# BIFX 553 - Discussion 3

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## Assessing Model Fit and Assumptions

### **Regression Assumptions**

We will primarily use visual inspection and the car package for checking regression assumptions, but there are many other resources in R to do this (e.g. the rms and gvlma packages).

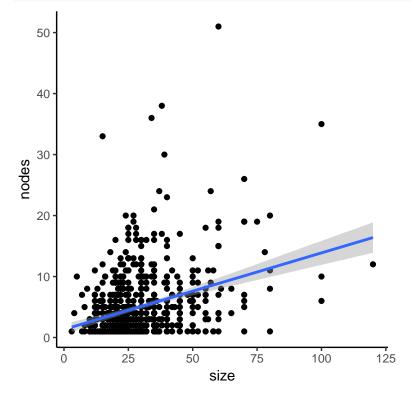
- Linear relationship
- Multivariate Normality
- No/little multicollinearity
- No autocorrelation
- Homoscedasticity

How does our model hold up?

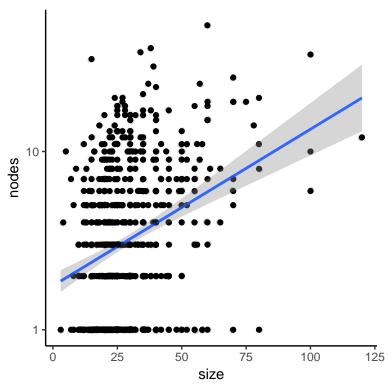
```
load('../1-26/gbsg.RData')

# model from Discussion2
gbsg.lm <- lm(nodes ~ age + meno + size + grade + pgr + er + hormon, data = gbsg)

ggplot(gbsg, aes(size, nodes)) +
  geom_point() +
  geom_smooth(method = 'lm')</pre>
```

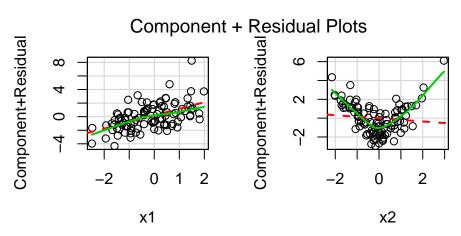


```
# this is probably a better way to look at the data
ggplot(gbsg, aes(size, nodes)) +
  geom_point() +
  geom_smooth(method = 'lm')+
  geom_jitter(alpha = .2) +
  scale_y_log10()
```



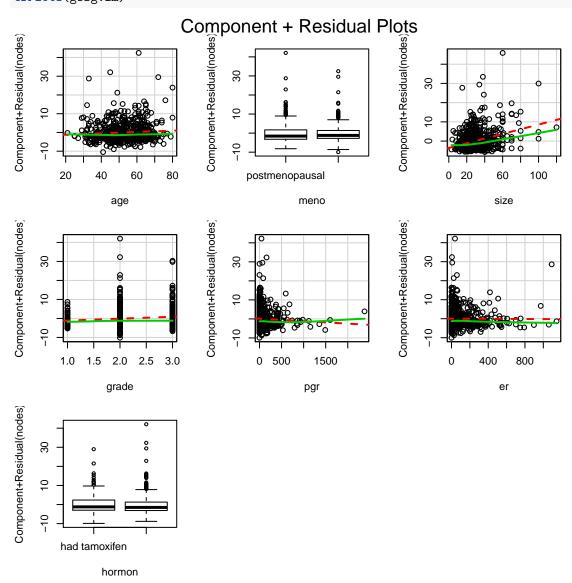
#### Linear Relationship

Component residual plots are a way to see if the predictors have a linear relationship with the outcome variable. The red, dashed line in the figures below represents the best fit of each preidictor and the residuals, and the solid, green line is a running, smoothed average along the x-axis. In this example,

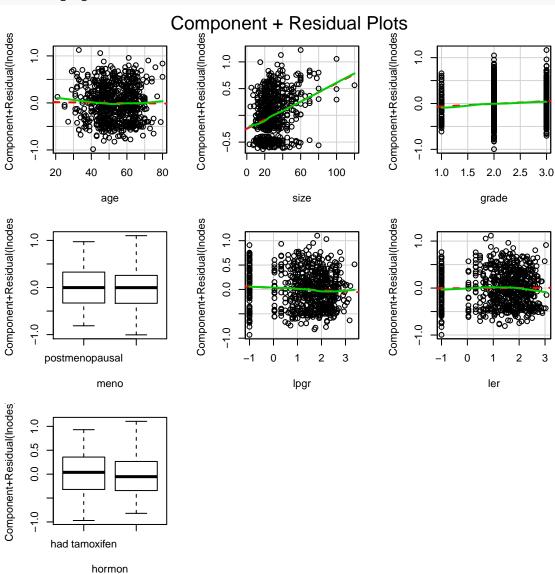


How does our model look?

