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Sub- Algorithms Analysis and Design-1 (CSE2631)

Full Marks-10

Date- 16/10/2025 Section-24E1R1 Time- 30 minutes

## CO1-To apply knowledge of computing and mathematics to algorithm, running time, Asymptotic analysis

In the following C function, let n ≥ m
 int gcd(n, m){
 if(n % m == 0)
 return m;
 n = n % m;
 return gcd(m, n);
 }
 How many recursive calls are made by this function?
 (a) Θ(log n)
 (b) Ω(n)
 (c) Θ(log log n)
 (d) Θ(√n)

- 2. The recurrence relation T(1) = 2, T(n) = 3T(n/4) + n has the solution T(n) equal to?
- 3. Consider the following two functions  $g_1(n) = \begin{cases} n^3 & \text{for } 0 \le n < 10,000 \\ n^2 & \text{for } n \ge 10,000 \end{cases}$  and  $g_2(n) = \begin{cases} n & \text{for } 0 \le n < 100 \\ n^3 & \text{for } n > 100 \end{cases}$  Which one of the following is TRUE?
  - (a)  $g_1(n)$  is  $O(g_2(n))$  (b)  $g_1(n)$  is  $O(n^3)$  (c)  $g_2(n)$  is  $O(g_1(n))$  (d)  $g_2(n)$  is O(n)
- 4. Let us consider two algorithms A, and B running on the same machine M. For inputs of size n, algorithm A runs in 8n<sup>2</sup> steps while algorithm B runs in 64nlgn steps. For which values of n does algorithm A beat algorithm B?
- 5. Solve the recurrence  $T(n) = 4T(\lfloor n/2 \rfloor) + \Theta(n)$  using Masters method and provide the asymptotic upper bound for T(n).