

Lasso & Ridge Regression

Mathematical Proof

Ridge (L2) → Used for overfitting
 θ would never go to 0

$$\text{Cost } J(\theta) = \frac{1}{2m} \sum (h(\theta) - y_i)^2 + \lambda (\theta / \text{slope} / \text{coeff})^2$$

finding minima

$$\frac{dJ}{d\theta} = 0$$

$$\frac{d}{d\theta} \left[\frac{1}{2} (\theta - z)^2 + \lambda (\theta)^2 \right]$$

$$(\theta - z) + 2\lambda \theta = 0$$

$$\theta(1 + 2\lambda) = z$$

$$\theta_{\text{ridge}} = \frac{z}{(2\lambda + 1)}$$

if $z \neq 0$

$\theta_{\text{ridge}} \neq 0$ for finite λ

Lasso (L1) → Used for feature selection
 θ could go to zero

$$\text{Cost } J(\theta) = \frac{1}{2m} \sum (h(\theta) - y_i)^2 + \lambda |\theta / \text{slope} / \text{coeff}|$$

Case a ($\theta > 0$)

$$\frac{1}{2} \frac{d}{d\theta} (\theta - z)^2 + \lambda \theta = 0$$

$$(\theta - z) + \lambda = 0$$

$$\theta = z - \lambda$$

as $\theta \rightarrow +ve$

$$z - \lambda > 0$$

$$z > \lambda$$

Case B ($\theta < 0$)

$$\frac{1}{2} \frac{d}{d\theta} (\theta - z)^2 - \lambda \theta = 0$$

$$(\theta - z) - \lambda = 0$$

$$\theta = z + \lambda$$

as $\theta < 0$

$$z < -\lambda$$

$\theta \rightarrow$ tell relation of particular independent variable to target variable

