

Image/ Object Feature extraction

# Texture of image

- General Textures are rough, silky, bumpy
- Image with
  - rough texture has a large difference between pixel intensities
  - smooth texture has little difference between pixel intensities
- Textures in images quantify Grey Level differences
- Second order texture features consider the relationship between groups of two pixels in the original image
- First order texture measures are statistics of pixel values, like variance  
and do not consider pixel relationships



rough



smooth

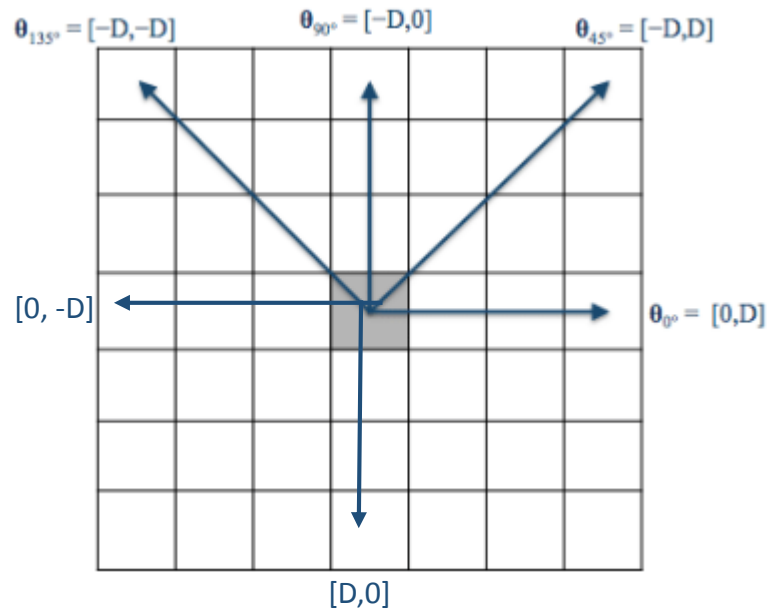
# gray-level co-occurrence matrix (GLCM)

- Statistical method of examining texture
- Considers the spatial relationship of pixels
- Shows how often pairs of pixel with specific values and with specified relationship occur in an image
- Statistical measures can be extracted from this matrix
- Statistics provide information about the texture of an image

# Create GLCM

- Is a tabulation of how often different combinations of pixel brightness values (grey levels) occur in an image
- Calculate how often a pixel with the intensity (gray-level) value  $i$  occurs in a specific spatial relationship to a pixel with the value  $j$
- Example of Spatial relationship is pixel of interest and the pixel to its immediate right (horizontally adjacent)
- Each element is the sum of the number of times pixels with value,  $i$  occurred in specified relationship to a pixel with value,  $j$  in the image
- Number of gray levels in the image determines the size of GLCM
- If image has 8 levels, GLCM has the size of  $8 \times 8$
- GLCM reveals certain properties about the spatial distribution of the gray levels in the texture image

# GLCM example



0	0	1	1
0	0	1	1
0	2	2	2
2	2	3	3

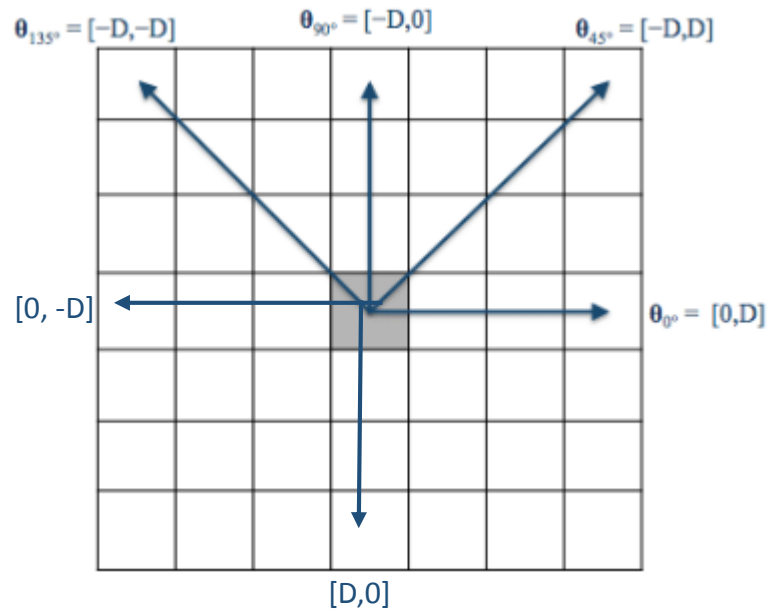
2-bit Image matrix

Pixel values,  $j \rightarrow$

	0	1	2	3
Pixel values, $i \rightarrow$	0	0	0	0
1	0	0	0	0
2	0	0	0	0
3	0	0	0	0

GLCM for (0,1) spatial relationship

# GLCM example



0	0	1	1
0	0	1	1
0	2	2	2
2	2	3	3

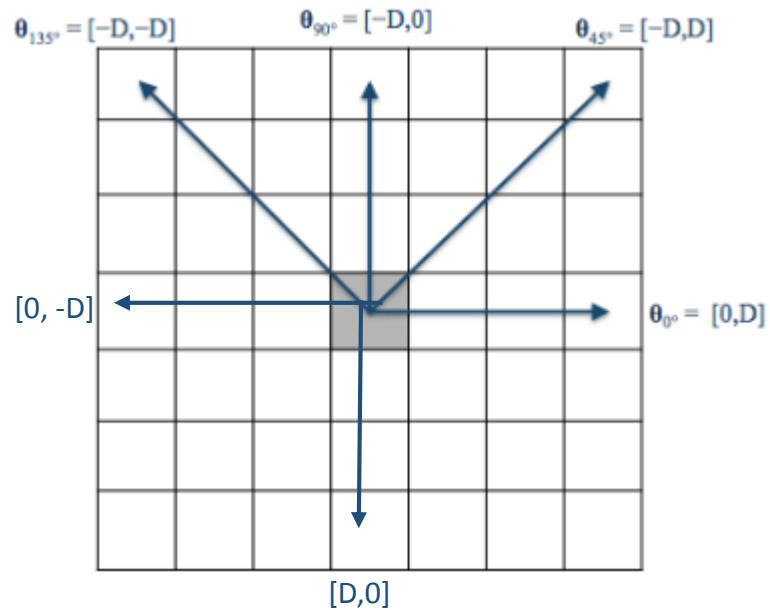
2-bit Image matrix

Pixel values,  $j \rightarrow$

	0	1	2	3
Pixel values, $i \rightarrow$	0	0	0	0
1	0	0	0	0
2	0	0	0	0
3	0	0	0	0

GLCM for (0,1) spatial relationship

# GLCM example



0	0	1	1
0	0	1	1
0	2	2	2
2	2	3	3

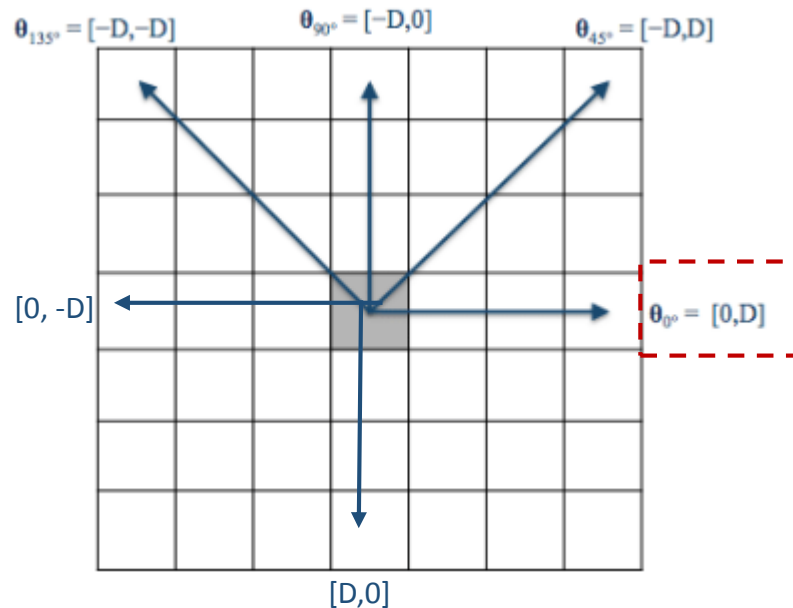
2-bit Image matrix

Pixel values,  $j \rightarrow$

	0	1	2	3
Pixel values, $i \rightarrow$	2	2	1	0
0	0	0	0	0
1	0	0	0	0
2	0	0	0	0
3	0	0	0	0

GLCM for (0,1) spatial relationship

# GLCM example



0	0	1	1
0	0	1	1
0	2	2	2
2	2	3	3

2-bit Image matrix

		Pixel values, $j \rightarrow$			
		0	1	2	3
Pixel values, $i \rightarrow$	0	2	2	1	0
	1	0	2	0	0
	2	0	0	3	1
	3	0	0	0	1

GLCM for (0,1) spatial relationship

- (0,1) relation- target pixel is 1 unit away on right side of reference pixel
- Other relationships like (1,0), (0,-2) etc are possible
- For each relationship one GLCM is constructed



# Features of GLCM

- Square
  - Reference pixels have the same range of possible values as the neighbor pixels
  - Range of row and column numbers is same
- Number of rows and columns is number of level of the image
  - For 3-bit image, it has 8 rows and 8 columns
  - It is too large to for computation.
  - For 8-bit data, image is scaled to 4 bit (16 x 16 matrix) or 5 bit (32x32 matrix)
  - Also, there are many 0s because spatial relationship may not have pairs
  - Since GLCM works on joint probability distribution, result may skewed

# Features of GLCM

- Symmetrical matrix around diagonal
  - GLCM is not symmetric
  - Texture calculations are best performed on a symmetrical matrix
  - Symmetry will be achieved if each pixel pair is counted twice: once "forwards" and once "backwards"
  - This operation would cover border pixels

# Features of GLCM

- If image contains objects of a variety of shapes and sizes and they are arranged in horizontal and vertical directions  
use offsets of varying direction and distance
- Spatial relationship can be in any direction and any distance between the pixels of interest

