RV COLLEGE OF ENGINEERING®, BENGALURU-560059

(Autonomous Institution Affiliated to VTU, Belagavi)

DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING



"Hybrid Programming with MPI + OpenMP" ASSIGNMENT REPORT

Submitted by

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in partial fulfillment for the requirement of 7th Semester

Parallel Architecture and Distributed Programming (16CS71)

Submitted to

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Academic Year 2020 - 2021

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1. Introduction

The basic aims of parallel programming are to decrease the runtime for the solution to a problem and increase the size of the problem that can be solved. The conventional parallel programming practices involve a a pure OpenMP implementation on a shared memory architecture or a pure MPI implementation on distributed memory computer architectures. The largest and fastest computers today employ both shared and distributed memory architecture. This gives a flexibility in tuning the parallelism in the programs to generate maximum efficiency and balance the computational and communication loads in the program. A wise implementation of hybrid parallel programs utilizing the modern hybrid computer hardware can generate massive speedups in the otherwise pure MPI and pure OpenMP implementations.

Hybrid application programs using MPI + OpenMP are now commonplace on large HPC systems. There are essentially two main motivations for this combination of programming models:

- 1. Reduction in memory footprint, both in the application and in the MPI library (e.g. communication buffers).
- 2. Improved performance, especially at high core counts where the pure MPI scalability is running out.

2. MPI support for threads

In general making libraries thread-safe can be difficult. Internal data structures in the library either have to be replicated (for example, one per thread), or else accesses to these structures must be protected by some form of synchronisation (typically locks). This may add significant overheads which can affect the performance of the library even when only one thread is being used. The MPI standard defines various classes of thread usage. The user can request a certain class for their application and the implementation can return the class that is actually supported.

The MPI specification defines the following four classes of thread safety:

- 1. **MPI THREAD SINGLE** Only one thread will execute.
- 2. **MPI_THREAD_FUNNELED** The process may be multi-threaded, but only the main thread will make MPI calls (all MPI calls are funneled to the main thread).
- 3. **MPI_THREAD_SERIALIZED** The process may be multi-threaded, and multiple threads may make MPI calls, but only one at a time.
- 4. **MPI_THREAD_MULTIPLE** Multiple threads may call MPI, with no restrictions.

3. MPI + OpenMP Programming Styles

MPI + OpenMP programs are classified into five distinct styles depending on how multiple OpenMP threads make MPI library calls:

1. Master-only

In Master-Only style all MPI calls are made by the OpenMP master thread, outside of parallel regions. This requires the MPI_THREAD_FUNNELED level of thread support, since other threads will be executing, but not calling MPI. It is implemented by identifying the most time consuming loops and using parallel constructs to multithread them. Disadvantage of this style is that threads other than the master are necessarily idle during MPI calls, and cannot do any useful computation.

Outline code for this style of MPI + OpenMP program is given by:

```
#pragma omp parallel
{
    work...
}
ierror=MPI_Send(...);
#pragma omp parallel
{
    work...
}
```

2. Funneled

In Funneled style, all MPI calls are made by the OpenMP master thread, but this may include calls from inside OpenMP parallel regions. The advantages of Funneled style are the code is still relatively simple to write and maintain and there are now cheaper ways available to synchronise threads before and after message transfers than closing and opening parallel regions. It is possible for other threads to do useful computation while the master thread is executing MPI calls.

An outline of code in this style is given by:

3. Serialized

In Serialized style, any thread inside an OpenMP parallel region may make calls to the MPI library, but the threads must be synchronised in such a way that only one thread at a time may be in an MPI call. This style requires MPI_THREAD_SERIALIZED support. Tags or communicators are used to distinguish between messages from (or to) different threads in the same MPI process.

Outline code in serialized style is given by:

4. Multiple

In Multiple style, any thread inside (or outside) a parallel region may call MPI, and there are no restrictions on how many threads may be executing MPI calls at the same time. This requires MPI_THREAD_MULTIPLE support.Synchronization is taken care of by the MPI library. Compared to Master-Only or Funneled style, the internal synchronisation overheads are high which degrades the communication performance. Outline code in multiple style is given by:

```
#pragma omp parallel
{
    ... work
    ierror=MPI_Send(...);
    ... work
}
ierror=MPI Send(...);
```

5. Asynchronous Tasks

In Asynchronous Tasks style, MPI calls occur inside OpenMP dependent tasks. Since multiple threads may make concurrent MPI calls, this is a special case of Multiple style, and thus requires MPI_THREAD_MULTIPLE support. The idea of using OpenMP dependent tasks is to minimise the synchronisation between threads and allow the OpenMP runtime as much flexibility as possible in scheduling computation and communication.

