

A simple model for assessing climate control trade-offs and responding to unanticipated climate outcomes

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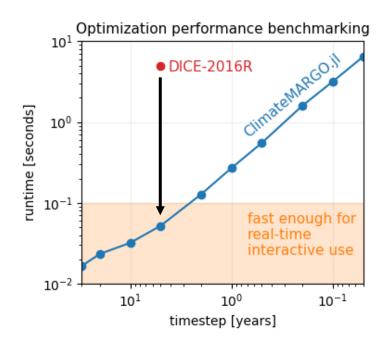
A simple model for assessing climate control trade-offs and responding to unanticipated climate outcomes

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ClimateMARGO.jl

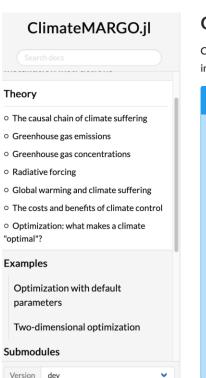
- Free for all
- Transparently developed
- Well-documented
- Understandable by beginners
- Efficient and fast
- Flexible and extendable
- Reactive web-app for teaching and outreach



ClimateMARGO.jl

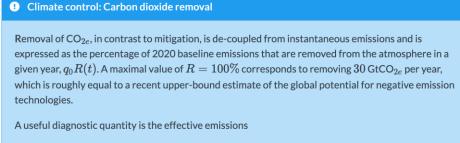
A Julia implementation of MARGO, an idealized framework for optimization of climate change control strategies.





Greenhouse gas concentrations &

 CO_{2e} continues to accumulate in the atmosphere and its concentrations $c(t) = c_0 + \int_{t_0}^t rq(t) dt$ will increase as long as the emissions q(t) are greater than zero.



 $rq(t)(1-M(t))-rq_0R(t),$

which is the annual rate of CO_{2e} accumulation in the atmosphere, including negative contributions from both emissions mitigation and CDR.

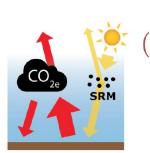
The change in CO_{2e} concentrations is simply the integral of the effective emissions over time,

$$c_{M,R}(t) = c_0 + \int_{t_0}^t rq(t') (1-M(t')) \; \mathrm{d}t' - rq_0 \int_{t_0}^t R(t') \; \mathrm{d}t'.$$

Code at github.com/ClimateMARGO

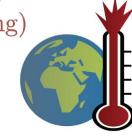
Carbon Dioxide Removal





Solar Radiation Modification (Geo-engineering)





Concentrations

$$c_{M,R}(t) = c_0 + \int_{t_0}^{t_f} rq(t')(1 - M(t')) - rq_0 \frac{R(t')}{dt'} dt' \qquad F_{M,R,G}(t) = a \ln\left(\frac{c_{M,R}}{c_0}\right) - \frac{G(t)}{F_{\infty}} \qquad T_{M,R,G}(t) = T_0 + \frac{F_{M,R,G}(t)}{B + \kappa} + T_{\text{slow}}(t)$$



$$F_{M,R,G}(t) = a \ln\left(\frac{c_{M,R}}{c_0}\right) - G(t)F_{\circ}$$

Temperature

$$T_{M,R,G}(t) = T_0 + \frac{F_{M,R,G}(t)}{B+\kappa} + T_{\text{slow}}(t)$$



Mitigation <

Emissions

$$q(t)(1-M(t))$$



Control costs

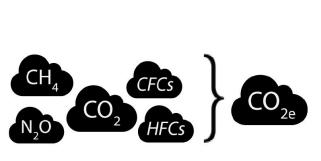
$$C_M M^2 + C_R R^2 + C_G G^2 + C_A A^2$$





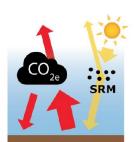
$$D_{M,\mathbf{R},G,A} = \beta \left(T_{M,\mathbf{R},G} - A(t)T \right)^2$$





Carbon Dioxide Removal

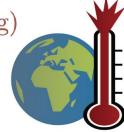




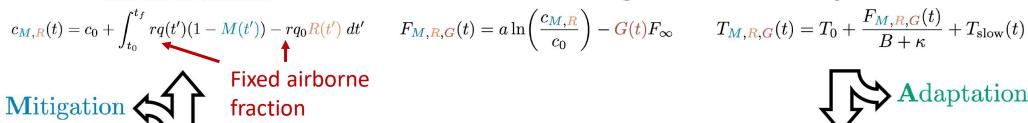
Solar Radiation Modification

(Geo-engineering)





