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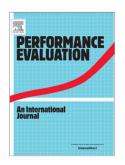
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Performance Svaluation

DeepComNet: Performance Evaluation of Notwork Topologies using Graph-Based Deep Learning

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Abstract

Modeling the performance of network protocols and communication networks generally relies on expert knowledge and understanding of the different elements of a network, their configuration, and a coverall architecture and topology. Machine learning is often proposed as a tool to help modeling such complex system. One drawback of this method is that high-level features are generally used – which require full understanding of the network correctly engineered, and measured – and the approaches are generally limited to a given network topolog.

In this article, we present *DeepComNet*, an approar and does so the challenges of working with machine learning by using lower-level features, namely only a description of the network architecture. Our main contribution is a method for applying deep learning on network topologies via the use of Graph Gated Neural Networks, a specialized recurrent neural network for graphs. Our approach enables us to make performance predictions based only on a graph-based representation of network topologies. To evaluate the potential of DeepComNet, we apply our approach to the tasks of predicting the throughput of TCP flows and the end-to-end latencies of UDP flows. In both cases, the same base model is used. Numerical results show that our approach is able to learn and predict performance properties of TC. and UDP flows with a median absolute relative error smaller than 1%, outperforming related methods from the literature by one order of magnitude.

Keywords: Network performance evaluation, Gra, 's seural Network, Deep Learning

1. Introduction

Understanding network per imance is an important task for architecture design and Quality-of-Service in an increasing number of applications. Training engineering aims at bringing an answer to this need in order to provide better services, avoid congestion and ptimize network topologies to support an increasing number of applications. Models for network and traffic are an important tool in order to predict how a given network architecture will behave. Different techniques have be a proposed, such as mathematical modeling, simulations or measurements in real networks. While these techniques can achieve accurate results, they often require precise measurements of key performance indicators such as round trip in me or loss probability in order to be applied and generate realistic performance predictions. However, limited access to instrumentation of real networks makes this measurement acquisition usually difficult.

An approach to 'ack' the challenges of performance modeling is a more data-driven way, where measurements are used in partial with machine learning to produce realistic performance predictions. For instance, Tian and Liu [1] applied the N R-based (Support Vector Regression) TCP bandwidth prediction application from [2] to improve

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Quality-of-Service of media streaming over HTTP. Tariq et al. [3] recently proposed WISE, a from nework for evaluating architecture changes in communication networks using Causal Bayesian Networks (CBNs) while these techniques and applications have been proven successful, high-level features about the studied network protocols are required, and the trained models are often limited to a given network topology.

Our main contribution in this work is *DeepComNet*, an approach combining formal and ting of network topologies and flows traversing them as graphs with deep learning methods tailored for the ining and inference on graph structures. This approach is illustrated in Figure 1 with its two main steps: we first model computer networks as graph structures, and then process those graphs using neural networks. We propose to use Conded Graph Neural Networks (GGNNs) [4] as a basis for our deep learning architecture, a recent extension of Graph Neural Networks (GNNs) [5, 6]. By directly training the underlying machine learning algorithm on the network structure, we avoid the task of engineering high-level protocol-specific input features such as round-trip time or drop probability, which usually require expert knowledge on the network protocol which is modeled. We comount to in this paper this modeling as graph is independent of a given network architecture or network protocol, producing a wide range of applicability compared to other methods.

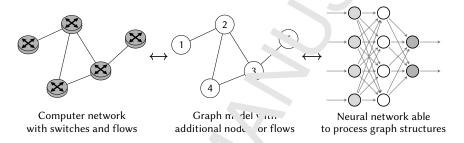


Figure 1: Illustration of the two diffe. at s. as of our approach DeepComNet

As concrete applications of our approach, we addred the two following tasks. First, we are interested in the performance evaluation of TCP flows, with the goal of predicting the average throughput of each flow in a given topology. Secondly, we look at the performance evaluation of UDP flows and the prediction of end-to-end latencies (average and quantile value). We use the same model or both tasks, highlighting the general applicability of our approach and potential for application to other use-case for performance evaluation of network topologies and protocols.

We show through a numerical evaluation that our approach is able to predict the performance of TCP and UDP flows by only using this low-level graph. Seed epresentation of the network topology and its flows. Overall, the predictions of bandwidths and end-o-end law icies have a median absolute relative error smaller than 1%. The results for the TCP dataset are also conferred against two approaches using high-level input features (round-trip time and loss probability), namely Support Vector Regression (SVR) as used in [2, 1] and a standard feed-forward neural network. Compared to both approaches, our method achieves better accuracy, with a median relative error one order of magnitude lower compared to SVR.

We also illustrate the scalability of our approach in term of execution time by numerically evaluating our implementation of GNN. Our measurements illustrate that our implementation scales quadratically with the number of edges, and linearly with the number of nodes. We show that our approach is able to process graphs with up to 1000 nodes and 150 000 ed es with a prediction time below 200 µs. Finally we illustrate a method for visualizing the learned model in order to apply it to more general questions such as root-cause analysis or bottleneck identification.

This work is structu. A as follows. In Section 2, we present similar research studies. We describe in Sections 3 and 4 our modeling approach and the neural network architecture used here, with an introduction to Graph Neural Networks and Galed Graph Neural Networks, followed by the application of those concepts to network topologies and flows. We numerically aduate our approach in Section 5 with the prediction of performance of TCP and UDP flows, compare agains the machine learning approaches, and evaluate our approach in term of scalability. Section 6 gives some insights on interpreting the learned weights of the neural network. Finally, Section 7 concludes our work.

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2. Related work

As shown in a recent survey by Fadlullah et al. [7], machine learning has been used for computer retworks for various applications such as traffic classification, flow prediction, and mobility prediction. It has also been applied in the area of performance evaluation of communication networks. Mirza et al. [2] used Suprort V ctor Regression (SVR) using input features such as transfer duration of files over TCP and active measurements in a refer to measure queuing latency, loss probability and available bandwidth. Tariq et al. [3] proposed WISE to study application performance using Causal Bayesian Networks (CBNs) in order to answer "what-if" questions. You set al. [8] also used CBNs to predict the throughput distribution of TCP flows, using similar features as in [2]. While these works proved to deliver accurate results, they are essentially based on high-level engineered features depend into on the studied protocol and those models are not easily transferable to other protocols. In case of TCP hows, these high level features usually include round-trip time and packet loss – following well known mathematical models such as [9] – which also often require active measurement. By having a simple process for abstracting the new results in the protocols. Our approach is also able to reason about performance evaluation at network level and not at incoming data. Lode level.

Various methods have been proposed for applying machine learning to graphs-based structures, either based on a spectral or spatial approach. Spectral approaches [10, 11] are usu. "Iv based on the Graph Laplacian, an analogous method to the Discrete Fourier Transform, which transforms graph signals to a spectral domain. The main limitation of these approaches is that the input graph samples are required to be be longereous. Concretely this means that only a fixed subset of network types may be analyzed and multiple machine learning models may be required in case multiple network types are required.

