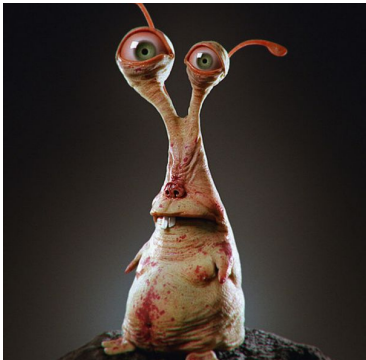
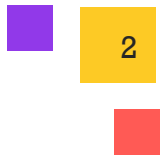


Ray Tracer extensions (part II)

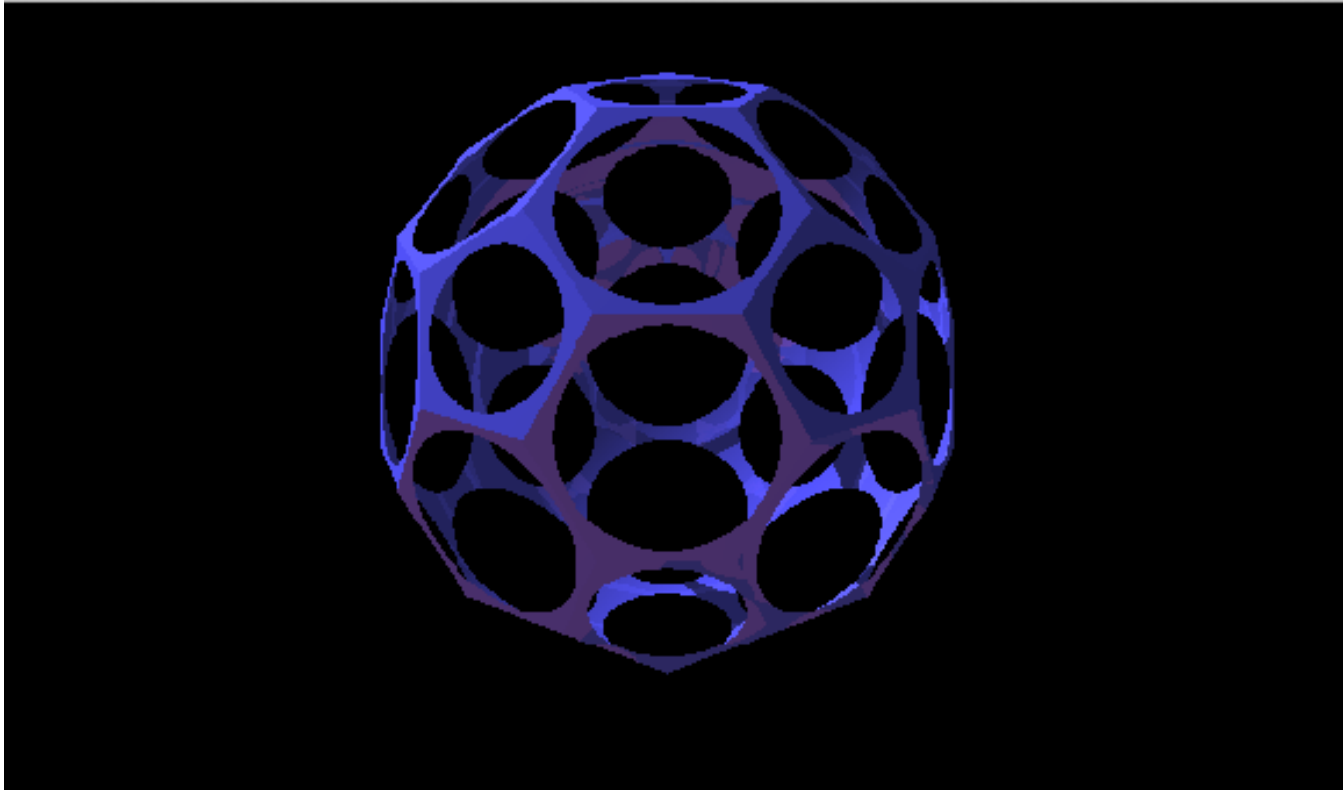
3D Computer Graphics (Lab 10)



Example



Can we render this image with our current rendering framework?





Constructive Solid Geometry

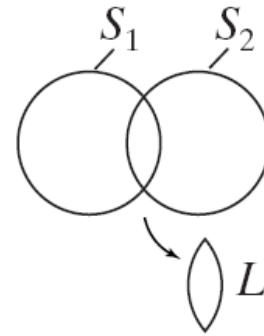
Constructive Solid Geometry

- Constructive Solid Geometry (**CSG**) is a method to create complex shapes by means of combining simple shapes.
- Arbitrary complex shapes are defined by **boolean operations** on simple shapes.

- Boolean operators

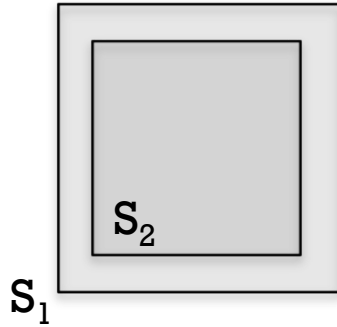
- Union
- Intersection
- Difference

Example: a lens shape constructed as the intersection of two spheres.



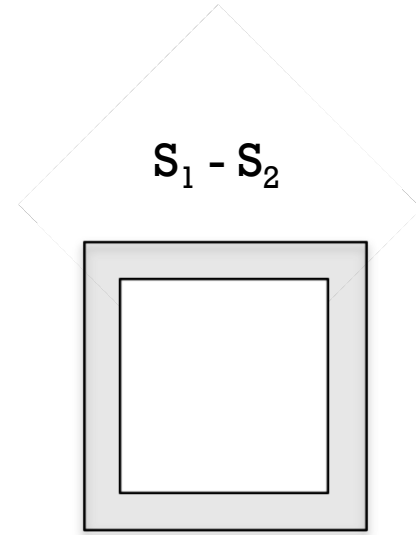
- The resulting shapes are called **compound**, **boolean** or **CSG objects**.
- We will add support for the difference operator in this Lab.

