

# OUTLIER ANALYSIS

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# What is an Outlier ?

Data objects which are grossly different from or inconsistent with the remaining set of data are called outliers.

# Applications of Outliers

- Fraud Detection
- Unusual Usage of Credit Cards
- Medical Analysis
- Customized Marketing

# Outlier Mining Problem

- It can be viewed as two Subproblems.
  - (1) Define what data can be considered as inconsistent.
  - (2) Find an efficient method to mine the outliers.

# Methods of Outlier Detection

- Statistical Distribution-Based Outlier Detection
- Distance-Based Outlier Detection
- Density-Based Local Outlier Detection
- Deviation Based Outlier Detection



# Distance Based Outlier Detection

- It was introduced to counter the main limitations imposed by statistical methods
- An object, **O**, in a dataset is a **distance based (DB) outlier** with parameters  $pct$  and  $dmin$ , that is, a *DB( $pct, dmin$ )-outlier*.

# Algorithms

- Index-based algorithm
- Nested-loop algorithm
- Cell-based algorithm
- *N DoT*

## ***N DoT***

- We introduce a term *Nearest Neighbour Factor* (**NNF**) measure the degree of outlieriness of a point.
- If *Nearest Neighbor Factor* of the point w.r.t majority of its neighbor is more than a threshold then the point is declared as a potential outlier.



# Basic Terminologies

- K Nearest Neighbor (knn) Set
- Average knn distance
- Nearest Neighbor Factor

# K Nearest Neighbor (knn) Set

- Let  $D$  be a dataset of and  $x$  be a point in  $D$ .
- For a natural number  $k$  and a distance function  $d$ , a set  $N_{nk}(x) = \{q_1 \in D \mid d(x, q_1) < d(x, q_2), q_2 \in D\}$  is called knn of  $x$  if the following two conditions hold.
  - (1)  $|N_{nk}| > k$  if  $q_2$  is not unique in  $D$  or  $|N_{nk}| = k$  otherwise.
  - (2)  $|N_{nk} \setminus N_{q_2}| = k - 1$ , where  $N_{q_2}$  is the set of all  $q_2$  point(s).

# Average knn Distance

- Let  $NN_k$  be the knn of a point  $x$  in dataset  $D$ . Average knn distance of  $x$  is the average of distances between  $x$  and  $q$  belongs to  $NN_k$ , i.e.,
- $$\text{Average knn distance}(x) = \frac{\sum_{q \in NN_k} d(x, q)}{|NN_k|}$$
- Average knn distance of a point  $x$  is the average of distances between  $x$  and its knn.
- If Average knn distance of  $x$  is less compared to other point  $y$ , it indicates that  $x$ 's neighborhood is more denser compared to that of  $y$ .

# Nearest Neighbor Factor(N N F)

- Let  $x$  be a point in  $D$  and  $NN_k(x)$  be the knn of  $x$  .
- The N N F of  $x$  with respect to  $q \in NN_k(x)$  is the ratio of  $d(x,q)$  and Average knn distance of  $q$ .
- $NNF(x,q)=d(x,q)/\text{Average knn distance}$ .

# How it Works ?

- Given a dataset  $D$ , it calculates  $knn$  and Average  $knn$  distance for all points in  $D$ .
- In the next step, it computes *Nearest Neighbor Factor* for all points in the dataset using the previously calculated  $knn$  and *Average  $knn$  Distance*.
- *NDoT* decides whether  $x$  is an outlier or not based on a voting mechanism.



- Votes are counted based on the generated NNF values with respect to all its  $k$  nearest neighbors.
- If  $NNF(x, q \mid q \in N_{nk}(x))$  is more than a threshold value(=1.5 in most experiments),  $x$  is considered as an outlier with respect to  $q$ .
- Subsequently, a vote is counted for  $x$  being an outlier point. If the number of votes are at least  $2/3$  of the number of nearest neighbors then  $x$  is declared as an outlier point.