

Introduction

3D Computer Graphics (Lab 1)



Terminology

3D Computer Graphics

*The generation of 2D images from
3D representations of geometric objects.*

CGI

Computer Generated Imagery,
the result of applying 3D Computer Graphics

Applications of 3D Computer Graphics



- Movie production, animation and special effects
- Computer games
- Art
- CAD (Computer-aided Design)
- Computer-aided Architectural Design
- Scientific Analysis and Visualization
- Displaying simulations

Movie production, animation and special effects

- The film industry has driven advances in 3D Computer Graphics
- Quest for
 - Photorealism
 - Seamless blending of CGI and live-action

A few milestones of CGI in the movies

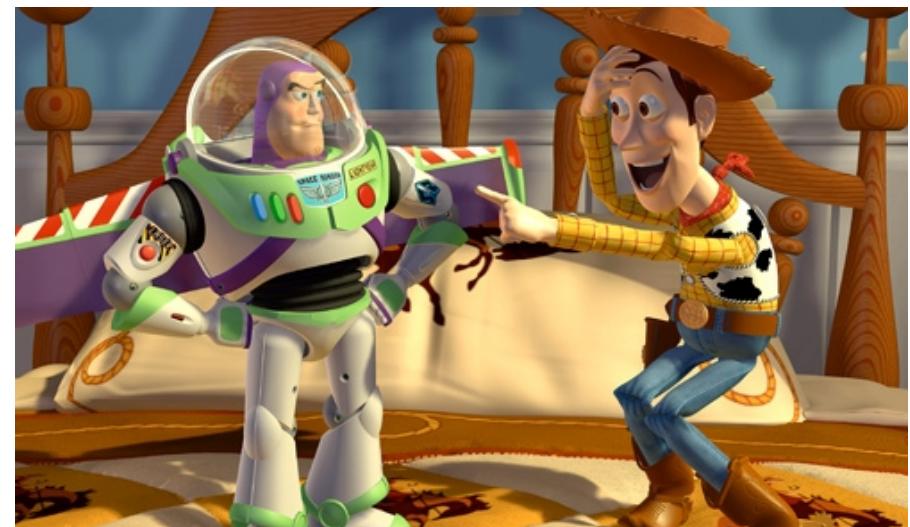


Toy Story (1995)

First full-length CG film

Jurassic Park (1993)

First photorealistic CG creatures



A few milestones of CGI in the movies



Titanic (1997)

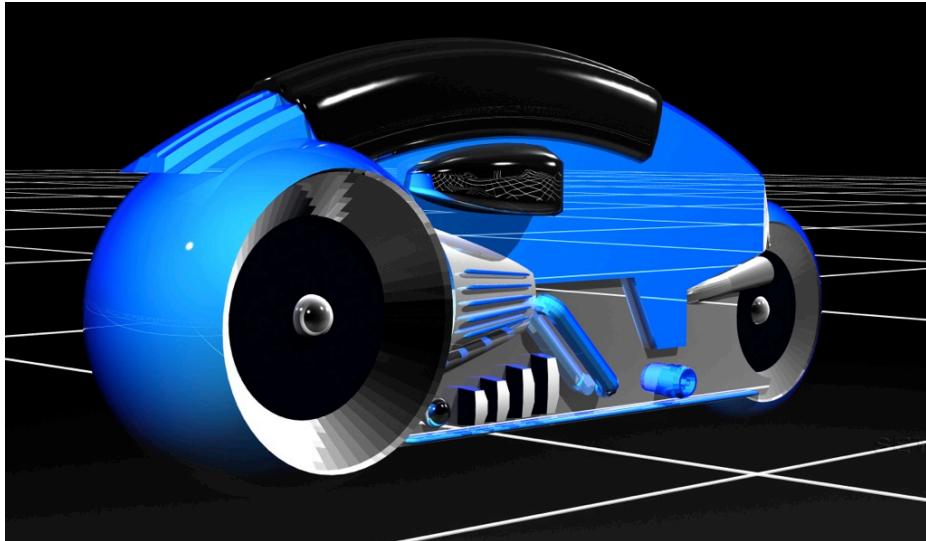
Landmark CG effects



Final Fantasy (2001)

First near-photorealistic character

Comparison ...



Tron (1982)



Tron Legacy (2010)

Computer games

- Heavily influenced by CGI techniques used in movies.
- But different constraints: interactivity and realtime rendering

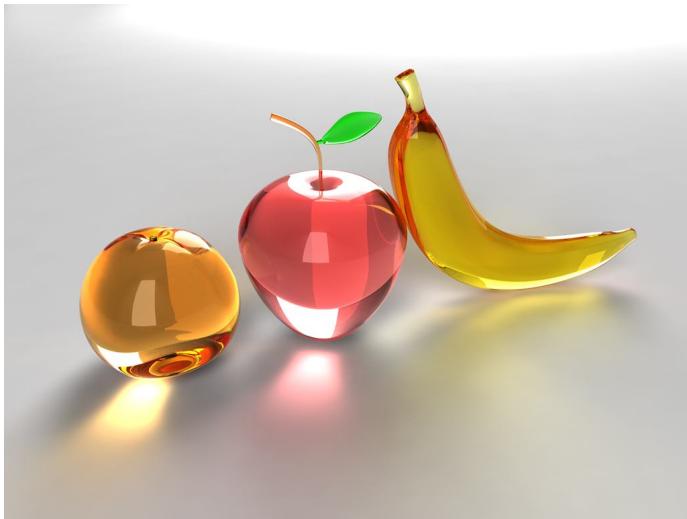


World of Warcraft



Second life

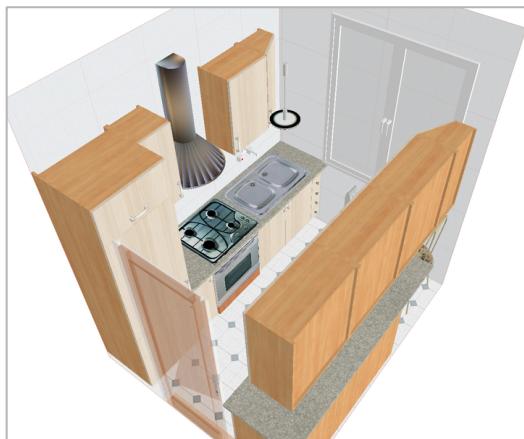
Art



Computer-aided (architectural) design



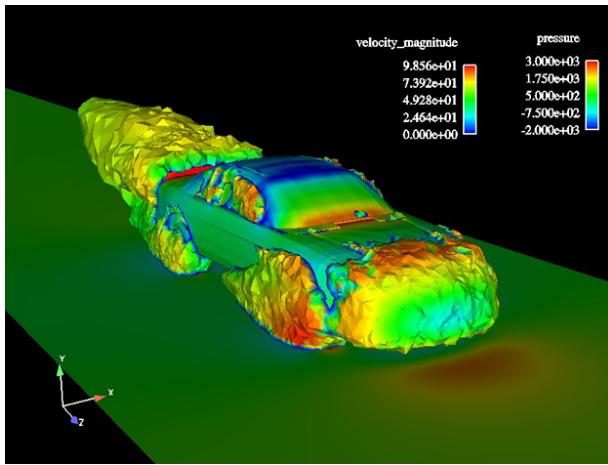
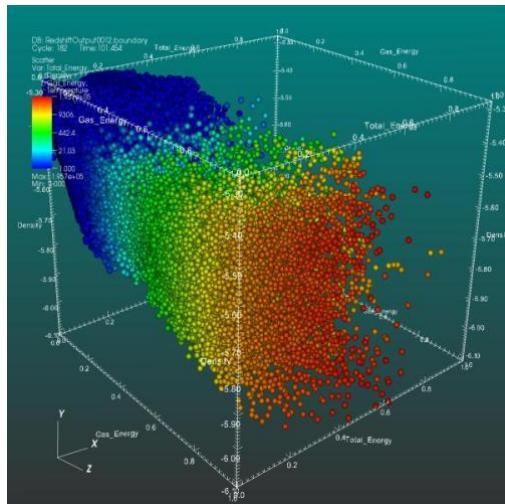
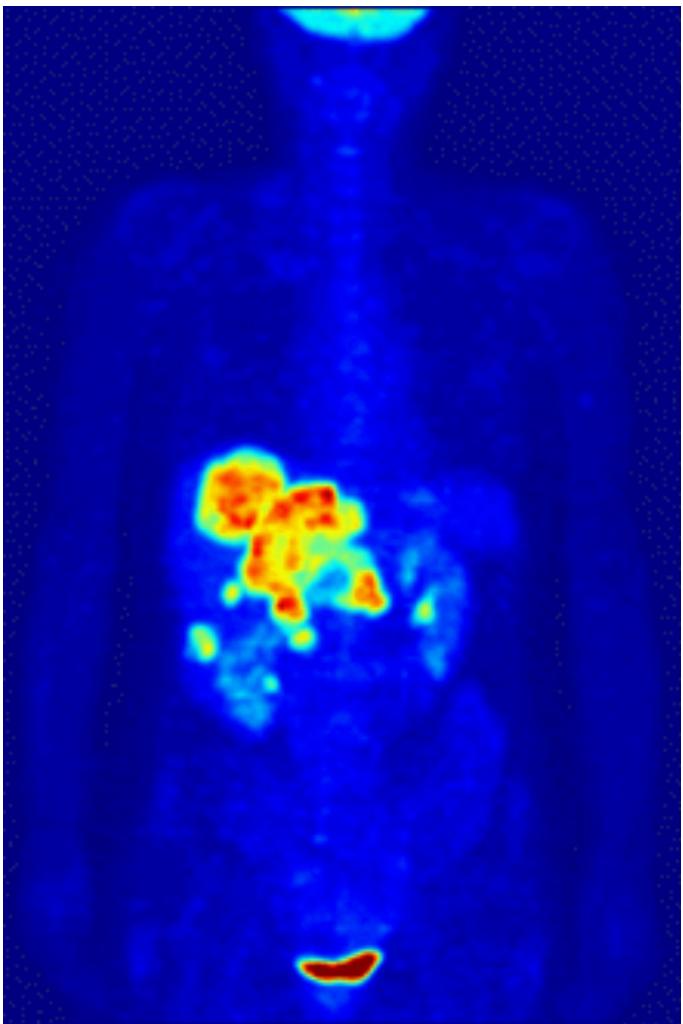
Virtual prototyping