Example



sdl file

```
square  
scale 0.75 0.75 0.75 square
```

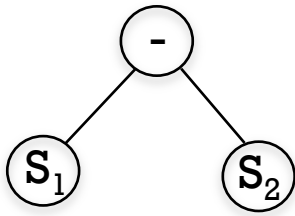


sdl file

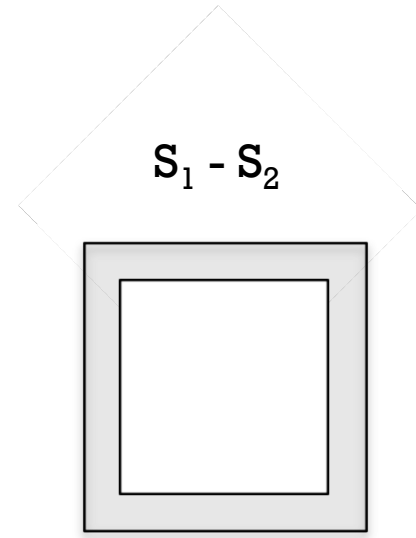
```
difference  
square  
scale 0.75 0.75 0.75 square
```

Example

How do we represent this boolean object?



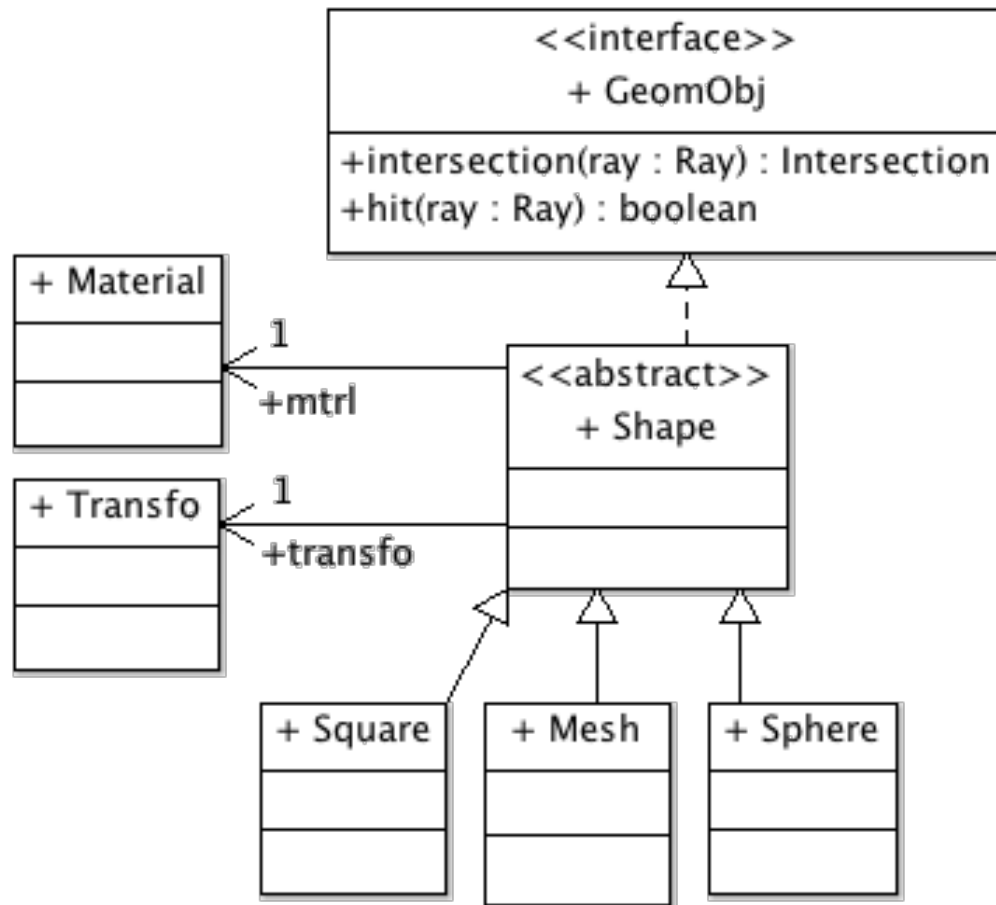
a binary tree structure



sdl file

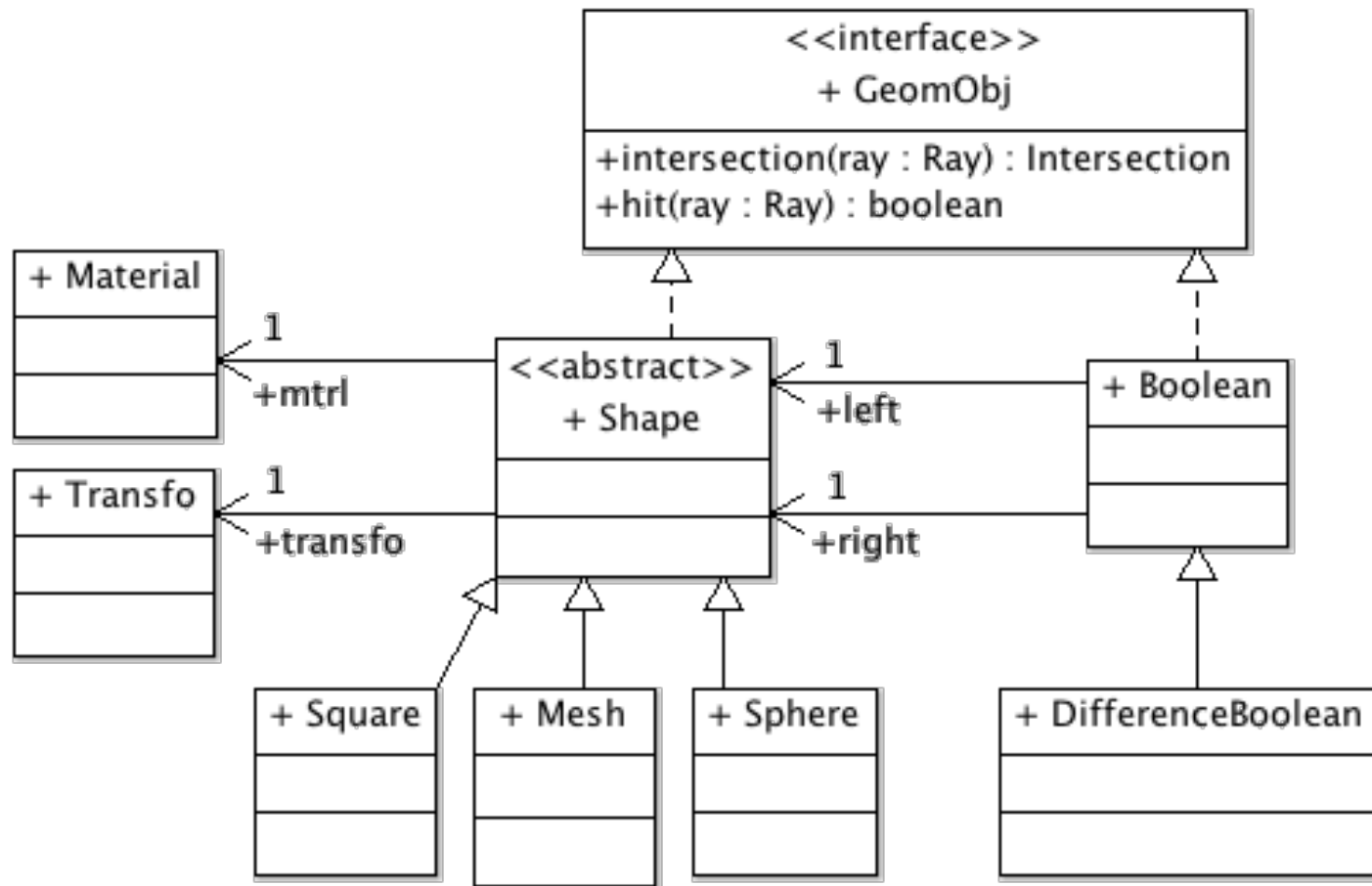
```
difference  
square  
scale 0.75 0.75 0.75 square
```