Outline code for this style is given by:

```
#pragma omp parallel
{
#pragma omp single
{
#pragma omp task depend (out:sbuf)
        { ... write sbuf }
... more tasks
#pragma omp task depend (in:sbuf) depend
(out:rbuf)
        { MPI_SendRecv(sbuf,...,rbuf,...); }
... more tasks
#pragma omp task depend (in:rbuf)
        { ... use rbuf }
}// end single
}// end parallel
```

4. Code

This project demonstrates the implementation of merge sort algorithm using several approaches - serial, parallelised using OpenMP, MPI, hybrid models and to observe the performance in each case.

Serial MergeSort

```
#include <stdlib.h>
#include <stdio.h>
#include <string.h>
#include <unistd.h>
#if POSIX TIMERS
#include <time.h>
#ifdef CLOCK MONOTONIC RAW
/* System clock id passed to clock gettime. CLOCK MONOTONIC RAW
   is preferred. It has been available in the Linux kernel
   since version 2.6.28 */
#define SYS RT CLOCK ID CLOCK MONOTONIC RAW
#else
#define SYS RT CLOCK ID CLOCK MONOTONIC
#endif
double get time(void)
    struct timespec ts;
    double t;
    if (clock gettime(SYS RT CLOCK ID, &ts) != 0)
        perror("clock gettime");
        abort();
    t = (double)ts.tv sec + (double)ts.tv nsec * 1.0e-9;
    return t;
}
#else /* ! POSIX TIMERS */
#include <sys/time.h>
double get time(void)
    struct timeval tv;
    double t;
    if (gettimeofday(&tv, NULL) != 0)
        perror("gettimeofday");
        abort();
    t = (double)tv.tv sec + (double)tv.tv usec * 1.0e-6;
    return t;
}
```

```
#endif
```

```
// Arrays size <= SMALL switches to insertion sort
  #define SMALL
                   32
  void merge (int a[], int size, int temp[]);
  void insertion sort (int a[], int size);
  void mergesort serial (int a[], int size, int temp[]);
  extern double get time (void);
  int main (int argc, char *argv[]);
  int main (int argc, char *argv[])
    puts ("-Serial Recursive Mergesort-\t");
    // Check arguments
    if (argc != 2)
                            /* argc must be 2 for proper execution!
        printf ("Usage: %s array-size\n", argv[0]);
        return 1;
      }
    // Get arguments
    int size = atoi (argv[1]); // Array size
    printf ("Array size = %d\n", size);
    // Array allocation
    int *a = (int*)malloc (sizeof (int) * size);
    int *temp = (int*)malloc (sizeof (int) * size);
    if (a == NULL || temp == NULL)
      {
        printf ("Error: Could not allocate array of size %d\n",
size);
        return 1;
    // Random array initialization
    int i;
    srand (314159);
    for (i = 0; i < size; i++)
        a[i] = rand () % size;
      }
    // Sort
    double start = get time ();
    mergesort serial (a, size, temp);
    double end = get time ();
    printf ("Start = %.2f\nEnd = %.2f\nElapsed = %.2f\n",
         start, end, end - start);
    // Result check
    for (i = 1; i < size; i++)
        if (!(a[i - 1] \le a[i]))
```

```
{
         printf ("Implementation error: a[%d]=%d > a[%d]=%d n", i
-1,a[i-1], i, a[i]);
         return 1;
       }
    puts ("-Success-");
    return 0;
  }
  void
  mergesort serial (int a[], int size, int temp[])
    // Switch to insertion sort for small arrays
    if (size <= SMALL)
        insertion sort (a, size);
        return;
      }
    mergesort serial (a, size / 2, temp);
    mergesort serial (a + size / 2, size - size / 2, temp);
    // Merge the two sorted subarrays into a temp array
    merge (a, size, temp);
  }
  void
  merge (int a[], int size, int temp[])
    int i1 = 0;
    int i2 = size / 2;
    int tempi = 0;
    while (i1 < size / 2 && i2 < size)
        if (a[i1] < a[i2])
         temp[tempi] = a[i1];
         i1++;
       }
        else
         temp[tempi] = a[i2];
         i2++;
        tempi++;
    while (i1 < size / 2)
        temp[tempi] = a[i1];
        i1++;
        tempi++;
      }
    while (i2 < size)
```

```
temp[tempi] = a[i2];
     i2++;
     tempi++;
  // Copy sorted temp array into main array, a
  memcpy (a, temp, size * sizeof (int));
}
void
insertion sort (int a[], int size)
  int i;
  for (i = 0; i < size; i++)
     int j, v = a[i];
     for (j = i - 1; j >= 0; j--)
      if (a[j] \le v)
        break;
      a[j + 1] = a[j];
     a[j + 1] = v;
   }
}
```

