Instructor name- Dr. Irshed Hussain

Sub- Algorithms Analysis and Design-1 (CSE2631)

Full Marks-10

Date-13/10/2025 Section-24E1Q2 Time- 30 minutes

## CO1-To apply knowledge of computing and mathematics to algorithm, running time, Asymptotic analysis

- 2. Two alternate packages A and B are available for processing a database having  $10^k$  records. Package A requires  $0.0001n^2$  time units and package B requires 10nlogn time units to process n records. What is the smallest value of k for which package B will be preferred over A?
  - [GATE-2010] 2
- 3. Consider the following two functions  $g_1(n) = \begin{cases} n^3 & \text{for } 0 \le n < 10,000 \\ n^2 & \text{for } n \ge 10,000 \end{cases}$  and  $g_2(n) = \begin{cases} n & \text{for } 0 \le n < 100 \\ n^3 & \text{for } n > 100 \end{cases}$  Which one of the following is TRUE?
  - (a)  $g_1(n)$  is  $O(g_2(n))$  (b)  $g_1(n)$  is  $O(n^3)$  (c)  $g_2(n)$  is  $O(g_1(n))$  (d)  $g_2(n)$  is O(n)
- 4. Suppose T(n) is the worst-case time complexity of an algorithm expressed in terms of the input size n as:  $T(n) = n^3 / 1000 100n^2 100n + 3$ . Find out the value of constants  $c_1 > 0$ ,  $c_2 > 0$ , and  $n_0$  (where  $n_0$  is an instance of n), such that  $T(n) = \Theta(n^3)$ .
- 5. Solve the following recurrence using iteration method and provide the asymptotic upper bound for T(n), where  $T(n) = 2T(n-1) + \Theta(1)$ .