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# **LegBuilder Documentation**

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contents

## DISCRETIZATION MODULE

Discretize the continuous hybridization function into a discretized model(DiscModel). checking method is also provided.

**class** discretization.**DiscHandler** (*token, Lambda, N, D=[-1.0, 1.0], Gap=[0.0, 0.0]*)

Bases: `object`

Handler for discretization of hybridization function.

**token:** the token of this handler, which is a string for saving/loading data.

**Lambda:** scaling factor.

**N:** the maximum discretization index.

**D:** the band range, [-1,1] for default.

**z:** number of z.

**Gap:** the gap range.

**check\_mapping2** (*rhofunc, Efunc, Tfunc, scalefunc, sgn, Nx=1000, Nw=200, smearing=0.02*)

check the mapping quality - the multi-band Green's function version.

**rhofunc:** the original hybridization function.

**Efunc/Tfunc:** the representative energy/hopping term as a function of x.

**scalefunc:** scale function.

**sgn:** the branch.

**Nx/Nw:** number of samples in x(index)- and w(frequency)- space.

**smearing:** smearing constant.

**get\_Efunc** (*wxfunc, sgn, bandindex=0, N=100000, rk=False*)

get representative Energy function E(x) -the python version.

**wxfunc:** a function of w(x), which is equal to t(x)^2.

**sgn:** the positive branch if sgn>0, else the negative one.

**bandindex:** the band index.

**N:** the number of samples for integration.

**rk:** use Ronge-Kutta if True(in this version, it's better to set False).

**get\_Efunc2** (*Efuncs, Ufunc*)

Get the Efunc for multi-band system.

**Efuncs:** energy functions for individual bands.

**Ufunc:** U function.

**get\_Tfunc2** (*wxfuncs*, *Ufunc*)

Get the hopping term for multi-band system.

**wxfuncs:** functions of weights for individual bands,  $t=\sqrt{w}$  in 1-band system and this is for multi-band.

**Ufunc:** U function.

**get\_Ufunc2** (*Efuncs*, *sgn*)

get the U(x) function.

**Efuncs:** the energy functions.

**get\_discrete\_model** (*funcs*, *z=1.0*, *append=False*)

get a discrete set of models for specific zs.

**funcs:** a super tuple -> (scalefunc\_positive, Efunc\_positive, Tfunc\_positive), (scalefunc\_negative, Efunc\_negative, Tfunc\_negative)

**z:** z or a list of zs.

**append:** append scale datas.

**get\_scalefunc\_log** (*sgn*)

get logarithmic scale tick function.  $\epsilon(x)=\Lambda^{(2-x)}$

**sgn:** return the scale function for the positive branch if  $sgn>0$ , else the negative one.

**get\_scalefunc\_sclog** (*sgn*)

get logarithmic scale tick function suited for superconductor(logarithmic for normal part).

**sgn:** return the scale function for the positive branch if  $sgn>0$ , else the negative one.

**get\_wxfunc** (*scalefunc*, *sgn*, *bandindex=0*, *N=10000*)

Get weight function  $w(x)$ , which is equal to  $\int^x e(x) dx$  d(w,bandindex) dw

**scalefunc:** the function for scale ticks.

**sgn:** specify the branch.

**bandindex:** the bandindex.

**N:** the number of samples.

**quick\_map2** (*tick\_type='log'*, *NN=1000000*)

Perform quick mapping(All in one suit!) for 2 x 2 hybridization matrix.

**tick\_type:** the type of tick, *log*->logarithmic tick, *sclog*->logarithmic ticks suited for superconductor.

**NN:** the number of samples for integration over  $\rho(w)$ .

**return:** a super tuple -> (scalefunc\_positive, Efunc\_positive, Tfunc\_positive), (scalefunc\_negative, Efunc\_negative, Tfunc\_negative)

**set\_rhofunc** (*rhofunc*, *NW=50001*)

**rhofunc:** the hybridization function.

**NW:** the number of ws for  $\rho(w)$ .

**unique\_token**

return a unique token, for saving/loading datas.

**class** discretization.**DiscModel** (*Elist*, *Tlist*, *z=1.0*)

Bases: `object`

discrete model.

**Elist/Tlist:** a list of on-site energies and hopping terms. The shape is (2N,nz,nband,nband)

**z:** the twisting parameters.

**N**  
number of particles for each branch(positive or negative).

**nband**  
number of bands.

**nz**  
number of twisting parameters.

## CHAINMAPPER MODULE

Map a discretized model into a Chain by the method of (block-)lanczos tridiagonalization. checking method is also provided.

**class** chainmapper.**Chain** (*t0, elist, tlist*)  
Bases: `object`

NRG chain.

