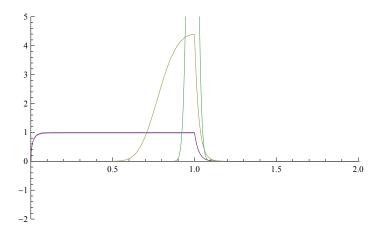
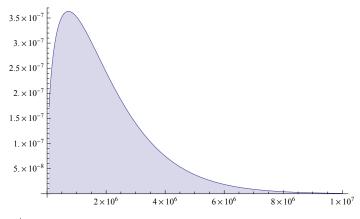
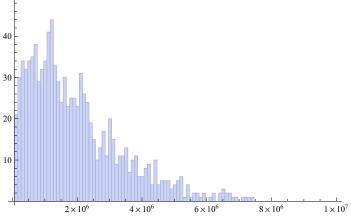
```
(* Here we simulate how many collisions
  are necessary to slow down a neutron on average *)
(* MassA: Mass number *)
alph[MassA ] := N[((MassA-1)/(MassA+1))^2];
(* Ef: energy after collision; Ei: original energy *)
(* simple scattering off an infinitely heavy nucleus at rest *)
Ef[Ei , a ] := RandomReal[{a * Ei, Ei}];
(* scattering kernel for a proton gas at temperature T *)
(* free atom scattering cross section for hydrogen *)
k = (8.6173324 * 10^{-5}); (* eV/K *)
T = 293; (* K *)
sigmaHfree = 1;
(* Duderstadt page 53 *)
ProtonKernel[Ei_, Ef_] := (sigmaHfree / Ei) *
        If [Ei \ge Ef, Erf[Sqrt[Ef/(k*T)]], Exp[(Ei-Ef)/(k*T)]*Erf[Sqrt[Ei/(k*T)]];
sigmaNfree = 1;
thet[MassA] := (MassA + 1) / (2 * Sqrt[MassA]);
ro[MassA ] := (MassA - 1) / (2 * Sqrt[MassA]);
f[Ei , Ef , MassA ] := sigmaNfree * (thet[MassA]) ^2 / (2 * Ei) * 1 *
        ((Erf[thet[MassA] * Sqrt[Ei / (k * T)] - ro[MassA] * Sqrt[Ef / (k * T)]] -
                  Erf[thet[MassA] * Sqrt[Ei / (k * T)] + ro[MassA] * Sqrt[Ef / (k * T)]]) +
             (Erf[thet[MassA] * Sqrt[Ef / (k * T)] - ro[MassA] * Sqrt[Ei / (k * T)]] +
                  Erf[thet[MassA] * Sqrt[Ef / (k * T)] + ro[MassA] * Sqrt[Ei / (k * T)]]));
(* Duderstadt page 388 *)
NuklideKernel[Ei , Ef , MassA ] :=
      If[Ei < Ef, sigmaNfree * (thet[MassA])^2 / (2 * Ei) * Exp[-(Ef - Ei) / (k * T)] * E
           ((Erf[thet[MassA] * Sqrt[Ei / (k * T)] - ro[MassA] * Sqrt[Ef / (k * T)]] +
                    Erf[thet[MassA] * Sqrt[Ei / (k * T)] + ro[MassA] * Sqrt[Ef / (k * T)]]) +
                (\texttt{Erf[thet[MassA]} * \texttt{Sqrt[Ef} / (k * T)] - \texttt{ro[MassA]} * \texttt{Sqrt[Ei} / (k * T)]] -
                    Erf[thet[MassA] * Sqrt[Ef / (k * T)] +
                          ro[MassA] * Sqrt[Ei / (k * T)]])), f[Ei, Ef, MassA]];
Plot[{0.98 * ProtonKernel[1, x], NuklideKernel[1, x, 1], NuklideKernel[1, x, 16],
     NuklideKernel[1, x, 235]}, \{x, 0, 10\}, PlotRange \rightarrow \{\{0, 2\}, \{-2, 5\}\}\}
```



```
(* prompt U235 fission spectrum *)
Nrm = 986229; (* normalized to 1 between 0.5 and 10 MeV *)
s235U[en] := 0.453 * Exp[-1.036 * en / 10^6] * Sinh[Sqrt[2.29 * en / 10^6]] / Nrm;
s235UP = ProbabilityDistribution[s235U[x], {x, 64700, 10 * 10^6}];
dis = RandomVariate[s235UP, 1000];
```

