

# Periodicity Enhanced Long Short-term Memory Network for Wind Power Forecasting

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## Abstract

Global warming and energy crisis have brought severe challenges to the world. Wind power provides a significant renewable energy. Nevertheless, volatility of wind power causes structural risk to power grid and thus hinders its application. Short-term power forecasting (STPF) provides immediate information so that the power load can be promptly adjusted. In this paper, we propose a new neural network for STPF, wherein the periodic information in wind power series is exploited to improve the prediction accuracy. Specifically, to capture the intrinsic seasonal trend and periodic patterns of wind power series, we propose to preprocess the wind power series by using the variational mode decomposition (VMD). We also define a seasonal contribution factor (SCF) to determine the optimal number of decomposition. For STPF, we introduce the periodicity enhancing gate into the long short-term memory (LSTM) structure, so that the new network can fully exploit the periodic pattern in the subseries. Experiments on two datasets from different districts show the superiority of our proposed method in prediction accuracy.

## 1 Introduction

The renewable energy is an important measure to cope with the increasingly urgent energy and environmental crisis. Abundant and readily available, wind power has become an important source of renewable energy. Nevertheless, wind power has strong uncertainty, volatility and randomness, which increases the structural risk of the power grid, and even worsely, grid overload or power cut. Wind power forecasting provides an indispensable means for overcoming this.

According to time horizon, wind power forecasting can be divided into short-term power forecasting (minutes ahead) [Shi *et al.*, 2011; Li *et al.*, 2020] and long-term power forecasting (hours or days ahead) [Ahmadi *et al.*, 2020]. Compared to the long-term forecasting, the short-term power forecasting (STPF) provides more immediate information so that the power load can be promptly adjusted. How-

ever, due to the unstable essence of the wind power time series, accurate STPF is still a challenging task.

Existing models can be roughly classified into three categories: the traditional models [Niu *et al.*, 2022; Hodge *et al.*, 2011; Eldali *et al.*, 2016], machine learning methods [Zendehboudi *et al.*, 2018; Zeng and Qiao, 2011; Kavousi-Fard *et al.*, 2014], and recently developed deep learning methods [Lin and 0044, 2021; Wang *et al.*, 2022b; Wang *et al.*, 2022a; Yu *et al.*, 2022]. The numerical weather prediction (NWP) model [Niu *et al.*, 2022], and the auto regressive integrated moving average model (ARIMA) [Hodge *et al.*, 2011; Eldali *et al.*, 2016] are two typical representatives of the first category. In contrast, the machine learning methods, especially the support vector machine (SVM) [Zendehboudi *et al.*, 2018; Zeng and Qiao, 2011; Kavousi-Fard *et al.*, 2014] have shown better nonlinear curve fitting capability, and better performance in STPF. Recently, deep learning methods, such as the transformer-like neural networks [Lin and 0044, 2021; Wang *et al.*, 2022b] and variants of recurrent neural networks (RNN), arouse more interests in STPF research [Wang *et al.*, 2022a; Yu *et al.*, 2022].

Among them, the long short term memory (LSTM) structure has shown outstanding performance in processing series data and exploiting long-term data. For example, [Duan *et al.*, 2021] develops correntropy long short-term memory (CLSTM) neural network, which employs correntropy to replace traditional mean square error (MSE) as loss function. [Han *et al.*, 2019a] utilizes an operator vector acted on input to suppress LSTM's long-term memory of random components. [Fu *et al.*, 2018] compares gated recurrent unit with LSTM and claimed that LSTM is more suitable for multi-step forecasting.

To facilitate forecasting, data processing methods are usually used to reduce the instability and mine the seasonal trend of wind power data. Decomposition methods [Wang *et al.*, 2020; Niu *et al.*, 2022; Qiu *et al.*, 2017] and cluster methods [Wang *et al.*, 2018] are two major means utilized in STPF, among which variational mode decomposition (VMD) is the most widely used one. [Sun and Zhao, 2020; Han *et al.*, 2019b] employs VMD before forecasting, and the results prove that VMD improves the accuracy greatly.