**t0:** the coupling term of the first site and the impurity.

**elist/tlist:** a list of on-site energies and coupling terms.

**class** chainmapper.**ChainMapper** (*prec=3000*)  
Bases: `object`

A Chain Model Mapper for NRG.

**prec:** the precision in mapping process.

**check\_spec** (*chain, dischandler, rhofunc*)  
check mapping quality.

**chain:** the chain after mapping.

**dischandler:** discretization handler.

**rhofunc:** hybridization function.

**map** (*model*)

Map discretized model to a chain model using lanczos method.

**model:** the discretized model(DiscModel instance).

**return:** a Chain object



## TRIDIAGONALIZE MODULE

Tridiagonalization methods for both scalar(`tridiagonalize`) and block(`tridiagonalize_qr`) versions. Some test functions are also included.

`tridiagonalize.check_tridiagonalize` (*H0*, *trid*)  
check the quality of tridiagonalization.

**H0:** the original hamiltonian.

**trid:** tridiagonalization result, a tuple of (data,offset).

`tridiagonalize.tridiagonalize` (*A*, *q*, *m=None*, *prec=None*, *getbasis=False*)

Use *m* steps of the lanczos algorithm starting with *q* to generate eigenvalues for the sparse symmetric matrix *A*.

**A:** a sparse symmetric matrix.

**q:** the starting vector.

**m:** the steps to run.

**getbasis:** return basis vectors if True.

**return:** (data,offset,vectorbase)

Use `scipy.sparse.diags(res[0],res[1])` to generate a sparse matrix

`tridiagonalize.tridiagonalize_qr` (*A*, *q*, *m=None*, *prec=None*)

Use *m* steps of the lanczos algorithm starting with *q* - the block version with QR decomposition.

*Note: we need to specify a two-column starting vectors here (q0,q1) with q0,q1 orthogonal to each other.*

**A:** a sparse symmetric matrix.

**q:** the starting othogonal vector *q*=(*q0*,*q1*).

**m:** the steps to run.

**return:** (data,offset), the trdiagonal matrix can be generated by `scipy.sparse.diags(data,offset)`.

## UTILS MODULE

Author: Jinguo Leo Date : 8 September 2014 Description : physics utility library

`utils.H2G(h, w, tp='r', geta=0.01, sigma=None)`

Get Green's function g from Hamiltonian h.

**h:** an array of hamiltonian.

**w:** the energy(frequency).

**tp:** the type of Green's function. 'r': retarded Green's function.(default) 'a': advanced Green's function.  
'matsu': finite temperature Green's function.

**geta:** smearing factor. default is 1e-2.

**sigma:** additional self energy.

`utils.eigh_pauliv_npy(a0, a1, a2, a3)`

eigen values for pauli vectors - numpy version.

**a0/a1/a2/a3:** pauli components.

`utils.mpconj(A)`

get the conjugate of matrix A(to avoid a bug of gmpy2.mpc.)

**A:** the input matrix.

`utils.ode_ronge_kutta(func, y0, tlist, **kwargs)`

Integrate use Ronge Kutta method.

**func:** the function of (x,y).

**y0:** the starting y.

**tlist:** a list of t.

**\*\*kwargs:** additional arguments for `scipy.ode.set_integrator`

`utils.qr2(A)`

analytically, get the QR decomposition of a matrix.

**A:** the matrix.

`utils.s2vec(s)`

Transform a 2 x 2 matrix to a 4 dimensional vector, corresponding to s0,sx,sy,sz component.

**s:** the matrix.

`utils.vec2s(n)`

Transform a vector of length 3 or 4 to a pauli matrix.

**n:** a 1-D array of length 3 or 4 to specify the *direction* of spin.

## HYBRI\_SC MODULE

Get the hybridization function of a conventional superconductor. wide-band approximation(`get_hybri_wideband`) version and finite-band width(`get_hybri`) version are available.

`hybri_sc.get_hybri` (*Gap*, *Gamma*, *D0=1.0*, *mu=0.0*, *eta=1e-10*)

D(w) for superconducting surface.

**Gap:** the Gap value.

**Gamma:** the overall strength.

**D0:** the band width of normal part.

**mu:** chemical potential.

**eta:** the smearing factor.

`hybri_sc.get_hybri_wideband` (*Gap*, *Gamma*, *D=1.0*, *mu=0.0*, *eta=1e-10*)

D(w) for superconducting surface, taking wide-band approximation.

**Gap:** the Gap value.

**Gamma:** the overall strength.

**D:** the band width.

**mu:** chemical potential.

**eta:** the smearing factor.

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