- 1. (Setting up sample spaces) Assume two standard six-sided dice are rolled one after the other.
 - i Restrict attention to the first roll, and list all possible outcomes of this random experiment.

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First roll can either be 1, 2, 3, 4, 5, or 6. \left(S = \left\{x \in \mathbb{N} \mid 1 \le x \le 6\right\}\right)
We do not care about the outcomes of the second roll.
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ii Now consider both rolls, and list the outcomes of the most general sample space you can define.

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Each roll can either be 1, 2, 3, 4, 5, or 6. Therefore outcomes are: \left(S = \left\{x, y \in \mathbb{N} \mid 1 \leq x, y \leq 6\right\}\right) or \left\{(1, 1), (1, 2), (1, 3), (1, 4), (1, 5), (1, 6), (2, 1), (2, 2), (2, 3), (2, 4), (2, 5), (2, 6), (3, 1), (3, 2), (3, 3), (3, 4), (3, 5), (3, 6), (4, 1), (4, 2), (4, 3), (4, 4), (4, 5), (4, 6), (5, 1), (5, 2), (5, 3), (5, 4), (5, 5), (5, 6), (6, 1), (6, 2), (6, 3), (6, 4), (6, 5), (6, 6) \right\}
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- 2. (Set theory) Consider two arbitrary events $A, B \in S$ and describe the following events using set operations.
 - i Both events occur.

$$A \cap B$$

ii At least one event occurs.

$$A \cup B$$

iii Neither event occurs.

$$\neg (A \cup B)$$

iv Only event A but not event B occurs, i.e. $\{s \in S : s \in A \text{ and } s \notin B\}$. Note: this set operation is called *difference* and is denoted A - B (minus) or $A \setminus B$ (back-slash).

$$A \cap \neg B$$

v Exactly one event occurs.

Note: this set operation is called *symmetric difference* and is denoted by $A\triangle B$. In logic it is also called *exclusive OR* (XOR).

$$(A \cap \neg B) \cup (\neg A \cap B) \cap \neg (A \cup B)$$