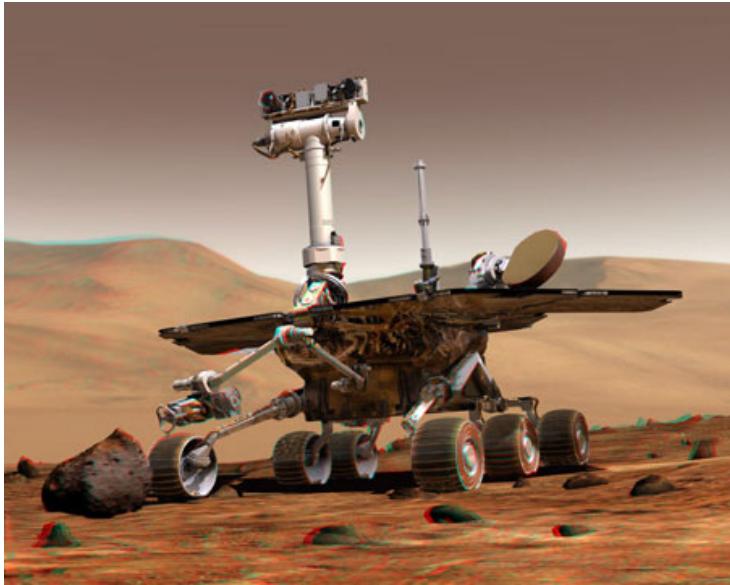
CAAD



Scientific analysis and visualization



Displaying simulations



Flight simulator

Movements of Mars Rover
on Martian surface



Video

Replica of King Tut's mummy

[http://www.youtube.com/watch?
feature=player_embedded&v=iQ4TCR9WoLY](http://www.youtube.com/watch?feature=player_embedded&v=iQ4TCR9WoLY)

Course

Goals

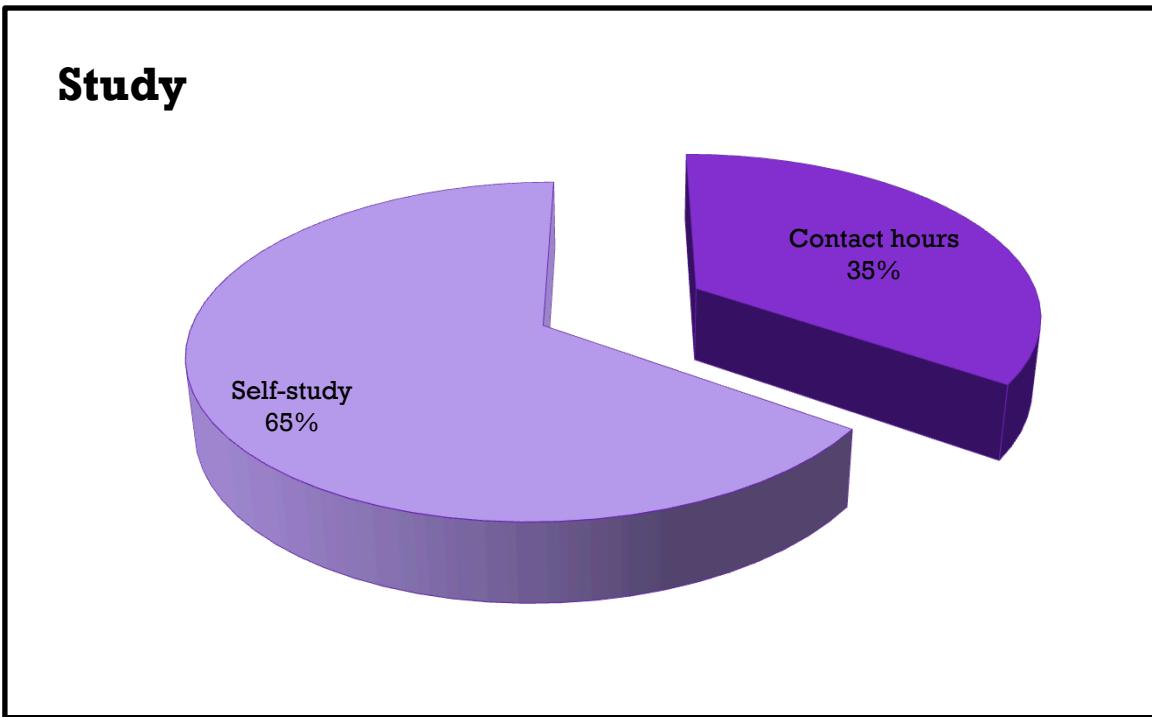
- Knowledge of and insight into the basic concepts and principles of 3D Computer Graphics.
- Knowledge of and insight into mathematical concepts and techniques for multimedia applications.
- Developing software to create and visualize virtual 3D scenes.

Material

All course material (slides, handouts, ...) will be made available online.

I/GT/Export/maaus/3D Computer Graphics/

Time management



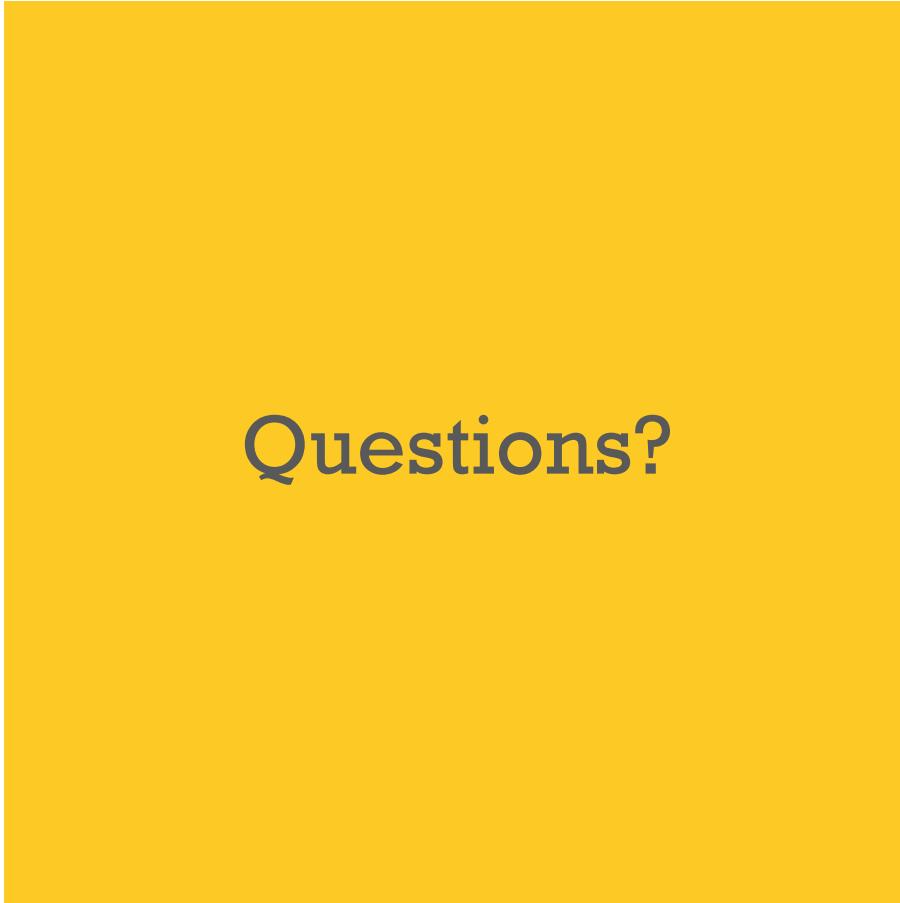
3 SP = 75 hour effort (*all inclusive*)

- Lectures and instruction: 26 hours
- Self-study: 49 hours

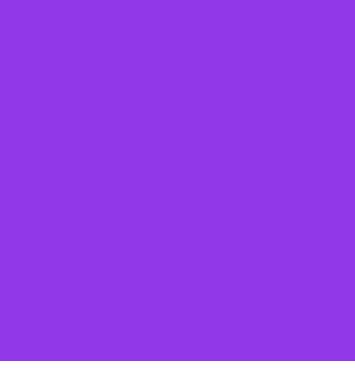
Evaluation

- No permanent evaluation
- No intermediate test/exam
- Exam in January counts for 100% of the final mark.
 - Written exam
 - Closed book
- Second examination is organised in the same way.

Individual feedback till the end of the week of the last lecture!



Questions?



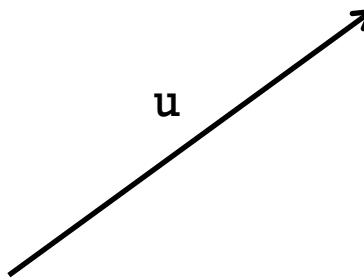
Mathematical preliminaries

Points vs vectors

- A **point** defines a location.
 - It has a position.
 - But it has no length or direction.
- A **vector** has length and direction.
 - But it has no position.
 - It can be moved anywhere.



