

Stats 10 Lab 3 Submission
Name: Enmin Zhou
UID: 104756697

Exercise 1

1) a)

```
> soil<-read.table("http://www.stat.ucla.edu/~nchristo/statistics_c173_c273/soil_complete.txt",  
header=TRUE)  
> linear_model <- lm(soil$lead ~ soil$zinc)  
> summary(linear_model)
```

Call:

```
lm(formula = soil$lead ~ soil$zinc)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-79.853	-12.945	-1.646	15.339	104.200

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	17.367688	4.344268	3.998	9.92e-05 ***
soil\$zinc	0.289523	0.007296	39.681	< 2e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

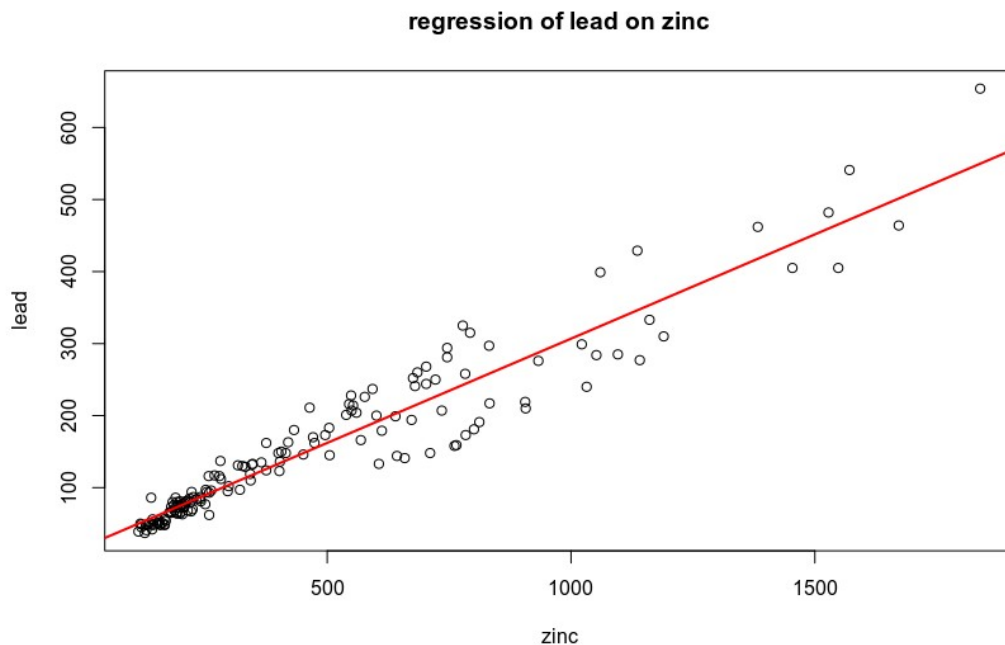
Residual standard error: 33.24 on 153 degrees of freedom

Multiple R-squared: 0.9114, Adjusted R-squared: 0.9109

F-statistic: 1575 on 1 and 153 DF, p-value: < 2.2e-16

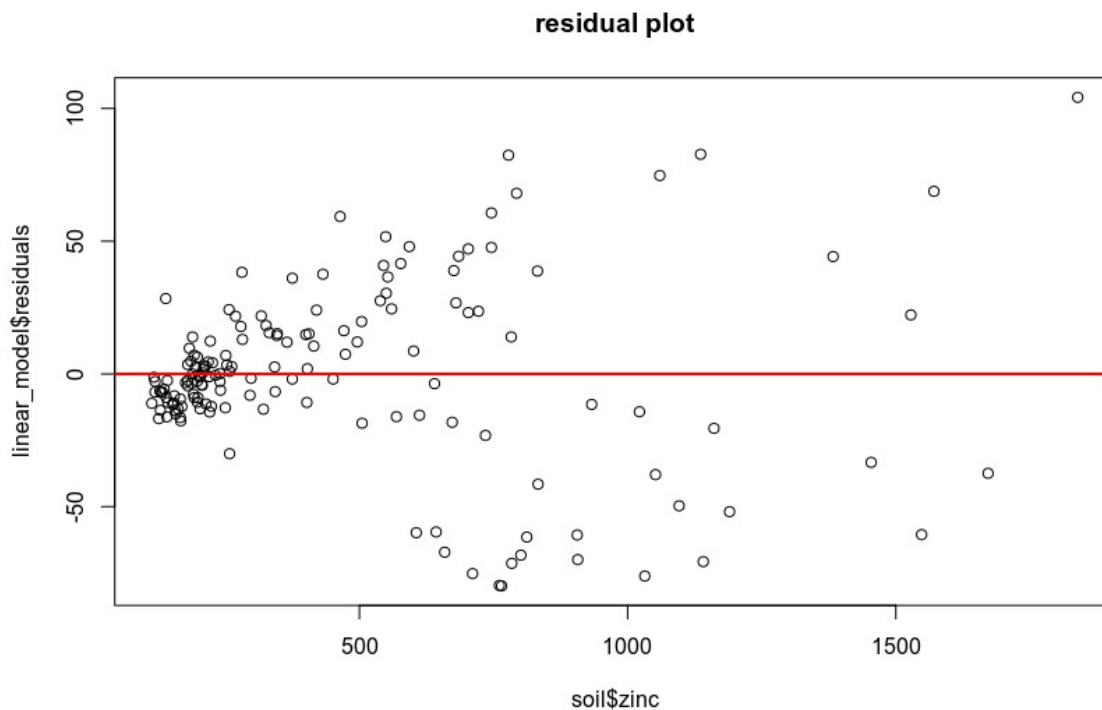
b)