# GLCM example

- Pixel in the last column do not have neighbour pixels
- Transpose changes the spatial relationship
- Add original and transposed GLCM
- Addition generates almost symmetric matrix
- Also, border pixels are also counted in GLCM

0	0	1	1
0	0	1	1
0	2	2	2
2	2	3	3

2-bit Image matrix

2	0	0	0
2	2	0	0
1	0	3	0
0	0	1	1

Transpose GLCM

		Pixel values, j →			
		0	1	2	3
Pixel values, i →	0	2	2	1	0
	1	0	2	0	0
	2	0	0	3	1
	3	0	0	0	1

GLCM for (0, 1) spatial relationship

4	2	1	0
2	4	0	0
1	0	6	1
0	0	1	2

Symmetric GLCM

# Features of GLCM

- Lines parallel to the diagonal are one cell away from the diagonal
- These lines represent pixel pairs with a difference of one grey level (0-1, 1-2, 2-3 etc.)
- Similarly, values in two cells away from the diagonal show how many pixels have intensity difference of 2
- The farther away from the diagonal, the greater the difference between pixel grey levels

# Normalized Symmetric GLCM

- Normalized matrix shows probability of occurrence of each pair of pixels
- sum of elements = 24
- Normalized symmetric GLCM = element of symmetric GLCM/24
- The diagonal elements represent pixel pairs with no grey level difference
- If there are high probabilities in these elements, then the image has low contrast
- That is most of the pixels are identical to their neighbours

4	2	1	0
2	4	0	0
1	0	6	1
0	0	1	2

Symmetric GLCM

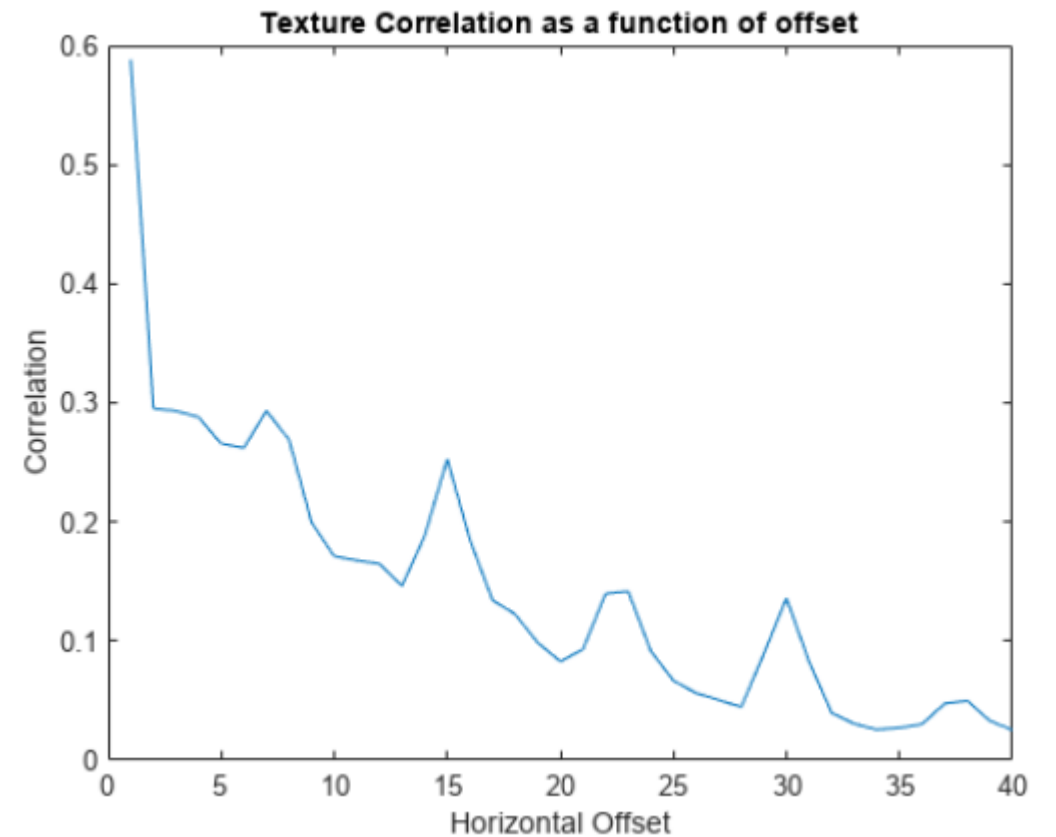
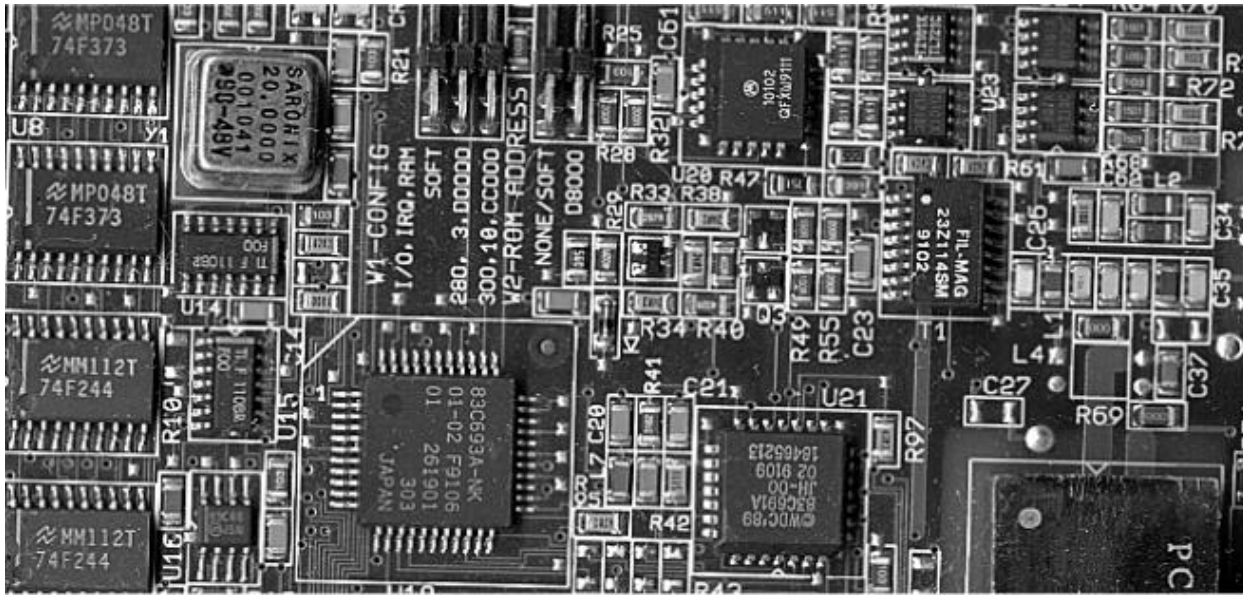
0.166	0.083	0.042	0
0.083	0.166	0	0
0.042	0	0.25	0.042
0	0	0.042	0.083

Normalized GLCM, Probability,  $p(i,j)$

# Application of texture image

- In remote sensing and medical imaging, value of a pixel is not important
- Pixel-to-pixel relationships is more important
- Ex: Forest can be smooth or variety of trees
- Generate GLCM for a small area of the image and determine texture features

# Texture feature (correlation)





# Statistics derived from Example GLCM

		j			
		0	1	2	3
GLCM	i	1	1	2	3
		1	0	2	0
		0	0	0	3

- Contrast: 2.8947
- Dissimilarity: 1.31
- Energy: 0.1191
- Homogeneity: 0.565

# Contrast of image derived from GLCM


- Also known as sum of squares variance or inertia
- Uses weights related to the *distance from the GLCM diagonal*
- Returns a intensity contrast between a pixel and its neighbor over the image
- Values on the GLCM diagonal show no contrast
- Contrast is more for pixels which are away from the diagonal
- Range is from 0 to the number of elements of GLCM
- If contrast = 0, image has pixels with constant intensity
- Increases exponentially as intensity difference between reference and target pixel increases
- Contrast is defined for a specific relationship used for GLCM
- For (0,1) relationship, it shows contrast in horizontal direction and with next pixel