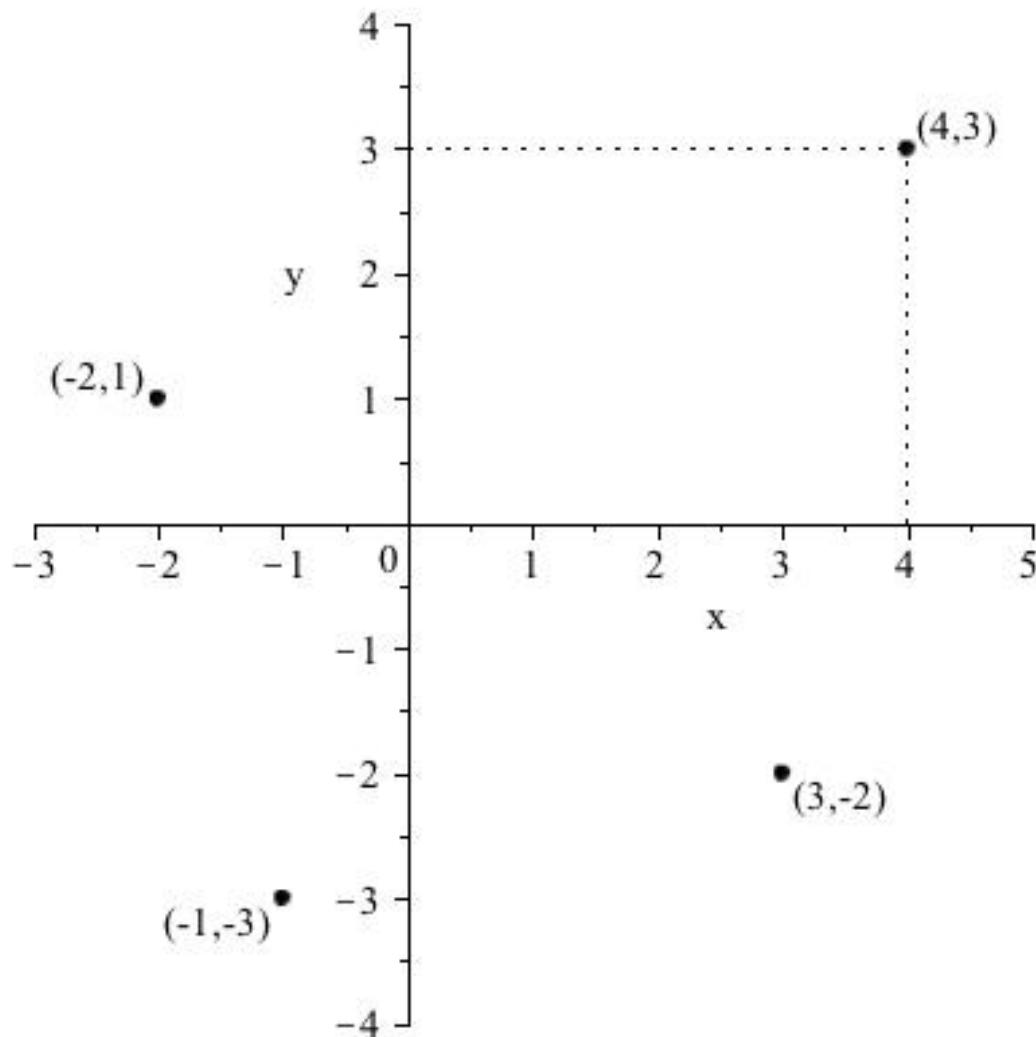
Notation: P, Q, \dots



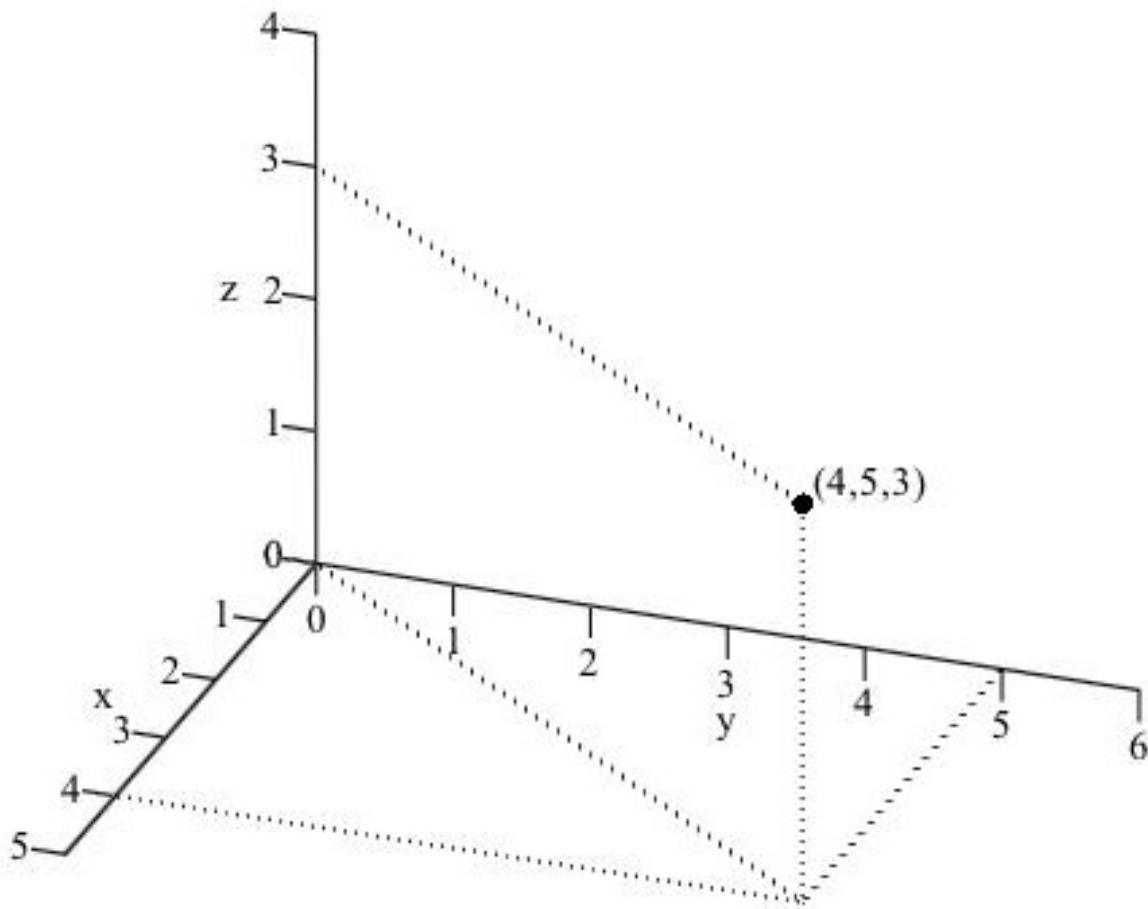
Notation: u, v, \dots

We need a way to quantify them ...