 ${\tt Plot[Evaluate[PDF[s235UP, x]], \{x, 0, 10*10^6\}, Filling \rightarrow Axis]}$ Histogram[dis, {64700, 10 \* 10^6, 100000}]





MyProb = ProbabilityDistribution[NuklideKernel[100, x, 235], {x, 1, 10 000}]; SlowMeDownNext = 1.0;

```
(* NGet235 is an approximaion to the computationally expensive
 solution of: NSolve[(f[Estart,Eff,kern]==0.1*f[Estart,Estart,kern]) &&
     (0.01*Estart<Eff<Estart), Eff, Reals, WorkingPrecision→1] *)
NGet235[Es , ke ] := Module[{j, soli},
   For [j = 1, j < 100, soli = f[Es, Es * (1 - j * 0.01), ke];
    If[soli < 0.01 * f[Es, Es, ke], Break[]];</pre>
    j++1;
   Es * (1 - j * 0.01)
  ];
SlowMeDown[Estart , kern ] := Module[{tup, sol, xk, Eff},
   If[kern = 1,
    MyProb = ProbabilityDistribution[NuklideKernel[Estart, x, kern],
       \{x, Max[0.0025, Estart/1000], If[Estart > 64700, Estart, 5 * Estart]\}];
    SlowMeDownNext = RandomVariate[MyProb];
    Clear[sol, xk, Eff, MyProb];
   ];
   If[kern > 200,
    (*
    sol=NSolve[(f[Estart,Eff,kern]==0.01*f[Estart,Estart,kern]) &&
          (0.0<Eff<Estart), Eff, Reals][[1]][[1]];</pre>
    xk=Eff/.sol;
    *)
    xk = NGet235[Estart, kern];
    MyProb = ProbabilityDistribution[NuklideKernel[Estart, x, kern] ,
       \{x, Max[0.0025, xk], If[Estart > 64700, Estart, 1.1 * Estart]\}\};
    SlowMeDownNext = RandomVariate[MyProb];
    (*SlowMeDownNext=RandomVariate[ProbabilityDistribution[NuklideKernel[Estart,
          x,kern] ,{x,Max[0.0025,xk],If[Estart>64700,Estart,1.1*Estart]}]];*)
    Clear[sol, xk, Eff, MyProb];
   ];
  ];
(* we have to catch Mathematica underflow issues here,
therefore above 64keV only downscattering *)
(* SetDirectory["C:\\MathematicWork\\endf\\"]; *)
SetDirectory["C:\\Users\\Documents\\n-ENDF-VII0.endf\\endf-sigmaPlot\\"];
H1Elastic = Import["H-1-elastic.txt", "csv"];
U235Total = Import["U-235-total.txt", "csv"];
U235Elastic = Import["U-235-elastic.txt", "csv"];
U235Gamma = Import["U-235-gamma.txt", "csv"];
U235Fission = Import["U-235-fission.txt", "csv"];
nh1e = Length[H1Elastic];
nu235t = Length[U235Total];
```

```
4 NeutronSlowDownSimulation.nb
       nu235e = Length[U235Elastic];
            j++;];
          lis
```

```
nu235g = Length [U235Gamma];
nu235f = Length[U235Fission];
CleanUp[data_] := Module[{i = Length[data], j, x1, x2, y2, lis},
   lis = data;
   For [j = 2, j < i,
    x1 = lis[[j]][[1]];
    x2 = lis[[j+1]][[1]];
    y2 = lis[[j+1]][[2]];
    If [x1 = x2, lis = ReplacePart[lis, (j+1) \rightarrow \{x2+0.0001, y2\}];];
  ];
U235Totalc = CleanUp[U235Total];
U235Elasticc = CleanUp[U235Elastic];
U235Gammac = CleanUp[U235Gamma];
U235Fissionc = CleanUp[U235Fission];
ihle = Interpolation[H1Elastic[[2;; nh1e]], InterpolationOrder → 0];
iu235t = Interpolation[U235Totalc[[2 ;; nu235t]], InterpolationOrder → 0];
iu235e = Interpolation[U235Elasticc[[2 ;; nu235e]], InterpolationOrder → 0];
iu235g = Interpolation[U235Gammac[[2 ;; nu235g]], InterpolationOrder \rightarrow 0];
iu235f = Interpolation[U235Fissionc[[2 ;; nu235f]], InterpolationOrder → 0];
nH = 1; nU = 0.1;
MYbinstore = HistogramList[{0}, {0.01, 10, 0.01}][[2]];
MYbins = HistogramList[{0}, {0.01, 10, 0.01}][[1]];
Print[{Length[MYbins], Length[MYbinstore]}];
SH[x] := nH * ihle[x]; SU[x] := nU * iu235f[x];
xss = {};
For [k = 1, k \le Length[MYbins],
  AppendTo[xss, SH[MYbins[[k]]] + SU[MYbins[[k]]]]; k++];
\texttt{ListLogLogPlot[xss, PlotRange} \rightarrow \{\{1,\,1000\},\,\{10,\,200\}\}\,,\,\texttt{Joined} \rightarrow \texttt{True}]
```

```
{1000, 999}
```

```
200 г
150
100
70
50
30
20
15
EventList[runs ] := Module[
   {Estart, Enext, tuppel, ti, slows, SigmaH, SigmaU, rs, r1, r2, r3, hit, x1, x2},
   Estart = RandomVariate[s235UP]; tuppel = {Estart};
   Do[
     (* Print[Estart]; *)
     (* determine total interaction frequencies *)
     SigmaH = nH * ih1e[Estart]; SigmaU = nU * iu235t[Estart];
     rs = RandomReal[];
     (* interaction with hydrogen *)
     If[rs \le SigmaH / (SigmaH + SigmaU) , rs = 1, rs = 2];
     (* interaction with uranium *)
     If[rs == 1, SlowMeDown[Estart, 1]; Enext = SlowMeDownNext;];