Although the methods mentioned above have made achievements, we observe the following issues:

- **Lacking a criterion to evaluate the decomposition's**

**effect.** The VMD [Dragomiretskiy and Zosso, 2013] involves some hyper-parameters, which seriously affect the decomposition results and the forecasting accuracy. Existing methods [Wang *et al.*, 2020; Niu *et al.*, 2022; Qiu *et al.*, 2017] set the parameters manually. As a result, the empirical setting may bias the succeeding forecasting results. In addition, manually selection takes time.

- **Ignoring the seasonal trend and periodic pattern of preprocessed data.** Most Existing deep learning methods [Lin and 0044, 2021; Wang *et al.*, 2022b; Wang *et al.*, 2022a; Yu *et al.*, 2022] focus on designing novel and sophisticated network modules and structures, but ignore the intrinsic seasonal trend and periodic pattern of the wind power data.

In this work, we propose a two-phase STPF method, wherein we provide solutions to the problems mentioned above. In the first phase, we apply VMD to wind power series, hoping to exploit latent seasonal and periodic components. In order to evaluate the results of decomposition before making prediction, we define the Seasonal Contribution Factor (SCF). It reflects the strength of seasonal trend of each component and the proportion of each sub-series in the original sequence. Decomposition with high SCF contains more seasonal and periodic components, which is believed to be helpful for forecasting. In the second phase, the decomposition results of the first phase is fed into our proposed network, named Periodicity Enhanced Long Short term Memory network (PELSTM) to make prediction. To fully exploit the seasonal trend and periodic pattern captured by the VMD, we introduce a new gate module, named Periodicity Enhanced Gate, which encourages the periodic component to be preserved in the hidden state.

## 2 Related Work

### 2.1 Wind Power Series And STPF.

Let real number  $\{X_t\}$  represent the numerical value of power generated from wind-driven generator at time  $t$ .

Wind power series  $\{X_t\}$  is a typical time series. or, a discrete sequence taken at successive equally spaced time instants. Therefore, STPF can be considered as a time series forecasting problem. It aims to predict future values based on previously observed values.

In order to utilize the previously observed data dynamically and avoid accumulation of error, 'Sliding Window' is a common strategy for time series forecasting. The detailed process of 'Sliding Window' is shown in Figure 2. Let  $X_{t-T}, X_{t-T+1} \dots X_t$  be previously observed data,  $\hat{X}_{t+1}$  be the predicted value at instant  $t$ ,  $f$  be a regression function, STPF can be formulated as follows:

$$X_{t-T}, X_{t-T+1} \dots X_t \xrightarrow{f} \hat{X}_{t+1} \quad (1)$$

Besides wind power series  $\{X_t\}$ , we employ  $\{X_t^i\}$  to represent the descomposed sub-series.

### 2.2 Variational Mode Decomposition.

VMD [Dragomiretskiy and Zosso, 2013] is an adaptive and entirely non-recursive variational mode decomposition model, where the modes are extracted concurrently. It looks for an ensemble of modes denoted  $\{X_t^k\}$  and their respective center frequencies, such that the modes collectively reproduce the 1D input signal  $\{X_t\}$  while each being smooth after demodulation into baseband. VMD has found wide applications in signal decomposition in audio engineering, climate analysis, various flux and neuromuscular signal analysis in medicine and biology, etc.

For a given wind power series  $\{X_t\}$ , let  $\{X_t^k\}_{k=1, \dots, K}$  represent the decomposed sub-series,  $K$  be the number of intrinsic mode function (IMF), or the number of sub-series. VMD achieves the decomposition by solving the following constrained optimization problem:

$$\begin{aligned} \min \sum_k^K ||\partial_t[(\delta(t) + \frac{j}{\pi t}) * X_t^k] e^{-jw_k t}||_2^2 \\ \text{s.t.} \sum_k^K X_t^k = X_t \end{aligned} \quad (2)$$

where  $\delta(t)$  denotes the Dirac distribution;  $*$  denotes convolution;  $w_k$  denotes the central frequency of sub-series  $\{X_t^k\}$  and  $j$  is the imaginary unit.