# old model
crPlots(gbsg.lm)

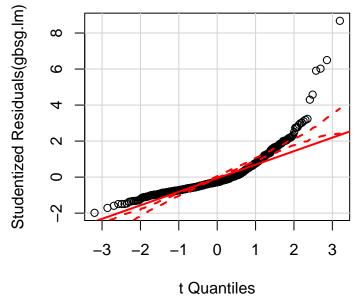




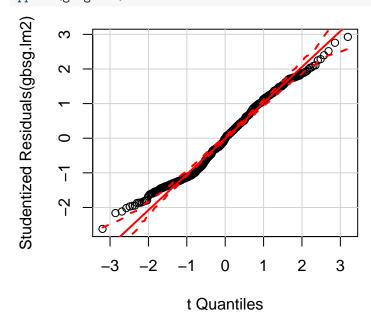


#### **Multivariate Normality**

There are a couple of ways we can look at normality. The Sapiro-Wilk test for normality will give you a quantitative measure of whether your residuals are normally distributed, and the QQ plot will give you a graphical way to see what is going on with your residuals.



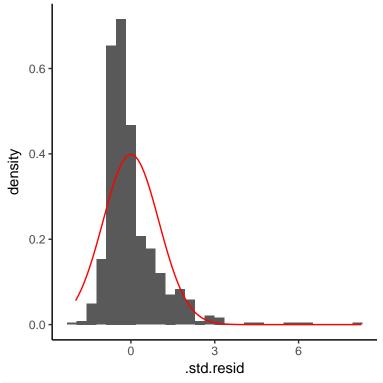
## qqPlot(gbsg.lm2)



You could also plot a histogram of your residuals along with a normal distribution.

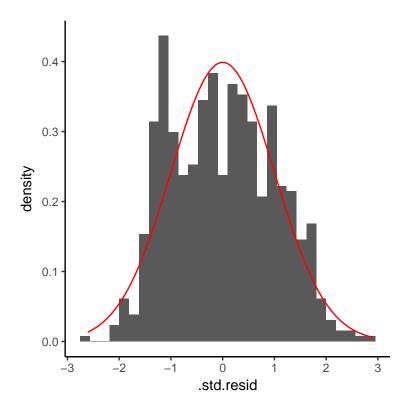
```
# take a look at the residuals
augment(gbsg.lm) %>%
ggplot(aes(.std.resid)) + # plot studentized residuals on x-axis
geom_histogram(aes(y = ..density..)) + # plot histogram as density, rather than frequency
stat_function(fun = dnorm, color = 'red') # put a N(0,1) density over the top
```

## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



```
augment(gbsg.lm2) %>%
   ggplot(aes(.std.resid)) + # plot studentized residuals on x-axis
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```

## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



#### No/little multicollinearity

Variance inflation factors give you a meeasure of how much the residuals are inflated when each predictor is added to the model (compared to the full model minus the predictor in question). This can give us an idea for what predictors might be correlated with eachother. Anything greater than 2 should certainly give us pause.

```
# variance inflation factors
vif(gbsg.lm)
##
        age
                meno
                          size
                                  grade
                                                        er
                                                             hormon
                                              pgr
## 2.579321 2.513984 1.016654 1.050404 1.220625 1.327381 1.096945
vif(gbsg.lm2)
        age
                size
                         grade
                                   meno
                                             lpgr
                                                       ler
                                                             hormon
## 2.516079 1.013574 1.160316 2.527746 1.949148 1.948627 1.093311
```

#### No autocorrelation

Autocorrelation most often occurs when there is a correlation between observations at regular time intervals. The Durbin-Watson test will give us a measure of autocorrelation (the null hypothesis is that there is no autocorrelation).