Current 3D object representation

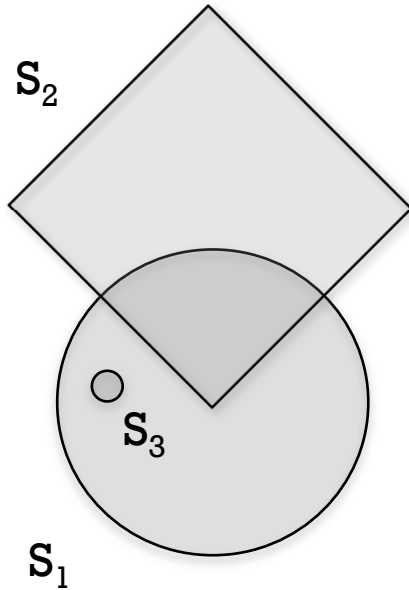
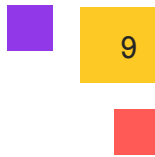


How do we add support for boolean objects?

Support for boolean objects

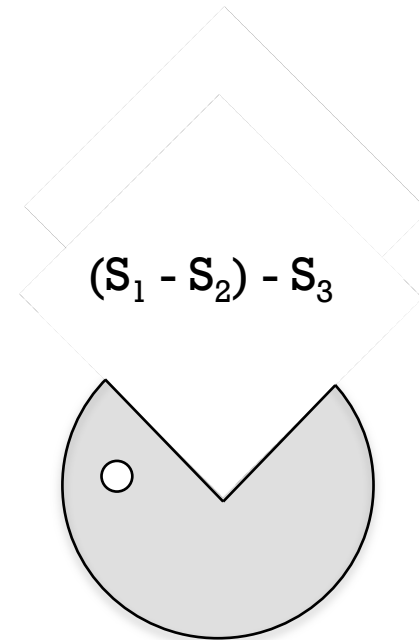


Example 2



sdl file

```
sphere  
push rotate 45 0 0 1 translate 1 1 0 mesh cube.txt pop  
translate -0.75 0.2 0 scale 0.1 0.1 0.1 mesh cylinder.txt
```



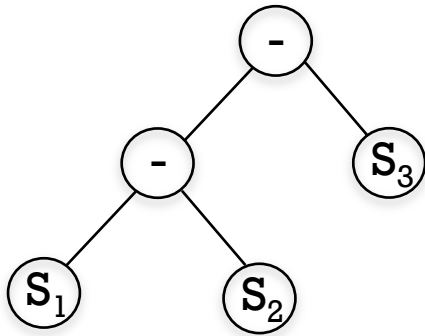
sdl file

```
difference  
difference  
sphere  
push rotate 45 0 0 1 translate 1 1 0 mesh cube.txt pop  
translate -0.75 0.2 0 scale 0.1 0.1 0.1 mesh cylinder.txt
```

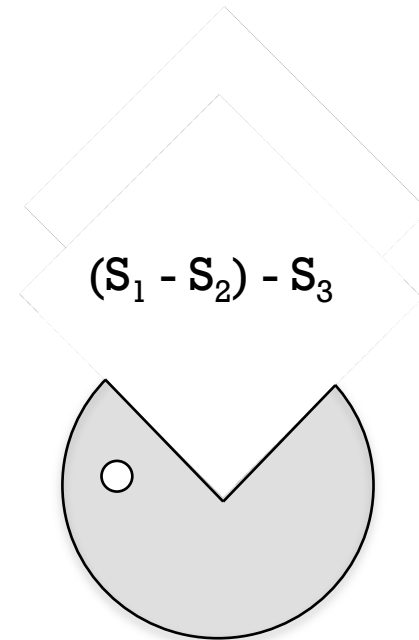
Example 2

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How do we represent this boolean object?



