# **LegBuilder Documentation**

Release 1.0.0

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September 08, 2015

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CONTENTS 1

### **DISCRETIZATION MODULE**

Discretize the continuous hybridization function into a discretized model(DiscModel). checking method is also provided.

 $\textbf{class} \ \texttt{discretization.DiscHandler} \ (\textit{token}, Lambda, N, D=[-1.0, 1.0], \ Gap=[0.0, 0.0])$ 

Bases: object

Handler for discretization of hybridization function.

token: the token of this handler, which is a string for saving/loading data.

Lambda: scaling factor.

N: the maximum discretization index.

**D:** the band range, [-1,1] for default.

**z:** number of z.

Gap: the gap range.

**check\_mapping\_eval** (*rhofunc*, *Efunc*, *Tfunc*, *scalefunc*, *sgn*, *Nx*=1000, *Nw*=200, *smearing*=0.02) check the mapping quality by eigenvalues - the multiple-band Green's function version.

**rhofunc:** the original hybridization function.

**Efunc/Tfunc:** the representative energy/hopping term as a function of x.

scalefunc: scale function.

sgn: the branch.

**Nx/Nw:** number of samples in x(index)- and w(frequency)- space.

smearing: smearing constant.

**check\_mapping\_pauli** (*rhofunc*, *Efunc*, *Tfunc*, *scalefunc*, *sgn*, *Nx*=1000, *Nw*=200, *smearing*=0.02) check the mapping quality by Pauli decomposition - only 2-band Green's function is allowed.

**rhofunc:** the original hybridization function.

**Efunc/Tfunc:** the representative energy/hopping term as a function of x.

scalefunc: scale function.

sgn: the branch.

Nx/Nw: number of samples in x(index)- and w(frequency)- space.

smearing: smearing constant.

get\_Efunc (Efuncs)

Get the Efunc for multi-band system.

**Efuncs:** energy functions for individual bands. **return:** a function of representative energy E(x). get\_Tfunc (wxfuncs, efuncs) Get the hopping term for multi-band system. wxfuncs: functions of weights for individual bands, t=sqrt(w) in 1-band system and this is for multi-band. **efuncs:** functions of representative energies e(x) for each band. **return:** a function of representative hopping terms T(x). get\_discrete\_model (funcs, z=1.0, append=False) get a discrete set of models for specific zs. funcs: a super tuple -> (scalefunc\_positive, Efunc\_positive, Tfunc\_positive), (scalefunc\_negative, Efunc\_negative, Tfunc\_negative, Tfunc\_negat z: twisting parameters, scalar or 1D array. append: append model informations instead of generating one. return: a discrentized model - DiscModel instance. get\_efunc\_singleband (scalefunc, sgn, bandindex=0, Nx=500000, rk=False) get representative Energy function e(x) for specific band and branch -the python version. **scalefunc:** a function of discretization points sepsilon(x). **sgn:** the positive branch if sgn>0, else the negative one. bandindex: the band index. Nx: the number of samples in x-space for integration. rk: use Ronge-Kutta if True(in this version, it's better to set False). **return:** a function of representative energy e(x) for specific band and branch. get\_wxfunc\_singleband(scalefunc, sgn, bandindex=0) Get weight function w(x), which is equal to int^e(x)\_e(x+1) d(w,bandindex) dw scalefunc: the function for scale ticks. **sgn:** specify the branch. **bandindex:** the bandindex. return: weight of hybridization function w(x) at interval epsilon(x)~epsilon(x+1)  $quick_map(tick_type='log', Nx=500000)$ Perform quick mapping(All in one suit!) for nband x nband hybridization matrix. **tick\_type:** the type of tick, *log-*>logarithmic tick, *sclog-*>logarithmic ticks suited for superconductor. **Nx:** the number of samples for integration over rho(epsilon(x)). return: a super tuple of functions -> (scalefunc\_positive, Efunc\_positive, Tfunc\_positive), (scalefunc\_negative, Efunc\_negative set\_rhofunc(rhofunc, Nw=50001)

unique\_token

return a unique token, for saving/loading datas.

**rhofunc:** the hybridization function. **Nw:** the number of ws for rho(w).

```
class discretization.DiscModel (Elist, Tlist, z=1.0)
     Bases: object
     discrete model.
     Elist/Tlist: a list of on-site energies and hopping terms. The shape is (2N,nz,nband,nband)
     z: the twisting parameters.
     N
           number of particles for each branch(positive or negative).
     nband
           number of bands.
     nz
           number of twisting parameters.
discretization.get_scalefunc_log(Lambda, D, Gap, sgn)
     get logarithmic scale tick function. epsilon(x)=Lambda^(2-x)
     Lambda: scaling factor.
     D/Gap: the bandwidth/Gap range.
     sgn: return the scale function for the positive branch if sgn>0, else the negative one.
     return: a scale function epsilon(x).
discretization.get_scalefunc_sclog(Lambda, D, Gap, sgn)
     get logarithmic scale tick function suited for superconductor(logarithmic for normal part).
     Lambda: scaling factor.
     D/Gap: the bandwidth/Gap range.
     sgn: return the scale function for the positive branch if sgn>0, else the negative one.
     return: a scale function epsilon(x).
```