# Contrast derived from Example GLCM

$j \rightarrow$

	1	2	3	4
$i \downarrow$ 1	0	1	2	3
2	1	1	2	3
3	1	0	2	0
4	0	0	0	3

GLCM



Sum of elements of GLCM = 19

# Contrast derived from Example GLCM

$j \rightarrow$

	1	2	3	4
$i \downarrow$ 1	0	1	2	3
2	1	1	2	3
3	1	0	2	0
4	0	0	0	3

GLCM

Sum of elements of GLCM = 19



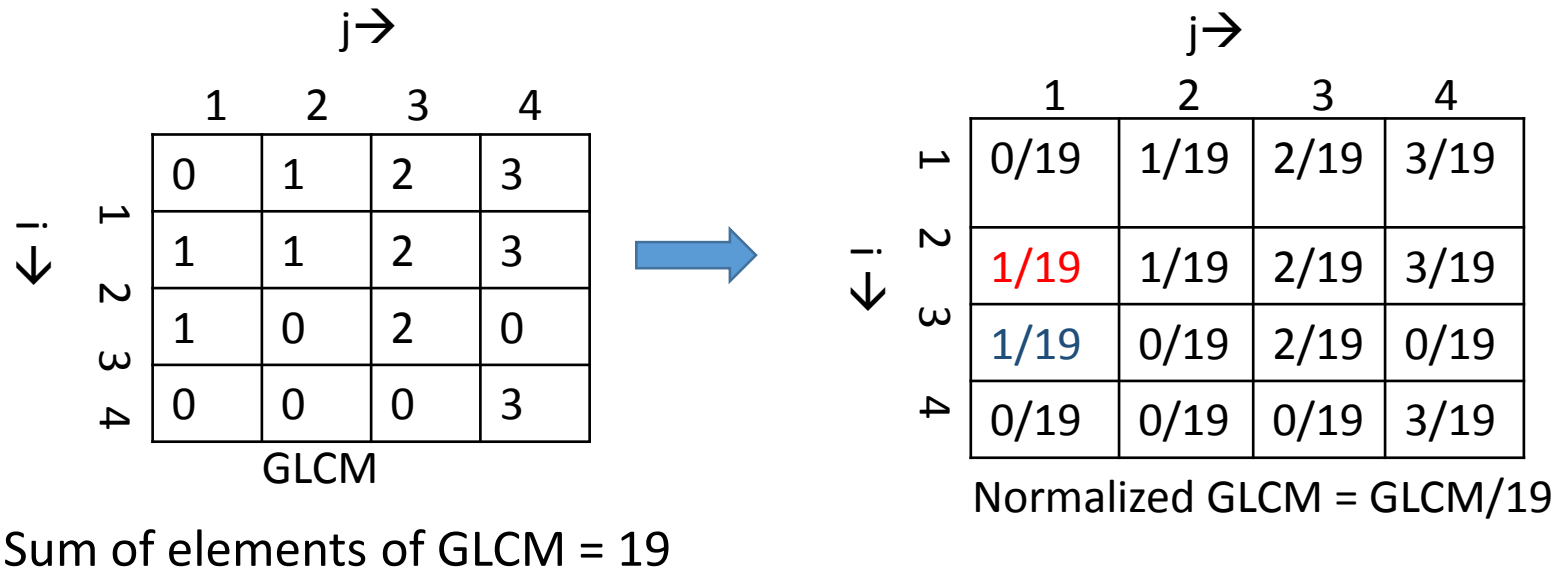
$j \rightarrow$

	1	2	3	4
$i \downarrow$ 1	0/19	1/19	2/19	3/19
2	1/19	1/19	2/19	3/19
3	1/19	0/19	2/19	0/19
4	0/19	0/19	0/19	3/19

Normalized GLCM = GLCM/19

- Elements of normalized GLCM = Probability,  $p(i,j)$
- Red elements show pairs of pixels with same value
- Blue elements show pairs of pixels with difference in pixel value of 1
- Green elements show pairs of pixels with difference in pixel value of 2

# Contrast derived from Example GLCM



Elements of normalized GLCM = Probability,  $p(i,j)$

$$Contrast = \sum_{i,j} |i - j|^2 p(i,j)$$

- Contrast =  $(1/19) + 2^2 \times (1/19) + (1/19) + 2^2 \times (2/19) + (2/19) + 3^2 \times (3/19) + 2^2 \times (3/19)$
- Contrast: 2.8947

Same procedure can be applied to symmetrical GLCM

# Dissimilarity derived from Example GLCM

		j→			
		1	2	3	4
i↓	1	0	1	2	3
	2	1	1	2	3
	3	1	0	2	0
	4	0	0	0	3

GLCM

Sum of elements of GLCM = 19

		j→			
		1	2	3	4
i↓	1	0/19	1/19	2/19	3/19
	2	1/19	1/19	2/19	3/19
	3	1/19	0/19	2/19	0/19
	4	0/19	0/19	0/19	3/19

Normalized GLCM = GLCM/19

$$dissimilarity = \sum_{i,j} |i - j| p(i, j)$$

- Dissimilarity increases linearly with pixel difference

$$\text{Contrast} = (1/19) + 2 \times (1/19) + (-1)(1/19) + (-2) \times (2/19) + (-1)(2/19) + (-3) \times (3/19) + (-2) \times (3/19)$$

Same procedure can be applied to symmetrical GLCM

# Energy derived from GLCM

- Returns the sum of squared elements in the GLCM
- Range is from 0 to 1
- Energy is 1 for a constant image
- The property Energy is also known as uniformity or angular second moment

$$Energy = \sum_{i,j} p(i,j)^2$$

# Energy derived from Example GLCM

		j→			
		1	2	3	4
i↓	1	0	1	2	3
	2	1	1	2	3
	3	1	0	2	0
	4	0	0	0	3
		GLCM			



		j→			
		1	2	3	4
i↓	1	0/19	1/19	2/19	3/19
	2	1/19	1/19	2/19	3/19
	3	1/19	0/19	2/19	0/19
	4	0/19	0/19	0/19	3/19
		Probability, $p(i,j) = \text{GLCM}(i,j)/19$			

$$\text{Energy} = \sum_{i,j} p(i,j)^2$$

- $\text{Energy} = 4(1/19)^2 + 3(2/19)^2 + 3(3/19)^2$   
 $= 0.1191$

Same procedure can be applied to symmetrical GLCM



# Homogeneity derived from GLCM

- Is inverse of the contrast
- Decreases exponentially if more pixels are away from the diagonal
- Returns a value that measures the closeness of the intensity distribution
- Range is from 0 to 1
- Homogeneity is 1 for diagonal GLCM

$$homogeneity = \sum_{i,j} \frac{p(i,j)}{1 + |i - j|}$$

# Homogeneity derived from Example GLCM

		j→			
		1	2	3	4
i↓	1	0	1	2	3
	2	1	1	2	3
	3	1	0	2	0
	4	0	0	0	3

GLCM



		j→			
		1	2	3	4
i↓	1	0/19	1/19	2/19	3/19
	2	1/19	1/19	2/19	3/19
	3	1/19	0/19	2/19	0/19
	4	0/19	0/19	0/19	3/19

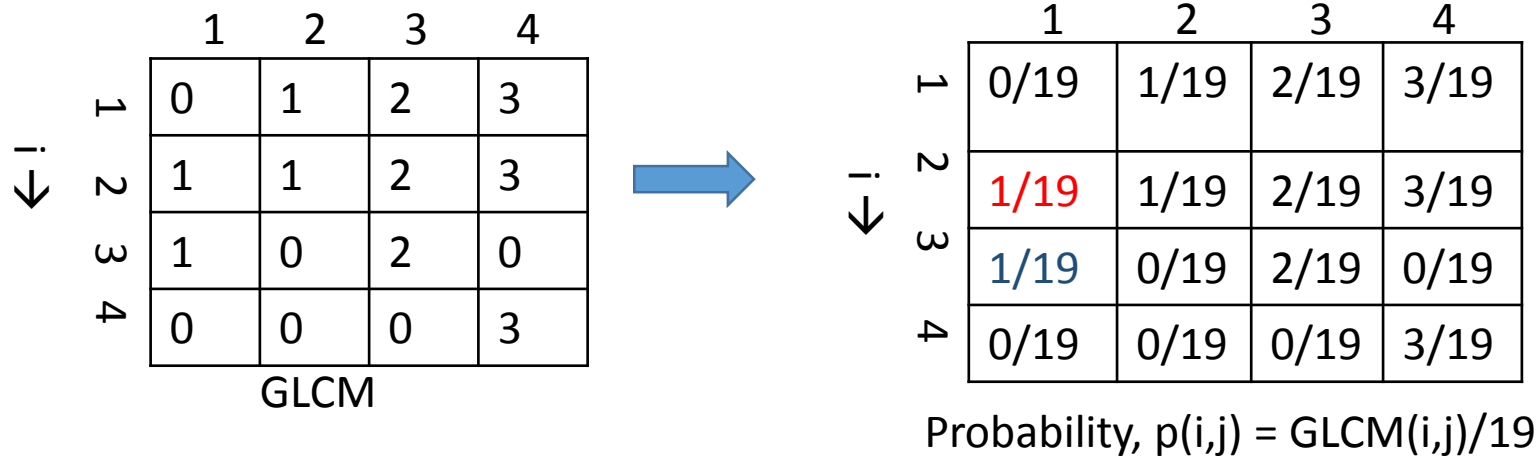
Probability,  $p(i,j) = \text{GLCM}(i,j)/19$

$$\text{homogeneity} = \sum_{i,j} \frac{p(i,j)}{1 + |i - j|}$$

$$\begin{aligned}
 \text{homogeneity} &= (1/19)[(1/2 + 1/3 + 1/2 + 1)] + (2/19)[(1/3 + 1/2 + 1/1)] + (3/19)[(1/4 + 1/3 + 1/1)] \\
 &= (1/19)[0.5 + 0.33 + 0.5 + 1 + 0.66 + 1 + 2 + 0.75 + 1 + 3] \\
 &= 0.5652
 \end{aligned}$$

Same procedure can be applied to symmetrical GLCM

# Entropy derived from GLCM



- If  $p(i,j)$  is small (i.e. occurrences of that pixel combination is low), entropy is large
- Measure of how pairs pixels with specific relationship are equally distributed

$$\text{entropy} = \sum_{i,j} -p(i,j) \ln(p(i,j))$$

$$\text{entropy} = -4(1/19)\ln(1/19) - 3(2/19)\ln(2/19) - 3(3/19)\ln(3/19)$$

Same procedure can be applied to symmetrical GLCM

# GLCM mean, variance

- GLCM mean is mean of number of times a pixel's occurrence with a specific relationship

$$\mu_i = \sum_{i,j} -ip(i,j) \qquad \mu_j = \sum_{i,j} -jp(i,j)$$

- Variance is dependent on the mean, and the dispersion around the mean
- It is not variance of grey levels in the original image

$$\sigma_i^2 = \sum_{i,j} p(i,j)(i - \mu_i)^2 \qquad \sigma_j^2 = \sum_{i,j} p(i,j)(j - \mu_j)^2$$

# Mean and Variance derived from Example GLCM

j→

	1	2	3	4
1	0	1	2	3
2	1	1	2	3
3	1	0	2	0
4	0	0	0	3

GLCM



j→

	1	2	3	4
1	0/19	1/19	2/19	3/19
2	1/19	1/19	2/19	3/19
3	1/19	0/19	2/19	0/19
4	0/19	0/19	0/19	3/19

Probability,  $p(i,j) = \text{GLCM}(i,j)/19$

$$\mu_i = \sum_{i,j} -ip(i,j)$$

$$\begin{aligned}\mu_i &= -1/19[(1+2+2+3)+2(1+2+3)+3(1+2)+4(3)] \\ &= 1/19[6+14+9+12] \\ &= 2.15\end{aligned}$$

$$\mu_j = \sum_{i,j} -jp(i,j)$$

$$\begin{aligned}\mu_j &= 1/19[(1+1)+2(1+1)+3(2+2+2)+4(3+3+3)] \\ &= 1/19[2+4+18+36] \\ &= 3.16\end{aligned}$$