### 2.3 Auto-correlation Function.

As a function of delay time lag, the auto-correlation function (ACF) is the correlation of a series with a delayed copy of itself, measuring the dependency between present data and past data. ACF is an important analytical tool employed in time series analysis, helping discover periodic patterns and seasonal trend obscured by noise. For a given wind power series  $\{X_t\}$ , ACF, denoted by  $\gamma_k$ , is defined as

$$\gamma_k = \frac{1}{N-k} \sum_{t=k+1}^N (X_t - \bar{X})(X_{t-k} - \bar{X}) \quad (3)$$

where  $X_t$  denotes original series and  $X_{t-k}$  denotes the delayed series with delayed time lag of  $k$ . While  $\bar{X}$  represents the expected value of the overlapping parts of  $\{X_t\}$  and  $\{X_{t-k}\}$ . The normalized ACF, also called auto-correlation coefficient (ACC) is defined as

$$\rho(k) = \frac{\gamma_k}{\gamma_0} \quad (4)$$

### 2.4 Variance Contribution Rate.

The variance measures the variability in the data, and can be used to measure the amount of information carried by a sequence. In principal component analysis (PCA), variance contribution rate (VCR) is the rate of sub-series variance in the original sequence variance, and it measures the amount of information that a sub-series carry. It can be computed as follows:

$$\begin{aligned} r_i &= \frac{\lambda_i}{\sum_{j=1}^K \lambda_j} \\ \lambda_i &= \frac{1}{N} \sum_{t=1}^N (X_t^i - \bar{X}^i)^2 \end{aligned} \quad (5)$$

