## Funcons-beta: Multisets \*

## The PLanCompS Project

Multisets.cbs | PLAIN | PRETTY

## Multisets (bags)

```
[ Type multisets
Funcon multiset
Funcon multiset-elements
Funcon multiset-occurrences
Funcon multiset-insert
Funcon multiset-delete
Funcon is-submultiset ]

Meta-variables GT <: ground-values

Built-in Type multisets(GT)
```

multisets(GT) is the type of possibly-empty finite multisets of elements of GT.

```
Built-in Funcon multiset(\_:(GT)^*):\Rightarrow multisets(GT)
```

Note that  $\operatorname{multiset}(\cdots)$  is not a constructor operation. The order of argument values is ignored, but duplicates are significant, e.g.,  $\operatorname{multiset}(1,2,2)$  is equivalent to  $\operatorname{multiset}(2,1,2)$ , but not to  $\operatorname{multiset}(1,2)$  or  $\operatorname{multiset}(2,1)$ .

```
Built-in Funcon multiset-elements(\_: multisets(GT)) : \Rightarrow(GT)*
```

For each multiset MS, the sequence of values  $V^*$  returned by multiset-elements(MS) contains each element of MS the same number of times as MS does. The order of the values in  $V^*$  is unspecified, and may vary between multisets.

```
Assert multiset(multiset-elements(S)) == S
```

Built-in Funcon multiset-occurrences( $\_: GT, \_: multisets(GT)$ ):  $\Rightarrow$  natural-numbers

multiset-occurrences (GV, MS) returns the number of occurrences of GV in MS.

Built-in Funcon multiset-insert( $\_: GT, \_:$  natural-numbers,  $\_:$  multisets(GT)) :  $\Rightarrow$  multisets(GT)

<sup>\*</sup>Suggestions for improvement: plancomps@gmail.com.
Reports of issues: https://github.com/plancomps/CBS-beta/issues.

 $\operatorname{multiset-insert}(GV, N, MS)$  returns the multiset that differs from MS by containing N more copies of GV.

```
\textit{Built-in Funcon} \quad \mathsf{multiset-delete}(\_: \mathsf{multisets}(\textit{GT}), \_: \textit{GT}, \_: \mathsf{natural-numbers}) : \Rightarrow \mathsf{multisets}(\textit{GT})
```

multiset-delete(MS, GV, N) removes N copies of V from the multiset MS, or all copies of GV if there are fewer than N in MS.

```
Built-in Funcon is-submultiset(\_: multisets(GT), \_: multisets(GT)) : \Rightarrow booleans
```

is-submultiset( $MS_1$ ,  $MS_2$ ) tests whether every element of  $MS_1$  has equal or fewer occurrences in  $MS_1$  than in  $MS_2$ .