Problem Set 10

UMC 202

November 2, 2023

1. Use the Linear Finite-Difference Algorithm with ${\cal N}=9$ to approximate the solution to the boundary value problem

$$y'' = -\frac{2}{x}y' + \frac{2}{x^2}y + \frac{\sin(\ln x)}{x^2},$$

$$1 \le x \le 2, \ y(1) = 1, \ y(2) = 2$$

and compare the results to those obtained using the linear shooting method for the same problem.

2. Consider the boundary value problem

$$y'' = -(x+1)y' + 2y + (1-x^2)e^{-x}, \ 0 \le x \le 1, \ y(0) = 1, \ y(1) = 0.$$

Use N=9 and N=19 respectively and apply the Linear Finite-Difference Algorithm with N=9 to approximate the solution to the above boundary value problem.

3. Use the Linear Finite-Difference Algorithm with N=4 to approximate the solution of the boundary value problem,

$$y'' + 4y = \cos x, \ 0 \le x \le \frac{\pi}{4}, \ y(0) = 0, \ y(\frac{\pi}{4}) = 0,$$

and compare the results to the actual solution where the actual solution is given by

$$y(x) = -\frac{1}{3}\cos 2x - \frac{\sqrt{2}}{6}\sin 2x + \frac{1}{3}\cos x.$$