Spatial approaches do not require a homogeneous grap, structure, meaning that they can be applied to a broader range of problems. Gori et al. proposed in [5, 6] the Gorb Normal Networks (GNNs) architecture, which propagates hidden representations of nodes to its adjacent nodes unit and fixed point is reached. GNNs were applied on different tasks such as object localization, ranking of web paras doctment mining, or prediction of graph properties [12]. This neural network architecture was subsequently refined in dinerent works. Li et al. [4] proposed Gated Graph Neural Networks (GGNNs), an extension of GNNs with application of more modern practice of neural networks, namely by using Gated Recurrent Units (GRU) [13]. GNNs are evaluated against basic logical reasoning tasks and program verification in [4] and shown to be as-good-ar or better than previous state of the art methods. Related approaches were proposed by Kipf and Welling [14] with Grapi. Confolutional Networks (GCN) and later extended by Schlichtkrull et al. [15] with Relational Graph Convolutional Networks (R-GCNs). GCN also use hidden node state information propagated across edges of the graph variety and direction of an edge. Finally, Battaglia et al. [16] recently introduce at the graph networks (GN) framework with the goal of providing a unified formalization of many concolution of GNNs and extensions of GNNs.

Those methods have been used in a vality of applications related to the study of data which can be modeled as graphs. Grover and Leskovec [1/1] a plied it to link prediction and classification in social networks, protein interactions and natural language processing. Marcheggiani and Titov [18] studied semantic role labeling in natural language processing. Gilmer et al. [1] used GNNs for the prediction of chemical properties of molecules. Allamanis et al. [20] performed source code and ysis by modeling source code and interaction between program variables as graphs, in order to predict variable. Ying Selsam et al. [21] modeled the interaction between variables in boolean satisfiability problems (SAT) a graphs, ith the goal of predicting their satisfiability. In all those applications, the results of graph-based deep lear ing weighted in the previously existing machine learning approaches.

On the challenge of predicting the performance of TCP flows, analytical models have been proposed since the late 1990s. Mathir at al. [22], and subsequently Padhye et al. [9], modeled the throughput of a single flow using TCP Reno as a function of round-trip time, drop probability and some configuration parameters of TCP. This work was then extended by Sardwe 1 et al. [23] to take into account the slow-start phase of TCP. While these models address the mathematical modeling of a single flow, the interaction between multiple flows on a given topology is of greater interest for the problem addressed in this paper. Firoiu et al. [24] proposed to reuse the results from [9] to analyze complete topologes. Those analytical models give great insights in the performance of TCP, but they usually suffer from poor applicability to real-world use-cases due to newer versions of TCP, simplifications of the mathematical model, or lack of modeling of non-intuitive behavior of TCP such as ACK compression or TCP Incast. Some later

works have partially addressed those shortcomings, such as the work from Velho et al. [25] an . Geyer et al. [26].

This article is an extension of our previous work [27], which applied GGNNs to the performance evaluation of TCP flows. In this article, we propose more advanced GGNNs architectures, provide an extended numerical evaluation with the performance of both TCP and UDP flows, compare against two other machine learning approaches using high-level features, and provide a discussion regarding scalability.

3. Neural networks for graph analysis

The main intuition behind our approach is to represent network topologies at a physical with additional nodes for modeling flows and additional edges for the paths followed by the flows. These graph representations are then used as input for a neural network architecture able to process general graphs. The ransformation between a given network topology and its graph representation will be detailed later in Section 4.

In this section, we review the neural network architecture used for 'anning neural networks on graphs, namely Graph Neural Networks (GNNs) [5, 6] and one of its recent extension, 'atr'. Gr ph Neural Networks (GGNNs) [4]. We also introduce notation and concepts that will be used throughout this artic. Alternate approaches for applying neural networks to graphs were presented in Section 2.

GNNs and GGNNs are a general neural network architecture ble to process graph structures as input. They are an extension of recursive neural networks which work by assig. ing in the fide a states to each node in a graph based on the hidden states of adjacent nodes. For the purpose of this work, or description of GNNs and GGNNs is limited to undirected graphs. The concepts presented here can also be appned to directed graph, as presented in the original works on GNNs and GGNNs [5, 6, 4].

Let $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ be an undirected graph with nodes $v \in \mathcal{V}$ and indeed $v \in \mathcal{E}$. Edges can be represented as pairs of nodes, such that $e = (v, v') \in \mathcal{V} \times \mathcal{V}$. The *hidden representative* v for node v is denoted by the vector $\mathbf{h}_v \in \mathbb{R}^{\mathcal{H}}$. Nodes may also have features l_v for each node v, and edges als $\mathbf{v}_v = l_{(v, v')}$ for each edge e = (v, v'). Let $\mathsf{NBR}(v)$ denote the set of neighboring nodes of v.

3.1. Graph Neural Networks

In Graph Neural Networks (GNNs), each $b^{\nu + 4}$ an representation \mathbf{h}_{ν} of a node ν is based on the hidden state of its neighboring nodes NBR(ν). The following pr $^{\nu}$ pagatio. model is used for expressing this relationship:

$$\mathbf{h}_{v}^{(t)} = \mathcal{I}\left(l_{v}, l_{\text{NBR}(v)}, \mathbf{h}_{\text{NBR}(v)}^{(t-1)}\right) \tag{1}$$

An illustrative application of Equation (1) given in Figure 2.

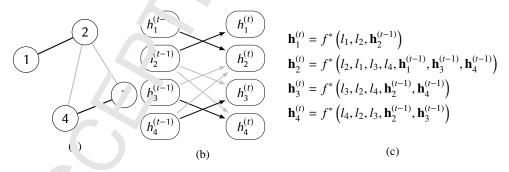


Figure 2: (a) Exampl graph. I ge colors denote edge types. (b) One step of the propagation of hidden node representation. (c) Application of Equation (1) to the graph.

As a concern function, [6] recommends to decompose $f^*(\cdot)$ as the sum of per-edge terms such that:

$$\mathbf{h}_{v}^{(t)} = \sum_{v' \in N_{BR}} f\left(l_{v}, l_{v'}, l_{(v,v')}, \mathbf{h}_{v'}^{(t-1)}\right)$$
(2)

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with $f(\cdot)$ a linear function of \mathbf{h}_{ν} or a feed-forward neural network. For example, $f(\cdot)$ can be formulated as a linear function:

$$f(l_{v}, l_{v'}, l_{(v,v')}, \mathbf{h}_{v'}^{(t)}) = \mathbf{W}^{(l_{v}, l_{v'}, l_{(v,v')})} \mathbf{h}_{v'}^{(t-1)} + \mathbf{b}^{(l_{v}, l_{v'}, l_{(v,v')})}$$
(3)

with **W** and **b** learnable weight and bias parameters. The hidden node representations are propagated throughout the graph until a fixed point is reached. As explained in [6], it implies that $f(\cdot)$ has the property that a fixed point for Equation (2) can be reached.