Same procedure can be applied to symmetrical GLCM

# Mean and Variance derived from Example GLCM

j →

	1	2	3	4
1 ↓	0	1	2	3
2	1	1	2	3
3	1	0	2	0
4	0	0	0	3

GLCM



j →

	1	2	3	4
1 ↓	0/19	1/19	2/19	3/19
2	1/19	1/19	2/19	3/19
3	1/19	0/19	2/19	0/19
4	0/19	0/19	0/19	3/19

Probability,  $p(i,j) = \text{GLCM}(i,j)/19$

$$\sigma_i^2 = \sum_{i,j} p(i,j)(i - \mu_i)^2$$

$$\begin{aligned} \sigma_i &= (1-2.15)^2 + 2(1-2.15)^2 + 3(1-2.15)^2 \\ &\quad + (2-2.15)^2 + (2-2.15)^2 + 2(2-2.15)^2 + 3(2-2.15)^2 \\ &\quad + (3-2.15)^2 + 2(3-2.15)^2 + 3(4-2.15)^2 \\ &= 12.38 \end{aligned}$$

$$\sigma_j^2 = \sum_{i,j} p(i,j)(j - \mu_j)^2$$

Same procedure is applied for  $\sigma_j$

# Correlation from GLCM

- Measure of how correlated a pixel is to its neighbor in the image
- Range is -1 to 1
- 1 or -1 for a perfectly positively or negatively correlated image.
- NaN for constant image

$$Correlation = \sum_{i,j} (i - u_i)(j - \mu_j)p(i,j)/(\sigma_i\sigma_j)$$

- Single patches of a particular ground cover usually have a higher correlation value within them than between adjacent objects

Same procedure can be applied to symmetrical GLCM

# Correlation derived from Example GLCM

		j→			
		1	2	3	4
i↓	1	0	1	2	3
	2	1	1	2	3
	3	1	0	2	0
	4	0	0	0	3

GLCM



		j→			
		1	2	3	4
i↓	1	0/19	1/19	2/19	3/19
	2	1/19	1/19	2/19	3/19
	3	1/19	0/19	2/19	0/19
	4	0/19	0/19	0/19	3/19

Probability,  $p(i,j) = \text{GLCM}(i,j)/19$

$$\text{Correlation} = \sum_{i,j} (i - u_i)(j - \mu_j)p(i,j)/(\sigma_i\sigma_j)$$

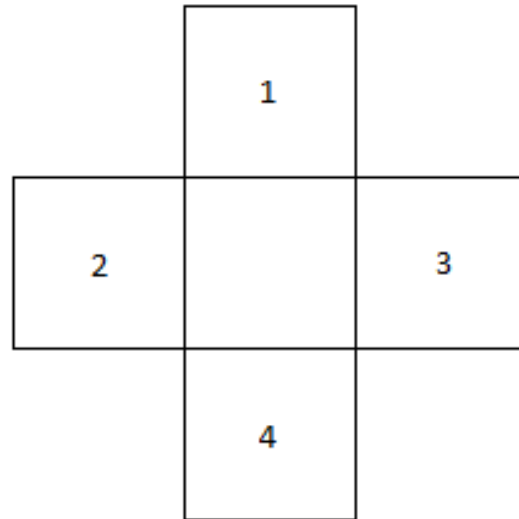
Correlation = 0.0783



# Connected Component Analysis

- Also known as Connected component labeling, blob extraction, or region labeling
- Used to determine the connectivity of “blob”-like regions in a binary image
- Used in computer vision to detect connected regions in binary images
- To extract separate objects from an image and describe these objects quantitatively

# 4- connectivity and 8-connectivity



4-connectivity



8-connectivity

# Pixel Connectivity

- Pixels that are directly next to each other
- and belong to the foreground class can be considered to belong to the same object

0	0	0	0	0	0	0	0
0	1	1	0	0	0	0	0
0	1	1	0	0	0	0	0
0	0	0	1	1	1	0	0
0	0	0	1	1	1	1	0
0	0	0	0	0	0	0	0

Image

0	0	0	0	0	0	0	0
0	A	A	0	0	0	0	0
0	A	A	0	0	0	0	0
0	0	0	B	B	B	0	0
0	0	0	B	B	B	B	0
0	0	0	0	0	0	0	0

4-connectivity

Assign different colors two objects

0	0	0	0	0	0	0	0
0	A	A	0	0	0	0	0
0	A	A	0	0	0	0	0
0	0	0	A	A	A	0	0
0	0	0	A	A	A	A	0
0	0	0	0	0	0	0	0

8-connectivity

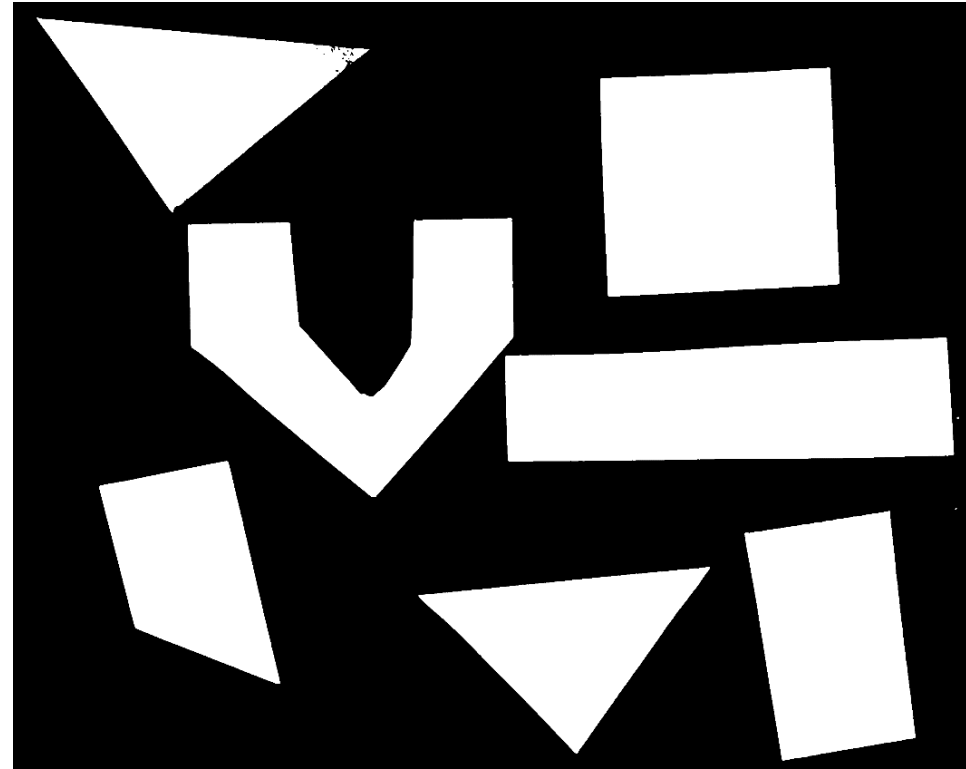
Assign one color object

# Connected Component Analysis for object detection

Objects with color are foreground and background is white



To count the number of objects, apply thresholding



7 objects are identified

# Connected Component Analysis

- Connectivity can be 4-connected neighborhood or 8-connected neighborhood
- Scans an image and group its pixels into components based on pixel connectivity
- All pixels in a connected component share similar pixel intensity values and are in some way connected with each other
- Once all groups have been determined, each pixel is labeled with a graylevel or a color (color labeling) according to the component it was assigned to
- Extracting and labeling of various disjoint and connected components in an image is useful for automated image analysis applications

# Steps for Connected Component Analysis

- Identifies connected pixel regions
- Identifies regions of adjacent pixels which have intensity from the given set,  $V$
- For binary image  $V=\{1\}$ .
- For gray image  $V$  can have a range of values
- Example:  $V = \{51, 52, 53, \dots, 77, 78, 79, 80\}$
- Scan the image by moving along a row until it comes to a point  $p$
- Where  $p$  denotes the pixel to be labeled in the scanning process) for which  $V=\{1\}$  or any other specified set

# Algorithm for Connected Component Analysis for object detection

- Label each connected component (or blob) with the same unique label
- Can find total number of individual blobs
- Output is different for different type of connectivity
- There are two common ways of defining whether or not a component is connected
  - A pixel has 4 neighbors (sometimes called 4-connectivity)
  - A pixel has 8 neighbors

# Algorithm for Connected Component Analysis for object detection

**First pass:** For each non-zero pixel, check its neighbours, if

- it has no non-zero neighbours, it is a new component, give it a new label
- it has one non-zero neighbor, these pixels are connected, give it the same label as the neighbour
- it has more than one non-zero neighbour, there are two cases:
  - neighbours have the same label, give the current pixel the same label
  - neighbours have different labels
    - Set the current pixel to the neighbours' lowest label
    - Keep a note of the equivalences of all the connected labels
    - Record which different labels should be the same
    - Solve equivalence in the second pass



# Algorithm for Connected Component Analysis for object detection

## Second pass

- For each pixel with a label,
- Check if this label has equivalent labels and change the label

# Algorithm for Connected Component Analysis for object detection

- Identify object/s
- Visually it shows that image has one object

0	0	0	1	1	1	0	0	0	0	1	1	1	1	0	1	1	1	1
0	0	0	1	1	1	1	0	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1

Image

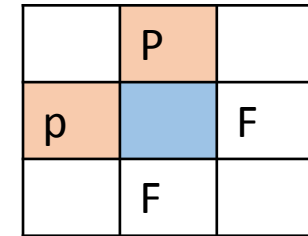
0	0	0	1	1	1	0	0	0	0	1	1	1	1	0	1	1	1	1
0	0	0	1	1	1	1	0	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1