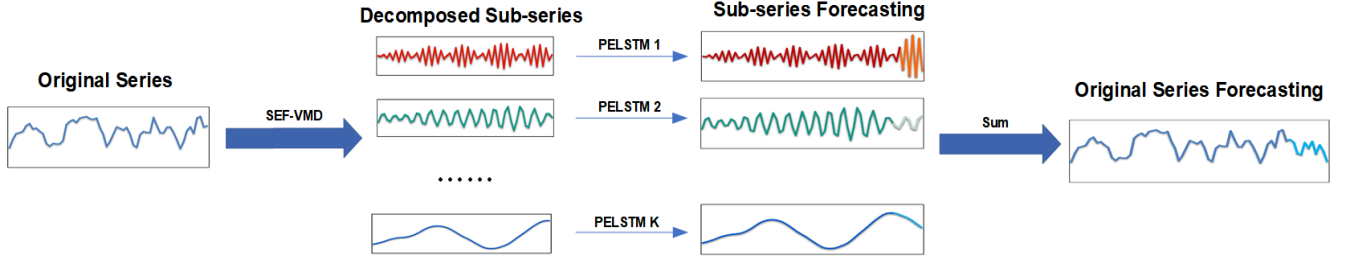


Figure 1: Illustration of STPF Framework

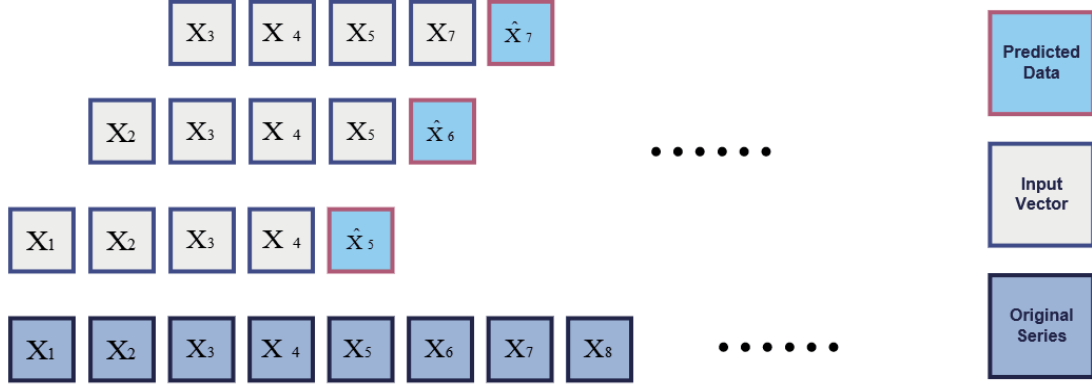


Figure 2: Illustration of Sliding Window

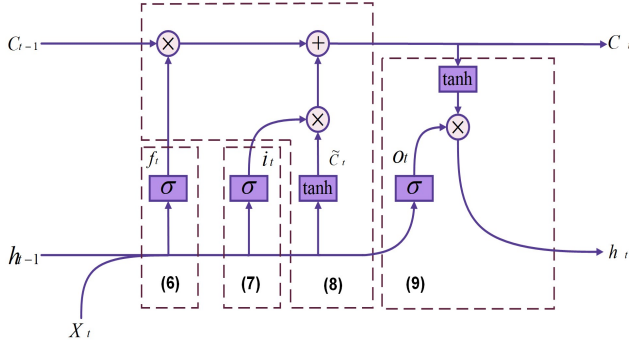


Figure 3: Illustration of LSTM Unit

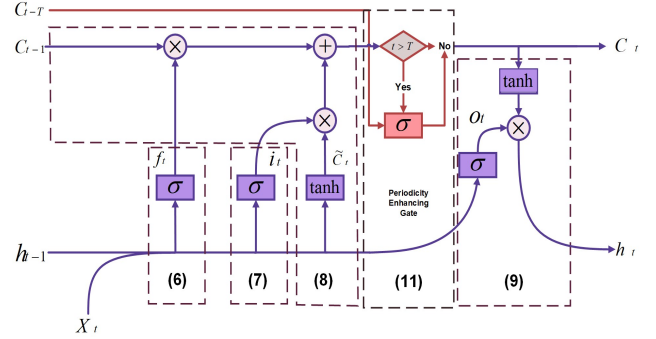


Figure 4: Illustration of PELSTM Unit

where  $r_i$  resembles VCR of sub-series  $\{X_t^i\}$ ,  $\lambda_i$  denotes the variance of sub-series  $i$ , and  $\bar{X}^i$  denotes the expected value of  $\{X_t^i\}$ .

## 2.5 Long Short-term Memory.

LSTM [Hochreiter and Schmidhuber, 1997] can make full use of long-term data and avoid vanishing or exploding gradients, and performs well in processing series data.

As illustrated in Figure 3, a LSTM network consists of an input layer, an output layer, and several cascaded recursive hidden layers. A recursive hidden layer is composed of several LSTM units. Each unit contains a memory cell and three gate functions that control the flow of information: forgetting gate, input gate and output gate. The gate functions are de-

finied as follow:

The forgetting gate:

$$f_t = \sigma(W_f \cdot [h_{t-1}, x_t] + b_f) \quad (6)$$

The input gate:

$$i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i) \quad (7)$$

The memory cell state updates:

$$\begin{aligned} \tilde{C}_t &= \tanh(W_c \cdot [h_{t-1}, x_t] + b_c) \\ C_t &= f_t \circ C_{t-1} + i_t \circ \tilde{C}_t \end{aligned} \quad (8)$$

The output gate:

$$\begin{aligned} o_t &= \sigma(W_o \cdot [h_{t-1}, x_t] + b_o) \\ h_t &= o_t \circ \tanh(C_t) \end{aligned} \quad (9)$$

where  $\sigma$  is the sigmoid activator and  $h_{t-1}$  is the hidden state or rather, the output of time  $t - 1$ .  $W_f$ ,  $W_i$ ,  $W_c$ ,  $W_o$  are the weight matrices and  $b_f$ ,  $b_i$ ,  $b_c$ ,  $b_o$  bias variables of three units and memory cell. What's more,  $\circ$  denotes the hadamard product. The forward propagation of LSTM unit is to execute the computation of gate functions in order, which is illustrated in Figure 2.

