Lattice QCD

- Lattice QCD is the numerical simulation of QCD
 - The QCD action, which expresses the strong interaction between quarks mediated by gluons:

$$S_{Dirac} = \overline{\psi} (D + m) \psi$$

where the Dirac operator ("dslash") is given by

$$\mathbb{D}\psi = \sum_{\mu} \gamma_{\mu} (\partial_{\mu} + igA_{\mu}(x))\psi(x)$$

- Lattice QCD uses discretized space and time
- A very simple discretized form of the Dirac operator is

$$D\psi(x) = \frac{1}{2a} \sum_{\mu} \gamma_{\mu} [U_{\mu}(x)\psi(x + a\hat{\mu}) - U_{\mu}^{\dagger}(x - a\hat{\mu})\psi(x - a\hat{\mu})]$$

where a is the lattice spacing