Visually identified object

# Algorithm for Connected Component Analysis

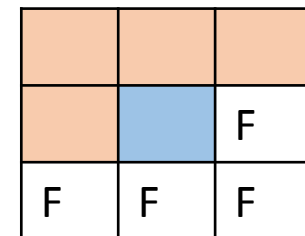
- Counter=0, label = 0
- Scan across row:
  - If pixel is 1 and connected, continue with lowest label above or behind (4-connected or 8-connected)
    - If 4-connectivity, 2 past values
    - If 8-connectivity, 4 past values
    - Record location of conflicts if any
  - If pixel is 1 and not connected, increment counter, and label = counter,
  - If pixel is 0 then label=0

4-connectivity



Has 2 past values and 2 future values

8-connectivity



Has 4 past values and 4 future values

# Algorithm for Connected Component Analysis

- Counter=0 and label = 0 and Scan across row
- If pixel is 1 and connected, continue with lowest label above or behind (4-connected or 8-connected)
- If pixel is 1 and not connected, increment counter, and label = counter
- If conflict continue with lowest label and record the location

0	0	0	1	1	1	0	0	0	0	1	1	1	1	0	1	1	1	1
0	0	0	1	1	1	1	0	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1

Image

0	0	0	1	1	1	0	0	0	0	2	2	2	2	0	3	3	3	3
0	0	0	1	1	1	1	0	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1

Scanned first row

# Algorithm for Connected Component Analysis

- Counter=0 and label = 0 and Scan across row
- If pixel is 1 and connected, continue with lowest label above or behind (4-connected or 8-connected)
- If pixel is 1 and not connected, increment counter, and label = counter
- If conflict continue with lowest label and record the location

0	0	0	1	1	1	0	0	0	0	2	2	2	2	0	3	3	3	3
0	0	0	1	1	1	1	0	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1

Scanned first row

0	0	0	1	1	1	0	0	0	0	2	2	2	2	0	3	3	3	3
0	0	0	1	1	1	1	0	0	0	2	2	2	2	0	0	3	3	3
0	0	0	1	1	1	1	1	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1

Scanned second row

# Algorithm for Connected Component Analysis

- Counter=0 and label = 0 and Scan across row
- If pixel is 1 and connected, continue with lowest label above or behind (4-connected or 8-connected)
- If pixel is 1 and not connected, increment counter, and label = counter
- If conflict continue with lowest label and record the location

0	0	0	1	1	1	0	0	0	0	2	2	2	2	0	3	3	3	3
0	0	0	1	1	1	1	0	0	0	2	2	2	2	0	0	3	3	3
0	0	0	1	1	1	1	1	0	0	2	2	2	2	0	0	3	3	3
0	0	0	1	1	1	1	1	1	0	2	2	2	2	0	0	3	3	3
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	0	0	0	0	0	0	1	1	1	1	1

Scanned next rows

0	0	0	1	1	1	0	0	0	0	2	2	2	2	0	3	3	3	3
0	0	0	1	1	1	1	0	0	0	2	2	2	2	0	0	3	3	3
0	0	0	1	1	1	1	1	0	0	2	2	2	2	0	0	3	3	3
0	0	0	1	1	1	1	1	1	0	2	2	2	2	0	0	3	3	3
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	3	3	3
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	0	3	3	3
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1

5<sup>th</sup> and 7<sup>th</sup> rows have conflict

$1 \equiv 2, 1 \equiv 3$

# Algorithm for Connected Component Analysis

- Counter=0 and label = 0 and Scan across row
- If pixel is 1 and connected, continue with lowest label above or behind (4-connected or 8-connected)
- If pixel is 1 and not connected, increment counter, and label = counter
- If conflict continue with lowest label and record the location

0	0	0	1	1	1	0	0	0	0	2	2	2	2	0	3	3	3	3
0	0	0	1	1	1	1	0	0	0	2	2	2	2	0	0	3	3	3
0	0	0	1	1	1	1	1	0	0	2	2	2	2	0	0	3	3	3
0	0	0	1	1	1	1	1	1	0	2	2	2	2	0	0	3	3	3
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	3	3	3
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	3	3	3
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1

5<sup>th</sup> and 7<sup>th</sup> rows have conflict

$1 \equiv 2, 1 \equiv 3$

0	0	0	1	1	1	0	0	0	0	1	1	1	1	0	1	1	1	1
0	0	0	1	1	1	1	0	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1

Change 2 and 3 to 1

# Algorithm for Connected Component Analysis

0	0	0	1	1	1	0	0	0	0	1	1	1	1	0	1	1	1	1
0	0	0	1	1	1	1	0	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1

Change 2 and 3 to 1

0	0	0	1	1	1	0	0	0	0	1	1	1	1	0	1	1	1	1
0	0	0	1	1	1	1	0	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	0	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	0	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	0	0	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	0	1	1	1	1	1	1	0	0	0	0	0	1	1	1	1	1

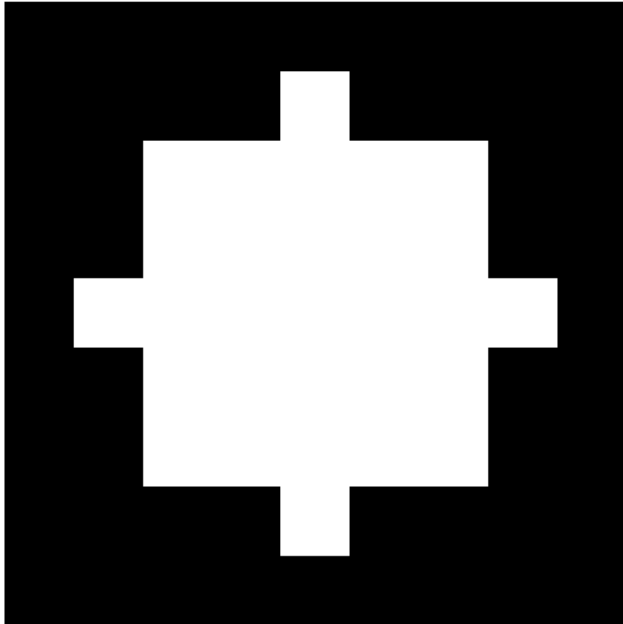
Assign a color to label 1



# Distance Transform

- A metric or measure of the separation of foreground pixels from background pixels
- Replaces each foreground pixel of a binary image with the distance to the closest background pixel
- Does not measure distance among foreground pixels
- Different grey levels are allocated to distance values

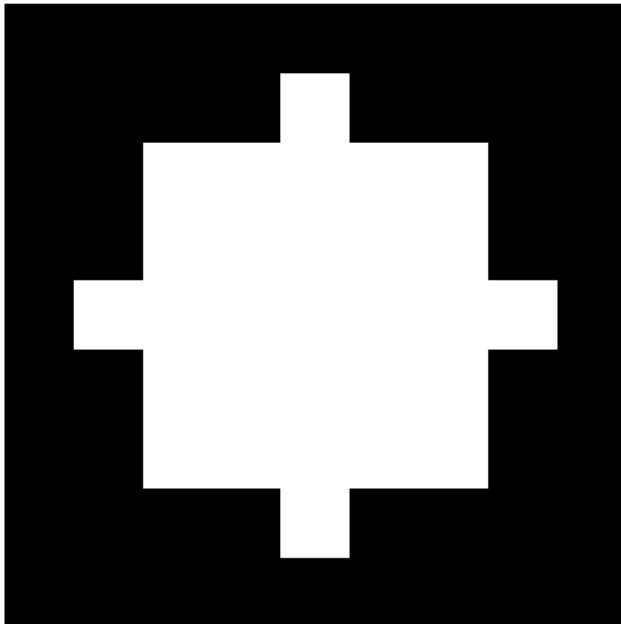
Binary image



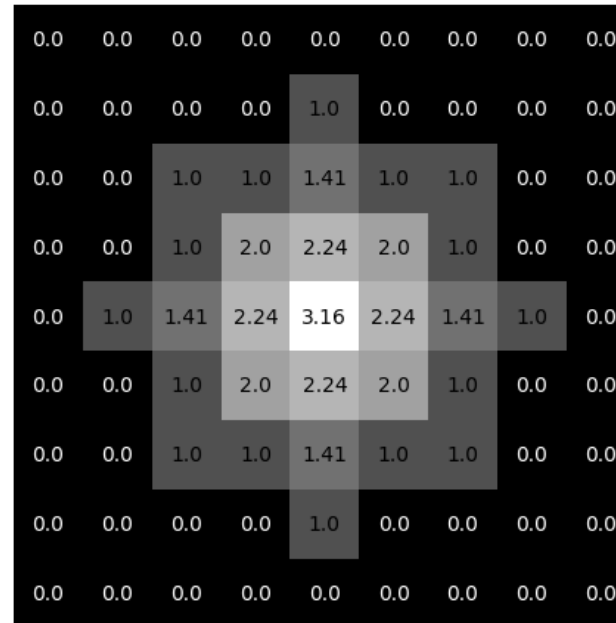
# Distance Transform

- A metric or measure of the separation of foreground pixels from background pixels
- Replaces each foreground pixel of a binary image with the distance to the closest background pixel
- Does not measure distance among foreground pixels
- Different grey levels are allocated to distance values

Binary image



## Distance transform



# Distance Transform

- Distance Metrics
  - Euclidean
    - Straight-line distance between p (foreground) and q (nearest background) pixels
    - Distance between two consecutive pixels is 1 unit

$$d = ((p_1 - q_1)^2 + (p_2 - q_2)^2)^{1/2}$$

0	0	0
0	1	0
0	0	0

Image

# Distance Transform

- Distance Metrics
  - Euclidean
    - Straight-line distance between  $p$  (foreground) and  $q$  (nearest background) pixels
    - Distance between two consecutive pixels is 1 unit

$$d = ((p_1 - q_1)^2 + (p_2 - q_2)^2)^{1/2}$$

0	0	0
0	1	0
0	0	0

Image

1.41	1.0	1.41
1.0	0.0	1.0
1.41	1.0	1.41

Distance Transform

# Distance Transform

- City Block (Manhattan Distance)
  - Measures the path between the pixels based on a 4-connected neighborhood
  - Pixels with edges touching foreground pixel are 1 unit apart
  - Pixels diagonally touching are 2 units apart

$$d = |p_1 - q_1| + |p_2 - q_2|$$

0	0	0
0	1	0
0	0	0

Image

2	1	2
1	0	1
2	1	2

Distance Transform

City Block distance

# Distance Transform

- Chessboard
  - measures the path between the pixels based on an 8-connected neighborhood
  - Pixels whose edges or corners touch are 1 unit apart