### 3 Methodology

In most existing work[Wang *et al.*, 2020; Qiu *et al.*, 2017], the hyperparameter  $K$  of VMD is set manually[Niu *et al.*, 2022]utilizes the envelope entropy as the criterion to measure the effect of VMD, but didn't discuss the improvements to forecasting accuracy. Meanwhile it ignored the seasonal trend and periodic pattern captured by the VMD. To solve this problem, we proposed SCF as a novel criterion to measure the effect of VMD, then select suitable hyperparameter  $K$ . SCF is aimed to maximize exploitable periodic components of decomposition, which is helpful for forecasting. We conducted experiments to prove that SCF improve the accuracy by 57.92% and 26.37% at most on two datasets compared to other hyperparameters.

Inspired by the seasonal trend and periodic pattern of data captured by VMD, we proposed PELSTM to exploit these information, which introduced 'Periodicity Enhanced Gate' structure to traditional LSTM. Experiments results show that PELSTM outperform LSTM on both datasets, especially on volatile series, which is close to application. Meanwhile, PELSTM avoids the abnormal fluctuations of LSTM forecasting outcome in flat series, which significantly improves the accuracy.

As shown in figure 1, our proposed framework consists of two major components: the wind power series decomposition module based on VMD and SCF, the forecasting module based on PELSTM. We employs SCF to evaluate the effect of decomposition, thus choosing the best number of IMF. Then, we deploy PELSTM on each IMF series, utilizing sliding windows to forecast the results.

#### 3.1 Seasonal Contribution Factor.

We define the SCF to measure the effect of decomposition. Usually, if a decomposition contains more seasonal trend and periodic pattern, it is easier for forecasting. The first maximum value of ACC of a sub-series measures the seasonal trend of the sub-series, thus we define it as seasonal factor(SF). The VCR measures the amount of information a sub-series contains. We define the SCF of a sub-series as the product of SF and VCR, and the sum of all sub-series' SCF as the SCF of a decomposition. The mathematical formulation of SCF is as follows:

$$\begin{aligned} SCF^i &= SF^i \times VCR^i \\ SCF &= \sum_i^K SCF^i \end{aligned} \quad (10)$$

where  $SF^i$  denotes the seasonal factor of sub-series  $\{X_t^i\}$  and  $SCF^i$  denotes the seasonal contribution factor of sub-series  $\{X_t^i\}$ . While  $SCF$  denotes the seasonal contribution factor of the decomposition.

We choose the best number of sub-series as the one corresponding to the largest SCF. In practice, we search time lag  $k$  from 0 to a finite number for SF. The finite number is set according to the computation time requirements. We define SF as 0 if there does not exist a maximum value. What's more, the maximum point we can be viewed as a period of the sub-series, which we will discuss in the next section.

#### 3.2 Periodicity Enhanced Long Short-term Memory.

To fully exploit the seasonal trend in data, we introduce a gate function named 'Periodicity Enhancing Gate' just following the update of memory cell state. Each time it propagates forward, except for the first period, it enhances the current cell state with the cell state one period ago. The structure of PELSTM is illustrated in Figure 3 and the operation of the periodicity enhancing gate is

$$C_t = \begin{cases} \sigma(W_{ps} * C_{t-T} + (1 - W_{ps} * C_t)) & t > T \\ C_t & t \leq T \end{cases} \quad (11)$$

where  $T$  is the period mentioned in section 3.1,  $W_{ps}$  is the weight matrix that can be updated in the training process.