a binary tree structure

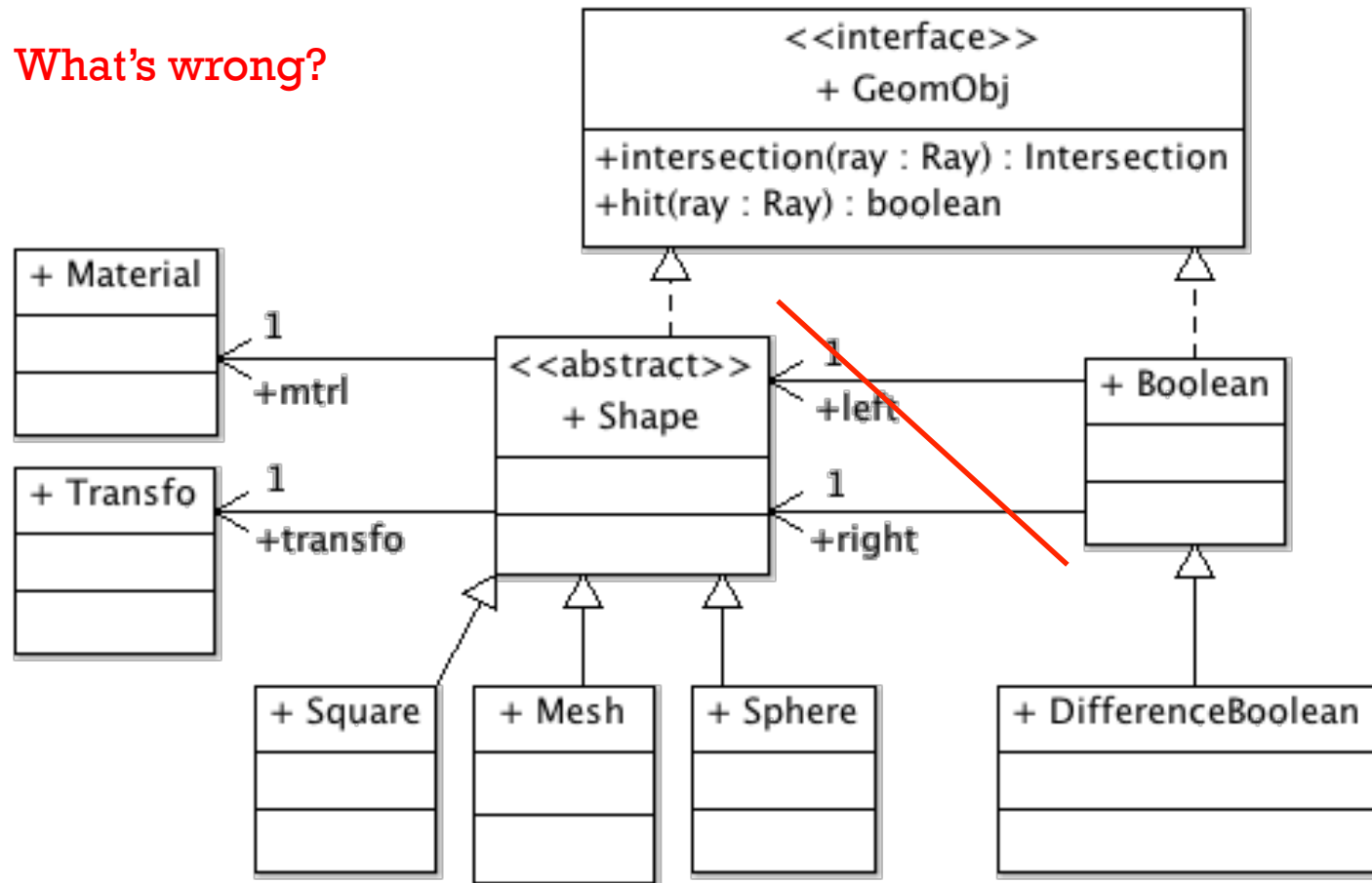


sdl file

```
difference  
difference  
sphere  
push rotate 45 0 0 1 translate 1 1 0 mesh cube.txt pop  
translate -0.75 0.2 0 scale 0.1 0.1 0.1 mesh cylinder.txt
```

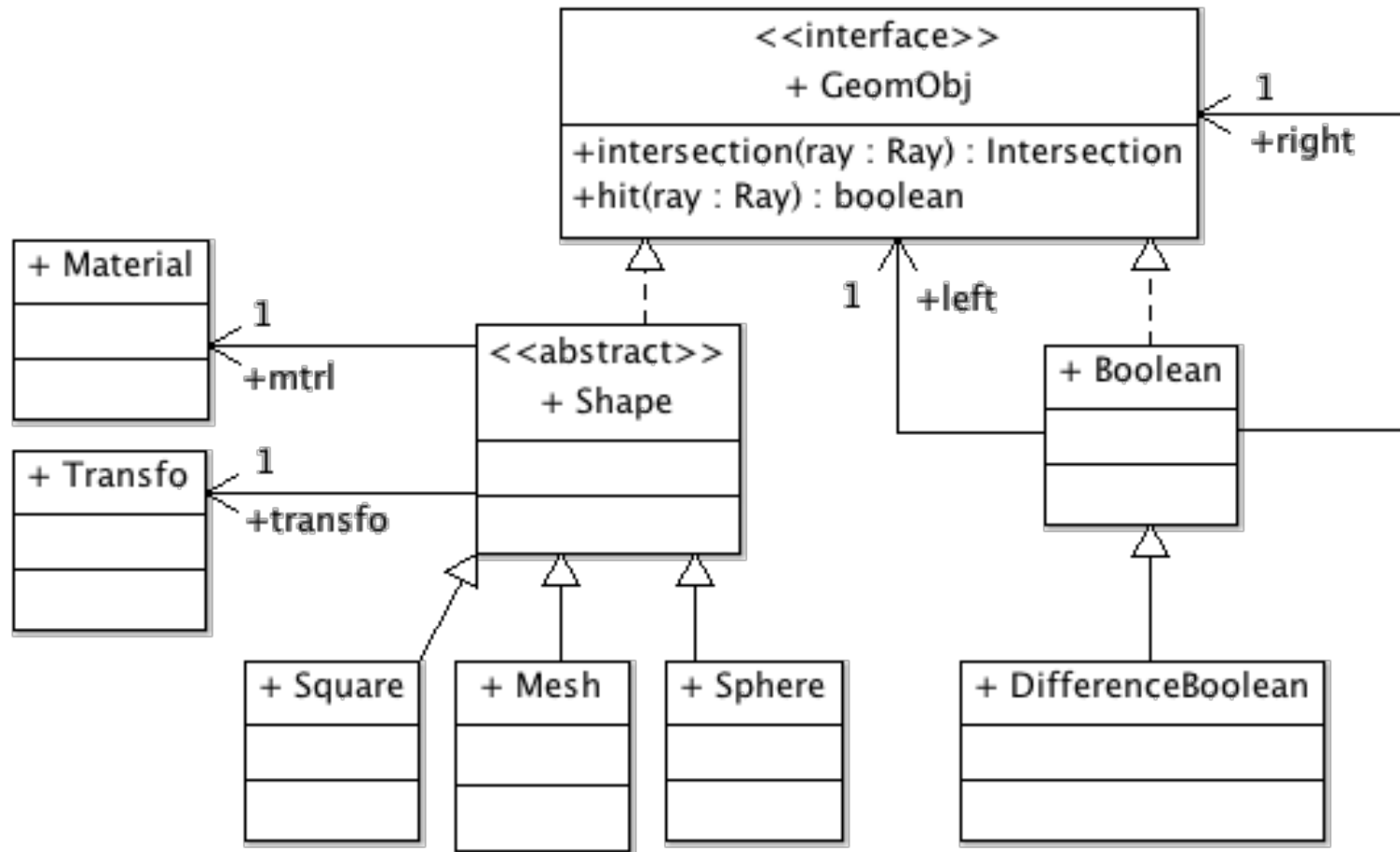
Support for boolean objects

What's wrong?



