Chapter 4: Advanced Design and Analysis Techniques

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1 Dynamic Programming

Dynamic programming applies when the subprobelms overlap. We typically apply dynamic programming to *optimization problems*.

When developing a dynamic programming algorithm, we follow a sequence of four steps:

- 1. Characterize the structure of an optimal solution.
- 2. Recursively define the value of an optimal solution
- 3. Compute the value of an optimal solution, typically in a bottom-up fashion.
- ${\bf 4.} \ \ {\bf Construct} \ {\bf an} \ {\bf optimal} \ {\bf solution} \ {\bf from} \ {\bf computed} \ {\bf information}.$

1.1 Rod Cutting

The $rod\ cutting\ problem$ is the following: Given a rod of length n inches and a table of prices p_i according to the length i, determine the maximum revenue r_n obtainable by cutting the rod and selling them.

length i	1	2	3	4	5	6	7	8	9	10
$\mathrm{price}\; p_i$	1	5	8	9	10	17	17	20	24	30