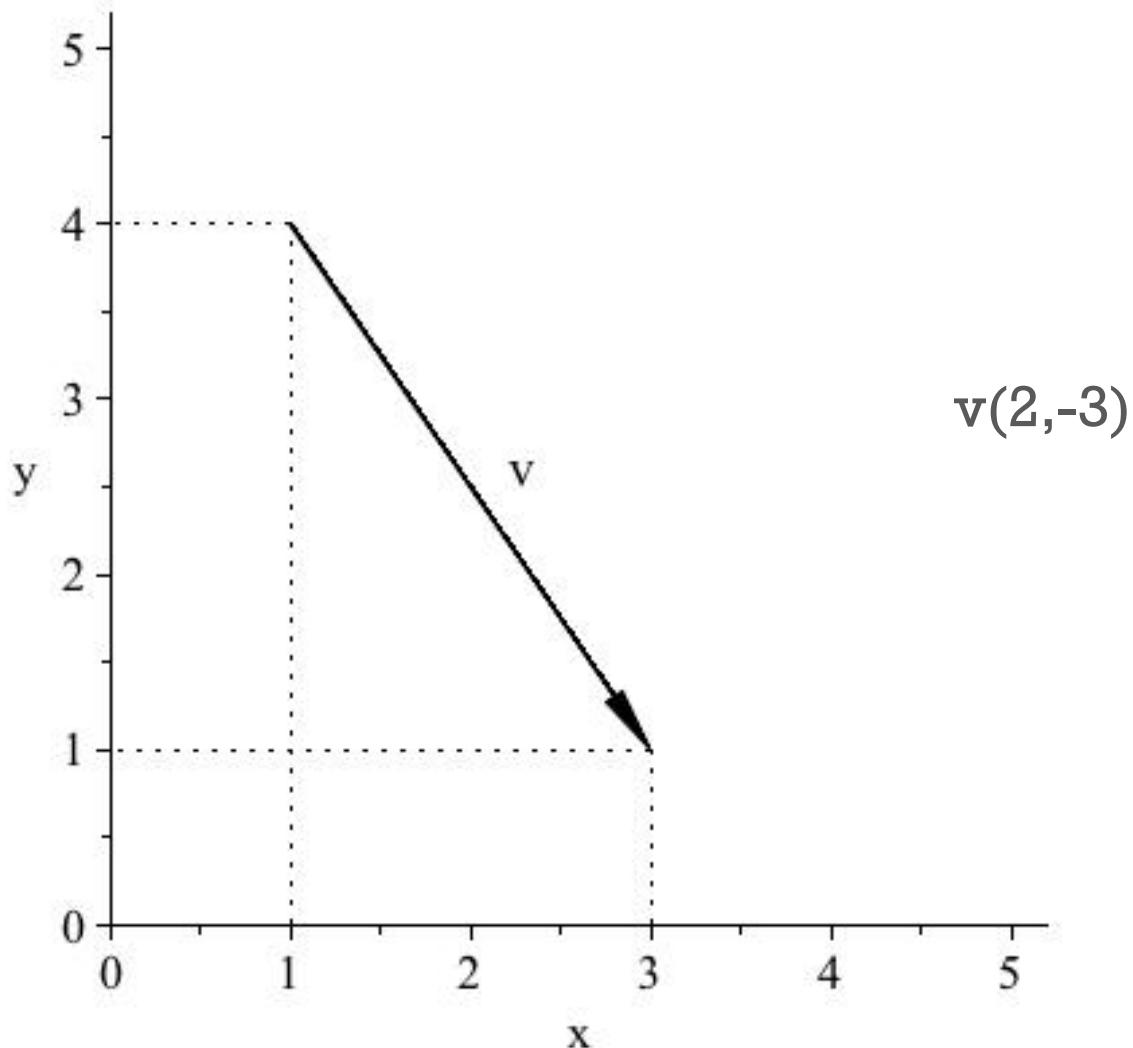
Points in 2D



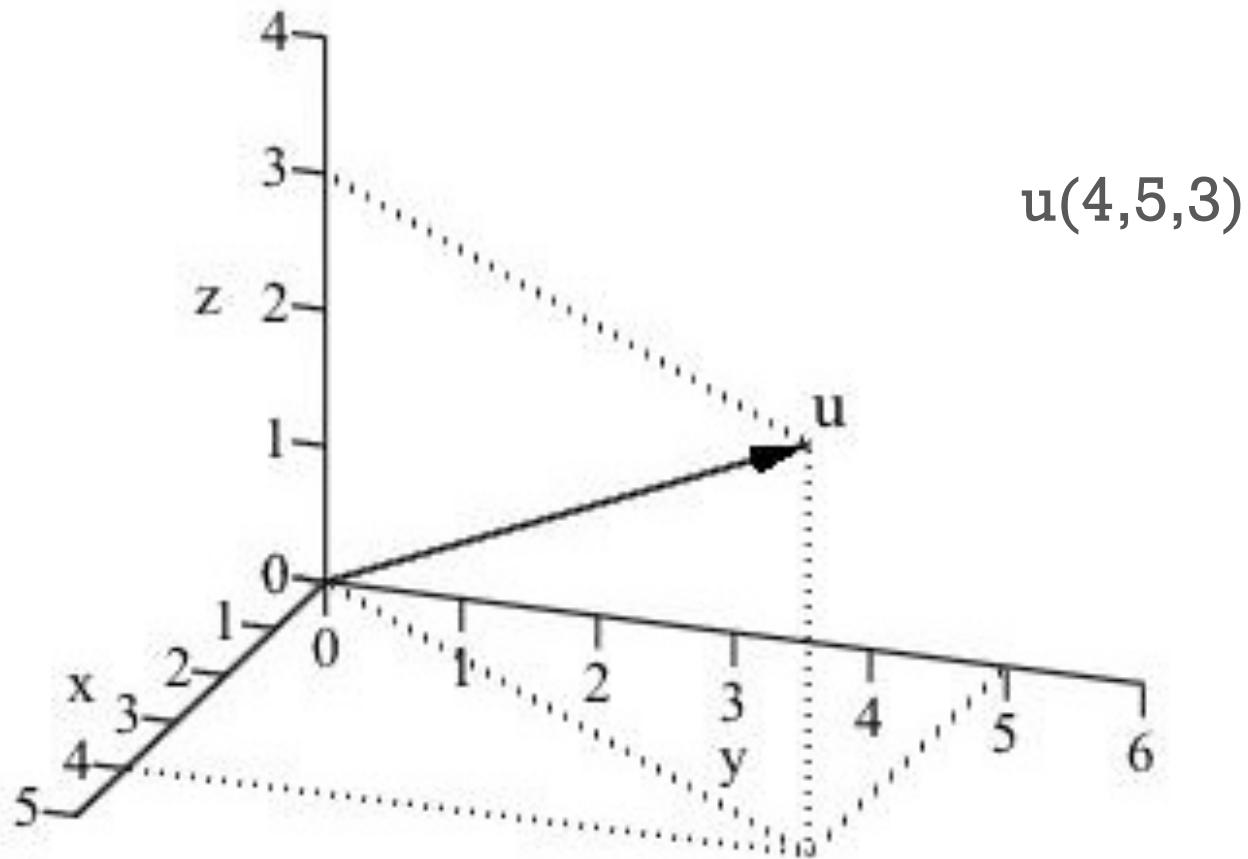
Points in 3D



Vectors in 2D



Vectors in 3D



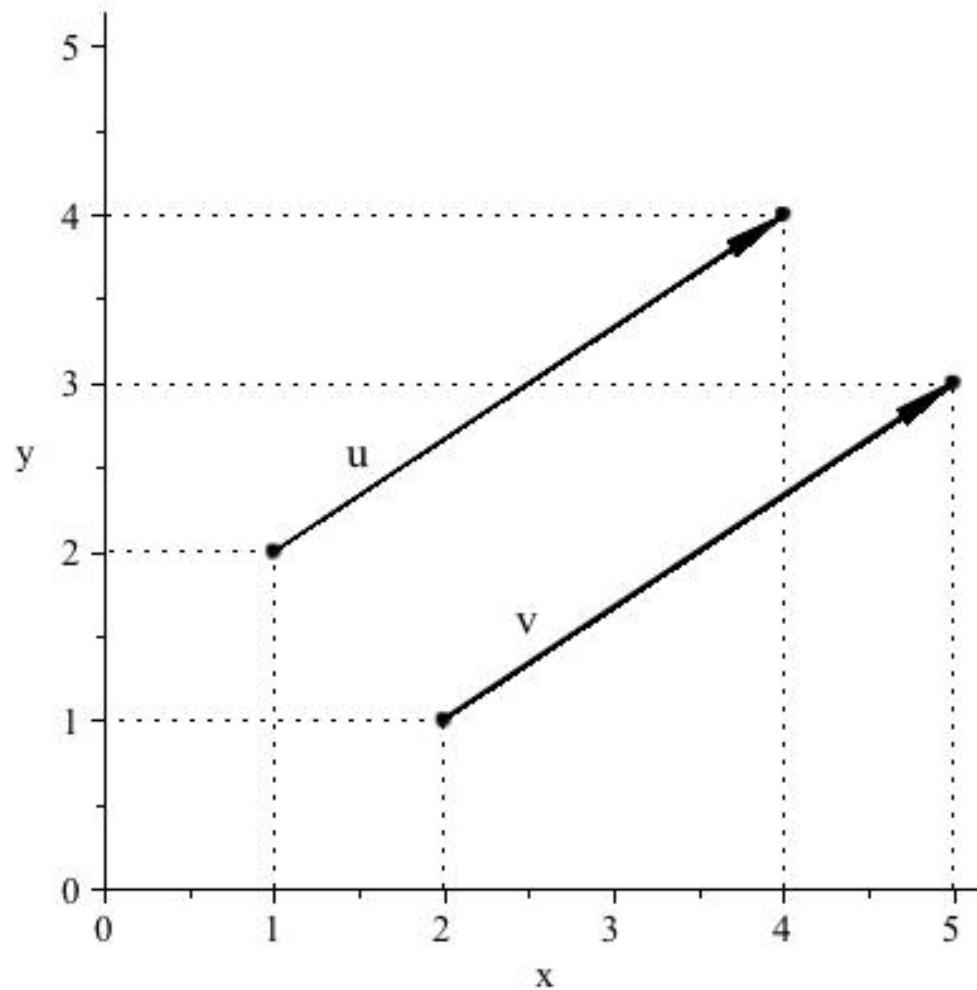
Conclusion

Once a coordinate system is fixed, points and vectors can be identified by means of

- an ordered set of two real numbers in 2D
- an ordered set of three real numbers in 3D

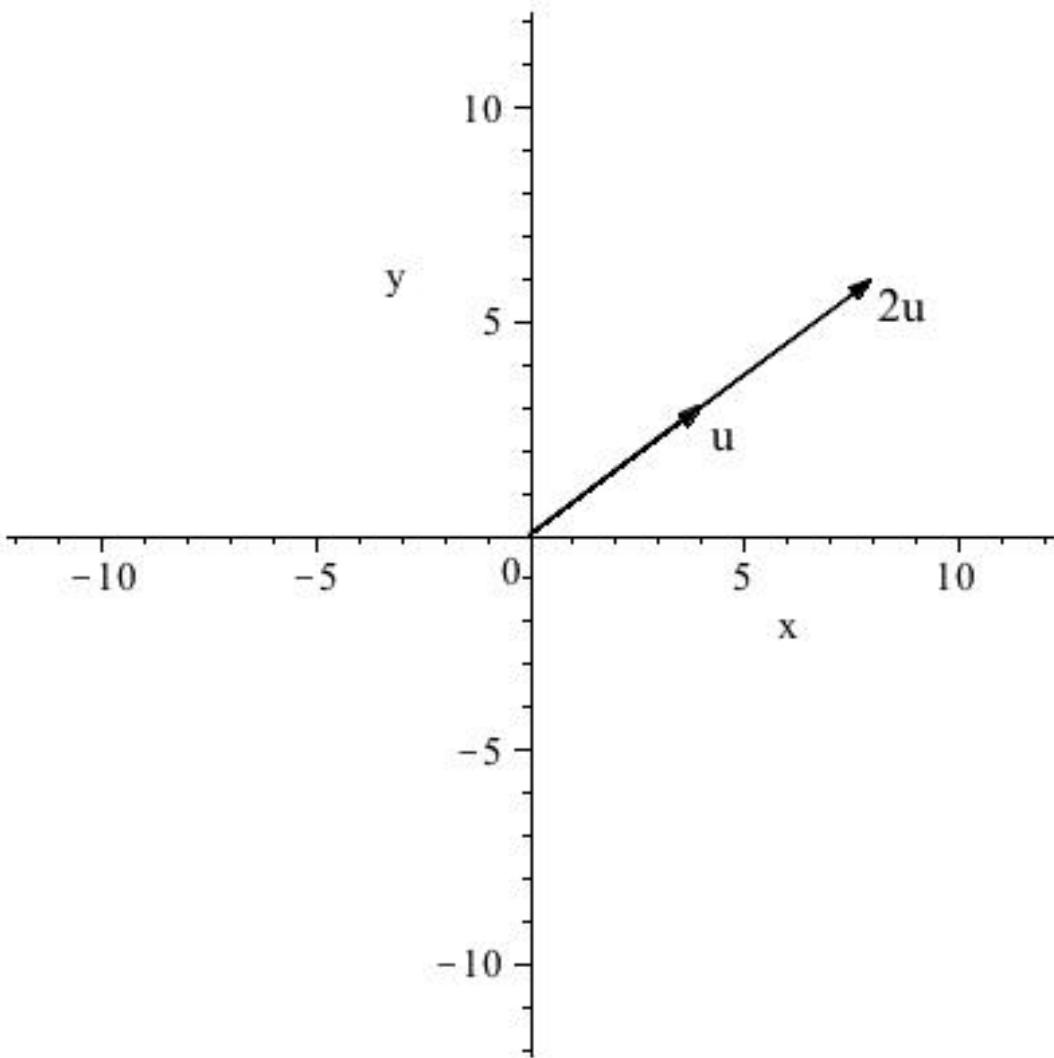
The ordered set of real numbers identifying a point/vector are called the **coordinates** of this point/vector.