MergeSort parallelized using OpenMP

```
#include <stdlib.h>
#include <stdio.h>
#include <string.h>
#include <omp.h>
#if POSIX TIMERS
#include <time.h>
#ifdef CLOCK MONOTONIC RAW
/* System clock id passed to clock gettime. CLOCK MONOTONIC RAW
   is preferred. It has been available in the Linux kernel
   since version 2.6.28 */
#define SYS RT CLOCK ID CLOCK MONOTONIC RAW
#else
#define SYS RT CLOCK ID CLOCK MONOTONIC
#endif
double
get time(void)
    struct timespec ts;
   double t;
    if (clock gettime(SYS RT CLOCK ID, &ts) != 0)
        perror("clock gettime");
        abort();
    }
    t = (double)ts.tv sec + (double)ts.tv nsec * 1.0e-9;
    return t;
}
#else /* ! POSIX TIMERS */
#include <sys/time.h>
double
get time(void)
    struct timeval tv;
    double t;
    if (gettimeofday(&tv, NULL) != 0)
        perror("gettimeofday");
        abort();
    t = (double)tv.tv sec + (double)tv.tv usec * 1.0e-6;
    return t;
}
#endif
// Arrays size <= SMALL switches to insertion sort
#define SMALL
                 32
```

```
extern double get time (void);
  void merge (int a[], int size, int temp[]);
  void insertion sort (int a[], int size);
  void mergesort serial (int a[], int size, int temp[]);
  void mergesort parallel omp (int a[], int size, int temp[], int
threads);
  void run omp (int a[], int size, int temp[], int threads);
  int main (int argc, char *argv[]);
  int
  main (int argc, char *argv[])
    puts ("-OpenMP Recursive Mergesort-\t");
    // Check arguments
                          /* argc must be 3 for proper execution!
    if (argc != 3)
       printf ("Usage: %s array-size number-of-threads\n",
argv[0]);
       return 1;
     }
    // Get arguments
    int size = atoi (argv[1]); // Array size
    threads
    // Check nested parallelism availability
    omp set nested (1);
    if (omp get nested () != 1)
       puts ("Warning: Nested parallelism desired but
unavailable");
    // Check processors and threads
    int processors = omp get num procs ();  // Available
processors
    printf ("Array size = %d\nProcesses = %d\nProcessors = %d\n",
         size, threads, processors);
    if (threads > processors)
        printf
       ("Warning: %d threads requested, will run omp on %d
processors available\n",
       threads, processors);
       omp set num threads (threads);
    int max threads = omp get max threads (); // Max available
    if (threads > max threads) // Requested threads are more than
max available
```

```
printf ("Error: Cannot use %d threads, only %d threads
available\n",
              threads, max threads);
        return 1;
      }
    // Array allocation
    int *a = (int*)malloc (sizeof (int) * size);
    int *temp =(int *) malloc (sizeof (int) * size);
    if (a == NULL | | temp == NULL)
        printf ("Error: Could not allocate array of size %d\n",
size);
       return 1;
    // Random array initialization
    int i;
    srand (314159);
    for (i = 0; i < size; i++)
        a[i] = rand () % size;
      }
    // Sort
    double start = get time ();
    run omp (a, size, temp, threads);
    double end = get time ();
    printf ("Start = %.2f\nEnd = %.2f\nElapsed = %.2f\n",
         start, end, end - start);
    // Result check
    for (i = 1; i < size; i++)
        if (!(a[i - 1] \le a[i]))
         printf ("Implementation error: a[%d]=%d > a[%d]=%d \setminus n", i
- 1,
              a[i - 1], i, a[i]);
         return 1;
       }
    puts ("-Success-");
    return 0;
  }
  // Driver
  void
  run omp (int a[], int size, int temp[], int threads)
    // Enable nested parallelism, if available
    omp set nested (1);
    // Parallel mergesort
    mergesort parallel omp (a, size, temp, threads);
```

```
// OpenMP merge sort with given number of threads
  void
  mergesort parallel omp (int a[], int size, int temp[], int
threads)
    if (threads == 1)
           printf("Thread %d begins serial merge sort\n",
omp_get thread num());
       mergesort serial (a, size, temp);
    else if (threads > 1)
  #pragma omp parallel sections
  //
                          printf("Thread %d begins recursive
section\n", omp get thread num());
  #pragma omp section
                      //printf("Thread %d begins recursive
call\n", omp get thread num());
         mergesort parallel omp (a, size / 2, temp, threads / 2);
  #pragma omp section
                      //printf("Thread %d begins recursive
call\n", omp get thread num());
         mergesort parallel omp (a + size / 2, size - size / 2,
                         temp + size / 2, threads - threads / 2);
        }
        // Thread allocation is implementation dependent
        // Some threads can execute multiple sections while others
are idle
        // Merge the two sorted sub-arrays through temp
        merge (a, size, temp);
    else
        printf ("Error: %d threads\n", threads);
        return;
  }
  void
  mergesort serial (int a[], int size, int temp[])
    // Switch to insertion sort for small arrays
    if (size <= SMALL)
        insertion sort (a, size);
        return;
    mergesort serial (a, size / 2, temp);
```

```
mergesort serial (a + size / 2, size - size / 2, temp);
  // Merge the two sorted subarrays into a temp array
 merge (a, size, temp);
}
void
merge (int a[], int size, int temp[])
  int i1 = 0;
  int i2 = size / 2;
  int tempi = 0;
  while (i1 < size / 2 && i2 < size)
      if (a[i1] < a[i2])
       temp[tempi] = a[i1];
       i1++;
     }
      else
       temp[tempi] = a[i2];
       i2++;
     tempi++;
  while (i1 < size / 2)
    {
      temp[tempi] = a[i1];
      i1++;
      tempi++;
    }
  while (i2 < size)
     temp[tempi] = a[i2];
      i2++;
     tempi++;
  // Copy sorted temp array into main array, a
  memcpy (a, temp, size * sizeof (int));
}
insertion sort (int a[], int size)
{
  int i;
  for (i = 0; i < size; i++)
    {
      int j, v = a[i];
      for (j = i - 1; j >= 0; j--)
       if (a[j] \le v)
         break;
```

```
a[j + 1] = a[j];
}
a[j + 1] = v;
}
```