Once a fixed point \mathbf{h}_v has been reached, a second model is then used to compute the output vector \mathbf{o}_v for each node $v \in \mathcal{V}$ such that:

$$\mathbf{o}_{\mathbf{v}} = g\left(\mathbf{h}_{v}, l_{v}\right) \tag{4}$$

5

Practically, $g(\cdot)$ is implemented using a feed-forward neural network [6]. The neural etwork architecture is differentiable from end-to-end, so that all parameters can be learned using standard ι chaiques for neural networks based on gradient-based optimization.

Due to the required fixed-point iterations, training of the parameter of (\cdot) nd $g(\cdot)$ of the GNN is done via the Almeida-Pineda algorithm [28, 29] which works by running the propagation of ne hidden representation to convergence, and then computing gradients based upon the converged solution.

3.2. Gated Graph Neural Networks

Li et al. [4] recently introduced Gated Graph Neural Networks ("GNNs) as an extension of GNNs using more recent neural network techniques, based on Gated Recurrent (GRU) [13]. GRUs are special types of neural network blocks with an internal memory. Such blocks are generally used to process time-dependent inputs such as audio or written words, which can be mathematically simplified.

$$output^{(t)} = func_i ... (inp_i..(t), output^{(t-1)})$$
 (5)

In GGNNs, each node aggregates the hidden regional adjacent nodes as in Equation (2), and uses that to update its own hidden representation sing a GRU cell. More specifically, the propagation of the hidden representations among neighboring nodes for one time-step is formulated as:

$$\mathbf{a}_{v}^{(t)} = \mathbf{A}_{v} \left[\mathbf{h}_{1}^{(t-)} \cdots \mathbf{h}_{|V|}^{(t-1)} \right]^{T} + \mathbf{b}_{a}$$

$$(6)$$

$$\mathbf{z}_{v}^{(t)} = \sigma \left(\mathbf{W}_{z} \boldsymbol{\omega}_{v}^{(t)} + \mathbf{U}_{z} \mathbf{h}_{v}^{(t-1)} + \mathbf{b}_{z} \right) \tag{7}$$

$$\mathbf{r}_{v} = \sigma \left(\mathbf{V}_{r} a_{v}^{(t)} + \mathbf{U}_{r} \mathbf{h}_{v}^{(t-1)} + \mathbf{b}_{r} \right)$$
 (8)

$$\mathbf{\tilde{N}}(t) = \tanh\left(\mathbf{W}a_{\nu}^{(t)} + \mathbf{U}\left(\mathbf{r}_{\nu}^{(t)} \odot \mathbf{h}_{\nu}^{(t-1)}\right) + \mathbf{b}\right)$$
(9)

$$\mathbf{h}_{\nu}^{(t)} = \left(1 - \mathbf{z}_{\nu}^{(t)}\right) \odot \mathbf{h}_{\nu}^{(t-1)} + \mathbf{z}_{\nu}^{(t)} \odot \widetilde{\mathbf{h}_{\nu}^{(t)}}$$

$$\tag{10}$$

where $\sigma(x) = 1/(1+e^{-x})$ is the log. ic sigmoid function and \odot is the element-wise matrix multiplication. $\{\mathbf{W}_z, \mathbf{W}_r, \mathbf{W}\}$ and $\{\mathbf{U}_z, \mathbf{U}_r, \mathbf{U}\}$ are learnable weights matrices, and $\{\mathbf{b}_a, \mathbf{b}_r, \mathbf{b}_z, \mathbf{b}\}$ are learnable biases vectors. $\mathbf{A} \in \mathbb{R}^{|\mathcal{V}| \times |\mathcal{V}|}$ is the graph adjacency matrix, determining now nodes in the graph \mathcal{G} communicate with each other.

Equation (6) corresponds to the propagation of the hidden representation of neighboring nodes to node ν , as formulated previously for Graph Neural Networks in Equations (1) and (2). Equations (7) to (10) correspond to the mathematical formulation of a GRU cell, with Equation (7) representing the GRU reset gate vector, Equation (8) the GRU update gate vector, and Equation (10) the GRU output vector as described in Equation (5). The initial hidden representation $\mathbf{h}_{\nu}^{(0)}$ is based on the node's feature vector l_{ν} , padded with zeros according to the dimensions of the 'ridden epresentation.

The output vector \mathbf{v}_v for each node v is computed as in Equation (4) using a feed-forward neural network. The overall archite ture of the GGNN is illustrated and summarized in Figure 3.

While with NNs the node propagation loop is performed until a fixed-point is reached, a fixed number of iterations is used in GGNNs. This process enables the use of traditional gradient-based training methods used for feed-forward neural networks such as RMSProp [30]. Since hidden representations are propagated iteratively to node

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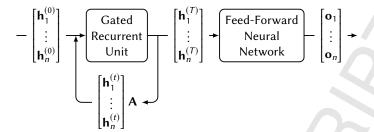


Figure 3: Representation of a Gated Graph Neural Network.

neighbors at each iteration, the number of iterations necessary for achieving and couracy depends mainly on the path length between relevant nodes in the analyzed graph. In the example in Figure 2, if the output vector of node 1 depends on the input features of node 4, at least two iterations of the vic agat on loop are required, since the hidden representation of node 4 is first propagated to node 2 in the first fration fefore reaching node 1 in the second iteration.

While the number of iterations is highly dependent on application, we propose here two simple heuristics for choosing the number of iterations. The first heuristic is to us, the animeter d of the studied graph, namely the greatest distance between any pair of nodes, which ensures that each node receives at least once the propagated hidden representation of all other nodes in the graph. The second heuristic is to use $2 \times d$, which ensures that the hidden representations between any pairs of nodes in the study qraph could be propagated in both directions. Numerical evaluations in Section 5.7 illustrate the influence of the number of iteration on the accuracy.

3.3. GGNN-LSTM: Extension of Gated Graph Neural 1 'e. "ork. with LSTM

In our approach we use an extension of Gated Graph Noura, Networks – called here GGNN-LSTM – based on the Long Short-Term Memory (LSTM) cell [31]. This . Turar ... twork architecture is based on the Gated Graph Neural Network architecture where the GRU memory cell is re, laced with a LSTM cell. The overall architecture of the GGNN-LSTM is similar to the GGNN illustrated in Figure 3.