Example



u en v are the same vector and have the same coordinates (3,2).

Scalar multiplication

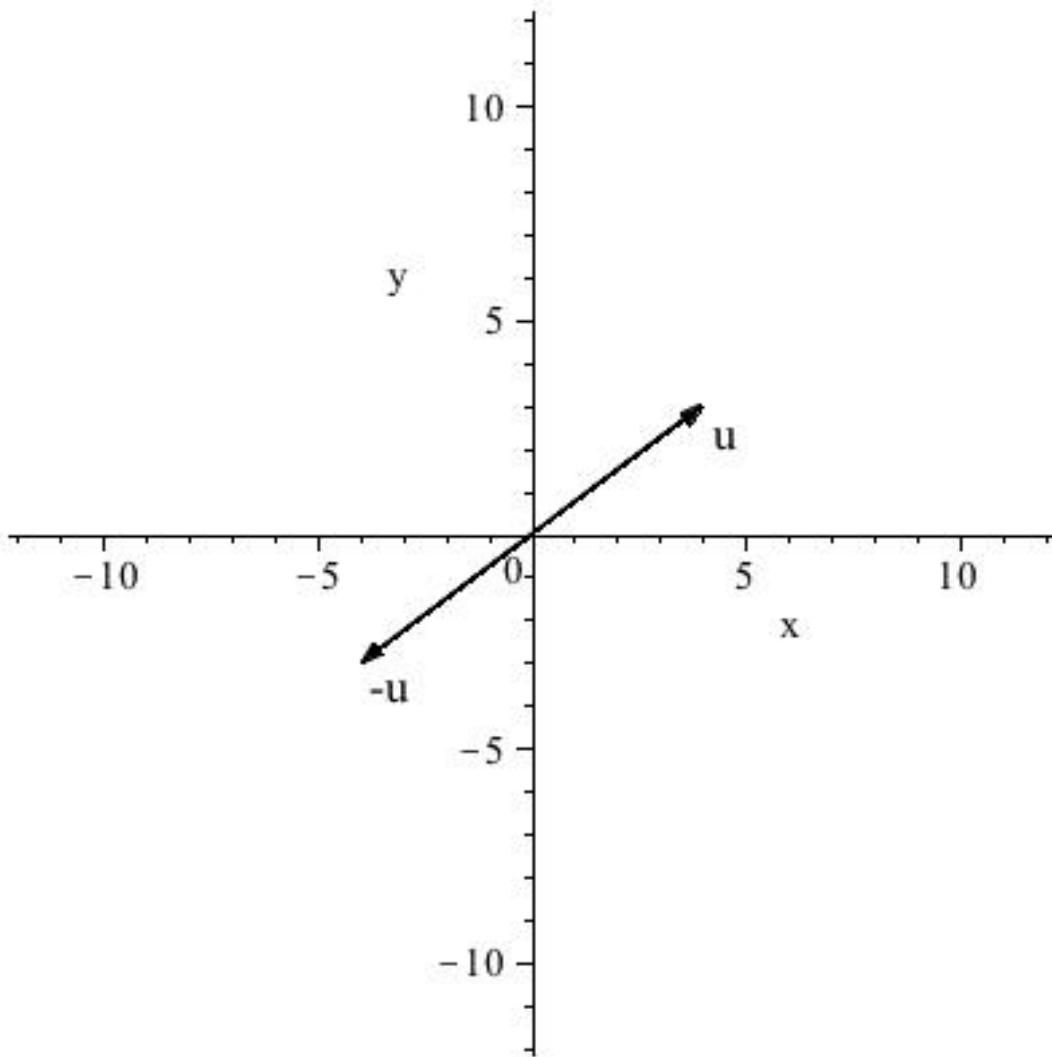


Assume $u = (4,3)$

$$2u = 2(4,3) = (8,6)$$

- same direction
- length $\times 2$

Scalar multiplication

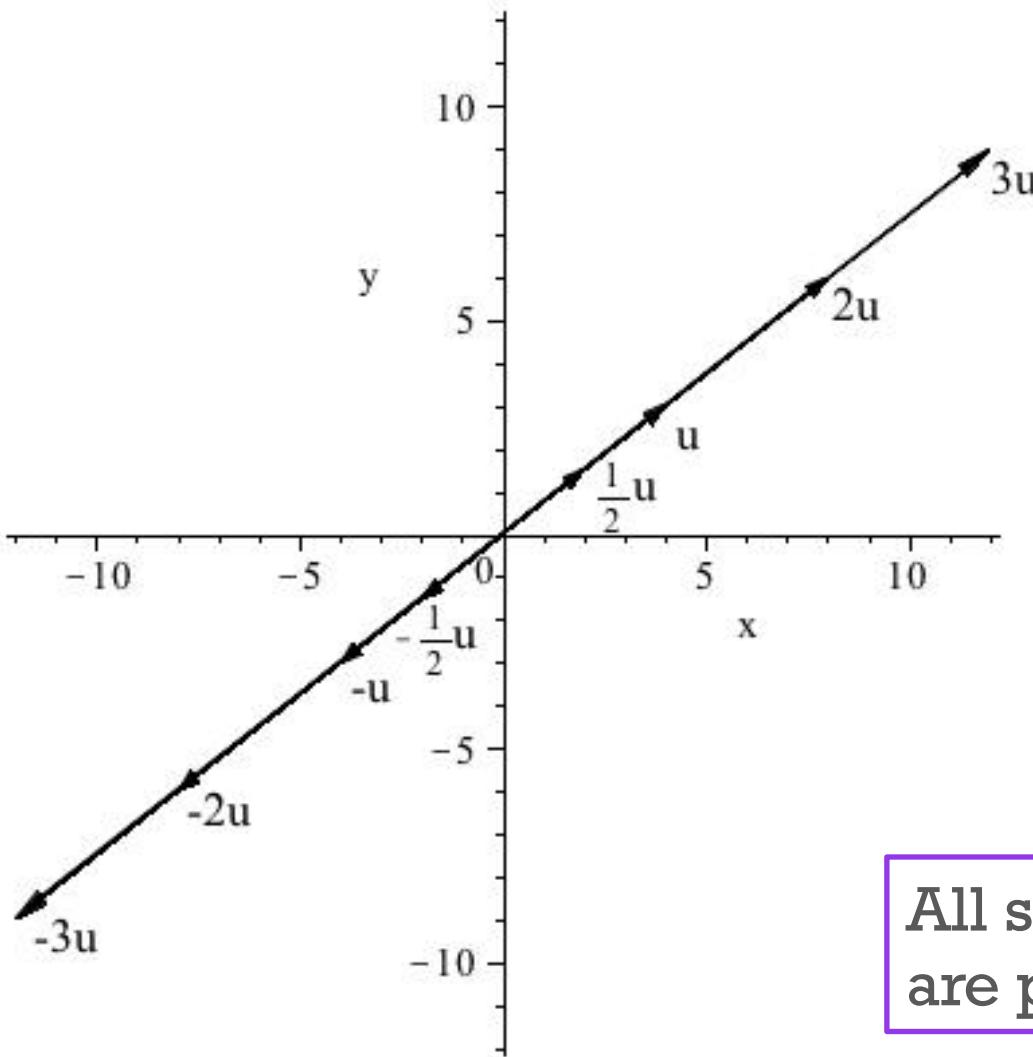


Assume $u = (4, 3)$

$$-u = -(4, 3) = (-4, -3)$$

- same length
- opposite/reverse direction

Scalar multiplication



Assume $u = (4,3)$

$$-3u = (-12,-9)$$

$$-2u = (-8,-6)$$

$$-u = (-4,-3)$$

$$-\frac{1}{2}u = (-2,-1.5)$$

$$\frac{1}{2}u = (2,1.5)$$

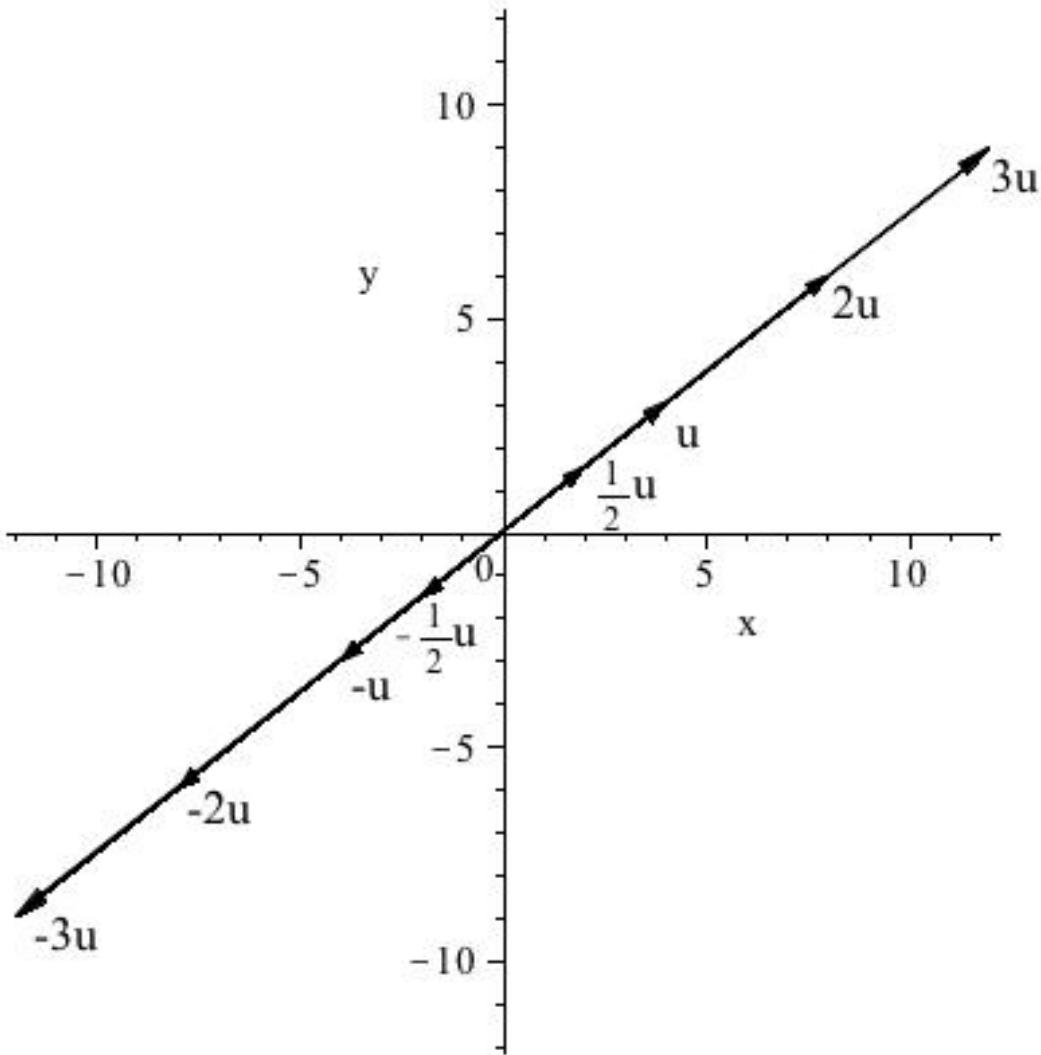
$$u = (4,3)$$

$$2u = (8,6)$$

$$3u = (12,9)$$

All scalar multiples of u are parallel to each other.

