
      if (n > 1) ans[n]++;
9
                                                                 Rabin-karp
                                                            8.1
      return ans;
10
11 }
                                                          vi rabin_karp(string const &s, string const &t) {
12
                                                                11 p = 31;
13 ll phi(ll n) {
                                                          2
                                                                11 m = 1e9 + 9;
      if (n == 1) return 1;
                                                          3
14
                                                                int S = s.size(), T = t.size();
                                                          4
15
      auto fs = factorization(n);
16
      auto res = n;
                                                                vll p_pow(max(S, T));
17
                                                          6
                                                          7
                                                                p_pow[0] = 1;
18
                                                                for (int i = 1; i < (int)p_pow.size(); i++)</pre>
      for (auto [p, k] : fs) {
                                                          8
19
                                                                    p_pow[i] = (p_pow[i - 1] * p) % m;
20
          res /= p;
                                                          9
          res *= (p - 1);
                                                          10
21
                                                                vll h(T + 1, 0);
                                                          11
22
                                                                for (int i = 0; i < T; i++)</pre>
                                                          12
23
                                                                    h[i + 1] = (h[i] + (t[i] - 'a' + 1) * p_pow[i]
                                                          13
      return res;
24
                                                                ]) % m;
25 }
                                                                11 h_s = 0;
                                                          14
26
                                                                for (int i = 0; i < S; i++) h_s = (h_s + (s[i] -
27 ll fexp(ll a, ll n, ll mod) {
                                                         15
                                                                'a' + 1) * p_pow[i]) % m;
      if (n == 0) return 1;
28
29
      if (n == 1) return a;
      11 x = fexp(a, n / 2, mod);
                                                         17
                                                                vi occurences;
30
                                                                for (int i = 0; i + S - 1 < T; i++) {
      return x * x * (n & 1 ? a : 1) % mod;
                                                         18
31
                                                                    11 cur_h = (h[i + S] + m - h[i]) % m;
                                                          19
32 }
                                                                    // IT DON'T CONSIDERE CONLISIONS !
                                                                    if (cur_h == h_s * p_pow[i] % m) occurences.
34 ll inv(ll a, ll mod) { return fexp(a, phi(mod) - 1,
                                                         21
                                                                push_back(i);
      mod); }
                                                         22
  7.18 Factorization
                                                                return occurences;
                                                         23
                                                          24 }
1 // O(sqrt(n))
                                                                 Trie-naive
                                                            8.2
2 map<11, 11> factorization(11 n) {
      map<ll, ll> ans;
                                                         _1 // time: O(n^2) memory: O(n^2)
      for (11 i = 2; i * i <= n; i++) {</pre>
                                                         2 using Node = map < char, int >;
          11 count = 0;
                                                         3 using vi = vector<int>;
          for (; n % i == 0; count++, n /= i)
                                                          4 using Trie = vector < Node >;
          if (count) ans[i] = count;
                                                          6 Trie build(const string &s) {
                                                               int n = (int)s.size();
      if (n > 1) ans[n]++;
10
                                                                Trie trie(1);
      return ans;
11
                                                          9
                                                                string suffix;
12 }
                                                                for (int i = n - 1; i >= 0; --i) {
  7.19 Gcd
                                                          11
                                                                    suffix = s.substr(i) + '#';
1 ll gcd(ll a, ll b) { return b ? gcd(b, a % b) : a; }
                                                                    int v = 0; // root
                                                                    for (auto c : suffix) {
  7.20 Combinatorics With Repetitions
                                                                        if (c == '#') { // makrs the poistion of
                                                          16
                                                                             trie[v][c] = i;
void combinations_with_repetition(int n, int k,
                                                         17
                                     function < void (const 18
                                                                             break:
       vector<int> &)> process) {
                                                         19
      vector < int > v(k, 1);
                                                                        if (trie[v][c])
                                                         20
      int pos = k - 1;
                                                                            v = trie[v][c];
                                                         21
                                                                         else {
                                                         22
      while (true) {
                                                                            trie.push_back({});
                                                          23
                                                                             trie[v][c] = trie.size() - 1;
         process(v);
                                                          24
```

v = trie.size() - 1;

```
}
26
27
           }
       }
28
       return trie;
29
30 }
31
32 vi search(Trie &trie, string s) {
33
      int p = 0;
       vi occ;
35
       for (auto &c : s) {
           p = trie[p][c];
36
           if (!p) return occ;
37
       }
38
       queue < int > q;
40
41
       q.push(0);
       while (!q.empty()) {
42
           auto cur = q.front();
43
           q.pop();
44
           for (auto [c, v] : trie[cur]) {
   if (c == '#')
45
46
                    occ.push_back(v);
47
48
49
                    q.push(v);
           }
50
51
       }
52
       return occ;
53 }
54
55 ll distinct_substr(const Trie &trie) {
       11 cnt = 0;
       queue < int > q;
57
       q.push(0);
58
       while (!q.empty()) {
59
```

```
auto u = q.front();
60
61
             q.pop();
62
             for (auto [c, v] : trie[u]) {
   if (c != '#') {
63
64
                       cnt ++;
65
66
                       q.push(v);
                  }
67
             }
69
        }
70
        return cnt;
71 }
```

8.3 String-psum

```
1 struct strPsum {
     11 n;
      11 k;
      vector < vll > psum;
4
      strPsum(const string &s) : n(s.size()), k(100),
5
      psum(k, vll(n + 1)) {
          for (11 i = 1; i <= n; ++i) {</pre>
6
               for (11 j = 0; j < k; ++j) {
                   psum[j][i] = psum[j][i - 1];
8
9
               psum[s[i - 1]][i]++;
10
11
12
      }
13
      ll qtd(ll l, ll r, char c) { // [0,n-1]
14
           return psum[c][r + 1] - psum[c][1];
15
16
17 }
```