Similarly to Equations (6) to (10), the propagation of the hidden representations among neighboring nodes for one time-step in a GGNN-LSTM is formulated as.

$$\mathbf{a}_{v}^{(t)} : \mathbf{A}_{(\cdot)} \left[\mathbf{h}_{1}^{(t-1)} \cdots \mathbf{h}_{|V|}^{(t-1)} \right]^{T} + \mathbf{b}_{a}$$

$$(11)$$

$$\mathbf{i}_{v}^{(\iota)} = \left(\mathbf{W}_{i} \mathbf{a}_{v}^{(t)} + \mathbf{U}_{i} \mathbf{h}_{v}^{(t-1)} + \mathbf{b}_{i} \right) \tag{12}$$

$$\mathbf{C}^{(t)} = \sigma \left(\mathbf{W}_f \mathbf{a}_v^{(t)} + \mathbf{U}_f \mathbf{h}_v^{(t-1)} + \mathbf{b}_f \right)$$
(13)

$$\mathbf{o}_{v}^{(t)} = \sigma \left(\mathbf{W}_{o} \mathbf{a}_{v}^{(t)} + \mathbf{U}_{o} \mathbf{h}_{v}^{(t-1)} + \mathbf{b}_{o} \right) \tag{14}$$

$$\mathbf{g}_{\nu}^{(t)} = \tanh\left(\mathbf{W}_{g}\mathbf{a}_{\nu}^{(t)} + \mathbf{U}_{g}\mathbf{h}_{\nu}^{(t-1)} + \mathbf{b}_{g}\right)$$

$$\mathbf{c}_{\nu}^{(t)} = \mathbf{c}_{\nu}^{(t-1)} \odot \mathbf{f}_{\nu}^{(t)} + \mathbf{g}_{\nu}^{(t)} \odot \mathbf{i}_{\nu}^{(t)}$$

$$(15)$$

$$\mathbf{c}_{v}^{(t)} = \mathbf{c}_{v}^{(t-1)} \odot \mathbf{f}_{v}^{(t)} + \mathbf{g}_{v}^{(t)} \odot \mathbf{i}_{v}^{(t)} \tag{16}$$

$$\mathbf{h}_{v}^{(t)} = \tanh\left(\mathbf{c}_{v}^{(t)}\right) \odot \mathbf{o}_{v}^{(t)} \tag{17}$$

with $\{\mathbf{W}_i, \ldots\}$ and $\{\mathbf{U}_i, \ldots\}$ learn able weight matrices, and $\{\mathbf{b}_i, \ldots\}$ learnable bias vectors.

Equation (11) is the propagation of the hidden representations among neighbors, as in Equation (6). Equations (12) to (14) correspond respectively to the input, forget and output gates of the LSTM cell. Equation (15) is a candidate hidden representation, with an initial value $\mathbf{c}_{v}^{(0)}$ set to zero. Equation (16) is the internal memory of the LSTM cell.

Our rationale to using this alternate neural network architecture is motivated by better accuracy than the GGNN based on GR p. arted in Section 3.2, as shown in the numerical evaluation in Section 5 for the TCP task.

3.4. Stacked Gate 1 Graph Neural Networks

Since the neural network architectures introduced earlier are based on a special variant of recurrent neural networks, advances made for standard RNNs may also be applied here. For this purpose, we make use of stacked RNNs

as proposed by Pascanu et al. [32], and illustrated in the following equation:

$$\mathbf{h}^{(t;l)} = r\left(A, \mathbf{h}^{(t-1;l)}, \mathbf{h}^{(t;l-1)}\right) \tag{18}$$

where $\mathbf{h}^{(t;l)}$ corresponds to the hidden representation at timestep t and layer l, and r a function describing the recurrent unit, i.e. Equations (6) to (10) for the GRU or Equations (12) to (14) for the LSTM unit

3.4.1. Edge attention

A recent advance in neural networks has been the concept of *attention*, which rovides the ability to a neural network to focus on a subset of its inputs. This mechanism has been used in a variety of roplications such as computer vision or natural language processing (eg. [33]). For the scope of GNNs, we introduce here so-called *edge attention*, namely we wish to give the ability to each node to focus only on a subset of its neighborhood. Formally, let $a_{(v,u)}^{(t)} \in [0,1]$ be the attention between node v and u. Equation (2) is then extended as:

$$\mathbf{h}_{v}^{(t)} = \sum_{u \in N_{BR}(v)} a_{(v,u)}^{(t)} \cdot f^{*} \left(\mathbf{h}_{\cdot}^{(t-1)} \right)$$
(19)

$$\mathbf{a}_{(v,u)}^{(t)} = f_A \left(\mathbf{h}_v^{(t-1)}, \mathbf{h}_u^{(t-1)} \right)$$
 (20)

We decompose $f_A(\cdot)$ as two feed-forward neural networks and use an element-wise matrix multiplication to compute a modified adjacency matrix.

To make the computation of $a_{(v,u)}^{(t)}$ for all edges more efficient, we use the modified adjacency matrix $\widetilde{A}^{(t)}$ defined as:

$$\widetilde{A}^{(t)} = A \odot softmax \left(f_{A_1} \left(\mathbf{V}_{\cdot}^{(t)} \right)^t \odot f_{A_2} \left(\mathbf{H}^{(t)} \right) \right)$$
(21)

with $f_{A_1}(\cdot)$ and $f_{A_2}(\cdot)$ feed-forward neural networks, and $f_{A_2}(\cdot)$ the normalized exponential function such that:

$$softmax(X)_{j} = \frac{e^{X_{j}}}{\sum_{i} e^{X_{i}}}$$
 (22)

4. Application to performance evaluation. I networks

We describe in this section the application of the deep learning architectures presented earlier to the performance evaluation of network topologies and nearly key roccols. In other words, our goal is to represent network topologies and the flows traversing them as grants which an be passed as inputs to a GGNN. Compared to other works on the application of machine learning to renamence evaluation, the main contribution is that this graph representation is a low-level input feature. This means that specific high-level features of the studied network protocol are not required and the trained machine learning algorithm is not restricted to a specific topology.

The main intuition behind u. ir jut feature modeling for the GGNN is to use the network of queues as input graph \mathcal{G} , with additional nodes representation of the flows in this network. An illustration of this network of queues is given in Figure 4b, which is the epresentation of the different queues in the example network depicted in Figure 4a. Note that we represent on Figure 1 on 1 the forward path of the flows. Figure 4b may also be extended to include the queues taken by the ac' nowledgment packets used by the flows if necessary, such as TCP ACK packets for example as explained later in S ction 5...

We formally define 'ere t'e transformation between an input computer network and the undirected graph $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ which will be analyzed by the GGNN. Figure 4c is an application of this transformation applied to the network presented in Figure 4a.