Scalar multiplication



if $c > 0$

cu and u have the same direction.

if $c < 0$

cu and u have the opposite/reverse direction.

if $-1 < c < 1$

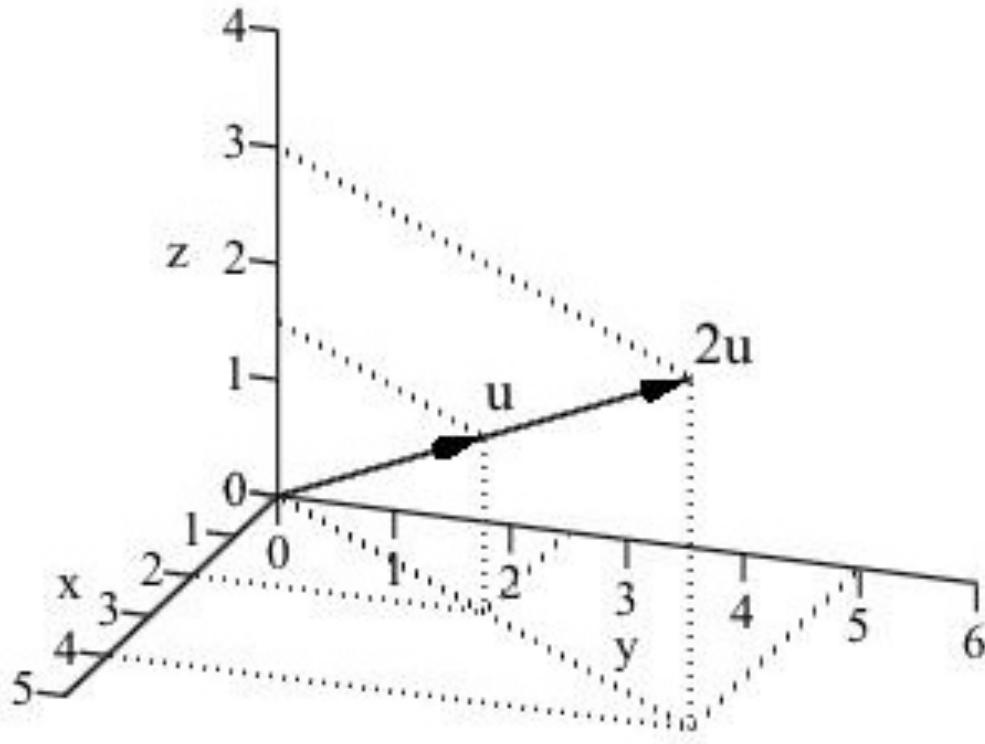
cu has a smaller length than u .

If $c < -1$ or $c > 1$

cu has a larger length than u .

Scalar multiplication

The same ideas apply in 3D



Assume $u = (2, 2.5, 1.5)$

$$2u = 2(2, 2.5, 1.5) = (4, 5, 3)$$

u and $2u$ are parallel vectors.

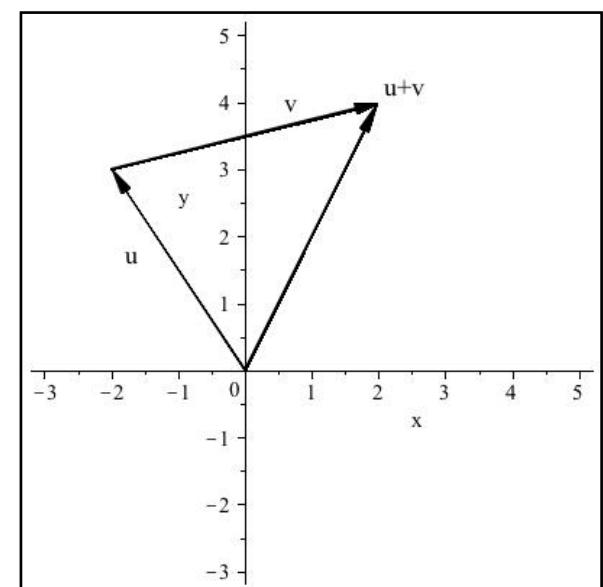
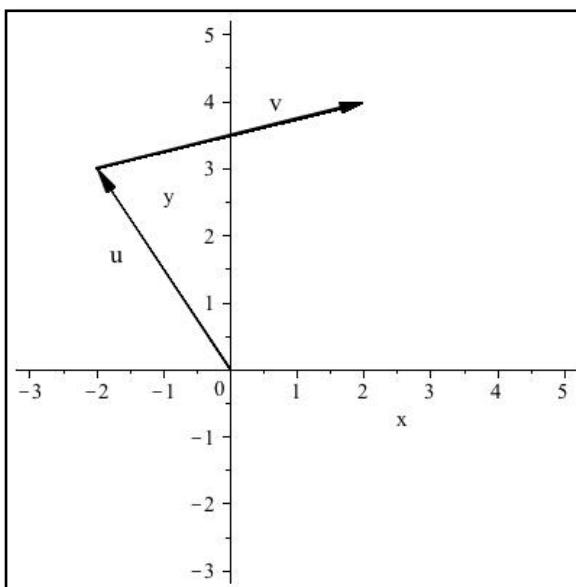
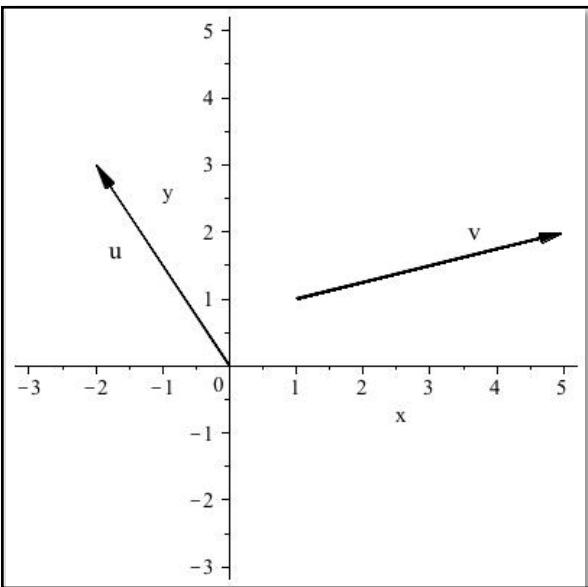
$2u$ has the same direction as u because $c = 2 > 0$.

$2u$ has a larger length than u because $c = 2 > 1$.

Sum of two vectors (in 2D)

Assume $u = (-2, 3)$ and $v = (4, 1)$

$$u + v = (-2, 3) + (4, 1) = (-2+4, 3+1) = (2, 4)$$



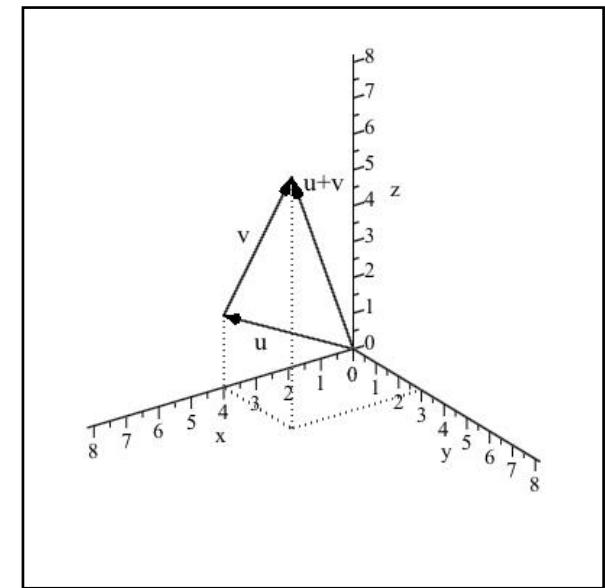
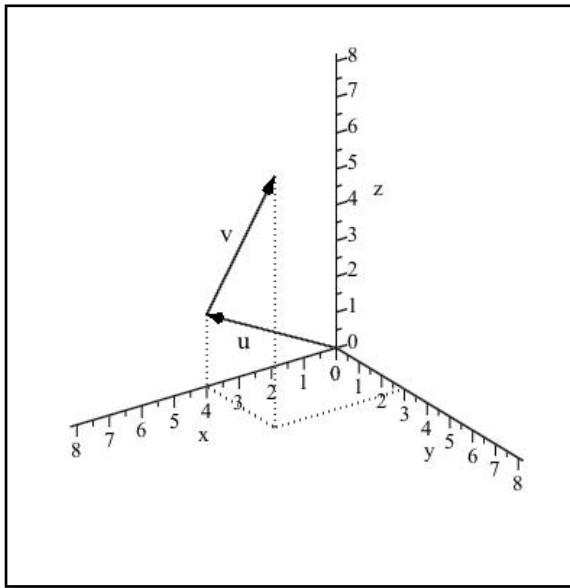
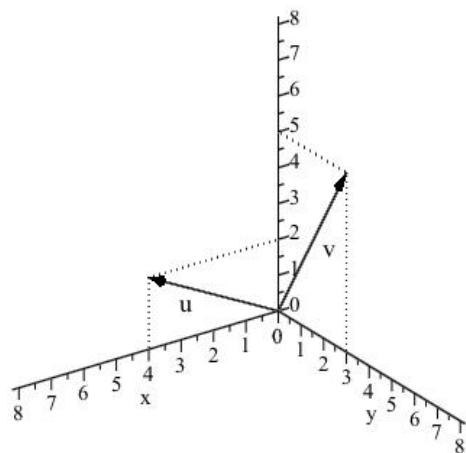
Move v so that its startpoint coincides with the endpoint of u .