0	0	0
0	1	0
0	0	0

Image

1	1	1
1	0	1
1	1	1

Distance Transform

Chessboard

# Distance Transform

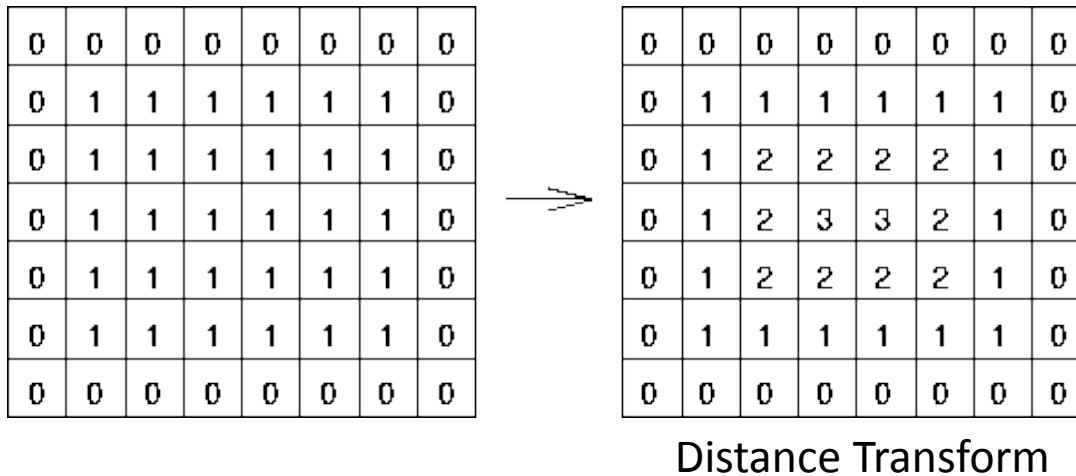
- Using chess board distance metric

0	0	0	0	0	0	0	0
0	1	1	1	1	1	1	0
0	1	1	1	1	1	1	0
0	1	1	1	1	1	1	0
0	1	1	1	1	1	1	0
0	1	1	1	1	1	1	0
0	0	0	0	0	0	0	0



# Distance Transform

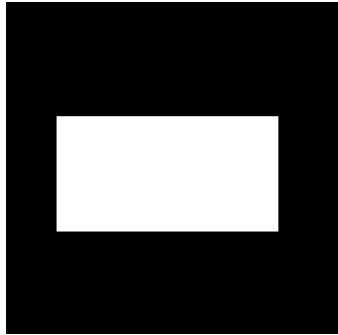
- Using chess board distance metric



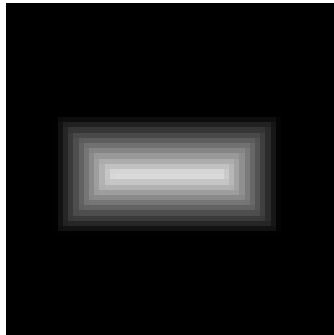
- Dual of distance transform produces the distance transform for the background
- Can be considered as a process of inverting the original image and then applying the standard transform



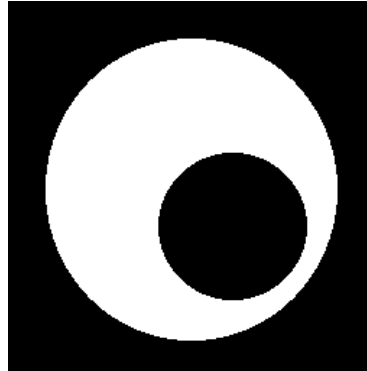
# Examples: Distance Transform



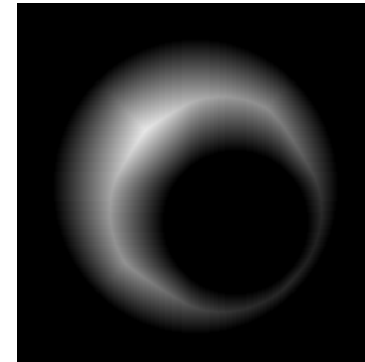
Binary image



Distance transform

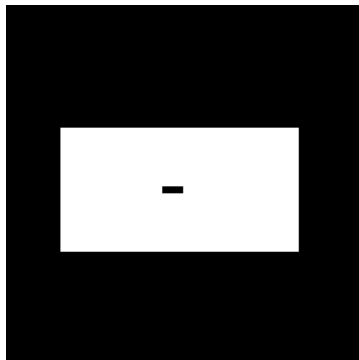


Binary image

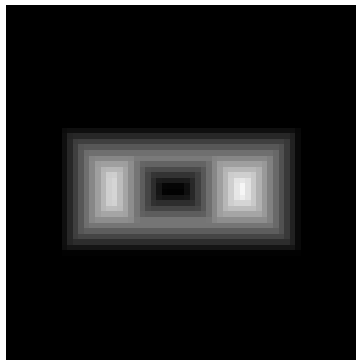


Distance transform

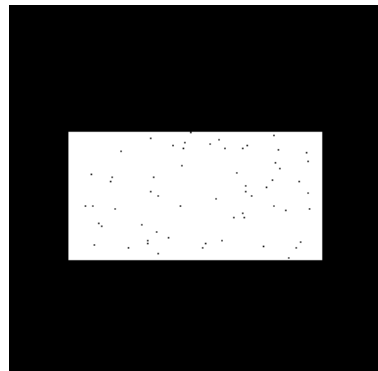
- distance transform is sensitive to small changes in the object



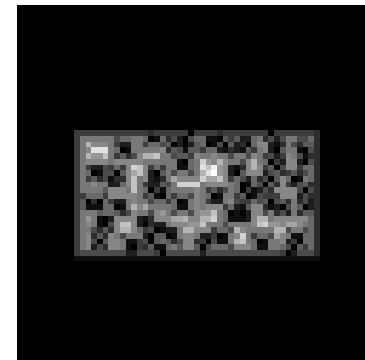
Binary image



Distance transform



Binary image



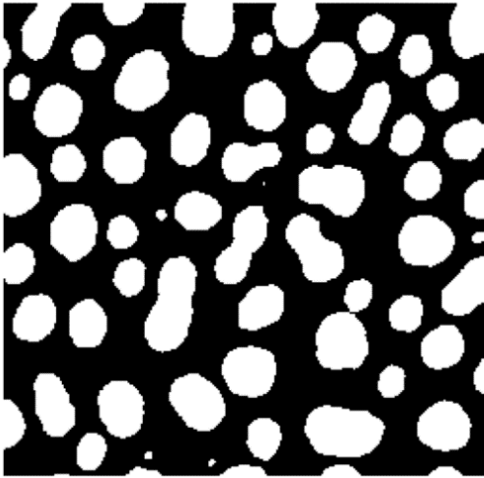
Distance transform

# Why distance transform?

- Eroding or dilating binary images by a large amount can be very slow using for morphology operations or spatial
  - because large maximum or minimum structuring element/ filters are required
- Instead apply distance map (transform) and apply global threshold
  - Much faster than morphology operation

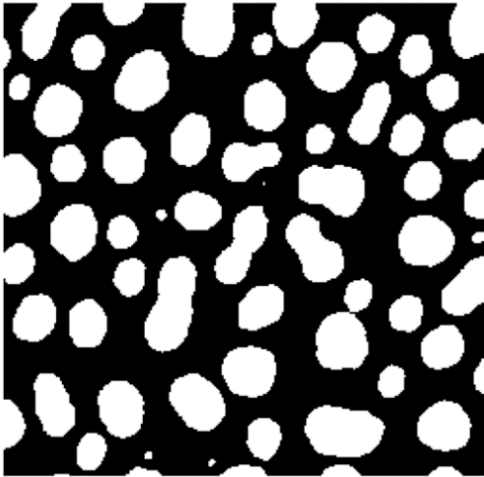
# Application of distance transform

(A) Binary image

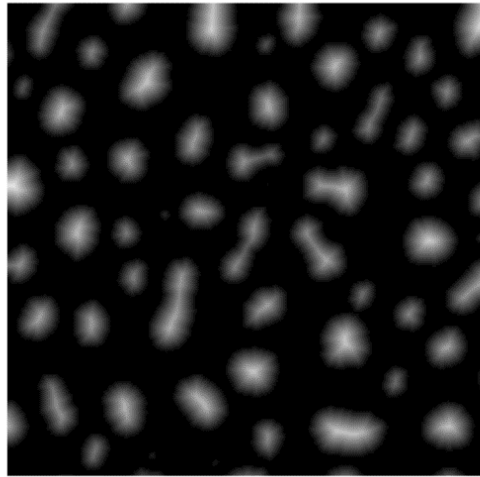


# Application of distance transform

(A) Binary image

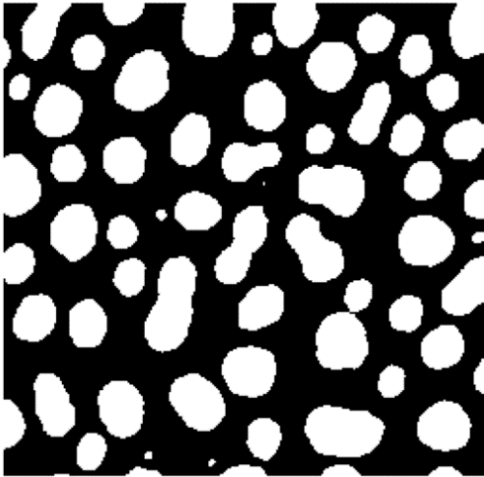


(B) Distance map of (A)