#### CHAINMAPPER MODULE

Map a discretized model into a Chain by the method of (block-)lanczos tridiagonalization. checking method is also provided.

```
class chainmapper.Chain (t0, elist, tlist)
     Bases: object
     NRG chain class.
     t0: the coupling term of the first site and the impurity.
     elist/tlist: a list of on-site energies and coupling terms.
class chainmapper.ChainMapper(prec=3000)
     Bases: object
     A Chain Model Mapper for NRG.
     prec: the precision in mapping process.
     check_spec (chain, dischandler, rhofunc, mode='eval', Nw=500)
           check mapping quality.
           chain: the chain after mapping.
           dischandler: discretization handler.
           rhofunc: hybridization function.
           mode: eval -> check eigenvalues pauli -> check pauli components
           Nw: number of samples in w-space.
     \mathtt{map}\ (model)
           Map discretized model to a chain model using lanczos method.
           model: the discretized model(DiscModel instance).
           return: a Chain object
chainmapper.load_chain(token)
     load a Chain instance from files.
     token: a string as a prefix to store datas of a chain.
     return: a Chain instance.
chainmapper.save_chain (token, chain)
     save a Chain instance to files.
     token: a string as a prefix to store datas of a chain.
```

chain: a chain instance.

## TRIDIAGONALIZE MODULE

Tridiagonalization methods for both scalar(tridiagonalize) and block(tridiagonalize\_qr) versions. Some test functions are also included.

tridiagonalize.check\_tridiagonalize(H0, trid)

check the quality of tridiagonalization.

**H0:** the original hamiltonian.

**trid:** tridiagonalization result, a tuple of (data, offset).

tridiagonalize(A, q, m=None, prec=None, getbasis=False)

Use m steps of the lanczos algorithm starting with q to generate eigenvalues for the sparse symmetric matrix A.

**A:** a sparse symmetric matrix.

**q:** the starting vector.

m: the steps to run.

getbasis: return basis vectors if True.

return: (data, offset, vectorbase)

Use scipy.sparse.diags(res[0],res[1]) to generate a sparse matrix

tridiagonalize\_qr(A, q, m=None, prec=None)

Use m steps of the lanczos algorithm starting with q - the block version with QR decomposition.

Note: we need to specify a two-column starting vectors here (q0,q1) with q0,q1 orthogonal to each other.

**A:** a sparse symmetric matrix.

**q:** the starting othogonal vector q=(q0,q1).

m: the steps to run.

return: (data, offset), the trdiagonal matrix can be generated by scipy.sparse.diags(data, offset).

## **UTILS MODULE**

```
Author: Jinguo Leo Date: 8 September 2014 Description: physics utility library
utils.H2G(h, w, tp='r', geta=0.01, sigma=None)
     Get Green's function g from Hamiltonian h.
     h: an array of hamiltonian.
     w: the energy(frequency).
     tp: the type of Green's function. 'r': retarded Green's function.(default) 'a': advanced Green's function.
           'matsu': finite temperature Green's function.
     geta: smearing factor. default is 1e-2.
     sigma: additional self energy.
     return: a Green's function.
utils.eigh_pauliv_npy (a0, a1, a2, a3)
     eigen values for pauli vectors - numpy version.
     a0/a1/a2/a3: pauli components.
     return: (evals, evecs)
utils.mpconj(A)
     get the conjugate of matrix A(to avoid a bug of gmpy2.mpc.)
     A: the input matrix.
     return: matrix with the same dimension as A
utils.ode_ronge_kutta(func, y0, tlist, **kwargs)
     Integrate use Ronge Kutta method.
     func: the function of (x,y).
     y0: the starting y.
     tlist: a list of t.
     **kwargs: additional arguments for scipy.ode.set_integrator
     return: return integrated array(like cumtrapz).
utils.qr2(A)
     analytically, get the QR decomposition of a matrix.
     A: the matrix.
     return: (Q,R), where QR=A
```

#### utils.s2vec(s)

Transform a 2 x 2 matrix to a 4 dimensional vector, corresponding to s0,sx,sy,sz component.

**s:** the matrix.

#### utils.vec2s(n)

Transform a vector of length 3 or 4 to a pauli matrix.

**n:** a 1-D array of length 3 or 4 to specify the *direction* of spin.

return: 2 x 2 matrix.

#### **CHAPTER**

## **FIVE**

## **HYBRI\_SC MODULE**

Get the hybridization function of a conventional superconductor. wide-band approximation(get\_hybri\_wideband) version and finite-band width(get\_hybri) version are available.

hybri\_sc.get\_hybri(Gap, Gamma, D0=1.0, mu=0.0, eta=1e-10)

D(w) for superconducting surface.

Gap: the Gap value.

Gamma: the overall strength.

**D0:** the band width of normal part.

mu: chemical potential.eta: the smearing factor.

return: hybridization function for superconductor.

hybri\_sc.get\_hybri\_wideband(Gap, Gamma, D=1.0, mu=0.0, eta=1e-10)

D(w) for superconducting surface, taking wide-band approximation.

**Gap:** the Gap value.

**Gamma:** the overall strength.

**D:** the band width.

mu: chemical potential.eta: the smearing factor.

return: hybridization function for superconductor with wideband approximation.

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