Concentrations



Radiative Forcing

$$F_{M,R,G}(t) = a \ln\left(\frac{c_{M,R}}{c_0}\right) - G(t)F_{\infty}$$

Temperature

$$T_{M,R,G}(t) = T_0 + \frac{F_{M,R,G}(t)}{B+\kappa} + T_{\mathrm{slow}}(t)$$



Emissions

$$q(t)(1-M(t))$$



Control costs

$$C_M M^2 + C_R R^2 + C_G G^2 + C_A A^2$$





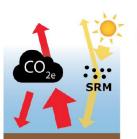
$$D_{M,R,G,A} = \beta \left(T_{M,R,G} - A(t)T \right)^2$$





Carbon Dioxide Removal

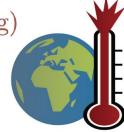




Solar Radiation Modification

(Geo-engineering)





Concentrations

$$c_{M,R}(t) = c_0 + \int_{t_0}^{t_f} rq(t')(1 - M(t')) - rq_0 \frac{R(t')}{dt'} dt' \qquad F_{M,R,G}(t) = a \ln\left(\frac{c_{M,R}}{c_0}\right) - \frac{G(t)}{c_0} F_{\infty} \qquad T_{M,R,G}(t) = T_0 + \frac{F_{M,R,G}(t)}{B + \kappa} + T_{\text{slow}}(t)$$



$$F_{M,R,G}(t) = a \ln\left(\frac{c_{M,R}}{c_0}\right) - G(t)F_{\infty}$$

Temperature







Emissions

$$q(t)(1-M(t))$$

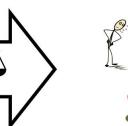


Control costs

$$C_M M^2 + C_R R^2 + C_G G^2 + C_A A^2$$



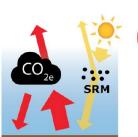
$$D_{M,\mathbf{R},G,A} = \beta \left(T_{M,\mathbf{R},G} - A(t)T \right)^2$$





Carbon Dioxide Removal

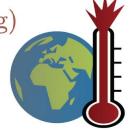




Solar Radiation Modification

(Geo-engineering)





Two-box energy balance model: fast and slow responses

Concentrations

$$c_{M,R}(t) = c_0 + \int_{t_0}^{t_f} rq(t')(1 - M(t')) - rq_0 \frac{R(t')}{dt'} dt' \qquad F_{M,R,G}(t) = a \ln\left(\frac{c_{M,R}}{c_0}\right) - \frac{G(t)}{F_{\infty}} \qquad T_{M,R,G}(t) = T_0 + \frac{F_{M,R,G}(t)}{B + \kappa} + T_{\text{slow}}(t)$$



$$F_{M,R,G}(t) = a \ln \left(\frac{c_{M,R}}{c_0} \right) - G(t) F_{\infty}$$

Temperature

$$T_{M,R,G}(t) = T_0 + \frac{F_{M,R,G}(t)}{R + \kappa} + T_{\text{slow}}(t)$$





Emissions

$$q(t)(1-M(t))$$



Control costs

$$C_M M^2 + C_R R^2 + C_G G^2 + C_A A^2$$



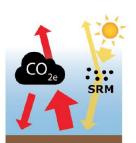
$$D_{M,\mathbf{R},\mathbf{G},A} = \beta \left(T_{M,\mathbf{R},\mathbf{G}} - A(t)T \right)^{2}$$





Carbon Dioxide Removal

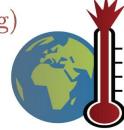




Solar Radiation Modification







Concentrations

$$c_{M,R}(t) = c_0 + \int_{t_0}^{t_f} rq(t')(1 - M(t')) - rq_0 \frac{R(t')}{dt'} dt' \qquad F_{M,R,G}(t) = a \ln\left(\frac{c_{M,R}}{c_0}\right) - \frac{G(t)}{F_{\infty}} \qquad T_{M,R,G}(t) = T_0 + \frac{F_{M,R,G}(t)}{B + \kappa} + T_{\text{slow}}(t)$$



