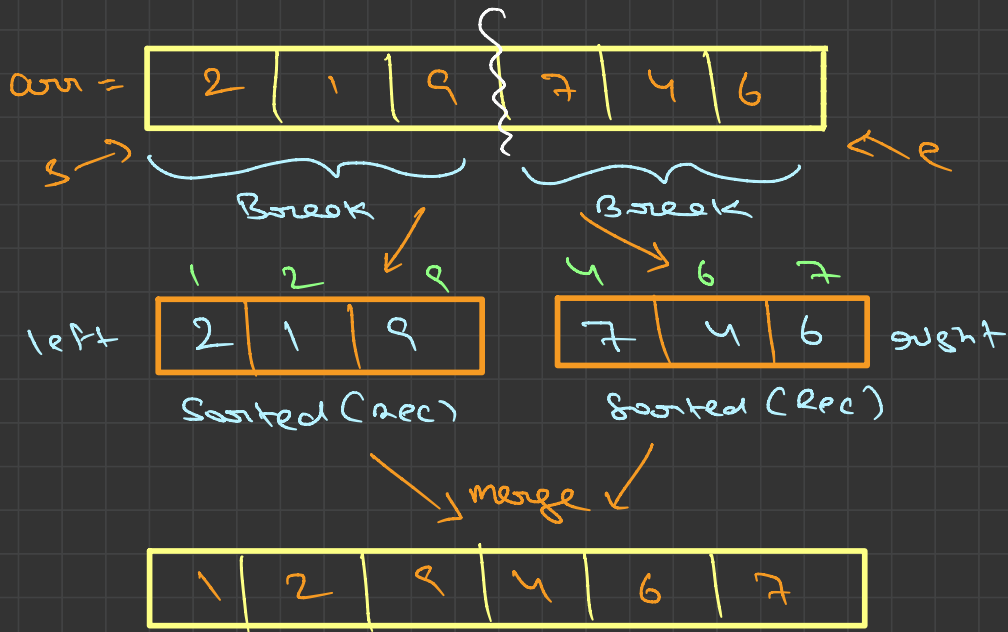



Merge Sort



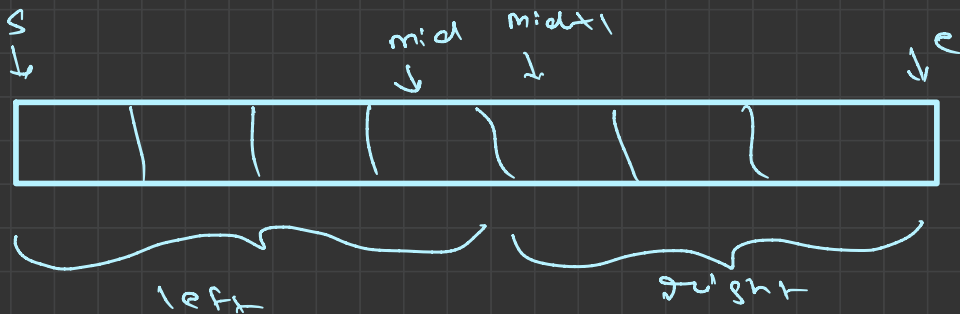
I \rightarrow Break

II \rightarrow Recursion

III \rightarrow merge 2 sorted array

Base Case Rec

```
if (s > e) return;  
if (s == e) return;
```



How to find length?