MergeSort parallelized using MPI

```
#include <stdlib.h>
#include <stdio.h>
#include <string.h>
#include <math.h>
#include <mpi.h>
#if POSIX TIMERS
#include <time.h>
#ifdef CLOCK MONOTONIC RAW
#define SYS RT CLOCK ID CLOCK MONOTONIC RAW
#else
#define SYS RT CLOCK ID CLOCK MONOTONIC
#endif
double get time (void)
    struct timespec ts;
    double t;
    if (clock gettime(SYS RT CLOCK ID, &ts) != 0)
        perror("clock gettime");
        abort();
    t = (double)ts.tv sec + (double)ts.tv nsec * 1.0e-9;
    return t;
}
#else /* ! POSIX TIMERS */
#include <sys/time.h>
double get time(void)
{
    struct timeval tv;
    double t;
    if (gettimeofday(&tv, NULL) != 0)
    {
        perror("gettimeofday");
        abort();
    t = (double)tv.tv sec + (double)tv.tv usec * 1.0e-6;
    return t;
#endif
```

```
extern double get time (void);
void merge (int a[], int size, int temp[]);
void insertion sort (int a[], int size);
void mergesort serial (int a[], int size, int temp[]);
void mergesort parallel mpi (int a[], int size, int temp[],
                    int level, int my rank, int max rank,
                    int tag, MPI Comm comm);
int my topmost level mpi (int my rank);
void run root mpi (int a[], int size, int temp[], int max rank,
int tag,MPI Comm comm);
void run helper mpi (int my rank, int max rank, int tag,
MPI Commcomm);
int main (int argc, char *argv[]);
int main (int argc, char *argv[])
  // All processes
 MPI Init (&argc, &argv);
  // Check processes and their ranks
  // number of processes == communicator size
  int comm size;
  MPI Comm size (MPI COMM WORLD, &comm size);
  int my rank;
  MPI Comm rank (MPI COMM WORLD, &my rank);
  int max rank = comm size - 1;
  int tag = 123;
  // Set test data
  if (my rank == 0)
                         // Only root process sets test data
    {
      puts ("-MPI Recursive Mergesort-\t");
      // Check arguments
      if (argc != 2) {
       printf ("Usage: %s array-size\n", argv[0]);
      MPI Abort (MPI COMM WORLD, 1);
     // Get argument
      int size = atoi (argv[1]); // Array size
     printf ("Array size = %d\nProcesses = %d\n", size,
     comm size);
      // Array allocation
```

```
int *a = malloc (sizeof (int) * size);
      int *temp = malloc (sizeof (int) * size);
      if (a == NULL || temp == NULL)
size); printf ("Error: Could not allocate array of size %d\n",
       MPI Abort (MPI COMM WORLD, 1);
      // Random array initialization
      srand (314159);
      int i;
      for (i = 0; i < size; i++)
       a[i] = rand () % size;
      // Sort with root process
      double start = get time ();
      run_root_mpi (a, size, temp, max rank, tag,
MPI COMM WORLD);
      double end = get time ();
      printf ("Start = %.2f\nEnd = %.2f\nElapsed = %.2f\n",
           start, end, end - start);
      // Result check
      for (i = 1; i < size; i++)
       if (!(a[i - 1] \le a[i]))
           printf ("Implementation error: a[%d]=%d >
a[%d]=%d\n", i - 1,
                a[i - 1], i, a[i]);
           MPI Abort (MPI COMM WORLD, 1);
     }
    }
                          // Root process end
  else
                          // Helper processes
      run helper mpi (my rank, max rank, tag, MPI COMM WORLD);
    }
  fflush (stdout);
  MPI Finalize ();
  return 0;
}
```

```
// Root process code
void run root mpi (int a[], int size, int temp[], int max rank,
int tag, MPI Comm comm)
  int my rank;
 MPI Comm rank (comm, &my rank);
  if (my rank != 0)
    {
      printf("Error: run root mpi called from process %d; must
be called from process 0 only\n", my rank);
     MPI Abort (MPI COMM WORLD, 1);
 mergesort parallel mpi (a, size, temp, 0, my rank, max rank,
tag, comm);
  /* level=0; my rank=root rank=0; */
 return;
}
// Helper process code
void run helper mpi (int my rank, int max rank, int tag,
MPI Comm comm)
  int level = my topmost level mpi (my rank);
  // probe for a message and determine its size and sender
  MPI Status status;
  int size;
  MPI Probe (MPI ANY SOURCE, tag, comm, &status);
  MPI Get count (&status, MPI INT, &size);
  int parent rank = status.MPI SOURCE;
  // allocate int a[size], temp[size]
  int *a = malloc (sizeof (int) * size);
  int *temp = malloc (sizeof (int) * size);
  MPI Recv (a, size, MPI INT, parent rank, tag, comm, &status);
  mergesort parallel mpi (a, size, temp, level, my rank,
max rank, tag, comm);
  // Send sorted array to parent process
 MPI Send (a, size, MPI INT, parent rank, tag, comm);
  return;
}
```

```
int my topmost level mpi (int my_rank)
  int level = 0;
  while (pow (2, level) <= my rank)
    level++;
 return level;
}
// MPI merge sort
void mergesort parallel mpi (int a[], int size, int temp[],
               int level, int my rank, int max rank,
               int tag, MPI Comm comm)
{
  int helper rank = my rank + pow (2, level);
  if (helper rank > max rank)
                         // no more processes available
    {
     mergesort serial (a, size, temp);
    }
  else
    {
//printf("Process %d has helper %d\n", my rank, helper rank);
      MPI Request request;
      MPI Status status;
      // Send second half, asynchronous
      MPI Isend (a + size / 2, size - size / 2, MPI INT,
helper rank, tag,
           comm, &request);
      // Sort first half
      mergesort parallel mpi (a, size / 2, temp, level + 1,
my rank, max rank, tag, comm);
      MPI Request free (&request);
      MPI Recv (a + size / 2, size - size / 2, MPI INT,
helper rank, tag, comm, &status);
      // Merge the two sorted sub-arrays through temp
      merge (a, size, temp);
    }
 return;
}
void mergesort serial (int a[], int size, int temp[])
  // Switch to insertion sort for small arrays
  if (size <= SMALL)
```

```
insertion sort (a, size);
      return;
    }
  mergesort serial (a, size / 2, temp);
  mergesort serial (a + size / 2, size - size / 2, temp);
  // Merge the two sorted subarrays into a temp array
 merge (a, size, temp);
}
void merge (int a[], int size, int temp[])
{
  int i1 = 0;
  int i2 = size / 2;
  int tempi = 0;
  while (i1 < size / 2 && i2 < size)
      if (a[i1] < a[i2])
      temp[tempi] = a[i1];
      i1++;
     else
      temp[tempi] = a[i2];
       i2++;
     }
     tempi++;
  while (i1 < size / 2)
      temp[tempi] = a[i1];
      i1++;
      tempi++;
    }
  while (i2 < size)
      temp[tempi] = a[i2];
      i2++;
      tempi++;
  // Copy sorted temp array into main array, a
  memcpy (a, temp, size * sizeof (int));
```

