

**NANYANG TECHNOLOGICAL UNIVERSITY**  
**School of Electrical & Electronic Engineering**

**EE4491 Probability Theory & Applications**

**Tutorial No. 3 (Sem 1, AY2021-2022)**

1. A pair of dice are tossed 8 times.
  - (a) Find the probability that a 7 will occur exactly 4 times.
  - (b) Find the probability that an 11 will occur 2 times.
  - (c) Find the probability that a 12 will occur more than once.
  
2. A file containing 8000 characters is to be transferred from one computer to another. The probability of any one character being transferred in error is 0.001.
  - (a) Find the probability that the file can be transferred without any error.
  - (b) Find the probability that there will be exactly 10 errors in the transferred file.
  - (c) What must the probability of error in transferring one character be in order to achieve the probability of transferring the entire file without error as large as 0.99?
  
3. When a pair of dice are rolled, let  $A$  be the event of obtaining a number of 6 or greater and let  $B$  be the event of obtaining a number of 6 or less. Are events  $A$  and  $B$  dependent or independent?
  
4. If  $A$  is independent of  $B$ , prove that
  - (a)  $A$  is independent of  $\bar{B}$ .
  - (b)  $\bar{A}$  is independent of  $\bar{B}$ .

**Answer**

- (1) (a) 0.02605; (b) 0.0613; (c) 0.0193
- (2) (a)  $p_0 = 3.335 \times 10^{-4}$ ; (b)  $p_{10} = 0.09926$ ; (c)  $p = 1.256 \times 10^{-6}$
- (3) dependent