### 4 Experiments

In this section, we conduct experiments to validate the effectiveness of SCF and PELSTM, respectively. We first introduce the datasets and data preprocessing. Then we conduct an experiment to verify the effectiveness of SCF. Finally, we conduct an experiment to compare PELSTM to other machine learning methods and LSTM variants.

#### 4.1 Datasets

We conduct experiments on two datasets collected from one wind farm in China(Datasets 1) and one from Turkey(Datasets 2). The data are extracted from sensors in wind turbine, which generates real-time wind power data. In Datasets 1, samples were taken at 10 minute intervals, and in Datasets 2, samples were taken at 15 minute intervals.

Both datasets contain some missing values. In order to maintain the seasonal trend of data, we only exploit the the longest continuous segment of data. In addition, the data are normalized to  $[0,1]$ .

After the data cleaning, Datasets 1 has 25234 data and Datasets 2 has 22712 data.

#### 4.2 Setting

We split these two datasets into training set, validation set and test set with ratio 7 : 1 : 2. Let  $T^i$  denote the period of a sub-series. We set the length of 'Sliding Window' as  $T^i$ . If  $T^i$  is larger than 20 or  $T^i$  doesn't exist, we set it as 20. We set the batch size of data as 5.

The hidden size of LSTM and PELSTM is 48. The models are trained by the optimizer 'ADAM'. We set the initial learning rate as 0.1 and choose exponential learning rate decay.

| Datasets1 |         | 8 IMF | 9 IMF | 10 IMF       | 11 IMF | 12 IMF |
|-----------|---------|-------|-------|--------------|--------|--------|
| LSTM      | RMSE    | 36.07 | 34.55 | <b>29.64</b> | 37.76  | 39.17  |
|           | MAE     | 23.24 | 23.05 | <b>18.77</b> | 26.20  | 24.30  |
|           | MAPE(%) | 12.46 | 12.80 | <b>10.19</b> | 14.06  | 13.71  |
| PSLSTM    | RMSE    | 30.98 | 30.72 | <b>23.88</b> | 28.43  | 34.77  |
|           | MAE     | 19.84 | 19.14 | <b>14.77</b> | 18.87  | 21.22  |
|           | MAPE(%) | 10.44 | 10.73 | <b>8.54</b>  | 10.92  | 12.46  |

Table 1: Prediction Errors of Datasets 1

| Datasets2 |         | 11 IMF | 12 IMF | 13 IMF      | 14 IMF | 15 IMF |
|-----------|---------|--------|--------|-------------|--------|--------|
| LSTM      | RMSE    | 10.80  | 9.58   | <b>8.52</b> | 11.37  | 13.91  |
|           | MAE     | 8.75   | 7.85   | <b>7.18</b> | 8.71   | 10.81  |
|           | MAPE(%) | 4.92   | 4.05   | <b>3.97</b> | 5.39   | 6.96   |
| PSLSTM    | RMSE    | 7.77   | 9.05   | <b>7.25</b> | 8.84   | 8.33   |
|           | MAE     | 6.46   | 7.60   | <b>5.97</b> | 6.79   | 6.54   |
|           | MAPE(%) | 3.47   | 3.99   | <b>3.43</b> | 3.92   | 3.50   |