```
> plot(soil$lead ~ soil$zinc, xlab="zinc", ylab="lead", main="regression of lead on zinc")  
> abline(linear_model, col="red", lwd=2)
```



c)

```
> plot(linear_model$residuals ~ soil$zinc, main="residual plot")
> abline(a=0, b=0,col='red',lwd=2)
```



d)

$\text{lead} = 17.367688 + 0.289523 \cdot \text{zinc}$

e)

$17.36788 + 0.289523 \cdot 1000 = 306.8909 \text{ ppm}$

f)

$0.289523 \cdot 100 = 28.9523 \text{ ppm higher}$

g)

0.91, it means that 91 percent of the change in the lead level can be explained by the zinc level.

h)

Linearity and symmetry assumptions are satisfied. The equal variance assumption is violated.

Exercise 2

2) a)

```
> linear_model2 <- lm(ice$Extent ~ ice$Date)
> summary(linear_model2)
```

Call:

```
lm(formula = ice$Extent ~ ice$Date)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-9.445	-5.439	1.442	5.599	7.564

Coefficients:

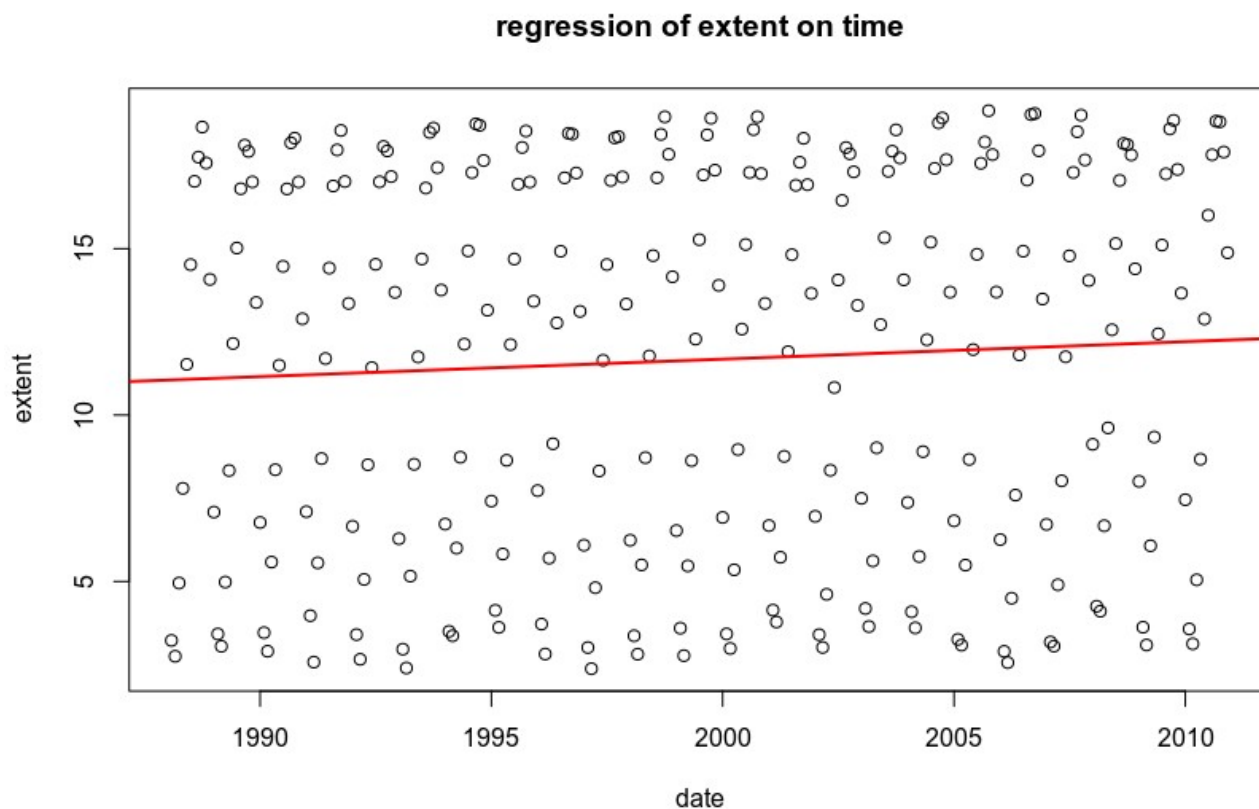
	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	1.011e+01	1.558e+00	6.486	4.11e-10 ***
ice\$Date	1.438e-04	1.411e-04	1.019	0.309