```
# Durbin-Watson test for autocorrelation
durbinWatsonTest(gbsg.lm)

## lag Autocorrelation D-W Statistic p-value
## 1 -0.004115498 2.005419 0.984
## Alternative hypothesis: rho != 0
```

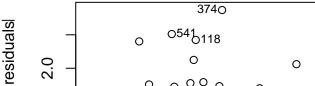
#### durbinWatsonTest(gbsg.lm2)

```
##
   lag Autocorrelation D-W Statistic p-value
##
            -0.01422531
                              2.025106
   Alternative hypothesis: rho != 0
```

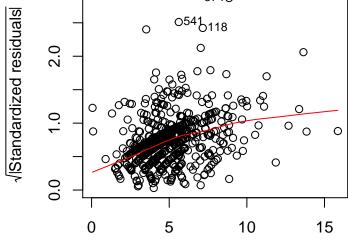
#### Homoscedasticity

Heteroscedasticity refers to a model where the variance about the predicted value of the outcome changes as the predicted value increases. We can check for this using a score test for non-constant error variance or graphically.

```
# statistical test for heteroscedasticity (null is that they are homoscedastic)
ncvTest(gbsg.lm)
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 165.5525
                           Df = 1
                                      p = 6.928119e-38
ncvTest(gbsg.lm2)
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 7.317349
                           Df = 1
                                         = 0.006829208
# scale-location plot
plot(gbsg.lm, which = 3)
```

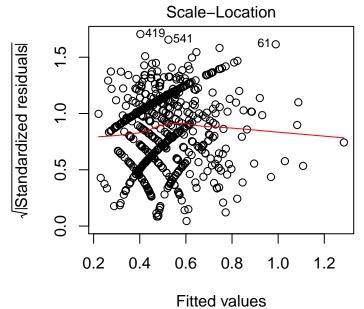


Scale-Location



Fitted values m(nodes ~ age + meno + size + grade + pgr + er + hol

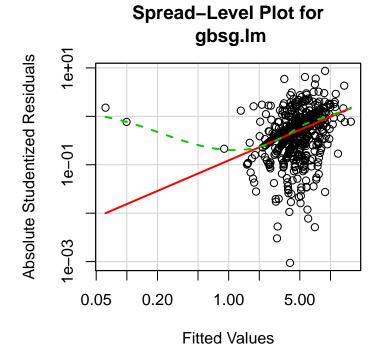
```
plot(gbsg.lm2, which = 3)
```



n(Inodes ~ age + size + grade + meno + lpgr + ler + hc

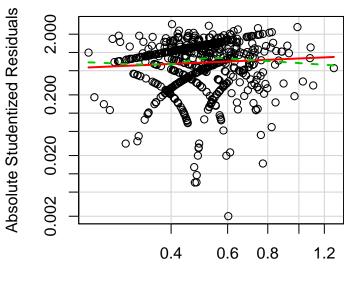
The spreadLevelPlot function gives us a slightly nicer picture of this. The solid red line is what we would hope to see under a homoscedastic model, and the green line is what is actually observed. These two plots (the one just above and the one just below) are representations of the exact same data. The plot below, however, is scaled differently to highlight departures from the expected.

# another scale-location plot
spreadLevelPlot(gbsg.lm)



##
## Suggested power transformation: 0.09857515

# Spread-Level Plot for gbsg.lm2



Fitted Values

##
## Suggested power transformation: 0.774467

#### Outliers / Influential Points

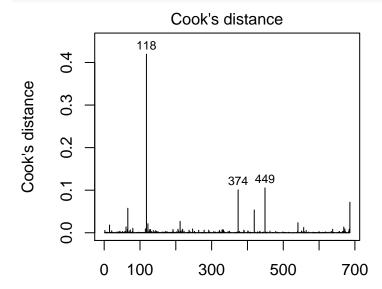
The outlierTest function gives us a list of the most significant outliers in a model by row number. The maxumum number of rows to return is controlled by the n.max function argument.

```
# returns the most significant outliers in the residuals
outlierTest(gbsg.lm)
```