Table 2: Prediction Errors of Datasets 2

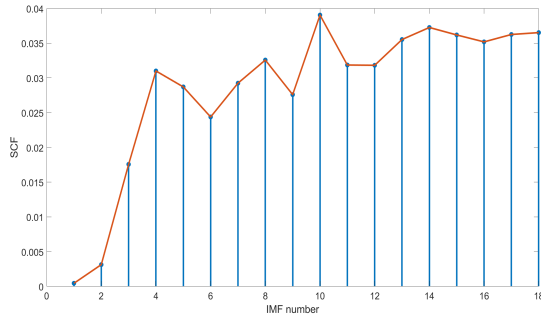


Figure 5: SCF of Datasets 1

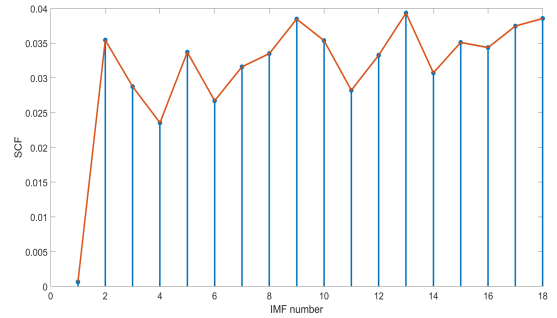


Figure 6: SCF of Datasets 2

### 4.3 Effectiveness of PELSTM and SCF

In this subsection we empirically validate the effectiveness of our PELSTM and SCF.

- Advantages of PELSTM over LSTM.** To show advantages of PELSTM over LSTM, we make predictions by using PELSTM and LSTM, respectively, and the root mean squared errors(RMSE), mean absolute deviations(MAE), and mean absolute percentage errors(MAPE) of the predictions are given in Table 1 and Table 2, respectively for Dataset 1 and Dataset 2. Before prediction, we first apply VMD to obtain different numbers of IMFs. Specifically, for Dataset 1,  $K \in \{8, 9, 10, 11, 12\}$  and for Dataset 2,  $K \in \{11, 12, 13, 14, 15\}$ . We can note that, on Dataset 1,  $K=10$  leads to the best results for both PELSTM and LSTM, while on Dataset 2,  $K=13$  leads to the best re-

sults for both PELSTM and LSTM. On the other hand, we can note that, on both datasets, our PELSTM outperforms LSTM consistently for different values of  $K$ .

We also illustrate some predicted values by PELSTM and LSTM for Dataset 1 in Figure 7 and Figure 8. We can note that, the predicted values obtained by LSTM shows abnormal periodic fluctuation in flat part of some sub-series while the predicted values obtained by PELSTM are more consistent with the observed values. This is because PELSTM can timely capture the periodic pattern.

Besides, our PELSTM shows better accuracy in predicting peaks. Figure 9 and Figure 10 shows the prediction results by LSTM and PELSTM for one subseries of the data from Dataset 1. We can see that PELSTM can better track local pattern in the data.

|           |         | ARIMA | SVM    | BP     | Transformer | LSTM  | BiLSTM | GRU   | ConvLSTM | CLSTM | PELSTM       |
|-----------|---------|-------|--------|--------|-------------|-------|--------|-------|----------|-------|--------------|
| Datasets1 | RMSE    | 87.04 | 35.31  | 131.37 | 33.28       | 28.72 | 26.72  | 44.28 | 31.27    | 33.58 | <b>23.17</b> |
|           | MAE     | 50.95 | 21.12  | 100.16 | 19.45       | 18.40 | 18.35  | 38.75 | 23.52    | 19.43 | <b>14.45</b> |
|           | MAPE(%) | 31.35 | 12.69  | 50.37  | 11.28       | 10.12 | 9.56   | 18.41 | 14.71    | 13.01 | <b>8.51</b>  |
| Datasets2 | RMSE    | 15.82 | 129.56 | 12.12  | 20.34       | 8.52  | 8.02   | 23.68 | 10.22    | 12.52 | <b>7.25</b>  |
|           | MAE     | 10.19 | 92.59  | 10.31  | 14.56       | 7.18  | 6.89   | 14.25 | 8.98     | 9.36  | <b>5.97</b>  |
|           | MAPE(%) | 6.04  | 49.67  | 5.73   | 9.59        | 3.97  | 3.52   | 9.59  | 5.62     | 6.01  | <b>3.43</b>  |