Support for boolean objects

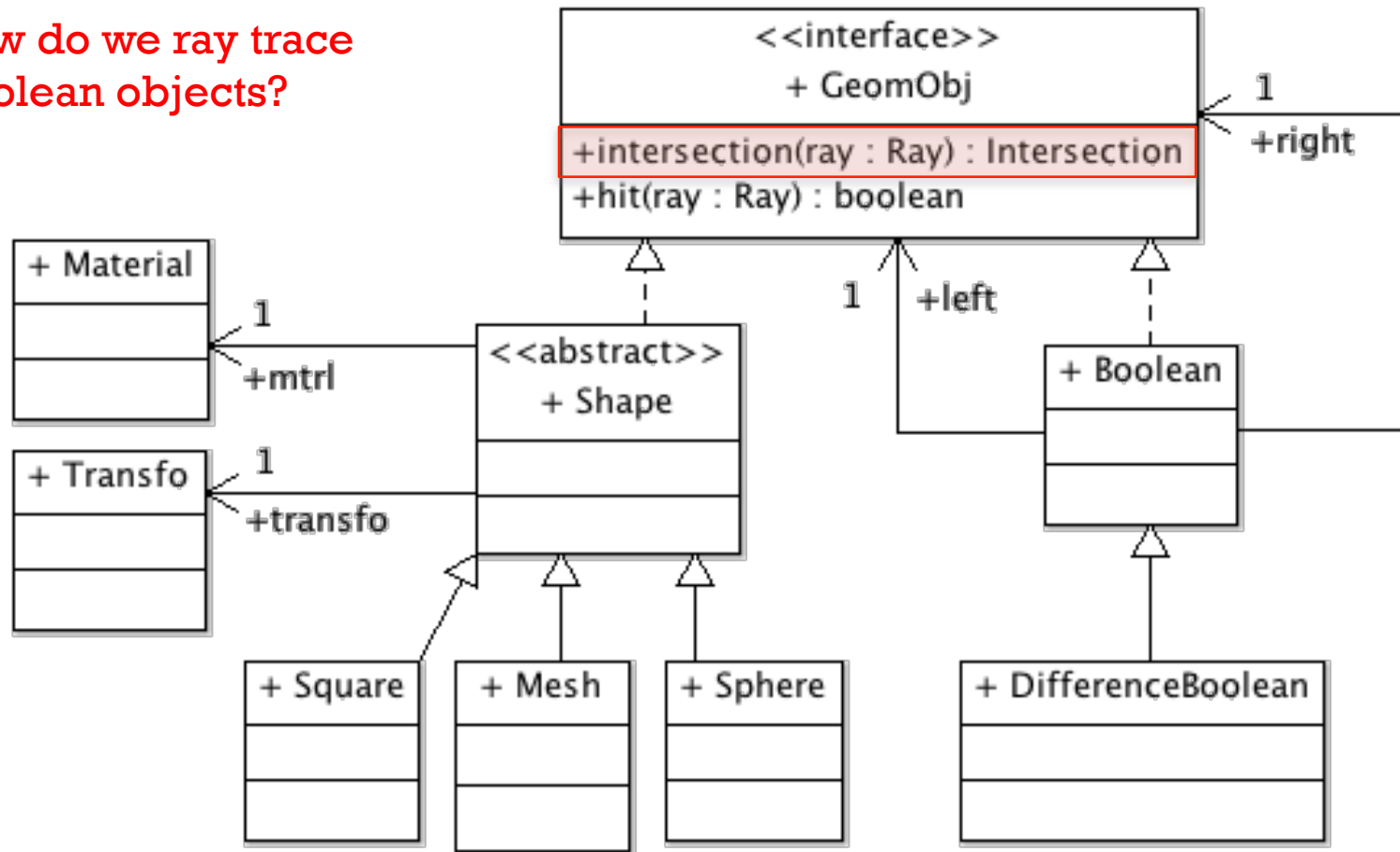
12



Support for boolean objects

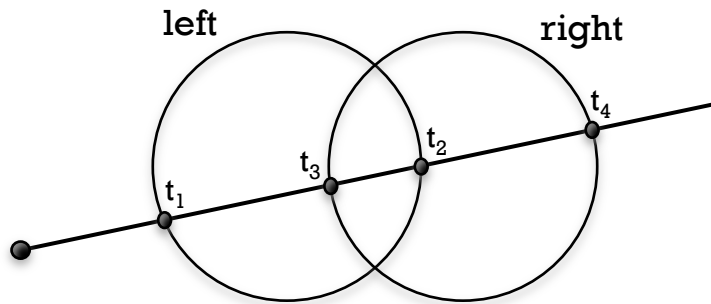
13

How do we ray trace
boolean objects?

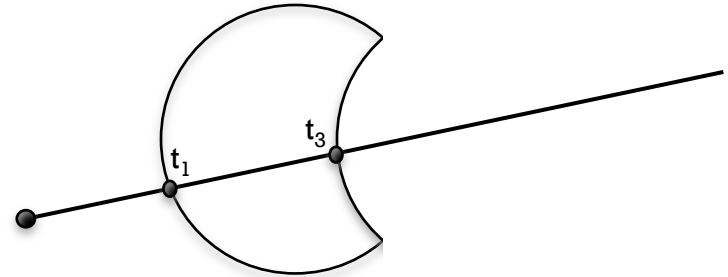


Example

14



comb = left - right



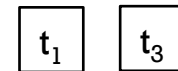
leftInter = left.intersection(ray)



?



combInter:



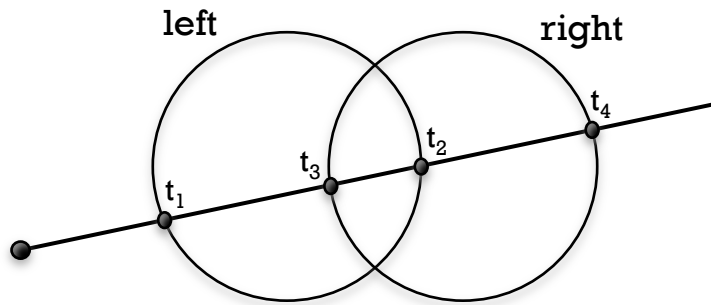
rightInter = right.intersection(ray)



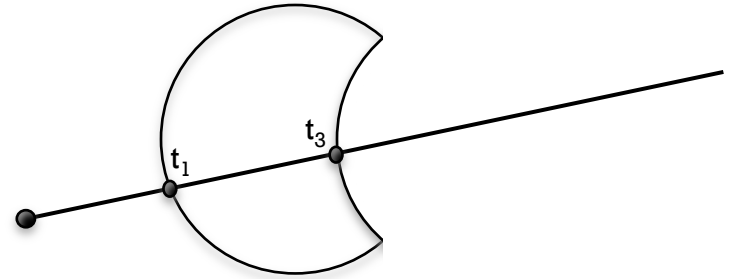
Pseudocode for DifferenceBoolean

```
Public Intersection intersection(Ray ray){  
    Intersection combInter = new Intersection();  
    Intersection leftInter, rightInter;    // and initialize values  
  
    ?  
  
    return combInter;  
}
```