We focus in the article on the study of simple Ethernet networks, where computers are connected via simple store-and-for and witches and exchanging data via flows. We assume that each flow in the network is unidirectional, with a single so in e and a single destination. Each flow f is represented as a node v_f in the graph \mathcal{G} . As illustrated in Section 5.2, bidirectional flows such as TCP flows may still be analyzed by using two unidirectional flows, modeled in \mathcal{G} by two nodes connected by an edge.

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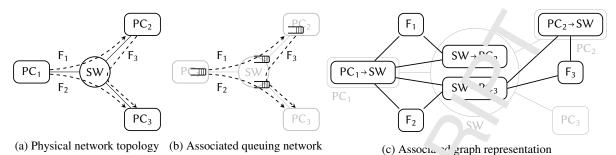


Figure 4: Graph encoding of an example network topology vath three lows

We assume here that the routing in the studied network is static, or mely that the path taken by a flow is fixed. Each queue traversed by a flow in the network is represented as a node v_i in the graph \mathcal{G} . For simplifications purpose we only consider the queues present in the network interfaces and not the queue. In the second systems. We model network interfaces using a simple drop-tail queue. In the second second state of Ethernet switches, multiple nodes are used since multiple interfaces are present. Queues are connected by edges according to the physical topology of the studied network. Let Q_f be the set of queues traversed by v_f and order to encode the path taken by a flow, edges connect the node representing the flow v_f with the nodes representing the traversed queues $\{v_q | q \in Q_f\}$.

Each node v in the graph \mathcal{G} is characterized by its input 10. Tures l_v , encoding parameters relevant to the studied network protocol. In the simple case illustrated here, we only encode the node type -i.e. if a node represents a flow or a queue – using one-hot encoding. Namely l_v is a vector with two values, with $[1,0]^T$ is for queue nodes, and $[0,1]^T$ for flow nodes.

Each node v in the graph \mathcal{G} is also characterized by us output features o_v corresponding to the values which are predicted. In this article, we study in Section 5 the case where the output vector o_{v_f} of each flow f corresponds to a bandwidth or an end-to-end latency. Since we do not have prediction on queues here, their corresponding nodes have no output vector. This is implemented by using a masked loss function for training the neural network, which only take into account the output vectors of flows.

Note that for simplification purpose, we 'mited this section – and description of transformation between network and graph – to the case where all nodes in the privor have the same behavior and that all links in the topology have the same capacity and latency. Additions features or distinguishing between different behaviors or node types (eg. link capacity, different vendors, operation system) may easily be added in case differences between nodes are present and relevant to the prediction, such as lifference of configurations, types or link capacities. In this case, l_v is extended with additional values representing those of "ferences and encoded using standard practices for feature encoding in machine learning. Example of such scenario where one has a unique attribute is given later in Section 5 where flow rates and packet sizes are additionally one ded in l_v .

We note that this network transformation process may easily be extended to more complex architectures and more refined models of queues, such as no ring network interfaces using multiple queues and a packet scheduler, or modeling more precisely network switche using additional queues depending on the internal architecture of switches. Since standard packet processing pirelines can easily be represented as graphs, additional nodes and edges representing more complex pipelines may be added in the graph.

Compared to more traditical approaches as in [2, 3, 8], we note that the graph and feature representations described here are independent of any studied network protocols or specific metrics (eg. bandwidth, latency, etc.).

5. Numerical evoluation

In this se in we evaluate Graph Neural Networks in the context of our approach described in Sections 3 and 4 on two represents are use-cases: prediction of the average steady-state bandwidth of TCP flows and prediction of end-to-end latences of UDP flows.

9

5.1. Implementation

For both use-cases, the same implementation, parameters and learning algorithm for the normal network were used. The GGNN architectures presented in Sections 3.2 and 3.3 were implemented using Tonsorflow [34] and trained using a Nvidia GeForce GTX 1080Ti GPU. The recurrent part of the GGNN and GGNN-L TM were respectively implemented according to Equations (6) to (10) and Equations (11) to (17). The function $\zeta(\cdot)$ in Equation (4) was implemented using a feed-forward neural network with two dense layers. Additional according to standard practices for recurrent neural networks [36] in order to avoid the property of the property of the control of

For each studied use-case, the model was trained multiple times using the parar and listed in Table 1. The learning rate used for training the models was optimized following standard practice of assed on Bayesian optimization. The learned weights producing the best result is then selected for the numerical result, presented in the rest of this section. All GNN models evaluated here were trained for the same number of iterations.

Parameter	Valv c
Size of hidden representation \mathbf{h}_{v}	96
Number of loops unrolling	12
Training algorithm	RMSr. pp [30
Mini-batch size	<4
Number of training iterations	20 000

Table 1: Parameters used for the training hase of the neural networks.

The following Graph Neural Network architectures were evaluated:

- GGNN-GRU: A Gated Graph Neural Network u. Tu. a GRU memory unit as presented in Section 3.2,
- GGNN-LSTM: A Gated Graph Neural Network and a LSTM memory unit as presented in Section 3.3,
- **GNN-RNN:** A simplified implementation of Graph Neural Network as described in Section 3.1 using a simple Recurrent Neural Network (RNN) architecture, where the hidden node representation is computed as:

$$\mathbf{a}_{v} = \mathbf{f}_{(v)} \left[\mathbf{h}_{1}^{(t-1)} \cdots \mathbf{h}_{|V|}^{(t-1)} \right]^{T} + \mathbf{b}_{a}$$

$$(23)$$

$$\mathbf{a}_{v}^{(t)} = \tanh\left(\mathbf{W}\mathbf{a}_{v}^{(t)} + \mathbf{U}\mathbf{h}_{v}^{(t-1)} + \mathbf{b}\right)$$
(24)

with W and U learnable weight matrices, and b a learnable bias vector.

• GNN-RNN² and GNN-RNN³ as stached versions of GNN-RNN following Section 3.4, with respectively 2 and 3 stacks, as indicating by the e-ponent in the architecture label.

In order to compare our opproach with other machine learning approaches, we evaluate also the following additional models:

- SVR: Support Vector K. The sion for the TCP bandwidth predictions using measured round-trip time and loss probability as in ut features. This model is comparable to one proposed by Mirza et al. [2]. We note that the use of such model r quires a tive measurement in the network. The implementation of SVR from scikit-learn [37] was used for the adulation.
- FFNN: A 'eed-forv and neural network with three dense layers for the TCP bandwidth predictions using the same feature. 38 th SVR model.

5.2. Use-case: r diction of average TCP flow bandwidths

In this first use case, we evaluate the capabilities of our approach at predicting the steady-state bandwidth of TCP flows sharing different bottlenecks.

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For the generation of the topologies, a random number of Ethernet switches is first sele ted using the discrete uniform distribution $\mathcal{U}(1,6)$ and connected according to a daisy chain as illustrated in Figure 7. A random number of nodes is then generated using the discrete uniform distribution $\mathcal{U}(2,32)$ and connected to a randomly selected Ethernet switch. For each node, a TCP flow is generated with a randomly selected destination mong the other nodes. The default parameters of ns-2 for the TCP stack are used, meaning that TCP Reno is rec' as a congestion control algorithm. The results of the simulations are used as a basis for the learning process of the neutral network.