$$\text{left} = \text{mid} - s + 1$$

$$\text{right} = e - (\text{mid} + 1) + 1$$

$$\hookrightarrow e - \text{mid} - \cancel{1} + \cancel{1}$$

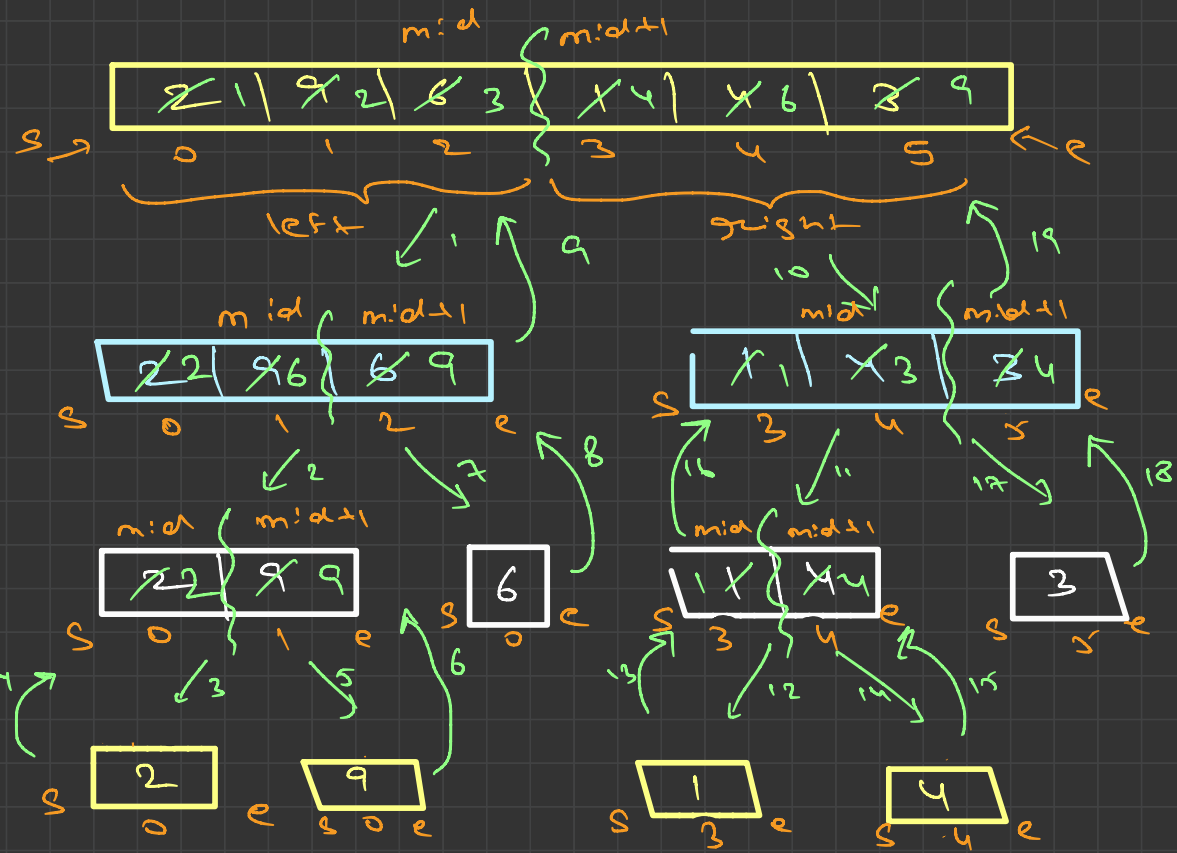
$$\hookrightarrow e - \text{mid}$$

```
void mergeSort (int arr[], int s, int e)
{
    // base case
    if (s > e) return ;
    if (s == e) return ;

    // break
    int mid = (s + e) / 2 ;

    // rec call
    mergeSort (arr, s, mid);
    mergeSort (arr, mid + 1, e);

    // merge
    merge (arr, s, e, mid);
}
```



```

void merge(int arr[], int s, int e)
{
    // find mid
    int m = (s + e) / 2;

    // find length of left and right array
    int lenLeft = m - s + 1;
    int lenRight = e - m;

    // create left and right array
    int *leftArr = new int[lenLeft];
    int *rightArr = new int[lenRight];

    // copy value in left and right array
    int k = s; // for tracking original array index

    // copy value in left array
    for(int i = 0; i < lenLeft; i++){
        leftArr[i] = arr[k];
        k++;
    }

    // copy value in right array
    for(int i = 0; i < lenRight; i++){
        rightArr[i] = arr[k];
        k++;
    }

    // compare both sorted left and right array and copy in original array in sorted way
    int leftIndex = 0;
    int rightIndex = 0;
    int orgIndex = s;

    while(leftIndex < lenLeft && rightIndex < lenRight){
        if(leftArr[leftIndex] < rightArr[rightIndex]){
            arr[orgIndex] = leftArr[leftIndex];
            leftIndex++;
            orgIndex++;
        }
        else{
            arr[orgIndex] = rightArr[rightIndex];
            rightIndex++;
            orgIndex++;
        }
    }

    while(leftIndex < lenLeft){
        arr[orgIndex] = leftArr[leftIndex];
        leftIndex++;
        orgIndex++;
    }

    while(rightIndex < lenRight){
        arr[orgIndex] = rightArr[rightIndex];
        rightIndex++;
        orgIndex++;
    }

    delete[] leftArr;
    delete[] rightArr;
}

```

$$T(n) = 1 + 2T\left(\frac{n}{2}\right) + 3 \times 1$$

$$2 \times T\left(\frac{n}{2}\right) = 1 + \cancel{2}T\left(\cancel{\frac{n}{2}}\right) + \cancel{\frac{n}{2}} \times \cancel{1} \times \cancel{2}$$

$$4 \times T\left(\frac{n}{4}\right) = 1 + \cancel{2}T\left(\cancel{\frac{n}{2}}\right) + \cancel{\frac{n}{2}} \times \cancel{1} \times \cancel{4}$$

$$8 \times T\left(\frac{n}{8}\right) = 1 + \cancel{2}T\left(\cancel{\frac{n}{4}}\right) + \cancel{\frac{n}{4}} \times \cancel{1} \times \cancel{8}$$

$$\vdots$$

$$\vdots$$

$$\vdots$$

$$2^{(a-1)} \times T(1) = 2^{a-1} \times 1$$

$\log_2 n$

$\frac{n}{2}$
 $\frac{n}{4}$
 $\frac{n}{8}$
 \vdots

$$T(n) = \underbrace{k_1(1+2+4+\dots+2^{n-1})}_{\text{g.p.}} + (q-1)n \times k$$

$$= k_1 \times n + q \times n \times k$$

$$= \cancel{k_1 n} + n \log n \times k$$

$$= n \log n \times \cancel{k}$$

$$\boxed{= n \log n}$$

==

Imploce