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 5.654 on 273 degrees of freedom
Multiple R-squared: 0.003787, Adjusted R-squared: 0.0001377
F-statistic: 1.038 on 1 and 273 DF, p-value: 0.3093

b)

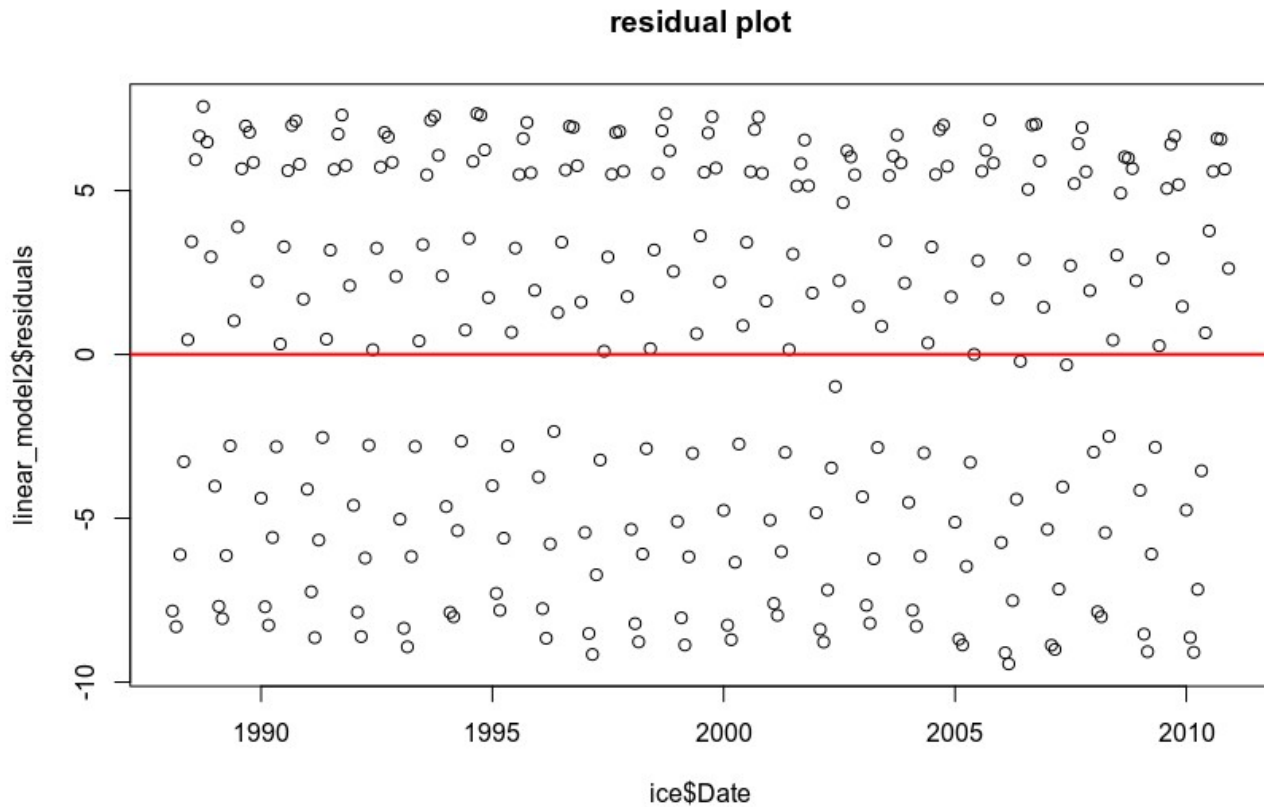
```
> plot(ice$Extent ~ ice$Date, xlab="date", ylab="extent", main="regression of extent on time")  
> abline(linear_model2, col="red", lwd=2)
```



No.

c)

```
> plot(linear_model2$residuals ~ ice$Date, main="residual plot")  
> abline(a=0, b=0,col='red',lwd=2)
```



The linearity is violated. The symmetry and equal variance assumption are satisfied.