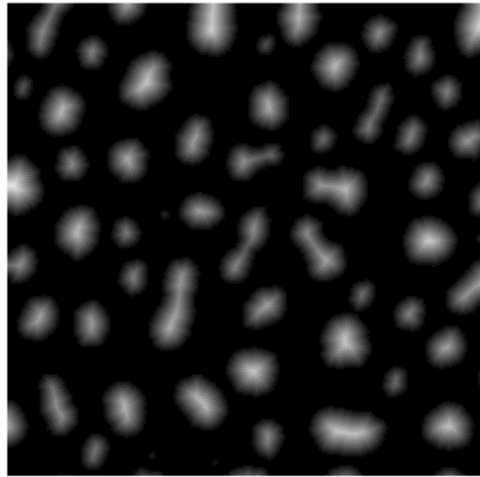


# Application of distance transform

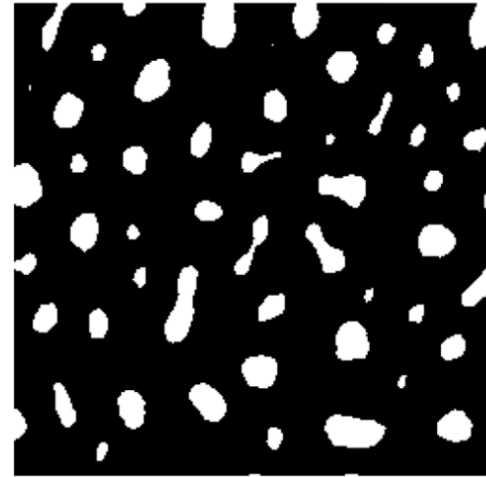
(A) Binary image



(B) Distance map of (A)

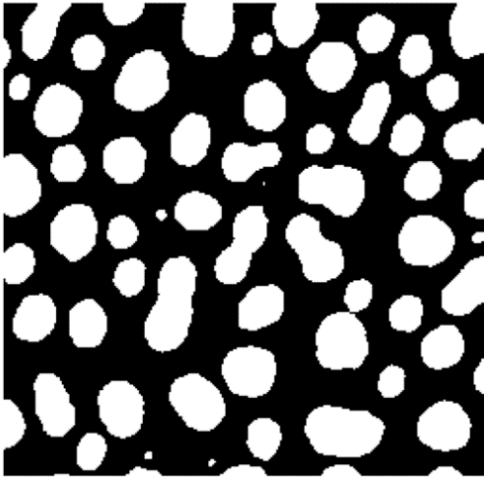


(C) Thresholded (B)  $> 5$

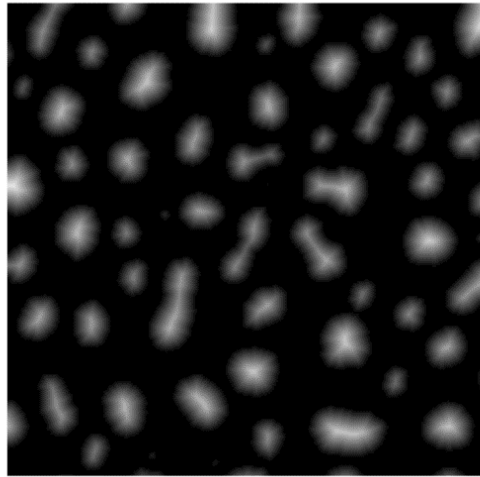


# Application of distance transform

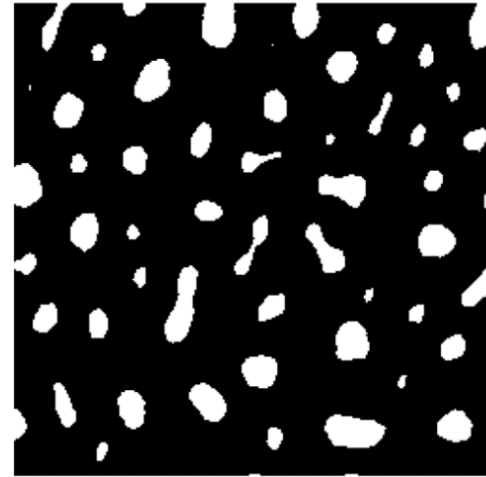
(A) Binary image



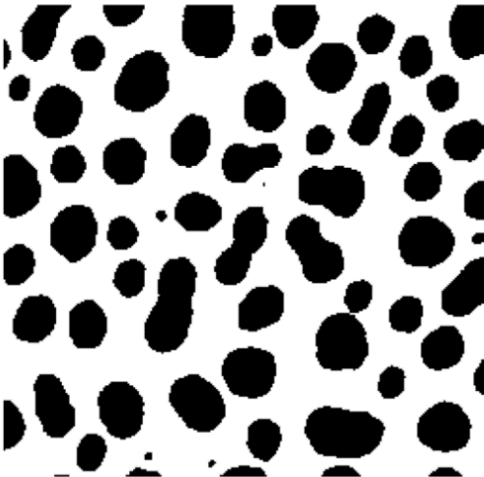
(B) Distance map of (A)



(C) Thresholded (B)  $> 5$

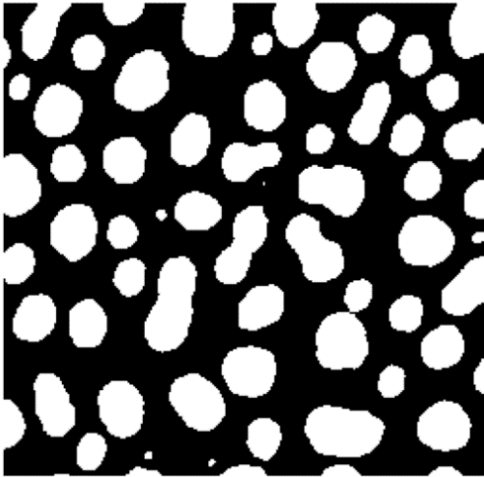


(D) Binary image (inverted)

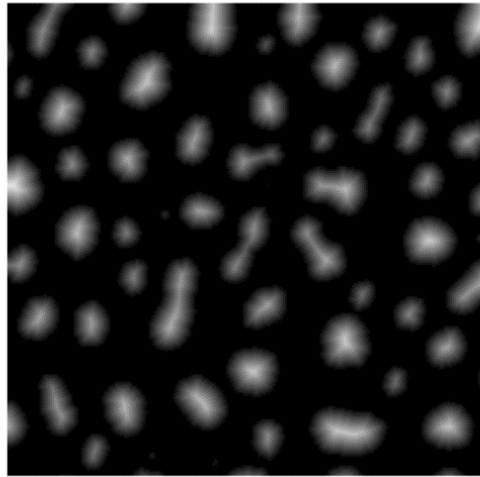


# Application of distance transform

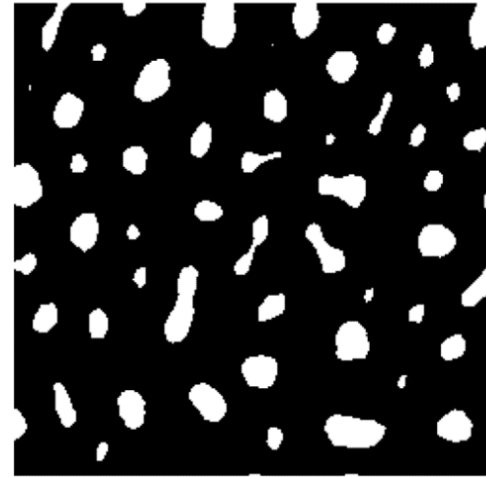
(A) Binary image



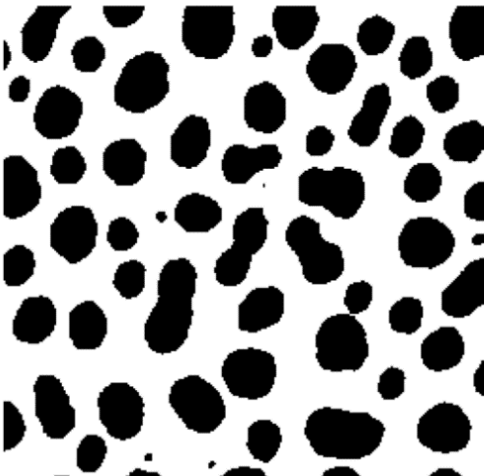
(B) Distance map of (A)



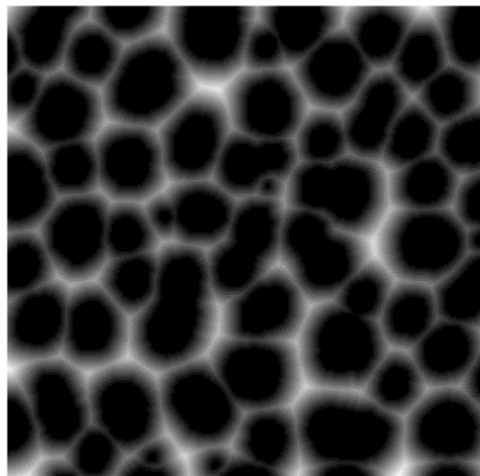
(C) Thresholded (B)  $> 5$



(D) Binary image (inverted)

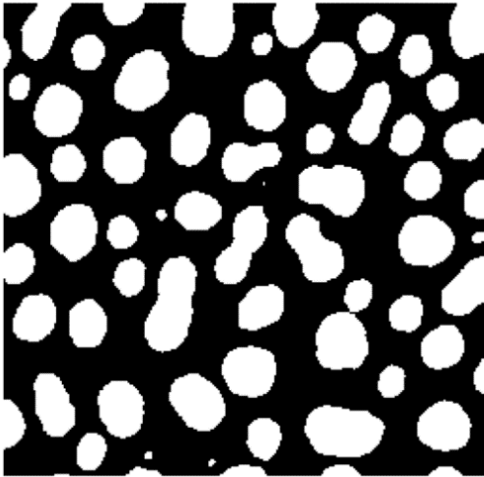


(E) Distance map of (D)