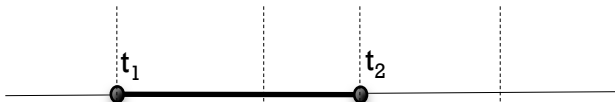
Example



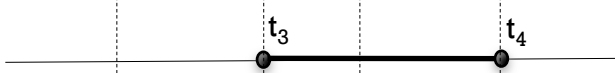
$$\text{comb} = \text{left} - \text{right}$$



left:



right:



leftInside

F T T F F

rightInside

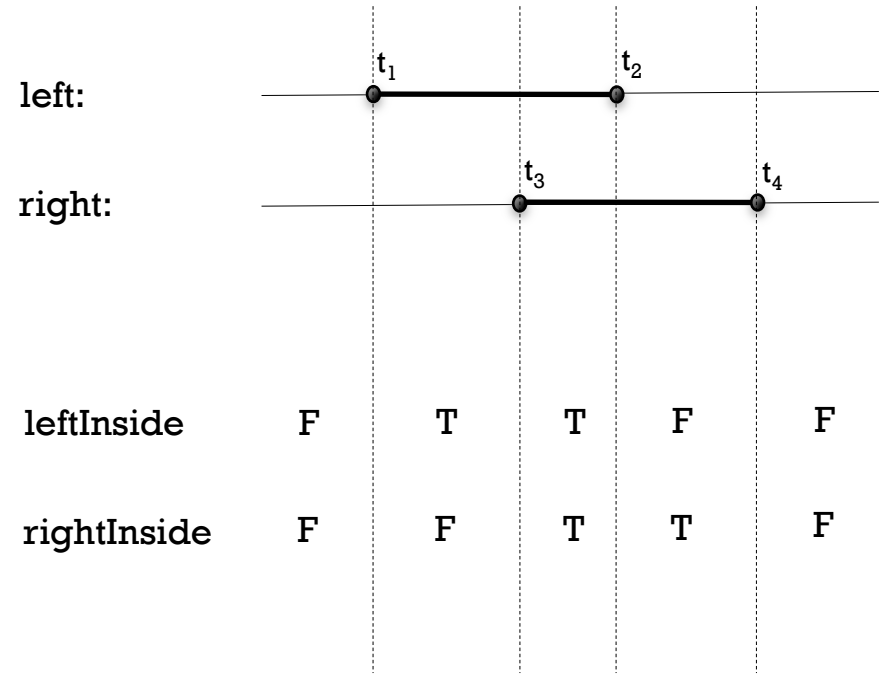
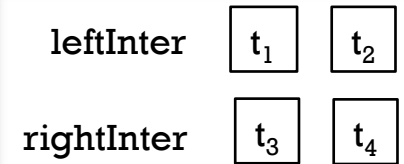
F F T T F

We will process the t-values in ascending order and keep track of whether we are currently inside the left object and/or inside the right object.

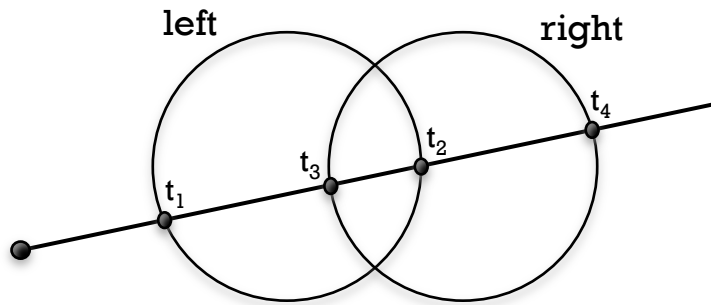
Pseudocode for DifferenceBoolean

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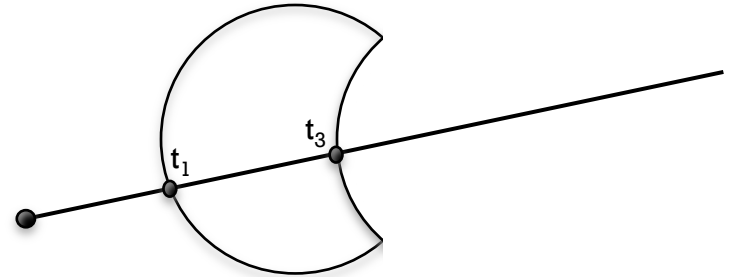
```
Public Intersection intersection(Ray ray){  
    Intersection combInter = new Intersection();  
    Intersection leftInter, rightInter;    // and initialize values  
    boolean leftInside, rightInside;    // and initialize values  
    while (there are still unprocessed hitPoints in leftInter and rightInter){  
        if(next unprocessed hitPoint in leftInter is closer than next unprocessed hitPoint in rightInter){  
            change leftInside  
        } else {  
            change rightInside  
        }  
    }  
    return combInter;  
}
```



Example



$$\text{comb} = \text{left} - \text{right}$$



left:		t ₁		t ₂		
right:			t ₃		t ₄	
comb:		t ₁	t ₃			
leftInside	F	T	T	F	F	
rightInside	F	F	T	T	F	
combInside	F	T	F	F	F	

- Apart from leftInside and rightInside, we will also keep track of combInside.
- How can we compute combInside if we know leftInside and rightInside?

$$\text{combInside} = \text{leftInside} \ \&\& \ !\text{rightInside}$$

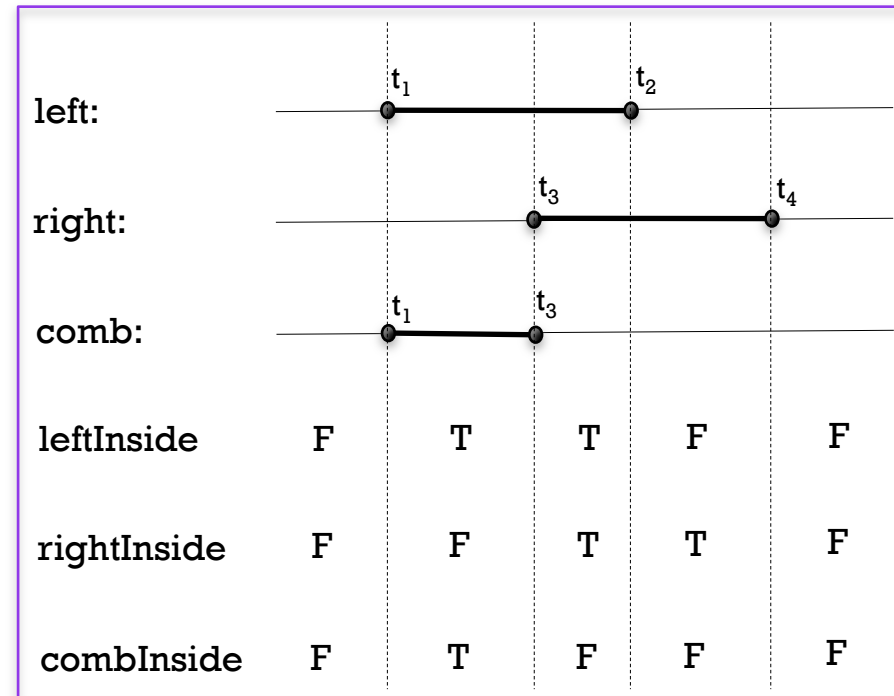
- Why is the value of combInside useful?