$u+v$ is the vector from the startpoint of u to the endpoint of v .

Sum of two vectors (in 3D)

Assume $u = (4,0,2)$ and $v = (0,3,5)$

$$u + v = (4,0,2) + (0,3,5) = (4,3,7)$$



Move v so that its startpoint coincides with the endpoint of u .

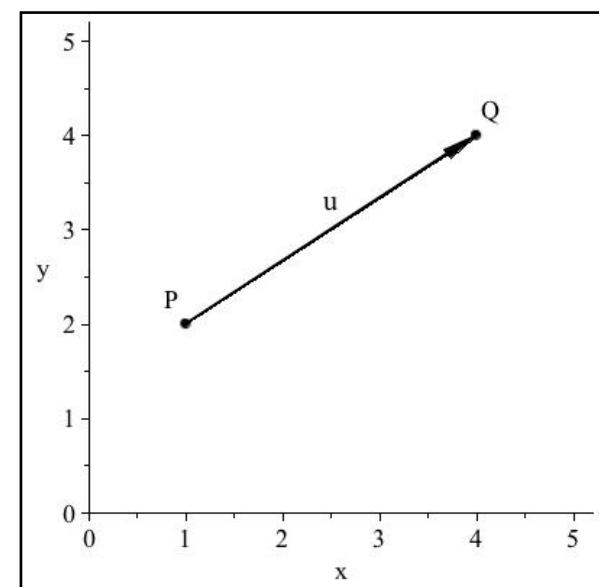
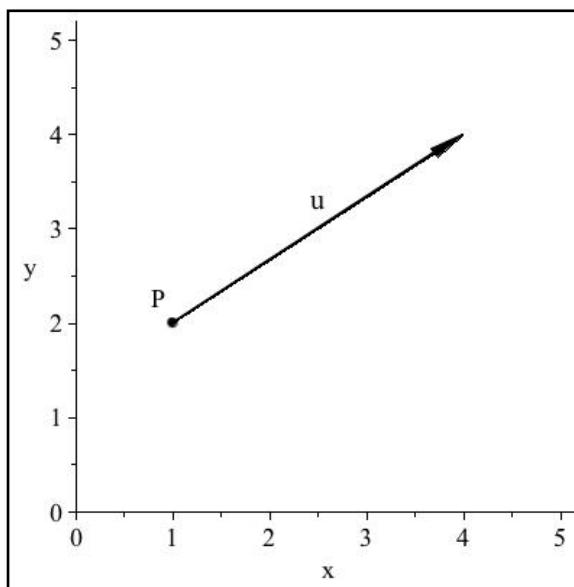
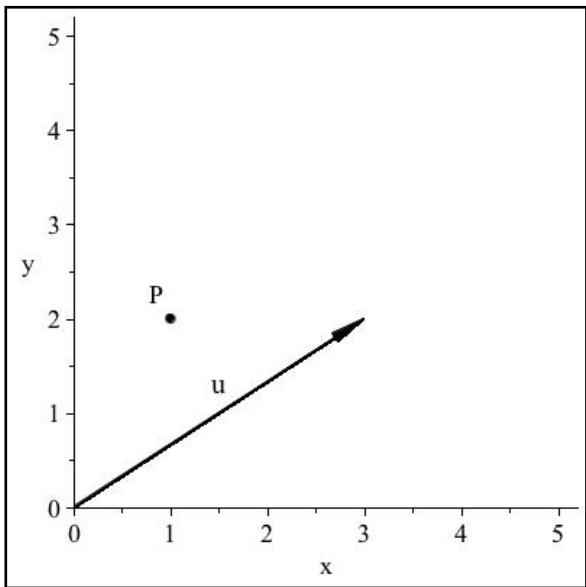
$u+v$ is the vector from the startpoint of u to the endpoint of v .

Sum of a point and a vector

Assume a point $P = (1,2)$ and a vector $u = (3,2)$

$$P + u = (1,2) + (3,2) = (4,4)$$

The same applies in 3D.



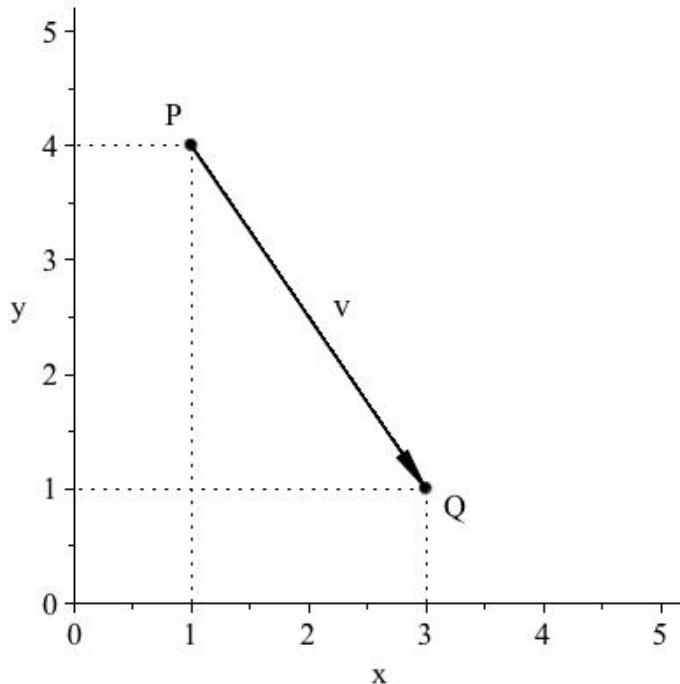
Move u so that its startpoint coincides with the point P .

$P+u$ is the point Q , the endpoint of u .

Exercise

Assume two points $P = (1,4)$ and $Q = (3,1)$.

What is the vector which starts at point P and ends at point Q?



We are looking for the vector v such that

$$P + v = Q$$

or

$$v = Q - P$$

This yields

$$\begin{aligned} v &= (3,1) - (1,4) \\ &= (2,-3) \end{aligned}$$

The difference of 2 points is a vector!

A vector from point P to Q can be obtained by computing $Q - P$. (Reverse order!)

Length of a vector

- The length of a 2D vector $\mathbf{v} = (v_x, v_y)$ is given by

$$|\mathbf{v}| = \sqrt{v_x^2 + v_y^2}$$

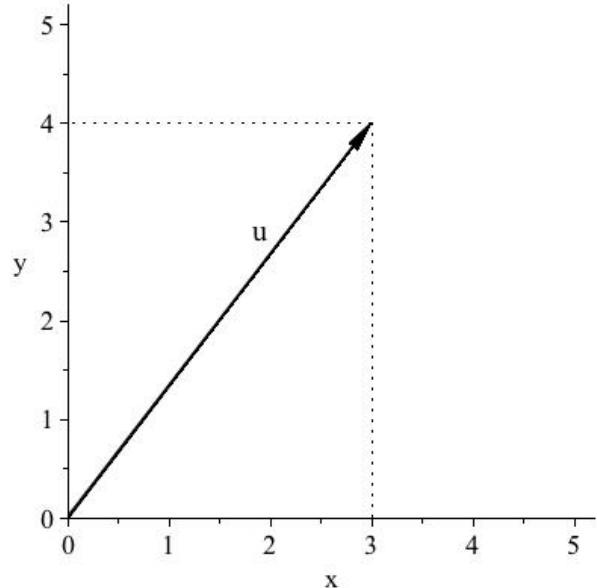
- The length of a 3D vector $\mathbf{v} = (v_x, v_y, v_z)$ is given by

$$|\mathbf{v}| = \sqrt{v_x^2 + v_y^2 + v_z^2}$$

Example

What is the length of the vector $\mathbf{u} = (3, 4)$?

$$|\mathbf{u}| = \sqrt{3^2 + 4^2} = 5$$



Normalizing a vector

Definition

Normalizing a vector u is

converting u to a vector with the same direction but length 1.

Example

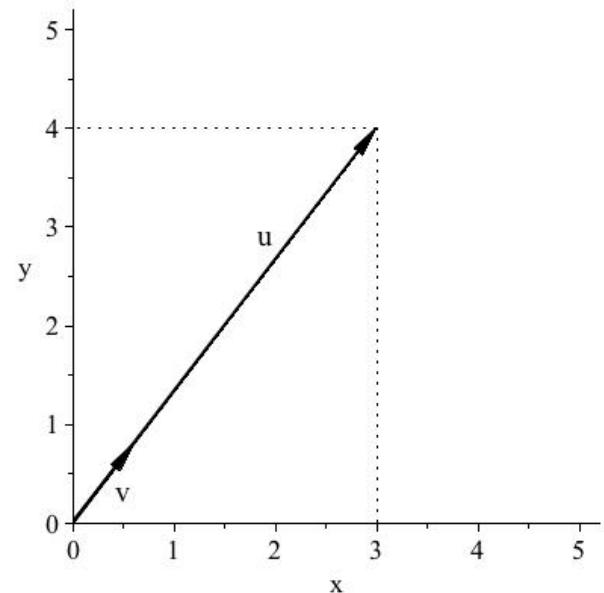
Given is a vector $u = (3,4)$. How can we find v which has the same direction as u but length 1?