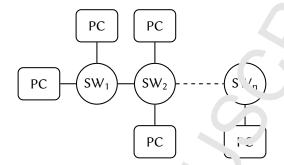


Figure 5: Daisy chain topology used for the nu. arical evaluation.

Since the performance of TCP flows is highly dependent on the songestion experienced by TCP acknowledgments, we extend our approach from Section 4 to also include TCP. CKs in the input graph representation. Figure 6 represents the graph encoding which has been used for this the property as simple topology. We follow the method explained in Section 4, where each queue in the network is represented by a node. Each TCP flows is encoded as two nodes in the graph: one node for representing the data sub-flow. To not node for the acknowledgment sub-flow, both connected by an edge. Each node i in the graph has a feature vector and ting node type as a one-hot vector:

- $[1,0,0]^T$ for nodes representing queues,
- $[0, 1, 0]^T$ for TCP data nodes.
- $[0,0,1]^T$ for TCP acknowledgment notes.

The output vector \mathbf{y}_i of each node representing a TCP data sub-flow is a single value corresponding to the normalized steady-state bandwidth. The output vector of the finer nodes is masked in the loss function.

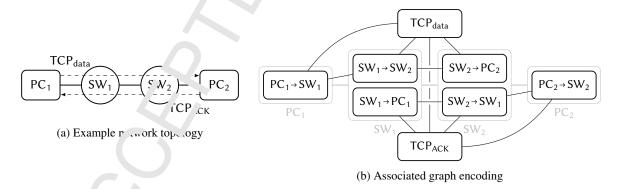


Figure 6: Graph encoding used for the TCP prediction task

As shown in purious studies about TCP [9, 24], the average throughput of TCP flows depends on various parameters such a time TCP congestion control algorithm, the configuration of the TCP stack, round-trip times or drop probabilities, as well as the interaction between flows. The graph encoding used here offers a more low-level representation.

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The neural network is trained against a mean-square loss function such that the following function is minimized:

$$\frac{1}{|flows|} \sum_{i \in flows} (\mathbf{y}_i - \mathbf{o}_i)^2 \tag{25}$$

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5.3. Use-case: prediction of UDP flows end-to-end latencies

In this second use-case, we evaluate the capabilities of our approach at predicing the and-to-end latencies of UDP flows sharing different bottlenecks. We follow the same approach as for the previous reservations are generated and evaluated using simulation. The same daisy-chain topology presented in Figure 5 is used here.

Each UDP flow i generates unidirectional traffic from a given pair of source S_i at 1 destination D_i , with constant rate r_i , using packets of random size taken from a uniform distribution from 0 to m Bytes. The parameters S_i , D_i , r_i and m_i are randomly generated for each UDP flow. For this use-case v are randomly generated for each flow in a given topology.

Regarding the graph encoding, we follow the approach illustrated in Section 4 with Figure 4 since flows are unidirectional. As for the TCP use-case, the feature vector of each node incodes the node type as a one-hot value and the traffic parameters:

- $[1, 0, \widetilde{r_i}, \widetilde{m_i}]^T$ for nodes representing flows, with $\widetilde{r_i}$ and $\widetilde{m_i}$ the 1. rmalized versions of r_i and m_i
- $[0, 1, 0, 0]^T$ for nodes representing queues

The output vector \mathbf{y}_i of each node representing a UDP flow contract to the normalized end-to-end latency. As for the TCP use-case, we use Equation (25) as loss function, where the output vector of the non-flow nodes are masked.

5.4. Prediction accuracy

In order to evaluate the accuracy of the different mounts presented here, we evaluate the predictions using the relative absolute error and residual metrics:

Refitive absolute error:
$$\frac{|\mathbf{y}_i - \mathbf{o}_i|}{\mathbf{y}_i}$$
 (26)

Residual:
$$\mathbf{y}_i - \mathbf{o}_i$$
 (27)

with \mathbf{y}_i and \mathbf{o}_i respectively measurements \mathbf{f}_i in \mathbf{t}_i is simulations, and predicted values.

Figure 7 illustrates the distributions of relative error of the different neural network architectures for the datasets previously described.

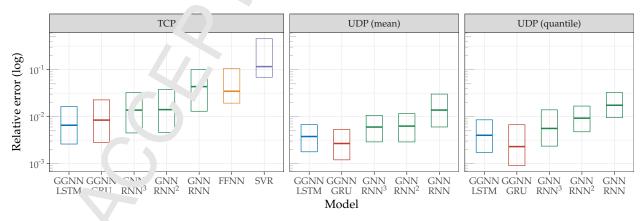


Figure 7: Comparison of the evaluated machine learning methods according to the relative error. Bars represent respectively the 25, 50 and 75 percentile values.

We first focus our interpretation of Figure 7 on the TCP use-case with machine learning rodels using high-level features (round-trip time and loss probability), namely SVR and FFNN. The median relative account error of 11.6% for the SVR model is in line with the results from [2], which reported a 10% median relative error. The feed-forward neural network provides better results, with a median relative error of 3.5%. Those values will be used as a baseline for comparison purposes.

Regarding the GGNN models, all architectures evaluated here are able to predict the CP bandwidths with a median relative error below 1%, outperforming the values from the SVR by one order or magnitude, and also outperforming the feed-forward neural network using high-level input features. This high into our main motivation for using GGNNs.

Regarding UDP latencies, we are also able to reach a median relative error bolow. %. The GGNN-LSTM architectures provide better results on the TCP use-case, while the GRU-based or is are note suited to the UDP use-case. We note that using stacked memory cells for the GGNN enables better accuracy for the TCP use-case, while not providing better results in the UDP use-case.

Compared to the more simpler GNN-RNN architecture, we notice that vore the better accuracy using a GRU or a LSTM memory cell, even in case of memory stacks. This motivates our choice of using more recent graph-based neural network architectures from [4] compared to the earlier results fro. [5, o].

In order to better understand the difference between both GRU- and LST 1-based architectures, we investigate the average residual as illustrated in Figure 8.

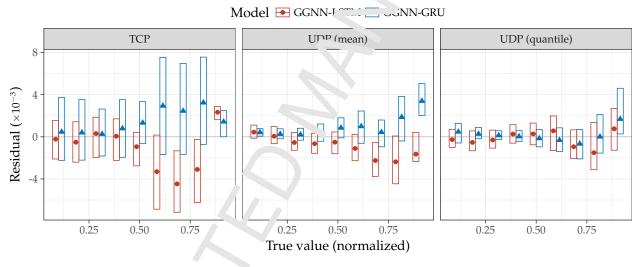


Figure 8: Comparison of real value agains the residual $(\mathbf{o}_i - \mathbf{y}_i)$ for the GGNN-GRU and GGNN-LSTM architectures. Values are normalized according to the studied dataset. Bars represent respectively the 25, 50 and 75 percentile values.