```
rstudent unadjusted p-value Bonferonni p
##
## 374 8.677313
                         3.0022e-17
                                      2.0595e-14
## 541 6.496241
                         1.5957e-10
                                      1.0946e-07
## 118 6.021028
                                      1.9493e-06
                        2.8416e-09
## 419 5.907297
                        5.5069e-09
                                      3.7777e-06
## 66 4.579290
                        5.5528e-06
                                      3.8092e-03
## 449 4.299970
                         1.9594e-05
                                      1.3442e-02
outlierTest(gbsg.lm2)
```

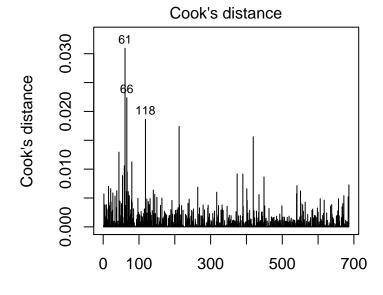
We can also graphically inspect the influence that each row of data (or each individual in the sample) has on the overall model. Cook's distance gives us a measure of how much each row of data influences the model. Ideally we would like them all to be close to the same, but we sometimes have some values that are overly influential (see this illustration of how one data point can influence a regression fit).

# Cook's Distance
plot(gbsg.lm, which = 4)



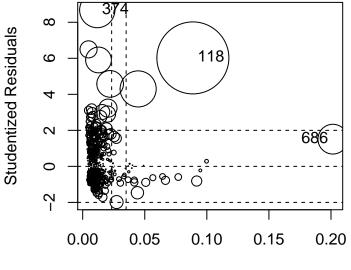
Obs. number | m(nodes ~ age + meno + size + grade + pgr + er + hoi

plot(gbsg.lm2, which = 4)



 $\label{eq:obs.number} Obs. \ number \\ n(Inodes \sim age + size + grade + meno + lpgr + ler + hc$ 

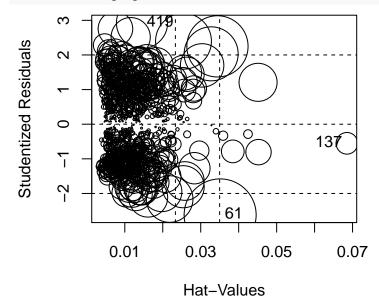
# Influence
influencePlot(gbsg.lm)



#### Hat-Values

```
## StudRes Hat CookD
## 118 6.021028 0.08875591 0.41956588
## 374 8.677313 0.01173853 0.10075428
## 686 1.510113 0.20151716 0.07180519
```

#### influencePlot(gbsg.lm2)



## StudRes Hat CookD ## 61 -2.619349 0.03511812 0.030946805 ## 137 -0.551649 0.06850720 0.002800518 ## 419 2.926259 0.01452950 0.015607198

#### Influence of terms in the model

We also want to make our model as parsemonious as we can. Sometimes we will include a prediction variable because we believe that it is important, but usually we will include preditors only if they appear to be statistically important to our model. To get a quick look at the statistical significance of a predictor, we can

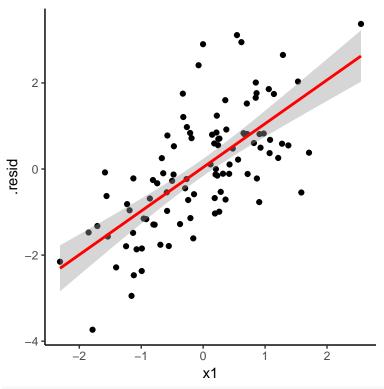
just look at the regression output.

```
tidy(gbsg.lm2)
```

```
##
                   term
                             estimate
                                       std.error statistic
## 1
            (Intercept) 0.2188534351 0.158828460 1.3779233 1.686816e-01
## 2
                   age -0.0004743639 0.002313088 -0.2050782 8.375726e-01
## 3
                  size 0.0084830687 0.001039319 8.1621425 1.603046e-15
## 4
                 grade 0.0575594521 0.027277523 2.1101422 3.521185e-02
## 5
     menopremenopausal -0.0262983051 0.047464585 -0.5540616 5.797194e-01
## 6
                   lpgr -0.0253118219 0.018632700 -1.3584624 1.747688e-01
## 7
                   ler 0.0026068067 0.019428389 0.1341751 8.933039e-01
## 8 hormonno tamoxifen -0.0304764028 0.032153444 -0.9478426 3.435473e-01
```

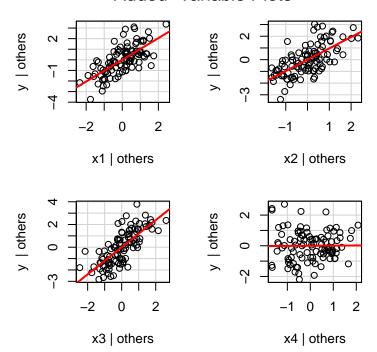
Added Vairiable Plots provide a graphical approach to identifying how much added predictive value a specific variable will give you. In order to generate an Added Variable Plot, we need to perform two additional regressions.