If the value of combInside changes, we have to add the current hitpoint to combInter.

Pseudocode for DifferenceBoolean

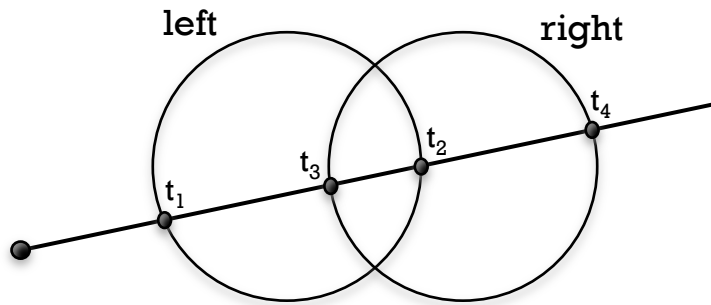
```

Public Intersection intersection(Ray ray){
    Intersection combInter = new Intersection();
    Intersection leftInter, rightInter;    // and initialize values
    boolean leftInside, rightInside, combInside;    // and initialize values
    while (there are still unprocessed hitPoints in leftInter and rightInter){
        boolean combInsideNew;
        if(next unprocessed hitPoint in leftInter is closer than next unprocessed hitPoint in rightInter){
            change leftInside
            combInsideNew = leftInside && !rightInside
            if(combInsideNew != combInside)
                update combInside
                add the current hitPoint of leftInter to combInter
        } else {
            change rightInside
            combInsideNew = leftInside && !rightInside
            if(combInsideNew != combInside)
                update combInside
                add the current hitPoint of rightInter to combInter
        }
    }
    return combInter;
}
    
```

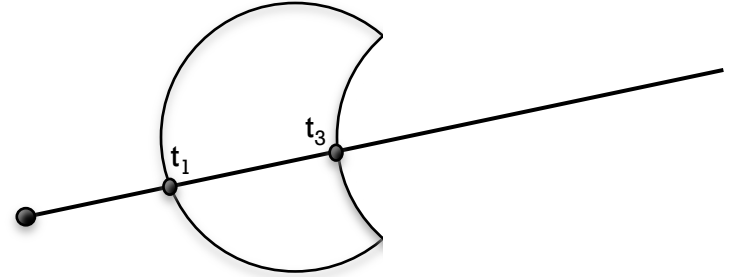


Example

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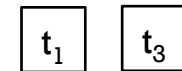
comb = left - right



leftInter = left.intersection(ray)



combInter:

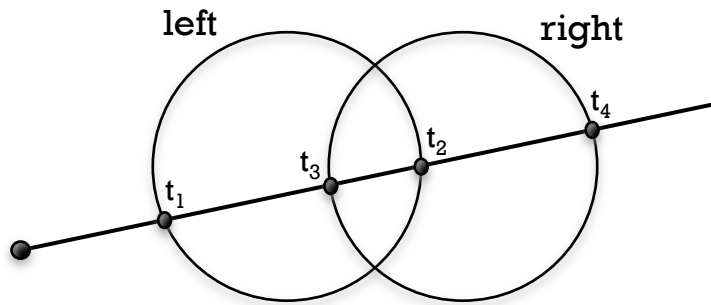


rightInter = right.intersection(ray)

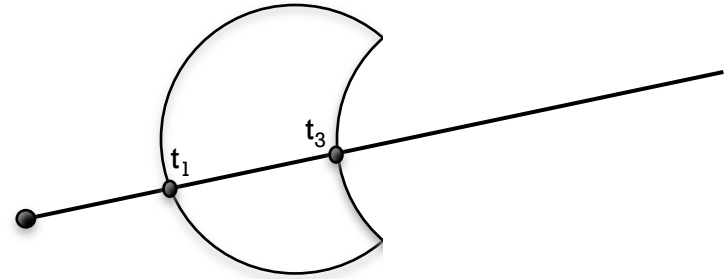


- The intersection method returns an Intersection object.
- An Intersection object contains a list of HitInfo objects.
- A HitInfo object contains more information than a t-value!

Example



comb = left - right



leftInter:

t_1
hitMaterialLeft
hitPoint₁
hitNormal₁
isEntering₁ = T

t_2
hitMaterialLeft
hitPoint₂
hitNormal₂
isEntering₂ = F

rightInter:

t_3
hitMaterialRight
hitPoint₃
hitNormal₃
isEntering₃ = T

t_4
hitMaterialRight
hitPoint₄
hitNormal₄
isEntering₄ = F

combInter:

t_1
hitMaterialLeft
hitPoint₁
hitNormal₁
isEntering₁ = T

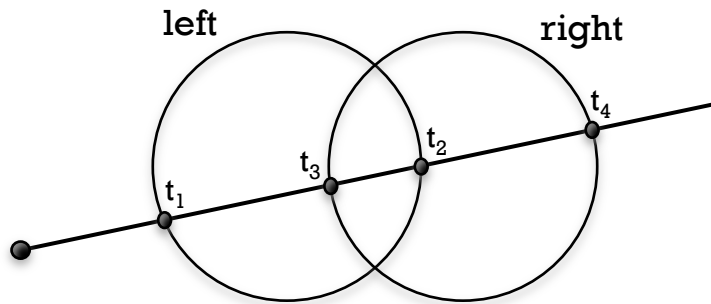
~~t_3
hitMaterialRight
hitPoint₃
hitNormal₃
isEntering₃ = T~~

Wrong

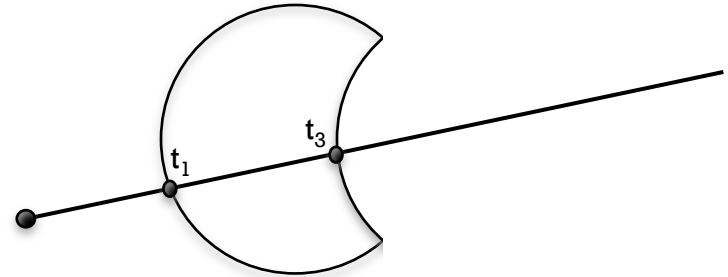
t_3
hitMaterialLeft
hitPoint₃
reverse of hitNormal₃
isEntering₃ = F