For both use-cases we notice similar values for normalized values below 0.5, where both architecture result in similar residual. In the TCP use-case, both architectures provide similar results across the range of measured values, with a tendency for the GRU-base architecture to underestimate bandwidths, while the GGNN-based one overestimates bandwidths. A similar convious exhibited for the UDP use-case.

5.5. Influence of moder ize

An important factor then comparing machine learning models and neural network architectures is their number of variables according to heir precision, as illustrated in Figure 9. For the SVR model, we quantify the number of variables as the size of the support vectors. For the neural network architectures, the number of variables presented in here are based of the size of the hidden node representation (as highlighted in Table 1). Since model size directly correlated with training time and evaluation time, an ideal model would be in the bottom left part of Figure 9, meaning it would provide the best accuracy with the lowest possible number of variables.

The difference between SVR and GGNN is also noticeable here, since both types of mode', use a similar number of variables, but with large differences in relative error. Figure 9 illustrates also the motivatio and using GGNNs with memory cells as the GGNN-GRU and GGNN-LSTM architectures outperform the other methods.

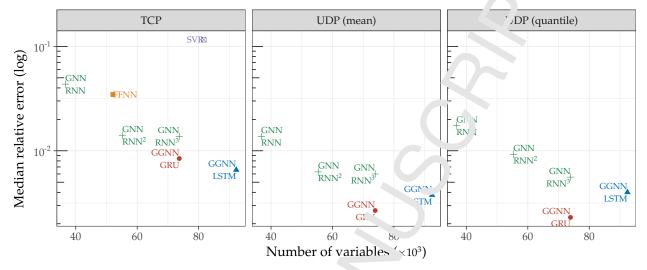


Figure 9: Evaluation of the precision of the architectu. against their number of variables.

We also notice that although the GNN-RNN 3 and GGNN GRU architectures have similar number of variables, the GGNN-GRU architecture outperforms the GNN-R N3 on motiving our choice of more advanced graph-based neural network architecture.

5.6. Influence of graph size

We investigate in this section the relationship between size of the network topology and the precision of the model. Figure 10 illustrates the influence of input grain size against the relative error. While some correlation between graph size and relative error are visible in Figure 10, it is dipendent on which dataset is investigated. We note that for the TCP use-case, increase in graph sizes result in an increase in the relative error. In the UDP use-case, the relationship between graph size and relative error is revered.

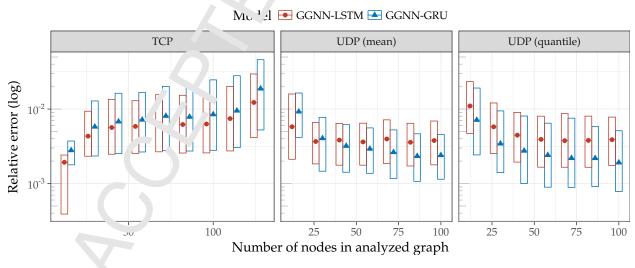


Figure 10: Evaluation of architecture precision against the size of the studied graph for the GGNN-GRU and GGNN-LSTM models. Bars represent respectively the 25, 50 and 75 percentile values.

5.7. Influence of number of unrolled loops

We noted in Section 3.2 that GGNNs are unrolled a fixed number of iterations T composed. GNNs. Figure 11 illustrates the influence of T against the relative error, where the illustrated GGNNs were trained with different values for T. Since increasing T also has an impact on training and evaluation time, a trade-off between accuracy and speed has to be established when designing the graph neural network's architecture and choosing its hyper-parameters. Increasing T improves the prediction accuracy in both use-cases for the studied architectures, with smaller effect for T larger than 12, motivating our choice of T = 12 as presented in Table 1.

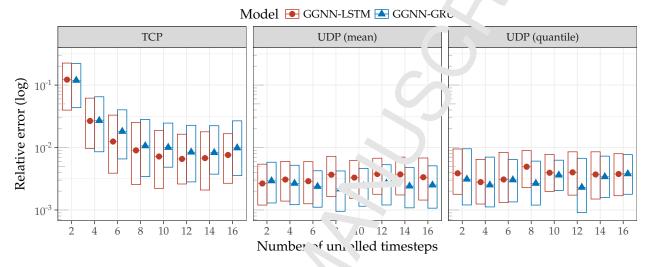


Figure 11: Evaluation of architecture precision against the number of violed iterations of hidden representation propagation. Bars represent respectively the 25, 50 and 75 percentile values.

We notice that the UDP use-case highlights a larger difference between both architectures, where larger values of T for the GGNN-GRU provide only min nal in pact on the prediction accuracy. This can be explained by the fact that end-to-end latencies depend more of local σ euling effects than topology-wide ones. This is opposed to the performance of TCP flows, where the in eraction τ etween flows on a larger scale across the topology have larger impact than local effects.

5.8. Execution time

In order to understand the scalability \cdot^c our model presented in Section 3, we evaluate in this section our implementation in term of execution t^i in Since our datasets with TCP or UDP flows contains mainly small networks, we evaluated our implementation \cdot gain \cdot randomly generated graphs. We followed the Erdős-Rényi model [38] for generating random graph with a randomly selected number of nodes |V| following the uniform distribution $\mathcal{U}(2, 1000)$ and a random number of e^i ges |S| following the uniform distribution |U|(N-1,D|V|(|V|-1)/2) with D the graph density parameter. The average graph density for both datasets used in Sections 5.2 and 5.3 was approximately 0.2.

Since the propagation of his 'o' node representations defined in Equations (2) and (6) may either be implemented in Tensorflow using d'inse mortix multiplication, or using sparse operations as noted by Allamanis et al. [20], we evaluated a dense and observe ersion of our model. According to the mathematical operations illustrated in Section 3 the runtime of one 'op unit oring of the GNN correspond to the sum of the following terms:

- Per-node o₁ erations namely Equations (7) to (10) for the GGNN-GRU, which scales linearly in execution time with the number of nodes, namely $O(|\mathcal{V}|)$;
- The proper ion of hidden node representations defined in Equations (2) and (6):
 - scaling linearly with the number of edges with sparse operations, namely $O(|\mathcal{E}|)$, i.e. $O(D|\mathcal{V}|^2)$ following that the max $(|\mathcal{E}|) = D|\mathcal{V}|(|\mathcal{V}| 1)/2$,

- scaling according to the multiplication of the hidden node representations with the raph adjacency matrix of size $|\mathcal{V}| \times |\mathcal{V}|$ with dense operations, namely $O(\mathcal{H}|\mathcal{N}|^2)$ with \mathcal{H} the size of hinder representation.

