

# Max-Subarray Sum Problem and Solution Algorithms

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**Abstract**—Maximum Subarray Sum is a well-known problem in the field of computer science. There are multiple number of solution algorithms with different complexities. In this paper, we demonstrated and compared 3 of these algorithms with quadratic, linear, and logarithmic complexities.

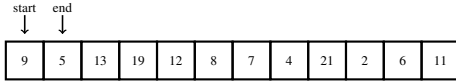
## I. THE PROBLEM

The Maximum Subarray Sum problem is the task of finding the contiguous subarray with largest sum in a given array of integers. Each number in the array could be positive, negative, or zero. For example: Given the array  $[-2, 1, -3, 4, -1, 2, 1, -5, 4]$  the solution would be  $[4, -1, 2, 1]$  with a sum of 6.

## II. SOLUTIONS

### A. Brute-Force Approach

This is the most intuitive solution to anyone. You basically traverse over the array and compare every possible combination of start and end index for the solution array.



The *start* index will be incremented by 1 everytime the *end* index reaches the end of the array. Then the *end* index will start from the element right next to the start element. At every iteration the sum between *start* and *end* indexes will be calculated. Hence, the maximum sum will be determined by computing every sum for the every possible sub-array. The complexity of this algorithm is  $\mathcal{O}(n^3)$ . With a little improvement we can convert this algorithm to be  $\mathcal{O}(n^2)$ . Instead of calculating the sum between two array indices at every iteration from scratch, we know that the current sum will be the (current element + previous sum). Consequently, eliminating the loop which is used for calculating the sum from the algorithm will reduce the time complexity.

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### Algorithm 1 Brute-Force

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 $y \leftarrow 1$ 
if  $n < 0$  then
   $X \leftarrow 1/x$ 
   $N \leftarrow -n$ 
else
   $X \leftarrow x$ 
   $N \leftarrow n$ 
end if
while  $N \neq 0$  do
  if  $N$  is even then
     $X \leftarrow X \times X$ 
     $N \leftarrow N/2$ 
  else  $\{N$  is odd $\}$ 
     $y \leftarrow y \times X$ 
     $N \leftarrow N - 1$ 
  end if
end while

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