MergeSort Using Hybrid (MPI + OpenMP)

```
#include <stdlib.h>
#include <stdio.h>
#include <string.h>
#include <math.h>
#include <mpi.h>
#include <omp.h>
#if POSIX TIMERS
#include <time.h>
#ifdef CLOCK MONOTONIC RAW
/* System clock id passed to clock_gettime. CLOCK_MONOTONIC_RAW
   is preferred. It has been available in the Linux kernel
   since version 2.6.28 */
#define SYS RT CLOCK ID CLOCK MONOTONIC RAW
#define SYS RT CLOCK ID CLOCK MONOTONIC
#endif
double
get time(void)
    struct timespec ts;
    double t;
    if (clock gettime(SYS RT CLOCK ID, &ts) != 0)
        perror("clock gettime");
        abort();
    t = (double)ts.tv sec + (double)ts.tv nsec * 1.0e-9;
    return t;
}
#else /* ! POSIX TIMERS */
#include <sys/time.h>
double
get time(void)
    struct timeval tv;
    double t;
    if (gettimeofday(&tv, NULL) != 0)
        perror("gettimeofday");
        abort();
    t = (double)tv.tv sec + (double)tv.tv usec * 1.0e-6;
    return t;
}
#endif
```

```
// Arrays size <= SMALL switches to insertion sort
#define SMALL
                 32
extern double get time (void);
void merge (int a[], int size, int temp[]);
void insertion sort (int a[], int size);
void mergesort serial (int a[], int size, int temp[]);
void mergesort parallel mpi (int a[], int size, int temp[],
                    int level, int my_rank, int max_rank,
                    int tag, MPI Comm comm, int threads);
int topmost level mpi (int my rank);
void run root mpi (int a[], int size, int temp[], int max rank, int
tag,
             MPI Comm comm, int threads);
void run node mpi (int my rank, int max rank, int tag, MPI Comm comm,
             int threads);
void mergesort parallel omp (int a[], int size, int temp[], int
threads);
int main (int argc, char *argv[]);
int main (int argc, char *argv[])
  // All processes
 MPI Init(&argc, &argv);
  // Enable nested parallelism, if available
 omp set nested (1);
  // Check processes and their ranks
  // number of processes == communicator size
 int comm size;
 MPI Comm size (MPI_COMM_WORLD, &comm_size);
 int my rank;
 MPI Comm rank (MPI COMM WORLD, &my rank);
 int max rank = comm size - 1;
  int tag = 123;
  // Check arguments
  if (argc != 3)
                        /* argc must be 3 for proper execution! */
    {
     if (my rank == 0)
      printf ("Usage: %s array-size
OMP-threads-per-MPI-process>0\n",
            argv[0]);
     }
     MPI Abort (MPI COMM WORLD, 1);
  // Get arguments
  int size = atoi (argv[1]); // Array size
  int threads = atoi (argv[2]); // Requested number of threads per
node
  if (threads < 1)
   {
      if (my rank == 0)
```

```
{
       printf
         ("Error: requested %d threads per MPI process, must be at
least 1\n",
         threads);
     MPI Abort (MPI COMM WORLD, 1);
    }
  // Set test data
  if (my rank == 0)
                         // Only root process sets test data
      puts ("-Multilevel parallel Recursive Mergesort with MPI and
OpenMP-\t");
      printf ("Array size = %d\nProcesses = %d\nThreads per process =
%d\n", size, comm size, threads);
      // Check nested parallelism availability
      if (omp get nested () != 1)
             puts ("Warning: Nested parallelism desired but
unavailable");
         }
      // Array allocation
      int *a = (int *)malloc (sizeof (int) * size);
      int *temp = (int *)malloc (sizeof (int) * size);
      if (a == NULL || temp == NULL)
       printf ("Error: Could not allocate array of size %d\n", size);
      MPI Abort (MPI COMM WORLD, 1);
      // Random array initialization
      srand (314158);
      int i;
      for (i = 0; i < size; i++)
       a[i] = rand () % size;
      // Sort with root process
      double start = get time ();
      run root mpi (a, size, temp, max rank, tag, MPI COMM WORLD,
threads);
      double end = get time ();
      printf ("Start = %.2f\nEnd = %.2f\nElapsed = %.2f\n", start,
end, end - start);
                    // Root process end
   }
  else
                         // Node processes
      run node mpi (my rank, max rank, tag, MPI COMM WORLD, threads);
  //fflush (stdout);
  MPI Finalize ();
  return 0;
```

```
}
// Root process code
void run root mpi (int a[], int size, int temp[], int max_rank, int
tag, MPI Comm comm, int threads)
 int my rank;
