# Homework 3 All-Pairs Shortest Path

Optimization

Parallel Programming 2020

## Algorithm

- Johnson's algorithm
  - $\circ$  O(V<sup>2</sup> log(V) + E)
  - Fast for sparse graph
- Floyd-Warshall
  - o O(V^3)
  - Fast for dense graph
- Blocked Floyd-Warshall

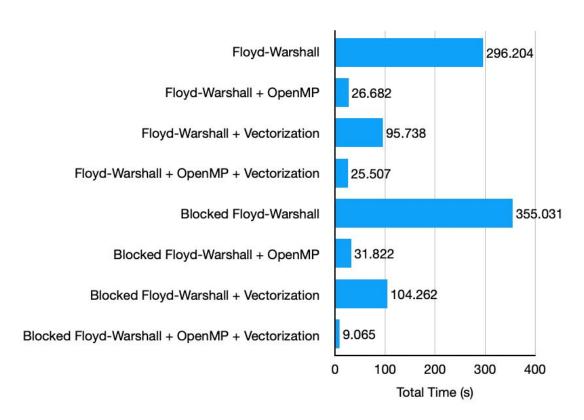
### Parallelization

- Using OpenMP
- Static scheduler

#### Vectorization

```
m128i as, bs, newdist, cs;
for (int k = 0; k < B; k++) {
   for (int i = 0; i < B; i++) {
       as = mm set1 epi32(a[i * pvn + k]);
       for (int i = 0; i < B; i += 4) {
           bs = mm \ lddqu \ si128(( \ m128i \ const*) \ \&b[k * pvn + j]);
           newdist = mm add epi32(as, bs);
           cs = mm \ lddqu \ si128(( m128i \ const*) \ \&c[i * pvn + j]);
           cs = mm min epi32(cs, newdist);
           mm store si128(( m128i*) &c[i * pvn + j], cs);
```

## Blocked Floyd-Warshall



#### I/O

- mmap
- Read all data in one fread()

```
// read the distances to a buffer first
int* buffer = (int*)malloc(m * 3 * sizeof(int));
fread(buffer, sizeof(int), m * 3, file);
// write the distance from buffer to array
#pragma omp parallel for
for (int i = 0; i < m; i++) {
    Dist[buffer[i * 3]][buffer[i * 3 + 1]] = buffer[i * 3 + 2];
}</pre>
```