Table 3: Prediction Errors by Baselines and Our Proposed Method

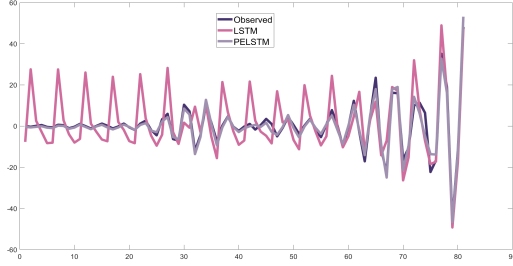


Figure 7: Abnormal Fluctuation Part of Sub-series from Dataset 1

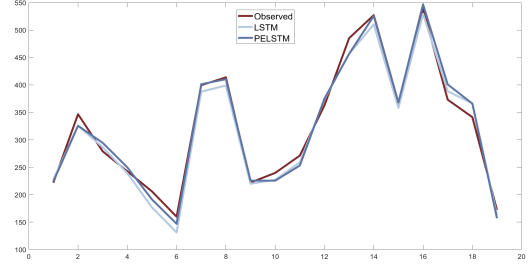


Figure 9: Peak Values of Original Series from Dataset 1

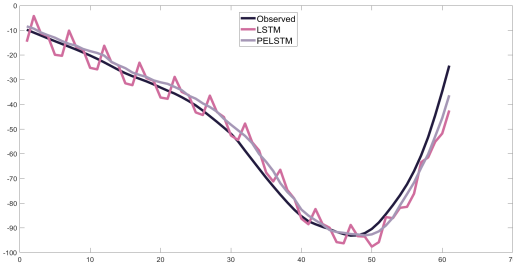


Figure 8: Abnormal Fluctuation Part of Sub-series from Dataset 1

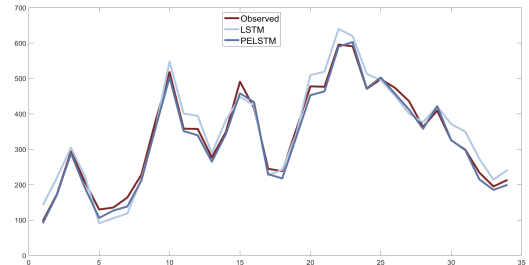


Figure 10: Peak Values of Original Series from Dataset 1

- **Effectiveness of SCF.** We apply VMD to Dataset 1 and Dataset 2, with  $K \in \{1, 2, \dots, 18\}$  and the corresponding SCFs are presented Figure 5 and Figure 6. For dataset1, the maximum SCF corresponds to the empirical best value of  $K=10$ (Table 1); and on for Dataset 2, the maximum SCF corresponds to the empirical best value of  $K=13$ (Table 2). Thus, we can conclude that our SCF is effective in inferring the best value of  $K$ .

#### 4.4 Comparison of related methods with ours

In this subsection, we conduct experiments to compare our proposed method with related methods: ARIMA, SVM, BP, LSTM and Transformer. Besides, some important variants of LSTM applied in wind power forecasting like BiLSTM[Niu *et al.*, 2022], GRU[Fu *et al.*, 2018], ConvLSTM[Sun and Zhao, 2020] and CLSTM[Duan *et al.*, 2021] are also compared. All prediction methods work on the same decomposition results obtained by VMD, with the best  $K$  determined by the maximum SCF. The prediction errors of all methods are given in Table 3. We can note that, our PELSTM significantly outperforms the baselines for both datasets. For Datasets 1 in

particular, which is rather volatile (with a large standard deviation), the prediction errors obtained by our method are much less than that obtained by others. In this sense, we believe that our PELSTM is more suitable for dealing with real data.

## 5 Conclusion

In order to solve STPF, this paper proposes a novel factor named 'Seasonal Contribution Factor' to select the number of IMF in the decomposition of power series. Then we propose a novel neural network architecture called 'Periodicity Enhanced Long Short-term Memory Network' to forecast the decomposed sub-series. Extensive experiments were conducted in two datasets from different districts, which proves the effectiveness of SCF and the better performance of PELSTM than baselines.

In the future, we plan to extend the model to enable more complex deep learning architectures such as attention mechanism. Furthermore, we will try to explore the accuracy of our proposed model in multi-step forecasting problem.

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