 MPI Comm rank (comm, &my rank);
 if (my rank != 0)
      printf("Error: run root mpi called from process %d; must be
called from process 0 only\n", my rank);
     MPI Abort (MPI COMM WORLD, 1);
 mergesort parallel mpi (a, size, temp, 0, my rank, max rank, tag,
                // level=0; my rank=root rank=0
comm, threads);
  return;
// Node process code
void run node mpi (int my rank, int max rank, int tag, MPI Comm comm,
int threads)
  // Probe for a message and determine its size and sender
 MPI Status status;
 int size;
 MPI Probe (MPI ANY SOURCE, tag, comm, &status);
 MPI Get count (&status, MPI INT, &size);
 int parent rank = status.MPI SOURCE;
 // Allocate int a[size], temp[size]
 int *a = (int *) malloc (sizeof (int) * size);
 MPI Recv (a, size, MPI INT, parent rank, tag, comm, &status);
  // Send sorted array to parent process
 MPI Send (a, size, MPI INT, parent rank, tag, comm);
 return;
}
// Given a process rank, calculate the top level of the process tree
in which the process participates
// Root assumed to always have rank 0 and to participate at level 0
of the process tree
int topmost level mpi (int my rank)
 int level = 0;
 while (pow (2, level) <= my rank)
   level++;
 return level;
}
// MPI merge sort
void mergesort parallel mpi (int a[], int size, int temp[], int level,
int my rank, int max rank, int tag, MPI Comm comm, int threads)
```

```
{
  int helper rank = my rank + pow (2, level);
  if (helper rank > max rank)
                         // no more MPI processes available, then use
OpenMP
      mergesort parallel omp (a, size, temp, threads);
      // Was: mergesort serial(a, size, temp);
  else
     MPI Request request;
      MPI Status status;
      // Send second half, asynchronous
      MPI Isend (a + size / 2, size - size / 2, MPI INT, helper rank,
tag, comm, &request);
      // Sort first half with OpenMP
      // mergesort parallel omp(a, size/2, temp, threads);
      mergesort parallel mpi (a, size / 2, temp, level + 1, my rank,
max rank, tag, comm, threads);
      // Free the async request (matching receive will complete the
transfer).
      MPI Request free (&request);
      // Receive second half sorted
      MPI Recv (a + size / 2, size - size / 2, MPI INT, helper rank,
tag, comm, &status);
      // Merge the two sorted sub-arrays through temp
      merge (a, size, temp);
  return;
// OpenMP merge sort with given number of threads
void mergesort parallel omp (int a[], int size, int temp[], int
threads)
  if (threads == 1)
      //printf("Thread %d begins serial mergesort\n",
omp get thread num());
     mergesort serial (a, size, temp);
  else if (threads > 1)
#pragma omp parallel sections
#pragma omp section
     mergesort parallel omp (a, size / 2, temp, threads / 2);
#pragma omp section
     mergesort parallel omp (a + size / 2, size - size / 2,
                             temp + size / 2, threads - threads / 2);
      // Thread allocation is implementation dependent
```

```
// Some threads can execute multiple sections while others are
idle
      // Merge the two sorted sub-arrays through temp
     merge (a, size, temp);
    }
 else
    {
     printf ("Error: %d threads\n", threads);
      return;
    }
}
void mergesort serial (int a[], int size, int temp[])
 // Switch to insertion sort for small arrays
 if (size <= SMALL)
      insertion sort (a, size);
      return;
 mergesort serial (a, size / 2, temp);
 mergesort serial (a + size / 2, size - size / 2, temp);
  // Merge the two sorted subarrays into a temp array
 merge (a, size, temp);
}
void merge (int a[], int size, int temp[])
 int i1 = 0;
 int i2 = size / 2;
 int tempi = 0;
 while (i1 < size / 2 && i2 < size)
    {
     if (a[i1] < a[i2])
      temp[tempi] = a[i1];
      i1++;
     }
      else
       temp[tempi] = a[i2];
      i2++;
      tempi++;
 while (i1 < size / 2)
     temp[tempi] = a[i1];
      i1++;
      tempi++;
    }
 while (i2 < size)
```

```
temp[tempi] = a[i2];
      i2++;
     tempi++;
   }
 // Copy sorted temp array into main array, a
 memcpy (a, temp, size * sizeof (int));
}
void
insertion sort (int a[], int size)
 int i;
  for (i = 0; i < size; i++)
      int j, v = a[i];
      for (j = i - 1; j >= 0; j--)
      if (a[j] \le v)
        break;
      a[j + 1] = a[j];
     a[j + 1] = v;
    }
}
```