Those operations are performed multiple times according to the number of loop unrolling. as c'scussed in Sections 3.2 and 5.7. In summary, our implementations should scale in execution time quadratically with the number of nodes in the graph, and linearly with the number of edges.

Numerical results are presented in Figures 12 and 13 for our two different implements from and three values for the maximal graph density. The execution time measurements were measured on a lerver equipped with an Intel Xeon CPU E5-2620 v4 at 2.10 GHz and a Nvidia GeForce GTX 1080Ti. Batching of graphs was used to take advantage of parallelization. Those measurements validate the theoretical results presented earlier and illustrate the difference between the two implementations. As expected, the implementation using sprise operations performs faster for small graph densities while the implementation using dense operations performs the same regardless of graph density.

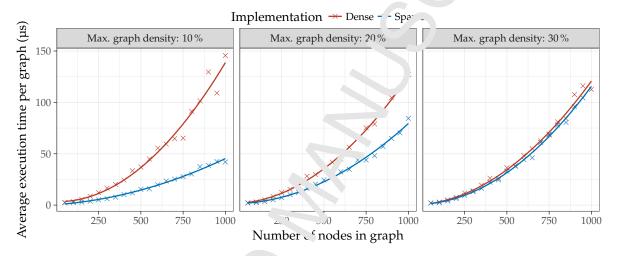


Figure 12: Average execution time of prediction against number f nodes in graph. The fitted lines correspond to a polynomial model of order 2.

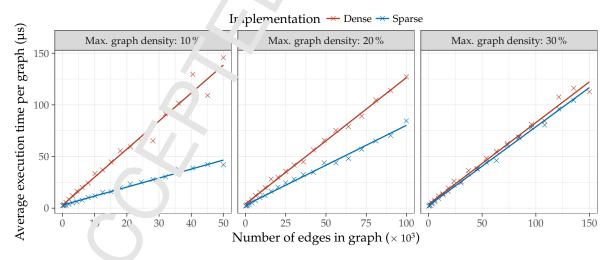


Figure 12. Average execution time of prediction against number of edges in graph. The fitted lines correspond to a linear model.

Those numer. all results illustrate also applicability in practical use-cases since the execution time for prediction is below $200\,\mu s$ even for graphs with 1000 nodes and $150\,000$ edges. This small execution time enable fast operation in real networks, where the predictions may be used to dynamically configure computer networks.

Finally, while we illustrated in Figures 12 and 13 the execution time for making a prediction on a given graph, our approach may still be limited by the size of the required dataset for larger networks in the training phase. Depending on the task which needs to be predicted, larger datasets may be required on larger graphs, since those larger cases may exhibit more complex behaviors. In the two use-case described in Sections 5.2 and 5.3 targer networks and larger number of flows will result in edge cases for the performance, namely low bandwidth for the TCP use-case and high latencies for the UDP one. Since those performance are inherently limited by link speed and maximum buffer sizes of the underlying topology in those edge cases, training and prediction on larger networks should still possible with moderate dataset sizes.

6. Interpreting GNNs

An important subject when working with neural network is the interpretacity of the learned model and its associated weights. A method often used for this purpose in computer vision, is feature visualization using optimization [39], where inputs are optimized such that a specific output feature is maximized.

In our case, we are interested in visualizing the interaction between selected lows and the traversed queues. Once the parameters of the graph neural network learned, we replace the adjace by \mathbf{A} with a modified matrix \mathbf{A} such that

$$\widetilde{\mathbf{A}} = \mathbf{A} \odot \sigma \left(\mathbf{B} + \mathbf{R}^T \right) \tag{28}$$

with $\mathbf{B} \in \mathbb{R}^{|\mathcal{V}| \times |\mathcal{V}|}$ a learnable matrix. $\mathbf{B} + \mathbf{B}^T$ ensures that $\widetilde{A} \propto$ a symmetrical matrix. For a given flow f, we then minimize the following loss function:

$$\left(\mathbf{y}_f - \mathbf{o}_f\right)^2 + \sum_{i,j} \widetilde{\mathbf{A}}_{\{i,j\}}$$
 (29)

Figure 14 illustrates the result of this optimization on a small topology with four TCP flows. We optimized **B** for each flow in the topology using gradient based optimization. The results are then aggregated according to the nodes in the network topology instead of the respective edge. The influence matrix corresponds to the aggregated value of **B**.

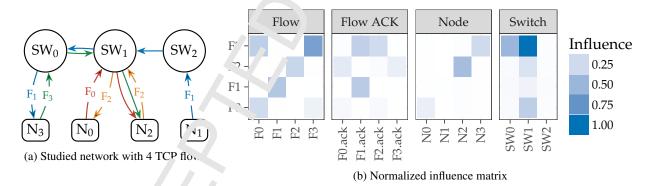


Figure 14: In. and of nodes, other flows, and flow acknowledgments on the flows' performance

As expected, bottl necks a d flows sharing the same bottleneck have an influence on each other, as shown for instance on the influence f_1 and f_2 on f_3 . Nodes having no influence on the performance of flows can also be found, as illustrated here f_1 by f_2 having no influence on f_3 . Using this visualization method, root-cause analysis of poor performance and bot leneck identification may be performed.

7. Conclusion

We presented in this article *DeepComNet*, a novel approach for the performance evaluation of network topologies and flows based on graph-based deep learning. Our approach is based on the use of Gated Graph Neural Networks

and a low-level graph-based representation of queues and flows in network topologies. Compared to other approaches using machine learning for performance evaluation of computer networks, the trained model is a specific to a given topology and high-level input features requiring more advanced knowledge on the studied protocol and not required.

We applied our approach to the performance evaluation of the bandwidth TCP flows and the performance evaluation of end-to-end latencies of UDP flows For both tasks, taking into account the topology in the performance evaluation is important: the throughput of TCP flows is dependent on the network architect. The and twork conditions (i.e. congestion and delays), and the end-to-end latencies depend on local queuing effects across the different queues from the topology. We showed via a numerical evaluation that our approach is able to reach gard accuracies, with a median absolute relative error below 1%, even on large network topologies with multipass. We compared the chosen neural network architecture against two other approaches based on machine learning thing high-level input features, and showed that our method outperforms those approaches by as much as or corder of magnitude. Different types of GGNNs and configuration parameters were evaluated in order to understand which CGNN architecture produce the best results according to the studied network protocol. Finally we also gardeness some insights into the interpretation of the neural network in order to see which nodes in a given topology have an induction protocol performances.

Since the network topology is directly taken as input of the neural network, at plications such as network planning and architecture optimization may benefit from the method developed in this article. Future work may include further study of end-to-end protocols performance as well as optimization technique; based on this method.

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