

upper

lower

$$r = r_{\#}$$

$$r = r_i$$