Fixed point Representation

$$X = \pm \left(d_1 d_2 - - d_{k-1} \cdot d_k - - d_n \right) \beta$$

Fixed points or
fleating points are
how numbers are
stored/represented in
a computer

Example

$$\chi = +(10.1)_2$$
 $\chi = -(123.12)_{10}$

Evaluating fixed point numbers in base 10:

$$(10.1)_{2} \rightarrow 1 \times 2^{1} + 0 \times 2^{\circ} + 1 \times 2^{-1}$$

$$= 2 + 0 + \frac{1}{2}$$

$$= (2.5)_{10}$$

Where β , di, $e \in \mathbb{Z} \rightarrow integers$

 $0 \le di \le \beta-1$

emin Le E emax

Evaluating flating point numbers in base to

Examples

Conventions:

$$M=3$$
 $e max = 2$

$$m=3$$
 e max = 2
 \Rightarrow highest possible FP number = $(0.111)_2 \times 2$

(2) Normalized Form:

Example

$$\beta = 2$$
 $emin = -1$

$$(0.1111)_2 \times 2^2$$

$$\beta = 2$$
 emin = -1 convention 1 [Standard form]

$$m=3$$
 $e_{max}-2$

Find the smallest and largest non-negative number

: Total possible # that can be represented = 4 x 4 = 16

Smallest #
$$(0.100)\times2^{-1}$$

$$= (1\times2^{-1})\times2^{-1}$$

$$= \frac{1}{4}$$

$$\frac{|\text{orgest } \#}{(0\cdot 1\ 11)_2} \times 2$$

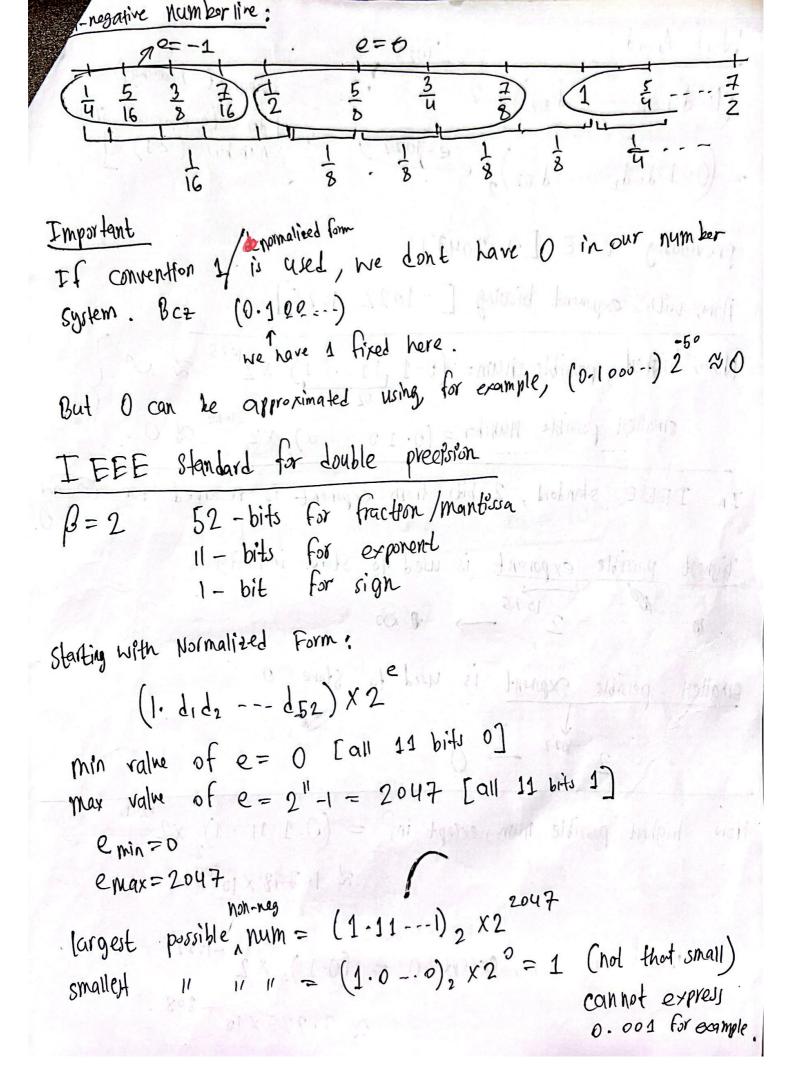
$$= (1\times 2^{-1} + 1\times 2^{-2} + 1\times 2^{-3}) \times 2^2$$

$$= (\frac{1}{2} + \frac{1}{4} + \frac{1}{3}) \times 2^2$$

$$= \frac{2}{4}$$

Considering sign bit Smallest possible # = - = smallest non-negative number = $(0.100) \times 2^{-1} = \frac{1}{4}$ $|1| = (0.101) \times 2^{-1} = (\frac{1}{4} + \frac{1}{8}) \times 2^{-1} = \frac{5}{16}$ 2hd 11 11 341 11 yt 11 11 1 5 3 7 16 NOT SURVEY LID SUSTAINS Equally spaced $\frac{5}{16} - \frac{1}{9} = \frac{3}{8} - \frac{5}{16} = \frac{7}{16} - \frac{3}{8} = \frac{1}{16}$ [exponent constant = equally 10=0 $(0.100) \times 2^{\circ} = \frac{1}{2}$ $(0.101) \times 2^{\circ} = \frac{5}{8}$ $(0.100) \times 2^{1} = 1$ 0 = 21 $(0.100) \times 2^2 = 2$

(0.111) x 22 = 3



Work Around (1. d, d2 --- d 62), 2 exporent biasing. [done to represent small = (0.1 d.d2 -.. d 52), e(e-1022 number (<1)] previously e E [0, 2047] Now, with exponent biasing [-1022, 1025] Now, highert possible num= (0.1,11...1) x 2¹⁰²⁵ $\approx \infty$ smallest passible number = (0.10-0) x2⁻¹⁰²² ≈ 0 In IEEE standard, 2 bits from expenent is reserved for 00 and Highest possible exporent is used to store infinity 2 1025 -> 100 smallest possible exponent is used to store o $2 \xrightarrow{-p^{2}2} \longrightarrow 0$

Now, highest possible num, except inf = (0.1 11--1), x2 1024 ≈ 1.798 × 10308

lowest 11 11, except 0 = (0-1), x2 × 2.225×10 -308.