     If[rs == 2, rs = RandomReal[];
      r1 = iu235e[Estart]; r2 = iu235g[Estart]; r3 = iu235f[Estart];
      If [rs \le r1 / (r1 + r2 + r3), (*Print[{"235 :",Estart}];*)
       SlowMeDown[Estart, 235]; Enext = SlowMeDownNext;];
      If [rs \le r2 / (r1 + r2 + r3) \& rs > r1 / (r1 + r2 + r3) , Enext = 0;];
      If [rs \ge r3 / (r1 + r2 + r3) , Enext = 0;];
     ];
     (* Print[{Estart,Enext,rs}]; *)
    Estart = N[Enext, 4];
     If[Estart > 0, AppendTo[tuppel, Enext],
      ti = Drop[tuppel, -1]; Clear[tuppel]; tuppel = ti;];
    Clear[rs, r1, r2, r3, SigmaH, SigmaU, Enext];
     If[Estart \le 0.0025, Break[]],
     {runs}];
   (* MYbinstore=HistogramList[tuppel, {0,10000,1}][[2]];*)
   Print[{Length[tuppel], tuppel}];
   For [r1 = 1, r1 \le Length[MYbins] - 1,
    x1 = MYbins[[r1]]; x2 = MYbins[[r1+1]];
    For[r2 = 1, r2 ≤ Length[tuppel],
      If [tuppel[[r2]] \geq x1 \&\& tuppel[[r2]] < x2,
       MYbinstore[[r1]] = MYbinstore[[r1]] + 1; Break[];];
```

```
r2++];
     Clear[x1, x2];
     r1++];
   Clear[Estart, tuppel];
  ];
$HistoryLength = 0;
Off[General::unfl];
Off[CompiledFunction::cfexe];
Off[Refine::fas];
Off[CompiledFunction::cfse];
N[NuklideKernel[10^6, 1.99999999 * 10^1, 235], 3]
(*
SlowMeDown[0.003,235];Print[SlowMeDownNext];
SlowMeDown[2.0*10^6,235];Print[SlowMeDownNext];
*)
\{iu235g[0.5], iu235f[0.5], iu235e[0.5], nH*ih1e[0.5], nU*iu235t[0.5]\}
0.
{9.45794, 78.3446, 13.0291, 20.2988, 9.76164}
For[h = 1, h < 100 000, EventList[1000]; ClearSystemCache[];</pre>
  If[FractionalPart[(h/1)] == 0, Print[{h, Total[MYbinstore]}];]; h++];
\{8, \{2.73921 \times 10^6, 1.19683 \times 10^6, 791161., 544118., 261710., 174538., 206533., 135854.\}\}
{1, 0}
{0, {}}
{2, 0}
\{1, \{1.68104 \times 10^6\}\}
{3, 0}
\{8, \{1.71032 \times 10^6, 1.23926 \times 10^6, 926121., 754196., 218315., 60510.8, 30759.9, 54849.9\}\}
{4,0}
\{21, \{1.22563 \times 10^6, 654312., 565810., 438695., 320290., \}
  236 856., 211 121., 110 853., 183 846., 246 377., 204 975., 167 046., 248 876.,
  87111.4, 104097., 132036., 228573., 146492., 213288., 128590., 208066.}}
{5, 0}
{1, {583305.}}
{6, 0}
\{1, \{7.18932 \times 10^6\}\}
{7, 0}
```

```
{3, {713684., 476581., 466780.}}
{8, 0}
{1, {388837.}}
{9, 0}
\{28, \{1.06423 \times 10^6, 574704., 537961., 461541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 110056., 198993., 285945., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 314541., 53695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695., 31695.,
     77 678., 13 979.7, 26 978.3, 50 821.9, 126176., 114 103., 11 942.6, 46 982.6, 102 881., 158 234.,
     175 885., 177 917., 54 839.4, 121 818., 192 262., 61 378.2, 48 327.8, 101 054., 135 225.}
{10, 0}
\{1, \{2.94838 \times 10^6\}\}
{11, 0}
{0, {}}
{12, 0}
\{1, \{3.21436 \times 10^6\}\}
{13, 0}
\{26, \{3.31953 \times 10^6, 466655., 155344., 158668., 79392.1, 156734., 139197., 179767., \}
     138 131., 21 516.2, 50 054.7, 115 882., 198 783., 201 417., 307 791., 239 870., 84 483.8,
     111 828., 140 727., 92 077.6, 75 541.3, 66 030.4, 102 941., 129 677., 191 964., 177 042.}
{14, 0}
{2, {635425., 614713.}}
{15, 0}
{0, {}}
{16, 0}
{11, {918368., 65242.1, 88066.4, 89106.2,
     110 933., 103 488., 89 046.5, 54 731.1, 86 469.9, 103 228., 49 605.4}}
{17, 0}
\{24, \{2.2917 \times 10^6, 1.52975 \times 10^6, 1.02624 \times 10^6, 350907., 395370., 454875., 554896., 454875.\}
     508 899., 557 937., 688 537., 88 436.4, 89 640.6, 148 663., 231 705., 162 652., 24 117.6,
     68133.7, 6507.09, 13169.8, 3784.52, 25051.6, 83078.7, 121507., 28834.8}
\{6, \{2.70143 \times 10^6, 2.053 \times 10^6, 712586., 691065., 511925., 236752.\}\}
{19, 0}
\{8, \{1.35506 \times 10^6, 995112., 448629., 363184., 266638., 241369., 62253.7, 48504.3\}\}
{20, 0}
\{2.5, \{2.73127 \times 10^6, 1.92437 \times 10^6, 1.97002 \times 10^6, 1.43923 \times 10^6, 305970., 73453.5, 107047., \}
     56629.1, 156132., 202443., 139376., 63390.7, 103928., 184289., 239822., 235255.,
     169790., 211704., 317360., 101145., 183994., 89655.4, 165726., 5399.87, 19823.6}
{21, 0}
```