5. Results

The execution of the above program gives the following output:

Mergesort - Serial execution:

```
    pratz@LAPTOP-R3NCRLFU: /mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort

                                                                                                                      OP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ g++ -lrt serial_mergesort.c
oratz@LAPTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 1000000
-Serial Recursive Mergesort-
Array size = 1000000
Start = 2633.10
End = 2633.24
Elapsed = 0.15
-Success-
pratz@LAPTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 10000000
-Serial Recursive Mergesort-
Array size = 10000000
Start = 2638.01
End = 2639.65
Elapsed = 1.64
-Success-
pratz@LAPTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 100000000
-Serial Recursive Mergesort-
Array size = 100000000
Start = 2653.31
End = 2702.49
Elapsed = 49.17
-Success-
ratz@LAPTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$
```

MergeSort - Openmp execution:

```
n
      ZGLAPTOP-R3NCRLFU:/mmt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ g++ -1rt omp_mergesort.c -fopenmp
zGLAPTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 100000 2
-OpenMP Recursive Mergesort-
Array size = 100000
 Processes = 2
Processors = 8
Start = 1609340349.23
End = 1609340349.24
Elapsed = 0.01
 Success-
  ratz@LAPTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 1000000 2
 -OpenMP Recursive Mergesort-
Array size = 1000000
 rocesses = 2
 rocessors = 8
Start = 1609340353.59
End = 1609340353.67
Elapsed = 0.08
 Success-
           APTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 10000000 2
-OpenMP Recursive Mergesort-
Array size = 10000000
 rocesses = 2
Processes = 2
Processors = 8
Start = 1609340357.12
End = 1609340358.02
Elapsed = 0.90
             PTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 1000000000 2
 -OpenMP Recursive Mergesort-
Array size = 100000000
 Processes = 2
Processors = 8
Start = 1609340373.65
End = 1609340402.53
Elapsed = 28.89
 Success-
```