$$F_{M,R,G}(t) = a \ln \left(\frac{c_{M,R}}{c_0} \right) - G(t) F_{\infty}$$

Temperature

$$T_{M,R,G}(t) = T_0 + \frac{F_{M,R,G}(t)}{B+\kappa} + T_{\text{slow}}(t)$$





$$q(t)(1-M(t))$$



Quadratic cost and damage functions



Adaptation

Control costs

$$C_M M^2 + C_R R^2 + C_G G^2 + C_A A^2$$



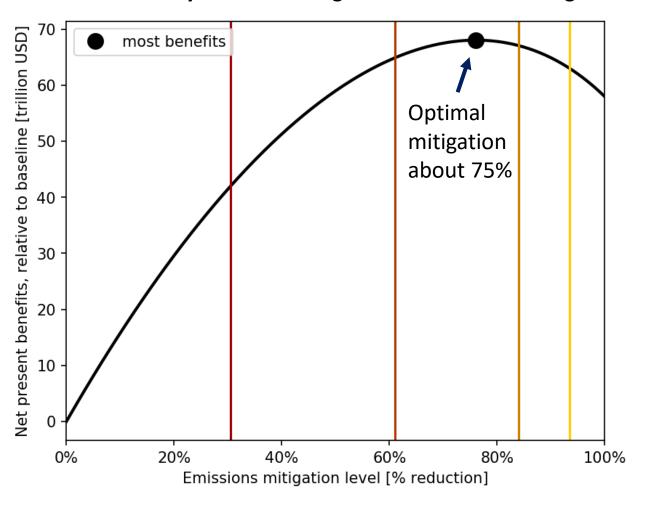
$$D_{M,\mathbf{R},\mathbf{G},A} = \beta \left(T_{M,\mathbf{R},\mathbf{G}} - A(t)T \right)^{2}$$





Visualizing MARGO's optimization problems in one dimension

Cost-benefit analysis: maximizing the net benefit of mitigation



Benefit = avoided damages

$${\cal B} = D - D_{M,R,G,A} = eta(T^2 - (T_{M,R,G,A})^2).$$

Maximize net benefits (benefits minus costs)

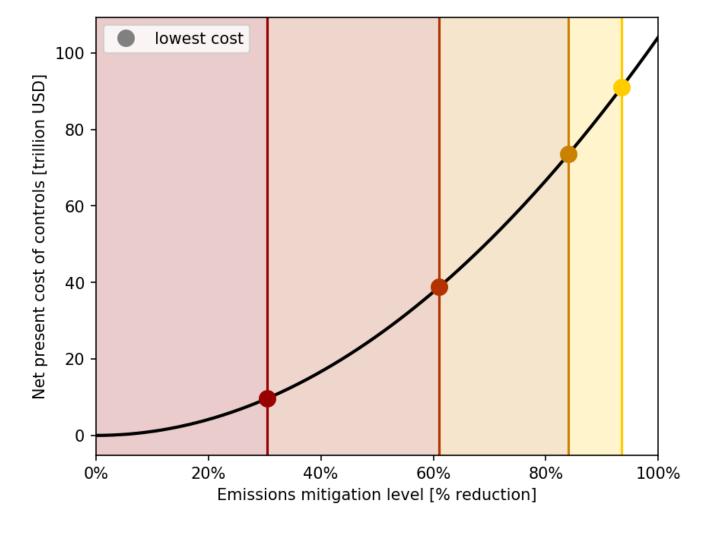
$$\max\left\{\int_{t_0}^{t_f}\left(\mathcal{B}_{M,R,G,A}-\mathcal{C}_{M,R,G,A}
ight)(1+
ho)^{-(t-t_0)}\,\mathrm{d}t
ight\},$$

Reduce dimensions by:

- Fixing $M(t) = M_0$ constant
- Removing other controls: R = G = A = 0

Visualizing MARGO's optimization problems in one dimension

Cost-effectiveness analysis: minimizing the cost of mitigation, subject to a temperature goal



Minimize control costs

$$\min\left\{\int_{t_0}^{t_f} {\mathcal C}_{M,R,G,A} (1+
ho)^{-(t-t_0)} \; \mathrm{d}t
ight\}$$

subject to a policy constraint (e.g. temperature threshold)

$$T_{M,R,G,A} < T^{\star},$$

Reduce dimensions by:

- Fixing $M(t) = M_0$ constant
- Removing other controls: R = G = A = 0