→ Scalar multiplication of u with $\frac{1}{|u|}$.

$$\text{Because } |u| = \sqrt{3^2 + 4^2} = 5$$

$$\text{is } v = \frac{1}{|u|} u = \frac{1}{5} u = \frac{1}{5} (3,4) = (0.6,0.8)$$

$$(\text{Check: } |v| = \sqrt{0.6^2 + 0.8^2} = 1.)$$



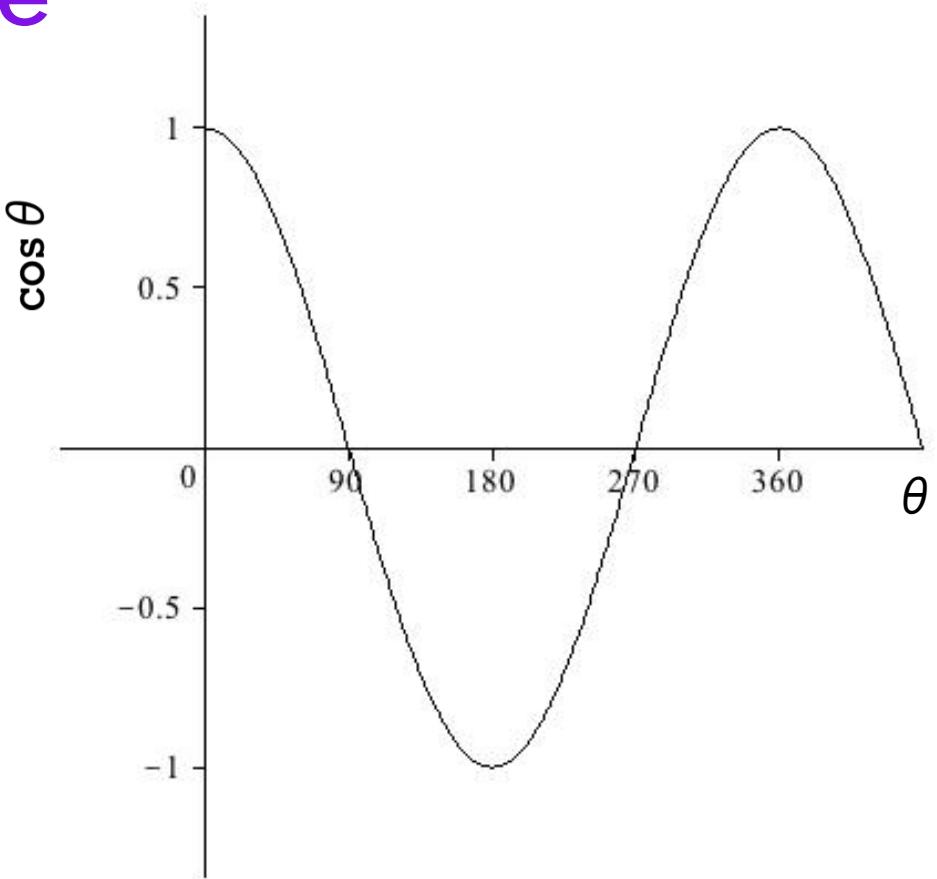
Intermezzo: cosine

■ Examples

$$\cos(0) = 1$$

$$\cos(90) = 0$$

$$\cos(180) = -1$$



If $0^\circ < \theta < 90^\circ$ then $\cos \theta > 0$

If $90^\circ < \theta < 180^\circ$ then $\cos \theta < 0$

Dot product

Definition

The **dot product** of two vectors $v = (v_x, v_y, v_z)$ and $w = (w_x, w_y, w_z)$ is a real number given by

$$v \cdot w = v_x w_x + v_y w_y + v_z w_z$$

Example

The **dot product** of two vectors $v = (1, 2, 3)$ and $w = (3, -2, 1)$ is given by

$$v \cdot w = 1 \cdot 3 + 2 \cdot (-2) + 3 \cdot 1 = 2$$

Dot product

Property

The **dot product** of two vectors v and w equals

$$v \cdot w = |v||w|\cos(\theta)$$

with θ the (smaller) angle between these two vectors.

This formula is often used in the form $\cos(\theta) = \frac{v \cdot w}{|v||w|}$

Example

What is the angle between $v = (3,0)$ and $w = (\sqrt{3},1)$?

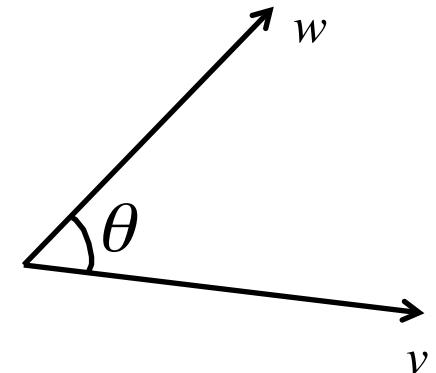
$$v \cdot w = 3\sqrt{3} + 0 \cdot 1 = 3\sqrt{3}$$

$$|v| = \sqrt{3^2 + 0^2} = 3$$

$$|w| = \sqrt{(\sqrt{3})^2 + 1^2} = 2$$

$$\left. \begin{array}{l} \\ \\ \end{array} \right\} \cos(\theta) = \frac{v \cdot w}{|v||w|} = \frac{3\sqrt{3}}{3 \cdot 2} = \frac{\sqrt{3}}{2}$$

$\rightarrow \theta = 60^\circ$



Cross product

Definition

The **cross product** of two vectors $a = (a_x, a_y, a_z)$ and $b = (b_x, b_y, b_z)$ is a vector given by

$$a \times b = (a_y b_z - a_z b_y, a_z b_x - a_x b_z, a_x b_y - a_y b_x)$$

Example

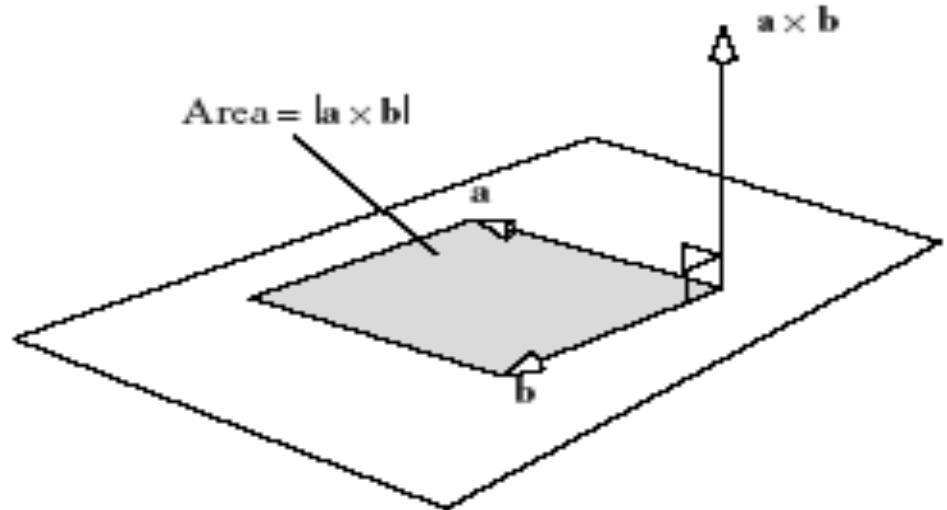
The **cross product** of two vectors $a = (1, 2, 3)$ and $b = (3, -2, 1)$ is given by

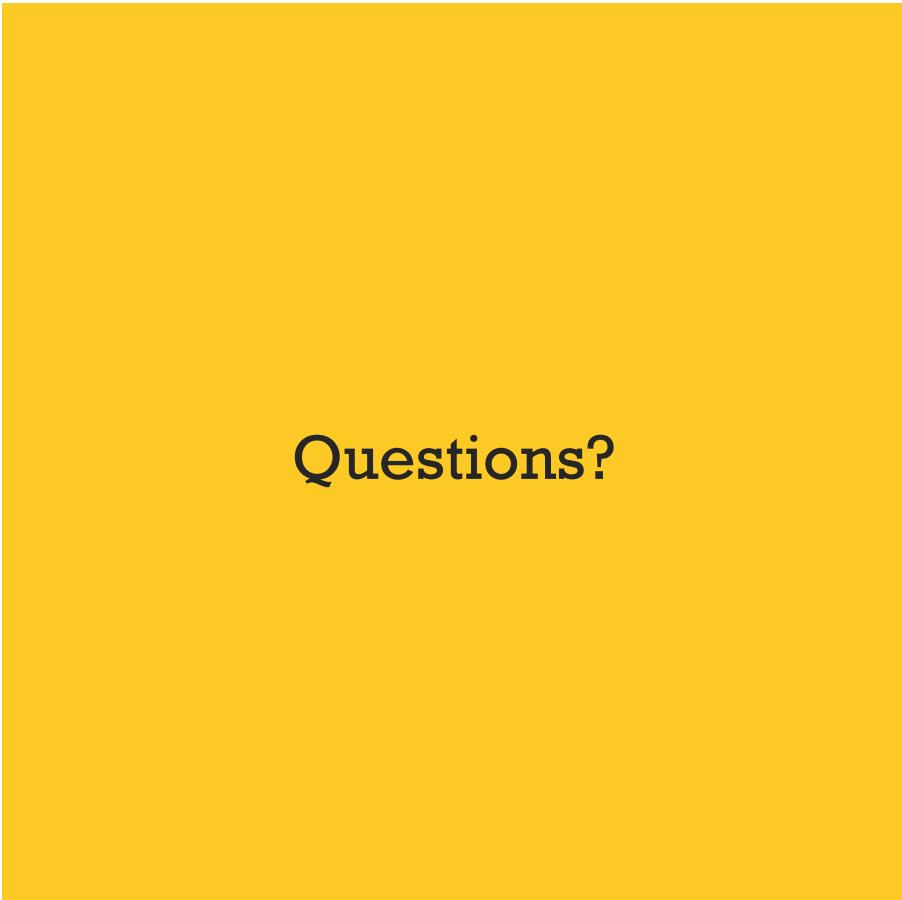
$$a \times b = (2 \cdot 1 - 3 \cdot (-2), 3 \cdot 3 - 1 \cdot 1, 1 \cdot (-2) - 2 \cdot 3) = (8, 8, -8)$$

Cross product

Property

- $a \times b$ is a vector perpendicular to a and b
- The direction of $a \times b$ can be found by the right hand rule.
- The length of $a \times b$ is the area of the parallelogram formed by a and b





Questions?