Mergesort - MPI execution:

```
O pratz@LAPTOP-R3NCRLFU: /mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort
                                                                                                                                                             O
         TOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ mpicc -lrt mpi_mergesort.c -lm
 ratz@LAPTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 100000
-MPI Recursive Mergesort-
Array size = 100000
Processes = 1
Start = 1609340566.56
End = 1609340566.58
Elapsed = 0.02
 ratz@LAPTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 1000000
-MPI Recursive Mergesort-
Array size = 1000000
Processes = 1
Start = 1609340573.86
End = 1609340574.01
Elapsed = 0.14
 ratz@LAPTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 10000000
-MPI Recursive Mergesort-
Array size = 10000000
Processes = 1
Start = 1609340585.16
End = 1609340586.71
Elapsed = 1.56
 ratz@LAPTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 1000000000
-MPI Recursive Mergesort-
Array size = 100000000
Processes = 1
Start = 1609340604.21
End = 1609340652.39
Elapsed = 48.18
 ratz@LAPTOP-R3NCRLFU:/mnt/c/Users/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$
```

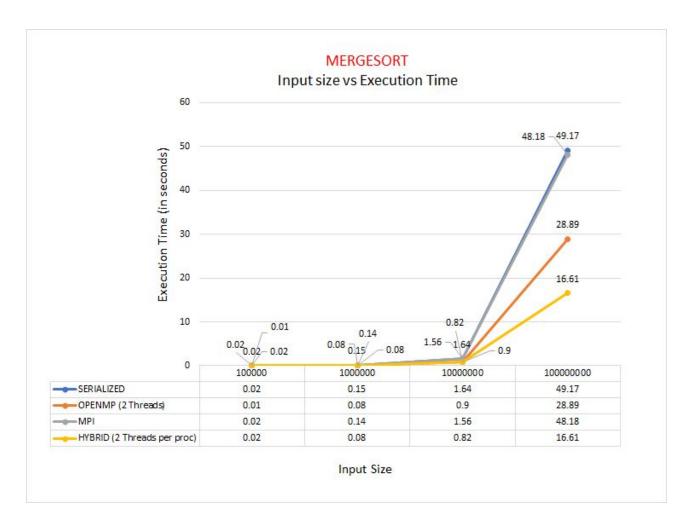
Mergesort - MPI + OpenMP (Hybrid) execution:

```
partsWAPPOPRINCERULymet/clusers/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ mpicc -1rt hybrid_mergesort.c -1m -fopenep partsWAPPOPRINCERULymet/clusers/Pratheeksha Prasad/Desktop/Pratz/PADP/mergesort$ ./a.out 100000 2

-Miltieval parallel Recursive Mergesort with MPI and OpenVP-
-Multieval parallel Recursive Mergesort with MPI and
```

The tabulation of execution times obtained by varying the input sizes with respect to different serial and parallel programming models is shown below:

INPUT SIZE	SERIALIZED	OPENMP (2 Threads)	MPI	HYBRID (2 Threads per proc)
100000	0.02	0.01	0.02	0.02
1000000	0.15	0.08	0.14	0.08
10000000	1.64	0.90	1.56	0.82
100000000	49.17	28.89	48.18	16.61



Observation - the hybrid model starts to perform better as the input size and the no of core counts increases.

6. Conclusion

Hybrid programming is an attempt to maximize the best from both OpenMP and MPI paradigms. However, it does not always imply better performance. This may be due to a number of reasons. OpenMP has less scalability due to implicit parallelism while MPI allows multi-dimensional blocking. All threads are idle except one while MPI communication. There is a thread creation overhead. The chances of cache miss problems increase due to data placement problems and larger dataset. Pure OpenMP performs slower than pure MPI within a node due to lack of optimized OpenMP libraries. Hybrid programs tend to work better when the communication to computation ratio is high.

Converting pure MPI codes into Hybrid codes is not a particularly difficult task. It is worth a try because if the nature of the problem is such that it can allow for faster hybrid codes, the speedups can be huge. Currently, there are very few benchmarked results for hybrid programs, and all of them are very problem specific.

7. References

- 1. Kushal Kedia, Hybrid Programming with OpenMP and MPI, MIT press, 2019
- 2. Rolf Rabenseifner, Georg Hager, Gabriele Jost, **Hybrid MPI and OpenMP Parallel Programming**, https://www.openmp.org//wp-content/uploads/HybridPP_Slides.pdf
- 3. https://www.cac.cornell.edu/education/Training/Intro/Hybrid-090529.pdf
- 4. https://docs.rc.fas.harvard.edu/kb/hybrid-mpiopenmp-codes-on-odyssey/