Sample Size Formula, Common SDs

Sample size is calculated by use of the following formula:

$$n = \frac{2 (z_{\alpha} + z_{\beta})^{2} (sd_{c}^{2} + (W^{2} sd_{q}^{2}) - (2 W \rho sd_{c} sd_{q}))}{(WQ - C)^{2}}$$

where n = sample size/group; z_{α} and z_{β} = z-statistics for α (e.g., 1.96) and β (e.g., 0.84) errors; sd = standard deviation for cost (sd_c) and effect (sd_q); W = maximum willingness to pay we wish to rule out; ρ = correlation of the difference in cost (C) and effect (Q)



Correlation

- When increasing effects are associated with decreasing costs, a therapy is characterized by a negative (win/win) correlation between the difference in cost and effect
 - e.g., asthma care
- When increasing effects are associated with increasing costs, a therapy is characterized by a positive (win/lose) correlation between the difference in cost and effect
 - e.g., life-saving care
- All else equal, fewer patients need to be enrolled when therapies are characterized by a positive correlation than when therapies are characterized by negative correlation



Willingness to Pay

- Moving willingness to pay "nearer to" or "further away from" the expected point estimate of the costeffectiveness ratio increases or reduces the sample size we need to be confident of value
 - Caution: "Nearer" and "further away" are not measured on the real number line

Implication: Sample size need not always decrease as willingness to pay increases

