And yet it moves: the momentum of static electromagnetic fields

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1 Momentum in "static" electromagnetic configurations

That a "static" electromagnetic field configuration can have non-zero momentum is today no longer a matter of discussion, with plenty of experimental evidence and theoretical analyses.[1]

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("de X" is listed under D, "van X" under V, and so on, regardless of national conventions.)

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[1] Page & Adams 1945; Feynman, Leighton, et al. 2010 Ch. 27; Pugh & Pugh 1967; Furry 1969; Calkin 1971; Wallace & O'Connell 1980; Casserberg 1982; Sharma 1988; Narayan 2021; Gralla & Lobo 2022; see also Poynting 1905; Page 1958 § 158; Jones & Richards 1954; Calkin 1966; Coleman & Van Vleck 1968; Scanio 1975; McDonald 2015; Majcen, Haaland, et al. 2000; McDonald 2003; 2019; Harbola 2010; Griffiths 2012; Morris & Styer 2012; McDonald 2022.

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