Exercise 3

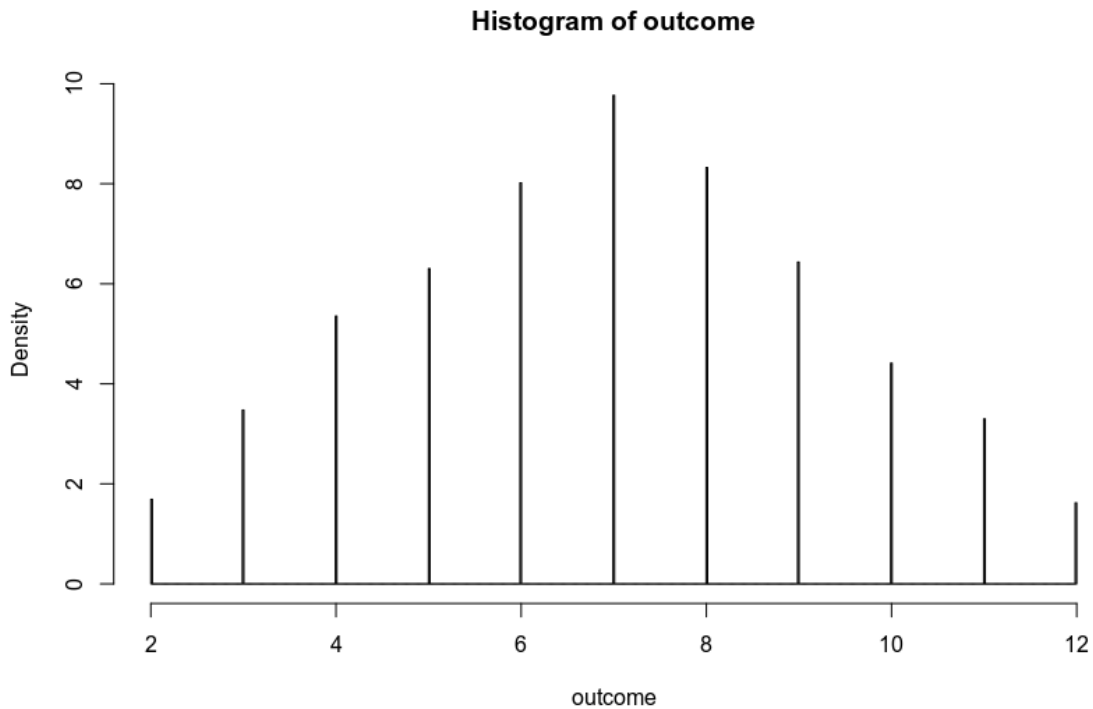
3) a)

double: $\frac{1}{6} \cdot \frac{1}{6} \cdot 3 \cdot 2 + \frac{1}{6} \cdot \frac{1}{6} \cdot 2 = \frac{2}{9}$

lose: $\frac{1}{6} \cdot \frac{1}{6} \cdot 2 + \frac{1}{6} \cdot \frac{1}{6} \cdot 2 + \frac{1}{6} \cdot \frac{1}{6} \cdot 2 = \frac{1}{6}$

b)

```
> set.seed(123)
> numbers = 1:6
> rand_dice = replicate(5000, sample(numbers, 2, replace = TRUE))
> outcome <- colSums(rand_dice)
> histogram(outcome)
```



c)

```
>> t<-table(outcome)
> double <- (t[6] + t[10])/5000
> lose <- (t[1]+t[2]+t[11])/5000
Double: 0.2226, Lose:0.1156
```

d)

These two events are disjoint since Adam cannot get (7,11) and (2,3,12) at the same time.

e)

$P(\text{double}) = 2/9$, $P(\text{lose}) = 1/6$, $P(\text{double} \& \text{lose}) = 0$. Therefore they are not independent events.

Exercise 4

4)a)

$p = 0.4$, $n = 365$

b)

mean: $np = 146$, standard deviation: $\sqrt{np(1-p)} = 9.36$

c)

```
> dbinom(145, size = 365, prob = 0.4)
[1] 0.04239996
```

Probability is 0.04239996

d)

```
> pbinom(175, size = 365, prob = 0.4) - pbinom(125, size = 365, prob = 0.4)
[1] 0.98543
```

Probability is 0.98543

e)

```
> 1-pnorm(230, mean=200, sd=20)
[1] 0.0668072
```

Probability is 0.0668702