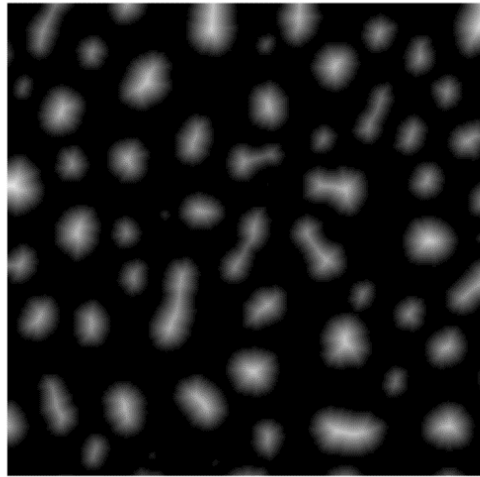


# Application of distance transform

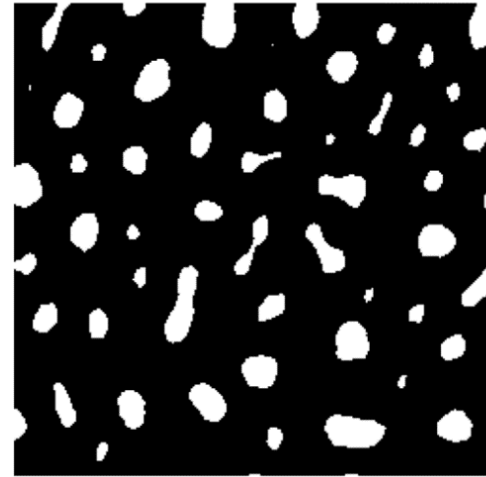
(A) Binary image



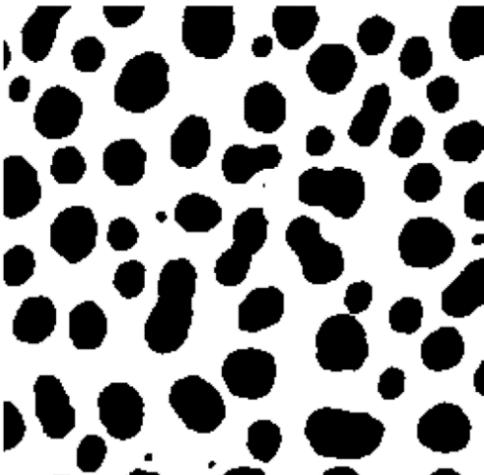
(B) Distance map of (A)



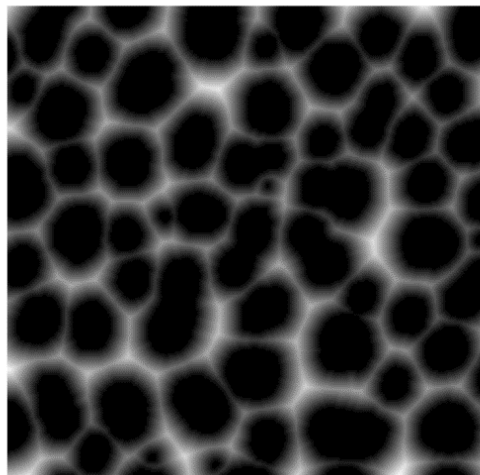
(C) Thresholded (B)  $> 5$



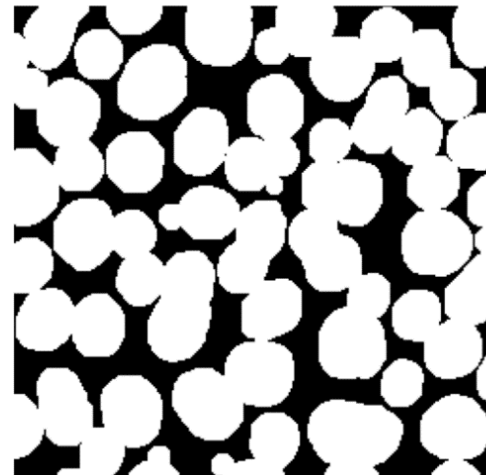
(D) Binary image (inverted)



(E) Distance map of (D)



(F) Thresholded (E)  $< 5$





# Skeletonization /Medial Axis Transform(MAT)

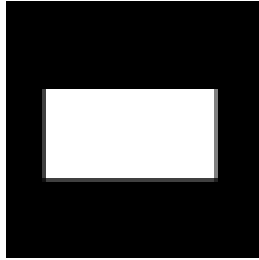
- The skeleton is a binary image showing the skeleton of objects
- MAT can also be used to determine skeleton of an object
- It generates gray image where each point on the skeleton has intensity which represents its distance to a boundary in the original object
- MAT is the similar to distance transform but with all points away from skeleton are suppressed to zero

# Skeletonization using morphology or MAT

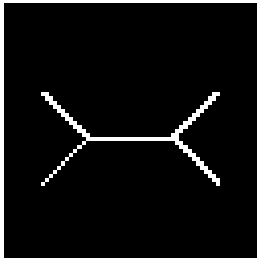
## Morphology

- Use thinning that successively erodes away pixels from the boundary
- while preserving the end points of line segments until no more thinning is possible
- Resulting image is skeleton
- MAT
  - Calculate the distance transform and apply threshold
  - more efficient than morphology

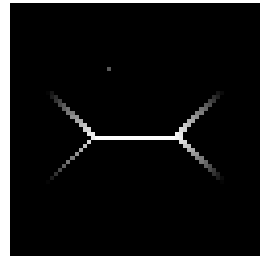
# Skeletonization /Medial Axis Transform



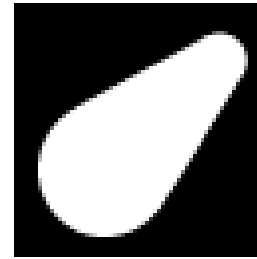
Binary image



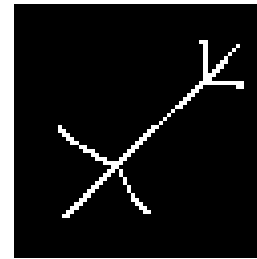
Morphology



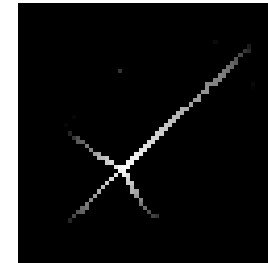
MAT



Binary image



Morphology

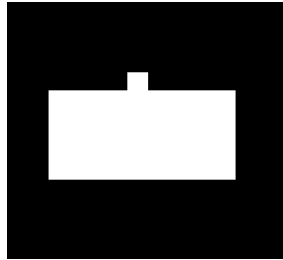
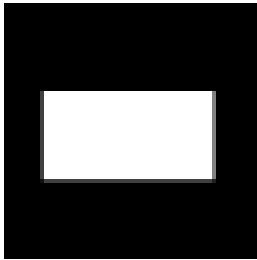


MAT

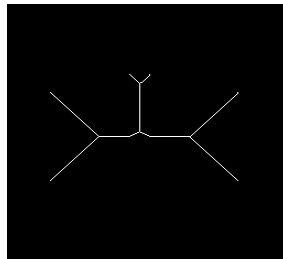
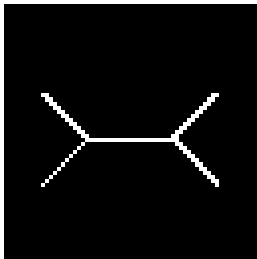
# Skeletonization /Medial Axis Transform

- Skeletonization using MAT is also very sensitive to noise

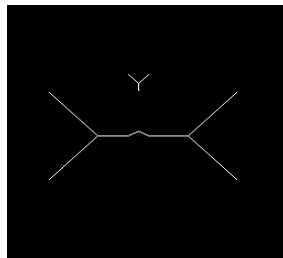
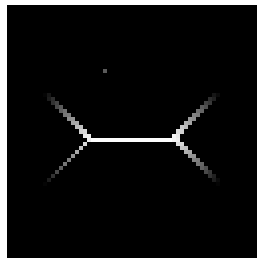
Binary image



Morphology

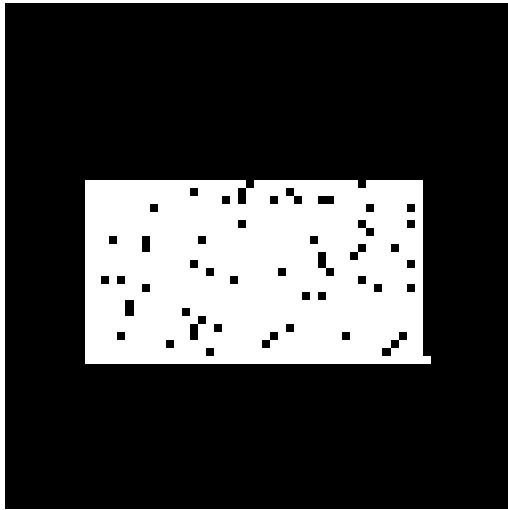


MAT

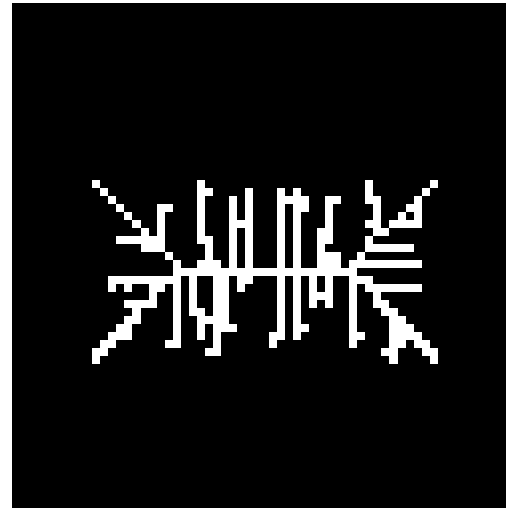


# Skeletonization /Medial Axis Transform

- Skeletonization using MAT is also very sensitive to noise
- Apply averaging/ median filter to reduce noise before applying MAT



Binary image with  
salt and pepper  
noise



MAT