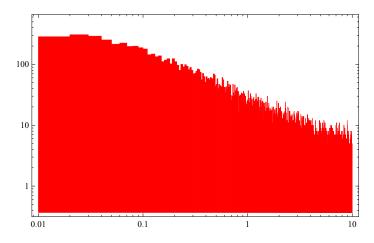
```
\{26, \{1.04837 \times 10^6, 1.17978 \times 10^6, 1.2811 \times 10^6, 151210., 161462., 187320., 181950., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 120297., 12
               50 301.6, 65 984.4, 121 584., 159 645., 220 146., 226 931., 217 022., 10 372.9, 18 077.5,
               64619.9, 26170.4, 80546., 109100., 190210., 187035., 251857., 319935., 259167.}
 {22, 0}
 \{4, \{2.12917 \times 10^6, 1.84352 \times 10^6, 1.44631 \times 10^6, 302921.\}\}
  {23, 0}
$Aborted
```

## Total[MYbinstore]

14 609

## data = {0};

Histogram[data, {MYbins}, MYbinstore &, Axes → True,  $Ticks \rightarrow Automatic$ ,  $FrameTicks \rightarrow Automatic$ ,  $Frame \rightarrow True$ , ScalingFunctions → {"Log", "Log"}, ChartStyle → {Red}]



Export["SlowMeDown05-13aData001.dat", {MYbins, MYbinstore}, "Table"]

SlowMeDown05-13aData001.dat