Example

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comb = left - right



Changeset A

Changes which have to be made to HitInfo objects before they are added to combInter:

- 1) All HitInfo objects of combInter have a hitMaterial equal to the material of the left shape.
- 2) If a HitInfo object of the right shape is added to combInter, the hitNormal should be reversed if combInside \neq rightInside.
- 3) The isEntering variable of all HitInfo objects of combInter should be set to combInside.

combInter:

t₁
hitMaterialLeft
hitPoint₁
hitNormal₁
isEntering₁ = T

~~t₃
hitMaterialRight
hitPoint₃
hitNormal₃
isEntering₃ = T~~

t₃
hitMaterialLeft
hitPoint₃
reverse of hitNormal₃
isEntering₃ = F

Pseudocode for DifferenceBoolean

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```

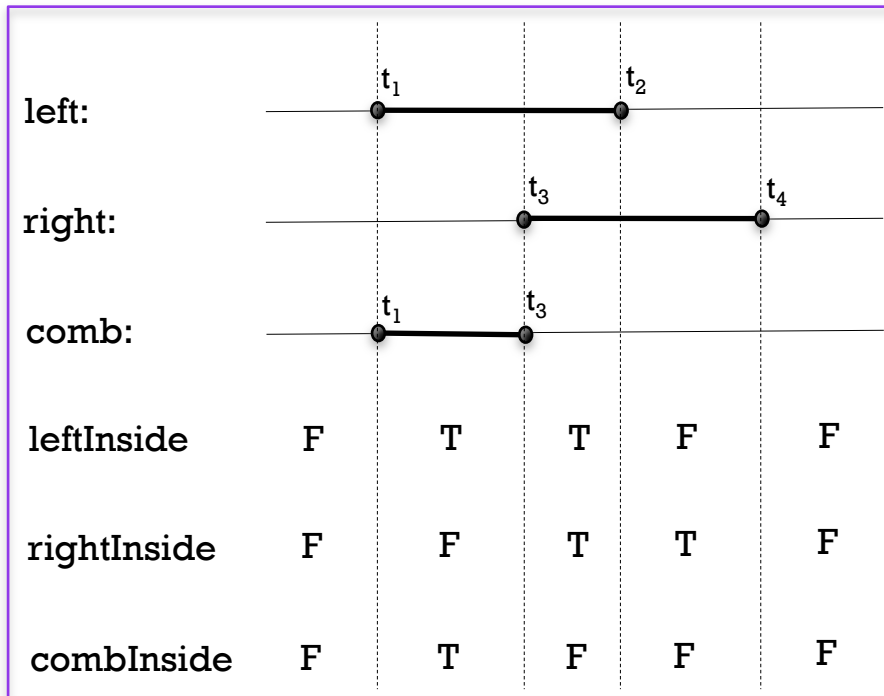
Public Intersection intersection(Ray ray){
    Intersection combInter = new Intersection();
    Intersection leftInter, rightInter;    // and initialize values
    boolean leftInside, rightInside, combInside;    // and initialize values
    while (there are still unprocessed hitPoints in leftInter and rightInter){
        boolean combInsideNew;
        if(next unprocessed hitPoint in leftInter is closer than next unprocessed hitPoint in rightInter){
            change leftInside
            combInsideNew = leftInside && !rightInside
            if(combInsideNew != combInside)
                update combInside
            add the current hitPoint of leftInter to combInter
        } else {
            change rightInside
            combInsideNew = leftInside && !rightInside
            if(combInsideNew != combInside)
                update combInside
            add the current hitPoint of rightInter to combInter
        }
    }
    return combInter;
}
    
```

When does the while loop end?

If the list of HitInfo objects of leftInter
OR rightInter is completely processed.

Should we still process the other list?

Yes, if it is the list of the left object.



Changeset B:
Process the remaining HitInfo
objects of the left shape.

Pseudocode for DifferenceBoolean

```
Public Intersection intersection(Ray ray){
```

```
    Intersection combInter = new Intersection();
```

```
    Intersection leftInter, rightInter;    // and initialize values
```

```
    boolean leftInside, rightInside, combInside;    // and initialize values
```

```
    while (there are still unprocessed hitPoints in leftInter and rightInter){
```

```
        boolean combInsideNew;
```

```
        if(next unprocessed hitPoint in leftInter is closer than next unprocessed hitPoint in rightInter){
```

```
            change leftInside
```

```
            combInsideNew = leftInside && !rightInside
```

```
            if(combInsideNew != combInside)
```

```
                update combInside
```

```
                add the current hitPoint of leftInter to combInter
```

```
        } else {
```

```
            change rightInside
```

```
            combInsideNew = leftInside && !rightInside
```

```
            if(combInsideNew != combInside)
```

```
                update combInside
```

```
                add the current hitPoint of rightInter to combInter
```

```
        }
```

```
    }
```

```
    return combInter;
```

```
}
```

Changeset C

What if the list of HitInfo objects of leftInter or rightInter is empty?

- If leftInter is empty, return an empty combInter immediately.
- If rightInter is empty, return leftInter immediately.

left:

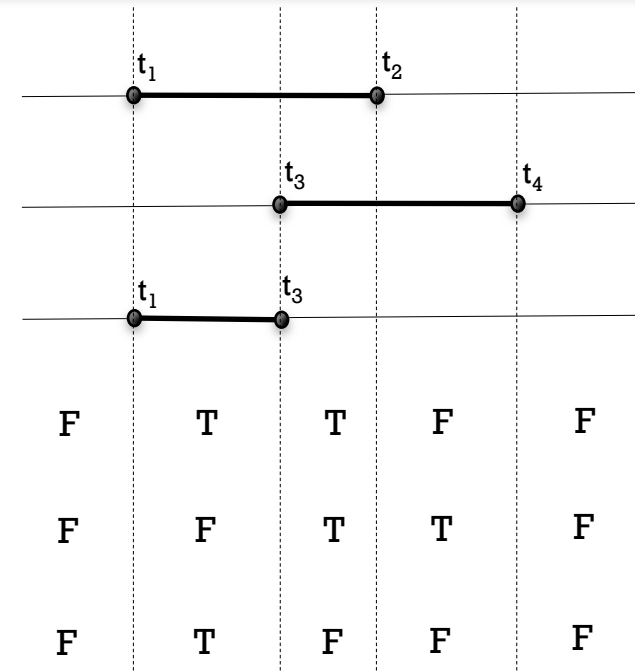
right:

comb:

leftInside

rightInside

combInside





Questions?