```
tmp <- data_frame(x1 = rnorm(100),</pre>
                  x2 = rnorm(100),
                  x3 = rnorm(100),
                  x4 = rnorm(100),
                  y = x1 + x2 + x3 + rnorm(100)
# full model
full_model \leftarrow lm(y \sim x1 + x2 + x3 + x4, data = tmp)
tidy(full_model)
##
            term
                     estimate std.error
                                          statistic
                                                          p.value
## 1 (Intercept) -0.029346033 0.1031488 -0.28450192 7.766450e-01
              x1 1.025008651 0.1115059 9.19241269 8.798286e-15
## 3
              x2 0.966155517 0.1146042 8.43036674 3.701227e-13
## 4
              x3 1.192778608 0.1097284 10.87028332 2.315127e-18
## 5
              x4 0.009432959 0.1137804 0.08290493 9.341016e-01
# model without x1
no_x1 <- update(full_model, . ~ . - x1) %>%
  augment()
no_x1$x1 <- tmp$x1 # put back into the data_frame, but not into the model
# now regress x1 onto y conditioning on the other variables
ggplot(data = no_x1, aes(x = x1, y = .resid)) +
  geom_point() +
  geom_smooth(method = 'lm', color = 'red')
```



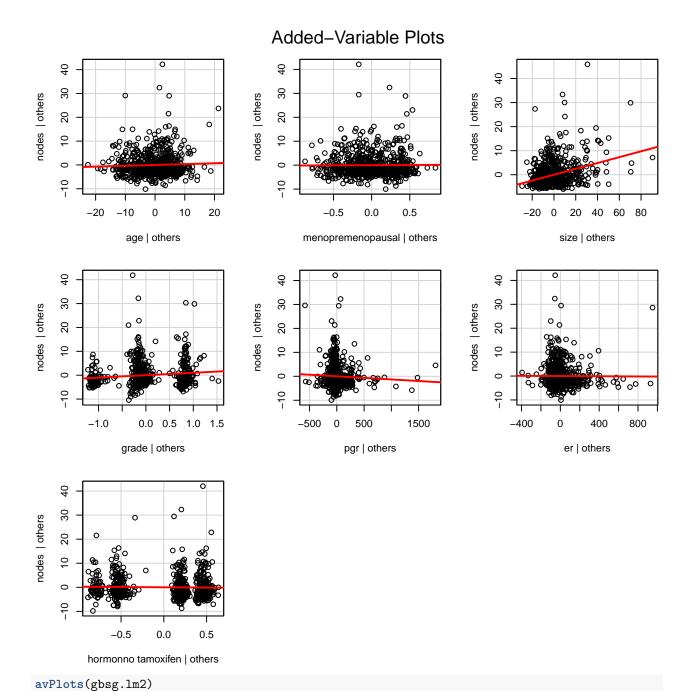
avPlots(full\_model)

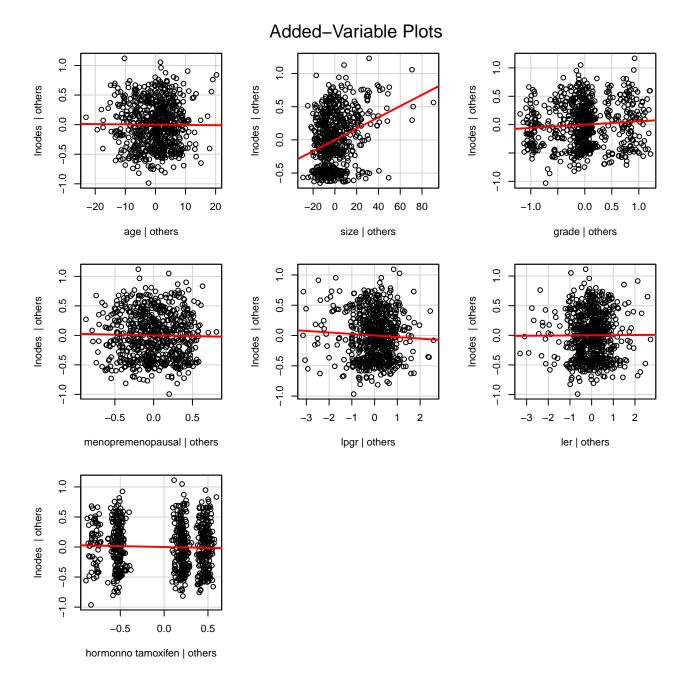
# Added-Variable Plots



Now lets take a look at all of the predictors in our model:

# added variable plots
avPlots(gbsg.lm)





#### Homework

Choose the best model for 'nodes' in the GBSG dataset (or log nodes), checking all model assumptions. A good place to start is with the full model we began with in Discussion 3. Be sure to take a look at the rubric associated with this for specific things I will be looking for. Submit a link to a gist with your code. All figures and tables you wish to include should be generated by your code (i.e. you don't need to include any images – I will run your code and generate any figures you wish to include). All comments and rationale for your final model should be included in the code.